Upper limit for the cross section of the overlapping scalar resonances $f_0(980)$ and $a_0(980)$ produced in proton-proton collisions in the range of the reaction threshold

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Abstract. Utilizing a missing mass technique we investigate the $pp \to ppX$ reaction scanning beam energies in the range permitting to create a mass close to that of the $f_0(980)$ and $a_0(980)$ scalar resonances, but still below the $K^+K^-$ threshold where they decay dominantly into $\pi\pi$ and $\pi\eta$ mesons, respectively. Prior to the data analysis we introduce a notion of the close to threshold total cross section for broad resonances. We estimated for the overlapping mesons $a_0$ and $f_0$ the total cross section to be smaller than 430 nb at excess energy of $Q = 5$ MeV. The experiment have been performed at the Cooler Synchrotron COSY using the COSY-11 facility.

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1. Introduction

A study of the 1 GeV/$c^2$ mass range is motivated by the continuing discussion on the nature of the scalar resonances $f_0(980)$ and $a_0(980)$, which have been interpreted as exotic four quark states \cite{1}, conventional $qq$ states \cite{2,3} or molecular like $KK$ bound

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Within the framework of the Jülich meson exchange model for $\pi - \pi$ and $\pi - \eta$ scattering the $K\bar{K}$ interaction dominated by vector meson exchange gives rise to a $K\bar{K}$ bound state identified with the $f_0(980)$ in the isoscalar sector, while the isovector $a_0(980)$ is concluded to be a dynamically generated threshold effect [7, 8]. Both shape and absolute scale of $\pi\pi \to K\bar{K}$ transitions turn out to depend crucially on the $K\bar{K}$ interaction, which, in turn is prerequisite of a $K\bar{K}$ bound state interpretation of the $f_0(980)$. Although the $K\bar{K}$ decay mode of $f_0(980)$ and $a_0(980)$ is rather weak in comparison to the dominant $\pi\pi$ and $\pi\eta$ decay channels [9], even a new theoretical analysis based on the chiral approach cannot account for the $f_0(980)$ and $a_0(980)$ if the $K\bar{K}$ channel is not introduced additionally to the $\pi\pi$ and $\pi\eta$ interaction [10]. An analysis of the $\pi\pi$ and $KK$ interaction [11] showed that $f_0$ corresponds to poles of three Riemann-Sheets which appears physically as an object with a decay width of about 400 MeV and a narrow peak width of about 50 MeV. The same parameters of the $f_0$ were found by utilizing a unitarized quark model, according to which $f_0$ was interpreted as a $q\bar{q}$ state with a large admixture of $K\bar{K}$ virtual state [12].

In high energy experiments, the $f_0$ meson is observed as a resonance in the system of two pions produced in the variety of hadro-production reactions [16, 17, 18, 19] or in hadronic decays of heavier mesons [20, 21, 22] or the $Z^0$ boson [23, 24]. These experiments study invariant masses of the created neutral ($\pi^0\pi^0$) [16, 22, 18] and charged ($\pi^+\pi^-$) [21, 20, 23, 19, 17] pion pairs. Similarly, charged [25, 26] and neutral $a_0$ [27] mesons were observed as a clear signal in an invariant mass spectrum of the $\eta\pi$ system.

Complementary to these approaches, which studied the interaction of $\pi\pi$, $KK$, and $\pi\eta$ meson pairs, we investigate the possible manifestation of the mesons $f_0$ and/or $a_0$ as "doorway states" leading to meson production in proton-proton collisions, namely $pp \to ppf_0(a_0) \to pp$ Mesons. By measuring the missing mass with respect to the pp-system we study the $f_0 - a_0$ system as a genuine particle produced in the proton-proton collisions. In section 3 we report of the first experimental investigation, which concerns the close to threshold production of the broad neutral resonances via proton-proton collisions in the 1 GeV/c$^2$ mass range. Moreover, we have studied the $f_0$ and $a_0$ mass range below the $K\bar{K}$ threshold, where they can decay into non-strange mesons only.

It is obvious that for the excitation of a broad resonance the phrase "close to threshold" is not well defined and implies here that the beam momentum is such that masses just in the range of the resonance can be excited. This issue will be discussed in section 2.

In a recent publication [28] the COSY-11 collaboration presented data on the close-to-threshold $K^+K^-$ production following the proton-proton interaction at the excess energy of $Q = 17$ MeV. The obtained distribution of the missing mass to the p-p system is shown in figure [1] Monte-Carlo simulations demonstrate that the non-resonant $K^+K^-$ production (solid line) is hardly distinguishable from the resonant $pp \to ppf_0(980) \to ppK^+K^-$ reaction sequence (dashed line) [29]. In fact, the statistics of the data was not sufficient to favour one of the two processes. The issue whether there is a chance to distinguish between $K\bar{K}$ pairs originating from the...
decay of genuine $f_0/a_0$ resonance and those produced by strong $\pi\pi-K\bar{K}$ correlation is at present under theoretical investigation [8].

**Figure 1.** Experimental spectrum of the $K^+K^-$ invariant mass measured for the reaction $pp \rightarrow ppK^+K^-$ at a beam momentum of 3.356 GeV/c (data points). The width of the bins corresponds to the experimental resolution of the mass determination (FWHM $\approx 2$ MeV). Solid and dashed lines show Monte-Carlo simulations under the assumption of the direct and resonance production, correspondingly [29].

Since there exists no experimental information of the close to threshold total cross section for the production of the $f_0$ and $a_0^0$ mesons\[\parallel\], before the presentation of the COSY-11 measurement, we will estimate an expected order of magnitude for the considered values at the excess energy of $Q = 5$ MeV at which theoretical predictions for the $K^+K^-$ production are available [20]. The calculation, based upon the one-pion exchange model and the Breit-Wigner prescription for the $f_0$ resonance, shows that the production of a $K\bar{K}$ pair through the $f_0$ resonance ($pp \rightarrow ppf_0(980) \rightarrow ppK^+K^-$) contributes at $Q = 5$ MeV, with respect to the $K^+K^-$ threshold, by a factor of at least 20 less than the non-resonant creation. Extrapolating the measured cross sections of the $pp \rightarrow ppK^+K^-$ reaction [28, 31] to $Q = 5$ MeV one obtains the value of 0.08 nb. Thus combining the above information and additionally taking into account that the branching ratio of $f_0$ meson decay into $K^+K^-$ is about 2% [30], one expects that very close to threshold at $Q = 5$ MeV (with respect to the $ppK^+K^-$ final state) the $f_0$ meson should be produced with a cross section in the order of 0.08 nb $\ast 50 / 20 = 0.2$ nb. However, the branching ratio of $f_0$ decay into $K\bar{K}$ pairs is not well established [9] and may be much smaller than the above assumed value of 2%. Naively one would expect it to be very small, since due to the energy conservation only a few per cent of the resonance can decay into strange particles and moreover only a fraction of that part will decay into a $K^+K^-$ pair.

In case of the $NN \rightarrow NN\,a_0$ reaction the total cross section was estimated using an effective Lagrangian approach taking into account the one-pion exchange mechanism and the production via t-channel exchanges with $\pi\eta$ and $\pi f_1$ mesons [32]. The assumption of the positive interference between s- and u-channel of the one-pion exchange results in the value of about 20 nb at $Q = 5$ MeV, however, an exchange of heavier mesons was not taken into account. In addition it should be noted that a different choice of coupling constants and cut-off parameter $\Lambda_{\pi NN}$ would easily change the expected cross section by a factor of five in either direction.

\[\parallel\] Recently the ANKE collaboration reported results on the close to threshold production of the $a_0^+$ meson via the $pp \rightarrow dK^+K^0$ reaction [42, 43]
The above appraisement indicates that at a few MeV above the production threshold a total cross section for the $pp \rightarrow pp\alpha_0(f_0)$ reactions is expected to be in the order of 1 nb to 100 nb.

2. Definition of the close-to-threshold total cross section for a broad resonance

The study of short-living (broad) particles in the $pp \rightarrow ppX$ reaction requires special care \[34\] when the energy in the center of mass is close to the sum of the masses of the two protons and the average mass of the meson. As already mentioned due to the broad mass distribution of such particles the notion of the reaction threshold is not well defined. It is naturally a matter of scale whether a given resonance is considered as a broad one. Experimentally, by a broad resonance we define a particle with its full width $\Gamma$ at half maximum of the mass distribution (spectral function) being much larger than the experimental accuracy of the mass determination, or with a width such broad that the acceptance of the detection system changes significantly over the resonance mass range. Both criteria apply for the measurements performed and discussed in the present contribution.

In the following we will propose a definition of the total cross section as a function of the excess energy $Q = \sqrt{s} - 2m_p - m_X$, which is valid also when $Q$ is small compared to the width $\Gamma$ of the produced meson.

\begin{figure}[h]
\centering
\includegraphics[width=0.8\textwidth]{figure2.png}
\caption{(a) Breit-Wigner distribution with a mean value of $m_0 = 980$ MeV/$c^2$ and a width $\Gamma = 70$ MeV/$c^2$. If the measurement would be performed with the $\sqrt{s}$ as depicted by the dashed line then the mass $m$ would be measured with the centre-of-mass excess energy equal to $Q$. (b) Simulations: Horizontal axis denotes the mass of the produced system $X$ via the $pp \rightarrow ppX$ reaction. Long–dashed line denotes a fraction of the Breit-Wigner distribution, as shown in figure (a). Thin–solid line represents the efficiency of the COSY-11 detection system for the simultaneous detection of the two outgoing protons from the $pp \rightarrow ppX$ reaction. Short–dashed line shows the decrease of the phase space volume with the increase of the created mass. The phase space volume was weighted by the proton-proton FSI enhancement factor taken from reference [34]. The thick–solid line results as a convolution of the above described distributions.}
\end{figure}
Performing the measurement with the total centre-of-mass energy $\sqrt{s}$ close to the sum of the average mass of the particles in the exit channel, different mass ranges of the broad particle are populated with different excess energies: $Q(m) = \sqrt{s} - (2m_p + m)$ (see figure 2a). This implies that the observed mass distribution appears to be different from the one which would be determined at an excess energy much larger than the width of the broad meson. Neglecting dynamical effects, in case of large $\sqrt{s}$ the mass distribution can be roughly approximated by the Breit-Wigner function, as shown in figure 2a.

The measurements of the $pp \rightarrow ppX$ reactions, reported here, have been performed by means of the COSY-11 detection system [35]. The thick solid line in figure 2b shows the expected missing mass distribution simulated for the total centre-of-mass energy $\sqrt{s}$ equivalent to a maximal produced mass ($\sqrt{s} - 2m_p$) smaller than the average mass of the simulated meson. The shape of this curve results from convoluting the meson spectral density (long-dashed line) with both (i) the decrease of the phase space volume with decreasing excess energy $Q$ weighted by the proton-proton FSI enhancement factor (short–dashed line) and with (ii) the efficiency of the COSY-11 detection system for the simultaneous registration of the two outgoing protons from the $pp \rightarrow ppX$ reaction (thin solid line).

The number of observed events per mass bin $\frac{dN}{dm}$ can be written as:

$$\frac{dN}{dm}(m, Q) = \frac{d\sigma}{dm}(m, Q) \cdot L \cdot E_{ff}(Q),$$  

with $L$ and $E_{ff}$ denoting the integrated luminosity and the efficiency of the COSY-11 detection system, respectively. As proven by extensive Monte-Carlo simulations, the COSY-11 efficiency is in a good approximation independent of the produced mass and depends on the excess energy $Q$ only. The cross section $\frac{d\sigma}{dm}$ for the creation of a mass $m$ is expressed by:

$$\frac{d\sigma}{dm}(m, Q) = |M(Q)|^2 \cdot V_{ps}(Q) \cdot FSI_{pp}(Q) \cdot SD(m, m_0, \Gamma),$$

$$\frac{d\sigma}{dm}(m, Q) = \sigma_{primary}(Q) \cdot SD(m, m_0, \Gamma),$$

where $M(Q)$ stands for the matrix element accounting for the production mechanism, and the last term $SD$ denotes the spectral density of the produced meson with the average mass and width equal to $m_0$ and $\Gamma$, respectively. The $V_{ps}(Q)$ and $FSI_{pp}(Q)$ represent the phase space volume available to the outgoing particles and the proton-proton FSI enhancement factor, respectively [36]. The term $\sigma_{primary}(Q)$ combines all excess energy dependent factors and could be referred to as a primary production cross section of producing a mass bin of the resonance which is by a value of $Q$ smaller than the maximum kinematically available mass. It should be noted that all factors in equations 1 and 2 depend on the excess energy $Q$ only, except the spectral density which is a function of the created mass $m$. This means that the number of events per mass bin can be expressed as follows:

$$\frac{dN}{dm}(m = \sqrt{s} - 2m_p - Q) = \text{const.}(Q) \cdot SD(m, m_0, \Gamma).$$

Scanning the resonance experimentally by changing the value of $\sqrt{s} = 2m_p + m + Q$ and keeping in the analysis a constant value of $Q$ allows to reproduce the mass distribution of the created meson, even without knowing exactly the energy dependence of the
detection efficiency and other factors. Note that if $\sqrt{s} - 2m_p$ is within the range of the broad resonance (see figure 2a) then not all parts of the resonance can be created. Thus, it is not trivial from such a single measurement how to extract the total cross section. However, by scanning the resonance with different values of $\sqrt{s} - 2m_p$ one can define the total cross section at a given excess energy $Q$ as an integral over the whole resonance region of the differential cross section $d\sigma/dm(m, Q)$ keeping in the integration $Q$ as a constant, thus:

$$\sigma(Q) = \int_{2m_p}^{\infty} d\sigma/dm(m = \sqrt{s} - 2m_p - Q, Q) \, d\sqrt{s}$$  \hspace{1cm} (5)$$

Please note that if the spectral density function is normalized to unity than $\sigma(Q)$ is directly equal to the primary cross section $\sigma_{primary}(Q)$. This can be inferred by substituting equation 3 in equation 5.

Assuming that similar to the production process for pseudoscalar mesons the value of $|M|^2$ will be constant with small values of $Q$ \cite{36, 37}, one expects that the energy dependence of $\sigma(Q)$ from equation (5) will be determined by the $Q$-dependence of the phase space and the dominant proton-proton FSI.

3. Measurement of the $pp \rightarrow ppX$ reaction close-to-threshold for the production of $f_0$ and $a_0$ mesons

In the following we will present the analysis of the measurements which were primordially devoted to production studies of the $\eta'$ meson in proton-proton collisions \cite{38}. The experiment was performed at seven different beam momenta (listed further down in table 1). The maximum mass ($\sqrt{s} - 2m_p$) available in these experiments covered a range from 959.6 MeV/c$^2$ to 981.4 MeV/c$^2$. This is the region below and close to the average mass of the $f_0(980)$ and $a_0(980)$ masses, and hence the signal from the production of these mesons should indeed influence the overall observed missing mass spectra. Figure 3 presents one of the missing mass distributions extracted from the experimental data taken at a total centre-of-mass energy equivalent to the maximum created mass of $M = 972$ MeV/c$^2$.

Certainly the shape of the “background” below the clear $\eta'$ peak differs from the shape of the missing mass distribution simulated for the Breit-Wigner like resonance shown as a thick solid line in figure 2b. This is due to the fact that the experimental missing mass spectrum comprises also contributions from non-resonant multi-pion, $\pi\eta$ and $\pi\omega$ production. Thus, taking also into account the well known yield originating from the $\eta'$ production, one can generally extend equation (4) to:

$$dN/dm(m, Q) = \text{const.}(Q) \cdot SD(m, m_0, \Gamma) + dN/dm(\text{multi} - \pi, \pi\eta, \pi\omega, \sqrt{s}) + dN/dm(\eta', \sqrt{s}).$$  \hspace{1cm} (6)$$

A mass bin corresponding to $Q = 5$ MeV $\pm$ $\Delta$ $Q$ with $\Delta$ $Q = 5$ MeV was chosen in the analysis for each of the seven measurements under investigation (see as an example the shaded area in figure 3). The number of events per this mass bin has been calculated for seven measurements and after the correction for the detection efficiency has been normalized to the corresponding integrated luminosity:

$$\Delta N(\sqrt{s}) = \frac{1}{L} \int_{Q=0 \text{ MeV}}^{Q=10 \text{ MeV}} \int_{m=0 \text{ MeV}}^{m=Q-2m_p} \frac{1}{E_{eff}(Q)} \frac{dN}{dm} \, dm$$

$$= \int_{Q=0 \text{ MeV}}^{Q=10 \text{ MeV}} \sigma_{primary} \cdot SD(\sqrt{s} - 2m_p - Q, m_0, \Gamma) \, dm +$$
\[
+ \int_{Q=0}^{Q=10 \text{ MeV}} \left( \frac{d\sigma}{dm}(\text{multi} - \pi, \pi\eta, \pi\omega, \sqrt{s}) + \frac{d\sigma}{dm}(\eta', \sqrt{s}) \right) \, dm
\]

**Figure 3.** Experiment: Missing mass distribution determined for the \( pp \rightarrow ppX \) reaction at 14 MeV excess energy above the threshold for the \( \eta' \) meson production \cite{38}. The peak at 958 MeV/c\(^2\) corresponds to the production of the \( \eta' \) meson. The shaded area denotes the part of the spectrum used in the present analysis.

**Figure 4.** Simulations: Missing mass distributions for the reactions \( pp \rightarrow pp2\pi \) (dashed line) and \( pp \rightarrow pp3\pi \) (solid line). Please note, that the shape of these spectra differ from each other and both are different from the missing mass distribution shown in figure 3b. Simulated distributions for the case of the direct \( 2\pi \) and \( 3\pi \) creation are shown in figure 4. One can observe that their shapes differ (i) from each other and (ii) again from the one determined experimentally. The latter discrepancy can be attributed at least qualitatively to contributions of the productions of the \( f_0(980) \) and/or \( a_0(980) \) mesons to the experimental spectrum.
Subsequently, if necessary, the well known values of \( \frac{d\sigma}{dm}(\eta', \sqrt{s}) \) were subtracted from the above defined \( \Delta N(\sqrt{s}) \):

\[
\Delta N'(\sqrt{s}) = \Delta N(\sqrt{s}) - \int_{Q=0 \text{ MeV}}^{Q=10 \text{ MeV}} \frac{d\sigma}{dm}(\eta', \sqrt{s}) \, dm \quad (8)
\]

Further, in order to account for the contribution from the multi-pion, \( \pi\eta \) and \( \pi\omega \) production we subtracted from each \( \Delta N'(\sqrt{s}) \) the value determined for the lowest measured energy. The result is shown in figure 5a, where the variable \( \Delta \) at the vertical axis reads:

\[
\Delta = \Delta N'(\sqrt{s}) - \Delta N'(\sqrt{s}_{\text{lowest}}) = 2 \cdot m_p + 959.6 \text{ MeV} \quad (9)
\]

On the other hand, assuming changes of the cross section for the non-resonant multi-pion \( \pi\eta \) and \( \pi\omega \) production to be negligible the value of \( \Delta \) can be expressed as follows:

\[
\Delta = \sigma_{\text{primary}} \int_{Q=0 \text{ MeV}}^{Q=10 \text{ MeV}} SD(m, \sqrt{s} - 2m_p - Q, \Gamma) \, dm - \sigma_{\text{primary}} \int_{Q=0 \text{ MeV}}^{Q=10 \text{ MeV}} SD(m, \sqrt{s}_{\text{lowest}} - 2m_p - Q, \Gamma) \, dm \quad (10)
\]

Values determined for \( \Delta \) are given in table 1 and also shown in figure 5a.

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**Figure 5.** (a) Points denote number of events, measured for the 10 MeV upper bin of the missing mass spectrum for the \( pp \to ppX \) reaction, as depicted by the shaded area in figure 3, normalized to the integrated luminosity. The value obtained at 959.6 MeV/c² was subtracted from each point. The x-axis denotes the mass corresponding to \( Q = 5 \) MeV. For example the point corresponding to the spectrum of figure 3 (\( \sqrt{s} - 2m_p = 972 \) MeV) is plotted at a mass value of 967 MeV/c². Lines show the result of simulations of the \( pp \to ppX \) reaction, with X being the Breit-Wigner type meson resonance of the following parameters: (dotted line) mass 990 MeV/c², width 65 MeV/c², and \( \sigma_{\text{primary}} = 750 \) nb, (solid line) mass 970 MeV/c², width 40 MeV/c², and \( \sigma_{\text{primary}} = 400 \) nb, (dashed line) mass 970 MeV/c², width 65 MeV/c², and \( \sigma_{\text{primary}} = 1200 \) nb. (b) \( \pi^+\pi^- \) event distribution in the \( J/\Psi \to \phi\pi^+\pi^- \) decay around the \( f_0 \) mass. Data were taken by DM2 [39] and MARK-III [40] collaborations. Solid line depicts the result of the calculations of reference [41].
The curves in this figure represent calculations performed according to equation 10 approximating the spectral function \( \text{SD}(m, m_0, \Gamma) \) by the Breit-Wigner distribution. The obtained result demonstrates that the data are sensitive to the average mass of the created meson or mesons but rather non-sensitive to the width of an assumed Breit-Wigner structure. The latest volume of the Review of Particle Physics [9] shows that the parameters for \( f_0(980) \) and \( a_0(980) \) mesons are very similar to each other:

- \( f_0(980) \): \( m = 980 \pm 10 \text{ MeV}, \quad \Gamma = 40 \text{ to } 100 \text{ MeV} \)
- \( a_0(980) \): \( m = 984.7 \pm 1.2 \text{ MeV}, \quad \Gamma = 50 \text{ to } 100 \text{ MeV} \)

and therefore we cannot distinguish between these two resonances in a missing mass analysis from the proton–proton interaction.

**Figure 6.** \( \chi^2 \) as a function of the total cross section. Number of degrees of freedom is equal to 3.

**Table 1.** Result of the analysis of the \( pp \rightarrow ppX \) reaction measured at COSY-11; \( \Delta \) is defined in equation 10

<table>
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<th>Beam momentum [MeV/c]</th>
<th>mass of X [MeV/(c^2)]</th>
<th>( \Delta ) [MeV]</th>
<th>error((\Delta)) [MeV]</th>
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<td>15.1</td>
<td>4.9</td>
</tr>
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</table>

A fit to the resonance–like structure of figure 5 results in values of:

\( m_0 = 969 \pm 3 \text{ MeV} \) and \( \sigma_{\text{primary}} = 430^{+2070}_{-100} \text{ nb} \) and is nearly identical to the solid line in figure 5. The quality of the fit can be estimated from the \( \chi^2 \) distribution shown in figure 6. It is worth to note, that the obtained structure is in line with the measurements of the \( \pi^+\pi^- \) invariant mass distribution of the \( J/\Psi \) decay into \( \phi\pi^+\pi^- \) system as shown in Figure 5b. It is rather well justified that the the total cross section of multi-pion and \( \pi\eta \) changes only insignificantly over the studied 22 MeV excess energy range since the present measurements were performed some 560 MeV and 300 MeV above the \( 3\pi \) and \( \pi\eta \) thresholds. Still, it cannot be excluded that the variations of \( \Delta \) are due to the growth of an unknown cross section for \( \pi\omega \) production since in this case the excess energy change from 42 to 64 MeV. Therefore the determined value of the total cross sections for \( a_0/f_0 \) resonances can only be treated as an upper limit.

### 4. Conclusion

For the example of the production of the \( f_0(980) \) and/or \( a_0(980) \) mesons we discuss the notion of the reaction threshold in case of broad resonances where the available phase space volume for a given mass bin changes significantly. Ansatz of equation 10 leads to a simple definition of the differential - and total cross section also in the case of the close-to-threshold production of a broad resonance.
The performed measurements of the $pp \rightarrow ppX$ reaction at seven beam momenta close to the threshold of $f_0$ and $a_0$ mesons revealed an enhancement in the missing mass spectrum. If the observed structure were due to the production of the object possessing a Breit-Wigner form its total cross section introduced in equation [4] would be equal to about 430 nb at excess energy of $Q = 5$ MeV. However, due to the unknown influence of the $\pi\omega$ production we can treat this value only as an estimation of an upper limit for the production of $f_0$ and $a_0$ meson via the $pp \rightarrow ppX$ reaction. Here we would like to stress that this is the first experimental investigation utilizing a missing mass techniques of the production of these scalar resonances close to the kinematical threshold. The determined upper limit of the total cross section is much larger than expected from existing theoretical estimations, which however take into account only a part of the possible production mechanisms. In case of $f_0$, for example, one could consider also a production via an excitation of baryonic resonances. PDG [9] reports a few $N^*$ resonances around 1700 MeV with widths of 50-250 MeV, which decay predominantly into the $N\pi\pi$ channel.

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