

Lattice dynamics and methyl rotational excitations of 2-butyne

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On the basis of the recently determined low temperature crystal structure the lattice dynamics of 2-butyne and a single particle methyl rotational potential are calculated using pair potential parameters given by Williams in 1974 within the model of semirigid molecules. In the regime of lattice modes the existence of four methyl librational bands with significant dispersion can explain the measured density of states. The single particle librational energy obtained for the rotational potential from the Schrödinger equation of the methyl rotor coincides well with the mean librational band energy. The calculated single particle tunneling frequency is only 17% lower than observed in experiment. Similarly well the activation energy is reproduced. Although the pair potential parameters developed for aromatic compounds need some scaling they are useful for materials with triple bond carbons. © 2002 American Institute of Physics. [DOI: 10.1063/1.1485729]

I. INTRODUCTION

The theory developed originally to describe rotational tunneling of molecular crystals is a mean field or single particle model (SPM).¹ Despite the more recent detection of systems with coupling and multidimensional tunneling^{2,3} the prominent number of molecular crystals can be well described within the original SPM.⁴ A data analysis going beyond a phenomenological use of this model has to explain the rotational potential on the basis of the crystal structure and fundamental intermolecular interactions.^{5,6} Often intermolecular interactions are modeled as transferable intermolecular pair interactions. There is an increasing number of systems analyzed this way. Their number is mainly limited by the knowledge of a precise low temperature crystal structures of systems whose tunnel splitting is known from high resolution neutron spectroscopy. Another difficulty is due to the reliability of the atom-atom potential ansatz for the intermolecular interaction. The more complex a compound is the more difficult is it to get reliable pair potential parameters from literature. For this second reason we concentrated at the beginning our work on simple systems, mainly pure hydrocarbons as toluene⁵ and *p*-xylene⁷ which belong to a class of materials most intensively studied by the concept of pair potentials.^{8,9} In the present paper we want to extend the successful earlier description to an only slightly different material. 2-butyne—also known as dimethylacetylene (DMA)—is again a pure hydrocarbon but with a triple bond between the two central carbon atoms. It is the simplest compound containing at the same time methyl groups but in contrast to other hydrocarbons there are no pair potentials (PP) available from literature for this material. The question arises whether pair potentials of DMA differ from those of aliphatic or aromatic hydrocarbons.

2-butyne is one of the first systems where rotational tun-

neling was observed by high resolution neutron spectroscopy.^{10,11} It was difficult to relate this tunnel splitting to the librational modes measured in a forthcoming experiment.¹² In this paper the missing knowledge of the crystal structure did not allow a mode analysis and the description had finally to be based on an ad hoc model allowing for dispersion of the librational modes.

Thus it became interesting to study this material in a more comprehensive way after the low temperature crystal structure became known,¹³ see Fig. 1. The technique of choice is to combine the structural information with transferable intermolecular pair potentials. The basic questions are threefold:

- (1) Is the assumption of a semirigid molecule justified?
- (2) How does the phenomenological explanation of the density of states of Ref. 12 compare with a mode analysis based on a lattice dynamics calculation?
- (3) Do the pair potential parameters need to be modified compared to those used for aromatic hydrocarbons¹⁴ due to triple bond between the center carbons?

II. EXPERIMENTAL RESULTS

A. Excitations

Inelastic neutron scattering was used to study excitations in the regime of phonons and internal excitations. Due to its wide accessible energy range up to 500 meV and its good energy resolution $\delta E/E \sim 0.02$ in the whole spectral range the inverse time-of-flight spectrometer TFXA of the ISIS spallation source at the Rutherford-Appleton Laboratories, UK, was used.¹⁵ At this crystal analyzer instrument energy transfer and momentum transfer are correlated. The INS spectrum is available from the INS database¹⁶ at www.isis.rl.ac.uk/insdatabase.

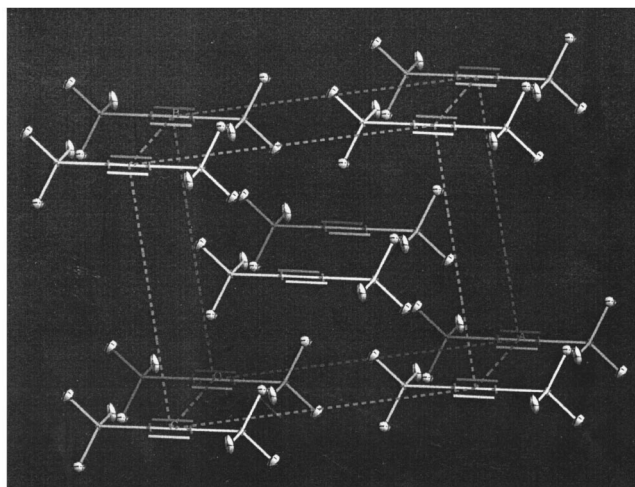


FIG. 1. Unit cell of DMA, space group $C2/m$ showing the triple bond between the central carbon atoms. The positions of the atoms are calculated according to Ref. 13.

A flat protonated sample of volume $30 \times 50 \times 1 \text{ mm}^3$ was cooled down to $T \leq 15 \text{ K}$ and measured for 24 h. This corresponds to an integrated proton dose of $2000 \mu\text{Ah}$. All detectors are summed up in a single spectrum shown in Fig. 2. The spectrum decomposes into two regimes. Above about 20 meV internal molecular vibrations, higher harmonics and combination bands are visible. Below 20 meV we have the regime of phonons. This part of the spectrum was measured already earlier at the direct time-of-flight spectrometer IN4 of the ILL, France.¹² Small differences in peak positions are likely due to the different ways the used instruments integrate over the dispersion curves.

B. Quasielastic scattering and activation energy

The quasielastic spectra of DMA had been obtained using the FOCUS spectrometer at the Swiss neutron source SINQ. The wavelength of the incoming neutrons were chosen to be $\lambda = 5.8 \text{ \AA}$ with a corresponding elastic energy resolution $\delta E = 50 \mu\text{eV}$. The energy transfer range of interest was between -2 and 1 meV . The experimental data were

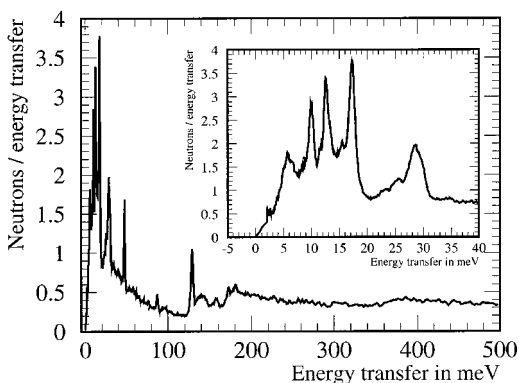


FIG. 2. Neutron spectrum of DMA up to 310 meV measured at a sample temperature $T \leq 15 \text{ K}$. There are no further excitations visible up to 500 meV likely due to recoil broadening. The regime of phonons/lattice modes below 20 meV is shown in the insert. Four peaks at 6, 9.9, 12.6, and 17.3 meV are clearly visible.

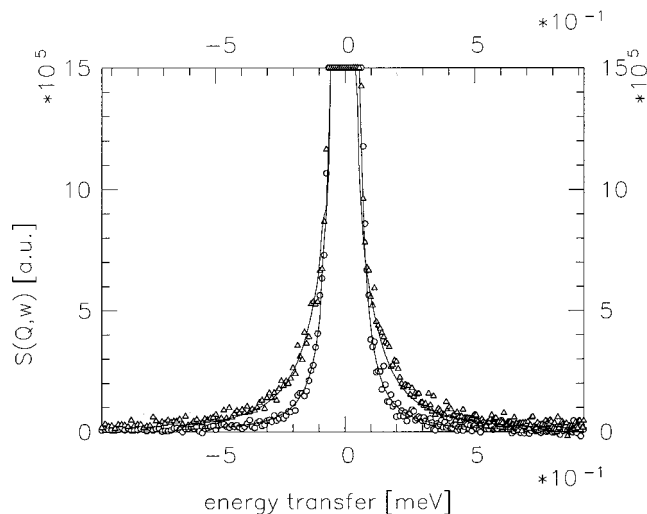


FIG. 3. Scattering function $S(Q, \omega)$ of DMA in the quasielastic regime. The temperature dependent quasielastic line broadening is shown for temperatures of 80 K (\circ) and 120 K (Δ).

transformed into $S(Q, \omega)$ using standard procedures. Figure 3 shows the broadening of the quasielastic line for two different temperatures. Since all methyl groups are crystallographical equivalent the resulting QNS spectra are described by a single Lorentzian.

The model used to analyze quasielastic spectra is a simple hopping model. Since the potential forces the molecule into the equilibrium position the only possibility for a hydrogen to move is to jump over the barrier into an equivalent position. The scattering function $S(Q, \omega)$ for a powder sample with protons jumping on a triangle with a jump frequency ν is given by

$$S(Q, \omega) = A_0(Q) \delta(\omega) + A_1(Q) \frac{1}{\pi} \frac{\frac{3}{2} \nu}{(\frac{3}{2} \nu)^2 + \omega^2} \quad (1)$$

with the prefactors $A_0(Q) = \frac{1}{3}(1 + 2j_0(Qd))$ and $A_1(Q) = \frac{2}{3}(1 - j_0(Qd))$, where Q is the value of the scattering vector and d the jump length, i.e., the proton-proton distance of 1.78 \AA inside the CH_3 group. The width of the Lorentzian in Eq. (1) is $\Gamma = (3/2) \nu$. Since jumps are thermally activated processes the jump frequency and thus the linewidth of the Lorentzian depends on the temperature and follows an Arrhenius behavior,

$$\begin{aligned} \Gamma(T) &= \Gamma_0 \cdot \exp\left(-\frac{E_a}{kT}\right) \\ &= \Gamma_0 \cdot \exp(-0.0116 \cdot E_a[\text{meV}] \cdot \Theta[\text{K}^{-1}]) \end{aligned}$$

with $\Theta = 10^3/T$.

The hopping model allows to derive the *activation energy* E_a which yields the energy difference between the ground state and the maximum of the methyl rotational potential.

In order to get the activation energy eight quasielastic spectra were collected in the temperature range of $70 \text{ K} \leq T \leq 150 \text{ K}$ (corresponding to $6.7 \text{ K}^{-1} \leq \Theta \leq 14.3 \text{ K}^{-1}$) and analyzed with respect to the temperature dependent FWHM of the Lorentzians. A least squares fit to the data yields E_a

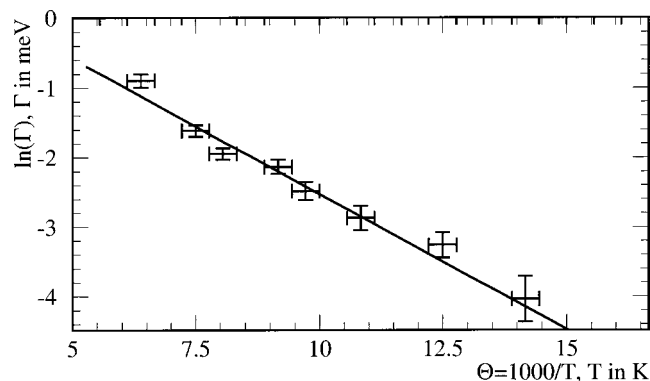


FIG. 4. Arrhenius plot $\Gamma(\Theta) = \Gamma_0 \cdot \exp(-0.0116 \cdot E_a \cdot \Theta)$ of the temperature dependent FWHM Γ of the incoherent quasielastic line broadening, see also Fig. 3.

$= 33.6$ meV (3.2 kJ/mol), Fig. 4. The prefactor $\Gamma_0 \approx 4$ meV is consistent with the attempt frequency found otherwise for methyl groups.

III. CALCULATIONS

Molecular crystals are most often described by the model of rigid or semirigid molecules: To reduce the number of degrees of freedom (DOF) all or most internal DOF are frozen. Indeed very often the hard internal vibrations do not overlap with the external modes. For molecules with attached rotating radicals like methyl groups, however, only semirigidity can be valid. The soft internal modes are now included into the external DOF. *Ab initio* calculations give a quantitative measure of the internal DOF which have to be included by the lattice dynamical calculation.

A. *Ab initio* calculations for the isolated molecule

In the gas phase, there is free rotation of the methyl groups, thus the D_{3h} (methyl groups eclipsed) and D_{3d} (methyl groups staggered) structures are equivalent. In the low temperature $C2/m$ phase¹³ the center of the molecule lies on a point of inversion, however, the molecule is slightly deformed, such that one of the C–H bonds is shorter than the other two and the symmetry is reduced to C_{2h} .

The vibrational modes of molecules containing up to a few tens of first row atoms can be calculated on a PC using *ab initio* methods. In the present case, density functional theory (DFT) as implemented in the GAUSSIAN 98 (Ref. 17) package was used with the B3LYP functional and 6-31G, 6-311+G, and 6-311+G(*d,p*) basis sets. All the methods yielded similar results, with the largest basis set providing the best results.

The D_{3h} , D_{3d} structures and a C_{2h} structure that used the crystallographic geometry as the initial input were examined. All gave stable structures, although in each case, the antiphase methyl torsion was close to zero. The C_{2h} structure converged to a geometry that was almost D_{3d} , this is also shown by the very small (< 0.1 meV) splitting of the degenerate modes. This result strongly suggests that the solid state structure is crystallographically imposed.

The observed intensity of an INS band is given by¹⁸

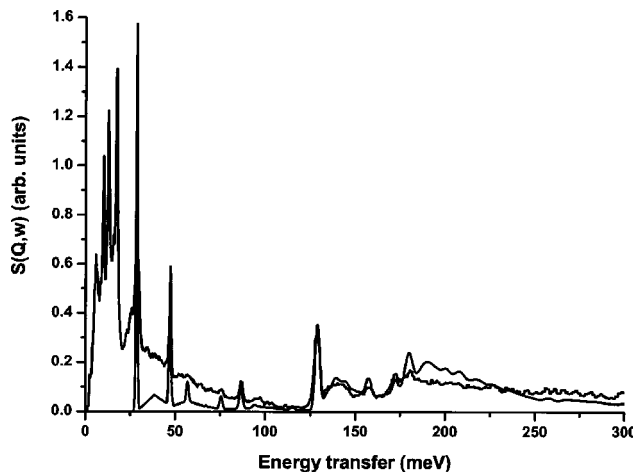


FIG. 5. Comparison between the measured TFXA and the calculated a-CLIMAX spectra, based on the calculated atomic displacements. See text for details.

$$S(Q, n\omega_i) \propto \frac{(Q \cdot U_i)^{2n}}{n!} \exp(-(Q \cdot U_{\text{Tot}})^2) \cdot \sigma, \quad (2)$$

where ω_i is the i th mode at frequency ω , $n=1$ for a fundamental, 2 for a first overtone or binary combination, 3 for a second overtone or ternary combination etc., Q is the momentum transfer defined earlier, U_i is the root mean square displacement of the atoms in the mode, U_{Tot} is the total root mean square displacement of all the atoms in all the modes, both internal and external, σ is the inelastic scattering cross section of the atom. The total scattering cross sections of hydrogen and carbon are 82.0 and 5.6 barns (1 barn = 1×10^{-28} m²), respectively¹⁹ and since the intensity is dependent on the amplitude of vibration, which is larger for light atoms, the spectra will be dominated by motions that involve displacement of hydrogen. The exponential term in Eq. (2) is a Debye–Waller factor. Equation (2) is based on an isolated molecule approximation, thus dispersion is not included. The narrow linewidths of the modes above 25 meV demonstrate that this is a reasonable assumption in the present case.

The output of GAUSSIAN 98 includes the atomic displacements for each mode, which can be used to visualize the mode and also to generate the INS spectrum. The program a-CLIMAX (Ref. 20) was used for this purpose. After minor adjustment of the frequencies to match the observed values and inclusion of events involving up to three quanta the result shown in Fig. 5 is obtained. The agreement between observed and calculated is excellent confirming the assignments given in Table I.

The width of the skeletal bending mode at 39.7 meV is significantly larger than the resolution function which results in an apparent mismatch for this band, although the integrated intensity is approximately correct. This is probably due to factor group splitting since there are two molecules in the unit cell. This frequency is significantly above the phonon energies so justifies the treatment of the molecule as a rigid body in the lattice dynamical calculations described in the following section.

TABLE I. Vibrational modes of DMA as calculated *ab initio* using the GAUSSIAN 98 program are compared to the excitation energies measured by neutron spectroscopy. Modes are assigned to each excitation energy.

Gaussian energies (MeV)	Multiplicity	Mode character	Observed (TFXA) energies (meV)
0	1	methyl torsion	6,9,9,12,6,17.3
26.4	2	backbone bend	28.5
47.1	2	backbone twist	47.4
87.5	1	backbone sym. stretch	87
132	4	methyl rock	129
141	1	backbone asym. stretch	
176	2	methyl sym. breath.	172
186	4	methyl deformation	181
290	1	backbone stretch	
378–386	6	proton stretch	

The strong mode at 129 meV is the methyl rocking mode and both the INS spectrum and the *ab initio* results show that the four (two doubly degenerate modes) are coincident. The low temperature Raman spectrum²¹ shows that the asymmetric methyl bending modes give rise to a broad, ~5 meV, band at 180 meV. The *ab initio* results suggests that these bands are very close in energy which is why the feature is apparently overestimated. Inspection shows that there is missing intensity in the calculated spectrum at 175 meV, suggesting that one of the modes is calculated too high in energy. Shifting one of the modes to lower energy would also reduce the overestimation of the phonon wings that are responsible for the intensity at ~185 meV.

The higher energy modes are poorly resolved from the phonon wings. This is due to the large Debye–Waller factor that results from a relatively light molecule and the large displacements in the coupled torsional/librational modes. Since the C≡C stretch has little proton motion, it is intrinsically weak in the INS spectrum and is not observed. At large energy transfers, the spectral detail is obliterated by molecular recoil. There is nearly no internal torsional restoring force. The next lowest eigenenergies around 26 meV belongs to a bend of the molecule backbone in two different but equivalent planes. Thus the lowest internal vibrational mode energy is (see below) above the largest phonon energies. Thus we describe the molecule in the following lattice dynamical calculations as completely rigid beside of the internal torsion.

B. Lattice dynamics of the crystal

Phonon dispersion curves are calculated by the program DYNAL which was successfully used for similar applications earlier.^{5,7,22} With DYNAL phonon energies and eigenvectors are obtained by diagonalizing the dynamical matrix. DMA contains two molecules in the unit cell with one soft internal degree of freedom each, the out-of-phase methyl librations. For otherwise rigid molecules this yields 14 phonon branches. The force constants are derived in harmonic approximation as second derivatives of atom–atom pair potentials. The intermolecular interactions were modeled in the following by a Born–Meyer potential:

TABLE II. Williams⁷⁴ and scaling parameters used to calculate the lattice dynamics of DMA.

Pair	A_{ij} (kcal/mol) ^a	B_{ij} (10 ³ kcal/mol)	α_{ij} (⁻¹)	k_{ij}	f
H–H	40.1	2.876	3.74	1.012	for all
H–C	134.2	14.310	3.67	0.700	types
C–C	449.0	71.430	3.60	0.484	1.016

^aReference 6.

$$V_{ij}(r) = k_{ij} \cdot \left(\frac{A_{ij}}{(f \cdot r_{ij})^6} + B_{ij} \cdot \exp(\alpha_{ij} \cdot (f \cdot r_{ij})) \right), \quad (3)$$

where *ij* stands for the respective atom-pair (H–H, H–C, and C–C). *A*, *B*, and α are pair potential parameters given by Williams¹⁴ (referred as Williams⁷⁴) and *k* and *f* are scaling parameters. These parameters allow one to adjust the potential which may be necessary since Williams derived the potential parameters for the class of aromatic molecules not containing carbon–carbon triple bonds. It is obvious that $V_{ij}(r)$ represents the classical Born–Meyer potential for $k_{ij} = f = 1$. The values used for the lattice dynamical calculations are given in Table II. They follow the condition of systematic transferability $k_{ij} = \sqrt{k_{ii} \cdot k_{jj}}$. The electrostatic interaction had been taken into account by an additional potential term

$$V_{ij}^{\text{el}}(r) = \frac{n_i \cdot n_j \cdot q_0^2}{r_{ij}}. \quad (4)$$

Here n_i and n_j are the charges in units of the elementary charge q_0 . Values for the partial charges are obtained from the *ab initio* calculations for the isolated molecule, see above and Fig. 6.

For technical reasons the lattice dynamical program requires the pair potentials as a power series.²³ The use of four terms of the series allowed a very good description for interatomic distances above 2.2 (2.0) Å for C–C (H–H, C–H) interactions.

Beside the pair potentials the lattice dynamical program requires the crystal structure to calculate the interatomic distances. The recently measured low temperature crystal structure¹³ is used.

The molecule is modelled as a linear semirigid one used with negligible internal torsional restoring force. While the *ab initio* calculation supports this description the observed deformation of the molecule—the carbon-backbone is bent in the crystal by $\pm 1.5^\circ$ —means that there is a coupling between external and internal modes. An analysis shows, however, that the overall behavior in the regime of lattice modes is unchanged if the molecular bend is frozen or not.

The program allows one to apply an internal restoring force to the methyl libration. This manipulation influences almost only the two librational modes with antiphase rotation of the two methyl groups of the same molecule. The in-phase modes are not shifted in energy under this action. A weak internal methyl–methyl coupling of 0.001 mdyn/Å was chosen. Under the given assumptions the librational modes show energies of 4.2, 11.4, 20.0, 22.8 meV at the Γ -point.

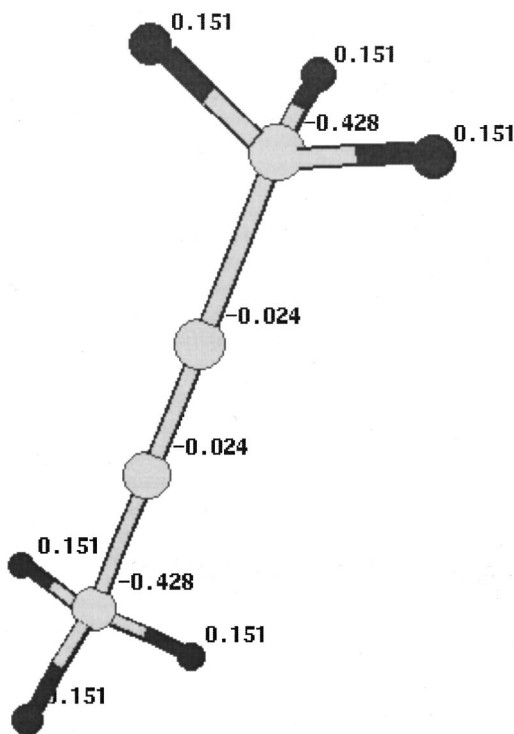


FIG. 6. Calculated charges in units of the elementary charge q_0 of the H and C atoms of DMA. The charges are derived *ab initio*, see text.

There is huge dispersion along the $[0,1,0]$ direction, little along $[1,0,0]$. In both these directions the dispersion curves look as if the unit cell would be a factor 2, too large. In $[0,0,1]$ direction the phonon branches flatten at the zone border yielding additional van Hove anomalies. Figure 7 shows the dispersion curve along the $[001]$ -direction. The four methyl groups in the unit cell require four modes with a librational character corresponding to an *in-phase* rotation of methyl groups inside a molecule and an *in-phase* rotation of the two molecules in the unit cell (*in-in*) and correspondingly *in-out*, *out-in*, and *out-out*. Figure 8 shows a view of the eigenvectors of the *out-out*-mode. Numerical results are summarized in Table III. They yield already a qualitative explanation of the multiline phonon spectrum of Fig. 2.

The lattice dynamical program contains all ingredients to calculate the neutron scattering function $S(Q, \omega)$ in the meV regime—or equivalently the DOS—as a weighted average of all excitations,

$$S(Q, \omega) \sim Q^2 \sum_i \sigma_i \sum_l \sum_j \langle u_{ijl}^2 \rangle \cdot DW(u) \cdot \delta(\omega - \omega_j(q_l)). \quad (5)$$

The summation runs again over all displacements u of $2 \cdot 10$ atoms i , the 14 modes j and a homogeneous grid of momentum transfers q_l of the Brillouin zone and includes the Debye–Waller factor $DW(u)$. The only difference to the spectrum of the internal modes, Eq. (2), consists of an additional summation l over the Brillouin zone required by phonon dispersion. Methyl librations are strongly anharmonic and show the largest mean square displacements. Further they invoke the proton with its dominant scattering cross section σ_i and causing the strongest peaks on the DOS. Fig-

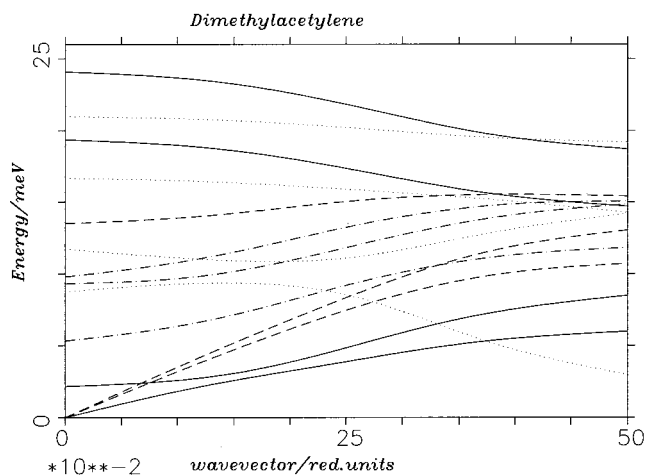


FIG. 7. Dispersion curve of DMA along the $[001]$ -direction. Pair potential parameters are taken from Williams'74 with the modifications according to Eq. (3) and Table II.

ure 9 shows the result of such a calculation. There is good agreement between the calculated (shaded) and measured (open dots) DOS although there are differences in the intensities of the peaks especially at ~ 6 meV and ~ 13 meV.

In Tili's work¹² it was the lack of knowledge of the low temperature crystal structure which allowed only a phenomenological access to the problem. The authors introduced a rotor–rotor coupling between neighboring methyl groups and therewith dispersion to explain two peaks of the DOS. Required parameters were chosen arbitrarily to fit the maxima at 12.9 and 17.7 meV of the measured DOS. This led to an average librational energy of E_{01} and a rotational single particle potential which is consistent with the observed tunnelling splitting, see Table IV.

C. Methyl rotational potentials

Besides the DOS, the rotational tunneling of the methyl group must be described by the chosen transferable pair potential, too. For this purpose a mean field rotational potential has to be calculated using the same pair interactions as for the lattice dynamics. A methyl group is rotated about the bond axis while all other atoms are fixed at their equilibrium positions. Adding up, for each CH_3 orientation, the pair interactions of the three methyl protons with all the other lattice atoms yields the potential energy of this configuration.

It contains an angle dependent part which can be identified as the mean field methyl rotational potential $V(\varphi)$. For further analysis the angle dependent potential energy of the crystal is described by Fourier expansion,

$$V(\varphi) = V_0 + \sum_{n=1}^2 \frac{V_{3n}}{2} (1 - \cos(3n\varphi + \varphi_n)). \quad (6)$$

The rotational potential has exactly threefold symmetry since the methyl group relaxes into identical equilibrium orientations after each $2\pi/3$ rotation. If one would rotate the CH_3 group as determined crystallographically with all the positional error bars as a rigid unit the proton sites would coincide only after 2π rotation. Thus when calculating $V(\varphi)$ we force the methyl protons to move on the common circle of

Mode(1, 1): 9 Emev= 11.3603 q= 0.000 0.000 0.000
Dimethylacetylene

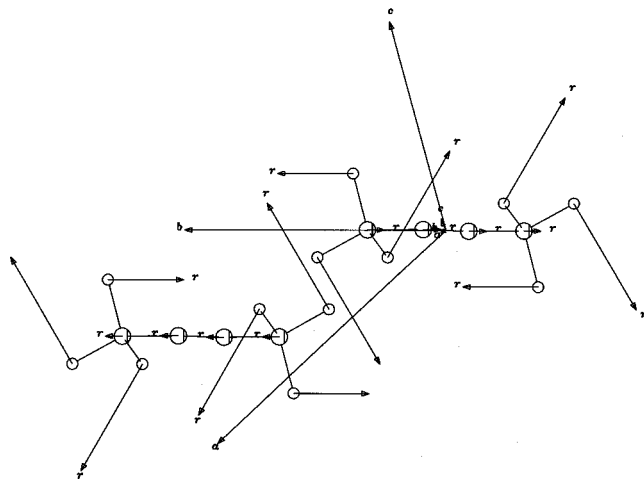


FIG. 8. Out-out eigenmode of energy 11.4 meV at the Γ point.

circumference between equilibrium positions of the two neighboring methyl protons. This procedure makes the protons coincide exactly after $2\pi/3$. The resulting potential is shown in Fig. 10 for $0^\circ \leq \varphi \leq 120^\circ$. The main contribution to $V(\varphi)$ stems from atoms within a radius of about 6 Å. Two features are visible in Fig. 10. At first, the potential minimum coincides well with the crystallographic orientation of the methyl group as required for a stable system. Secondly, the potential is exactly symmetric to the maximum. This is due to the presence of the a - c mirror plane intersecting the methyl group in the $C2/m$ space group. The potential has a minimum flatter than harmonic, a somewhat narrower large maximum indicating a contribution with sixfold symmetry and coinciding maxima of the two Fourier terms.

The potential determines the rotational excitations of the methyl group—tunneling, librations etc.—through the single particle Schrödinger equation of the one-dimensional three-fold rotor,

$$H = -B \frac{\partial^2}{\partial \varphi^2} + V(\varphi). \tag{7}$$

$B = 0.655$ meV is the rotational constant of the rotating methyl group about the rotation axis. The broadened minimum

TABLE III. Calculated libron energies according to Eq. (3) and Table II. The mode characters are described by the phase relation within one molecule and between the two molecules in the unit cell. For example “in-in” means, that all methyl groups rotate in phase.

q-point	Energy (meV)	Character
(0,0,0)	4.2	in-in
	11.4	out-out
	20.0	out-out
	22.8	in-in
(0,0,0.5)	4.9	in-in
	8.7	out-in
	18.0	in-in
	18.7	out-out

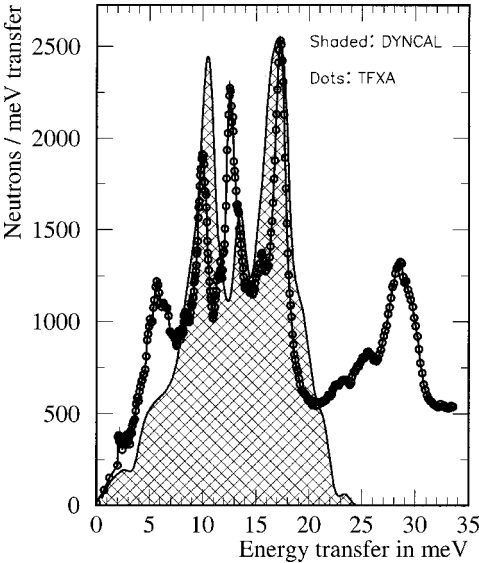


FIG. 9. Scattering function of DMA in the meV regime as calculated from the crystal structure using Williams’74 pair interaction parameters.

of the potential leads to lowering of the librational modes compared to a pure $\cos(3\varphi)$ potential. The calculated librational energy of $E_{01} = 14.16$ meV has no direct counterpart in the observed DOS but the calculated value of E_{01} can be interpreted as an average of the dispersive librational bands. The value is slightly lower than the experimental value of 15 meV derived by Kollmar and Alefeld¹¹ but still in good agreement. The tunnel frequency of $\hbar\omega_t = 1.45 \mu\text{eV}$ coincides within 17% with the observed tunnel splitting of $1.74 \mu\text{eV}$.¹⁰ The derived rotational potential is further confirmed by the quasielastic scattering experiment. The measured activation energy E_a differs from the calculated one by only 6%. Table IV shows the librational and tunnel energies together with the extracted potential parameters. The parameters of the fitted rotational potential are shown in the lowest line of the table.

An artificial increase of the size of the unit cell and a restriction to one molecule per unit cell allows one to simulate the case of the isolated molecule with the lattice dynamical program. In agreement with the GAUSSIAN 98 result the rotational potential is completely removed under these con-

TABLE IV. Comparison between observed energies and calculated ones (tunneling, libration, activation, and potential). Experimental values are boldfaced, calculated ones are italic.

$\hbar\omega_t$ (μeV)	E_{01} (meV)	V_3 (meV)	V_6 (meV)	E_a (meV)	Origin
1.74		45.0			Alefeld and Kollmar ^a
	15	45.0			Kollmar and Alefeld ^b
1.74	15.2	43.3	3.5		Tilli and Alefeld ^c
	6–17.3				Experiment, TFXA
				33.6	Experiment, FOCUS
1.45	14.16	50.5	–3.9	35.2	This work, calculation

^aReference 10.

^bReference 11.

^cReference 12.

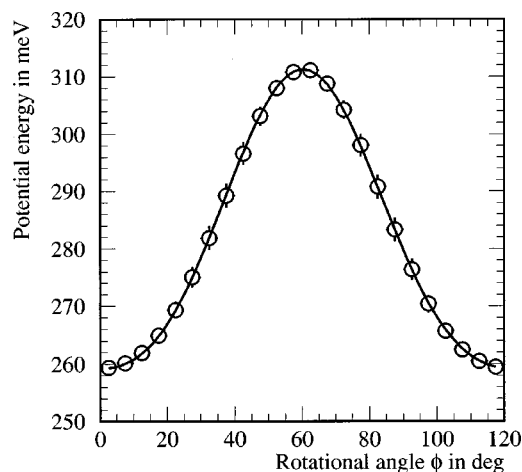


FIG. 10. Rotational potential of the methyl group based on Williams'74 pair potentials. The equilibrium orientation of the rotated CH_3 group in the crystal is well reproduced by the pair potentials used. $\phi = 0^\circ$ corresponds to the equilibrium position.

ditions and the methyl group of the isolated molecule in the lattice dynamical model represents a perfect free rotor.

The case of an isolated dimer can be studied in a similar way. Due to reduced symmetry there are two types of methyl groups in this case. The interesting one is the one with the short distance to the triple bond carbon atoms (the other is again close to a free rotor). Here the potential has reached already 40% of its final strength in the crystal but its minimum is out of phase by $\sim 60^\circ$ from the crystallographic equilibrium orientation. Only the phase-shifted superposition of interactions with all neighbors leads to consistency. The relatively weak rotational potential results from such compensation effects. An analysis of interatomic distances or the view along the molecular symmetry axis shows that the triple bond carbon belongs to the atoms nearest to the CH_3 group. Thus they give an important contribution to the rotational potential and tunneling probes especially among all others the hydrogen-carbon(3) atom-atom potential.

IV. CONCLUSION

For a long time it was impossible to merge rotational tunneling and librational peaks of the density of states within the single particle model. Based on the measured crystallographical structure the idea that rotor-rotor-coupling causes this discrepancy suggested by Tilli could be confirmed and elaborated. This shows that it may be misleading to identify a peak in the density of states with a single particle methyl librational excitation as it is done often. The analysis of the quasielastic spectra based on classical jump rotation yields the correct barrier height (activation energy E_a). Thus it may

be better to base an analysis on tunneling and quasielastic scattering instead of tunneling and misinterpretable raw data of the density of states.

The suspicion that DMA requires different pair potentials due to its triple bond carbon atoms was confirmed. Only a modified set of the Williams'74 pair potential parameters used reproduce successfully not only the density of states but also the rotational tunneling, mean librational energy and activation energy of the respective methyl group. Since the triple bond carbons belong to the nearest neighbors of the methyl protons this interaction is really tested with DMA. From this point the Williams parameters seem to be a good starting point to describe hydrocarbon systems which are not single or π bonded.

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