Fast Decision in Favor of the Slow Fission Process

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The fission probability $P_f$ of highly excited targetlike nuclei produced in reactions of 2.5 GeV protons on Au, Bi, and U was studied as a function of excitation energy $E^*$ whereby $E^*$ is deduced eventwise from the multiplicity of evaporated light particles. At the highest $E^*$ of 1000 MeV $P_f$ amounts to $\approx 30\%$ with all 3 target nuclei irrespective of the initial fissility. Statistical-model calculations satisfactorily reproduce the observed evolution of $P_f$ with $E^*$—provided that no extra transient delay is introduced. Fission thus is decided upon very fast and early in the long deexcitation chain towards scission which comprises as much as $\approx 80\%$ of all evaporated alpha particles.

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At low excitation energy nuclear fission is strongly influenced by nuclear shell effects, resulting, for instance, for U in the well known binary split into two mass asymmetric fission fragments. With increasing excitation these nuclear structure effects are washed out, and macroscopic properties such as nuclear dissipation dominate the collective flow of nuclear matter from the equilibrium deformation via the saddle towards scission into two fragments of about equal size. The overall time elapsed from the equilibrium deformation up to scission is found to be a few times $10^{-20}$ s. This time is quite long compared to other processes such as the emission of neutrons which is 10 to 100 times faster. This observation has led to the notion of fission being a slow process [1].

Since the magnitude of nuclear dissipation is most likely deformation dependent [2], the characteristic time governing the flow over the saddle point, where the decision about fission is made, might be considerably shorter than the one close to the scission point. In particular, at high excitation energies, where the emission times of light charged particles are very short, a long transient delay for fission at the saddle point would strongly favor the emission of charged particles, thus reducing the fissility and, consequently, second- and higher-chance fission probabilities. Conversely, low dissipation at the saddle or a minimum transient delay tends to keep fission competitive with particle evaporation even at high excitation. In other words, although the entire fission process is slow, the decision to fission can be fast.

We have chosen 2.5 GeV proton-induced reactions to excite three target nuclei, Au, Bi, and U with different fissilities $Z^2/A = 31.7$, 33.0, and 35.6, respectively, in order to study the evolution of the inelastic reaction, $\sigma_{inel}$, and the fission cross section, $\sigma_f$, as a function of excitation energy, $E^*$, and fissility. Their ratio, the fission probability $P_f(E^*) = \sigma_f(E^*)/\sigma_{inel}(E^*)$, provides the best possible evidence for the presence of dissipative or transient effects in fission. The selected reactions, similar to antiproton [3,4] or peripheral relativistic heavy-ion reactions [5,6], are thought to deposit high thermal excitation with minimum ballistic from collective excitations (angular momentum, shape distortions, or compression) which could have a detrimental influence on the decay.

The maximum $E^*$ reached in the present investigation is only about 4–5 MeV/nucleon or $\approx 1000$ MeV, as will be shown below. This excitation is well below that reported for the onset of multifragmentation [7], the decay of a hot nucleus into multiple clusters and nucleons. Thus the two main reaction channels expected are spallation induced fission and evaporation, the latter process leading to the survival of a heavy targetlike residue (HR) plus many evaporated neutrons and light charged particles (LCPs).

The amount of energy dissipated into excitation is deduced event by event from the total number of evaporated light particles ($n$, H, He), a well proven technique, the details of which are described in [8,9]. It presupposes a 4$\pi$ coverage and high acceptance at high granularity of the detectors, requirements fulfilled by the combination of our two detectors, the Berlin Neutron Ball (BNB) and the Berlin Silicon Ball (BSiB). BNB is a large spherical tank with 1500 l of Gd-loaded scintillator liquid, which in its central reaction chamber houses the BSiB, a self-supporting shell of 151 individual Si detectors. These Si detectors provide a total geometrical acceptance of about 80$\%$ of their energy thresholds as low as 2 MeV.

The experiment was performed at the COSY accelerator in Jülich with targets of Au ($2 \times 324$ µg/cm$^2$), Bi (629 µg/cm$^2$), and UF$_6$ (725 µg/cm$^2$) + C (36 µg/cm$^2$). The hardware threshold of BNB was adjusted to detect all reactions with an inelasticity larger than 3 MeV. The high ($\approx 85\%$) detection efficiency of BNB for slow neutrons and the low ($\approx 15\%$) efficiency for energetic ($\approx 100$ MeV)
ones makes BNB sensitive rather to evaporative neutrons than to fast ones from the direct interaction of the incident proton with the target nucleus. In BSIB the identification of LCPs and the reconstruction of the mass of heavier fragments, i.e., of intermediate-mass fragments (IMFs), fission fragments (FFs), and HRs, are based on the measurement of time of flight and energy.

While the excitation energy, $E^*$, can be deduced from the experiment, the $A$ and $Z$ content of the excited nucleus after the fast intranuclear cascade (INC) is accessible from INC calculations only. Since the knowledge of $A$ and $Z$ is necessary for the calculation of $P_f$, the reliability of the employed INC model needs to be ascertained by comparing calculated inclusive $E^*$ distributions with the data. Such a comparison is made in Fig. 1 exhibiting, indeed, a good agreement for the three target nuclei between experiment and the simulation with the INC2.0 model from Cugnon [10]. We conclude that also the $A, Z$ population is correctly described by the model.

The mass resolution in BSIB is relatively poor, in particular, for the heavier fragments, chiefly due to the short flight path of only 10 cm. Setting limits on the total mass of all detected reaction products, $A_{\text{tot}}$, and on the mass of the heaviest, $A_1$, and second heaviest particle, $A_2$, allows one to separate the three major fragmentation products HRs, FFs, and IMFs, as is illustrated in Fig. 2(a). It exhibits, for the case of Bi as an example, the correlation between $A_1, A_2$ data have been symmetrized. Here, the events with both FFs detected are centered in the middle at $A_1, A_2 = 80$. Events with a HR detected together with some lighter masses appear close to the x and y axes near $A_1, A_2 = 150$, while most of the events with only one FF and some lighter masses detected are suppressed by the requirement $A_{\text{tot}} > 70\%$ of $A_{\text{targ}}$. Also, as expected, there are hardly any multifragmentation events, which would populate the lower left corner of the plot with $A_1, A_2 \leq 30$. In order to separate events with two FFs detected from HR events we use the further condition $A_1, A_2 > 32$ indicated by the dashed lines.

The two other panels in Fig. 2 are meant to demonstrate that fission events selected according to the above criteria also fulfill the more conventional conditions on the total kinetic energy (TKE) and the folding angle between the FFs. Indeed, Fig. 2(b) shows that these events are grouped around the solid line calculated with the Viola formula (TKE) = 0.1189 $Z^2/A^{1/3}$ + 7.3 MeV [11] with $Z = 0.45(A_1 + A_2)$, whereas they lie somewhat above the dashed line with $Z$ values chosen according to the $\beta$ stability—in agreement with other investigations [12]. As to the folding angle distribution plotted in Fig. 2(c), we witness a growing broadening and deviation from 180° with increasing $E^*$ as the result of more and more numerous emission of lighter particles and increasing momentum transfer. Because of this strong evolution with $E^*$, we refrained from choosing a limiting folding angle.

Once the FFs have been selected with the two conditions $A_{\text{tot}} > 70\%$ of $A_{\text{targ}}$ and $A_1 \geq A_2 > 30, 32, \text{ and } 35$ for Au, Bi, and U, respectively, their yield is corrected for detection efficiency as described in Ref. [9] to give $\sigma_f(E^*)$, shown in Fig. 1 as a function of $E^*$. The total fission cross sections deduced amount to $\sigma_f = 200 \pm 60$ mb, $320 \pm 50$ mb, and $1350 \pm 120$ mb for Au, Bi, and U, respectively, in reasonable agreement with previous measurements [13]. The fission probability is then obtained directly as the ratio $P_f(E^*) = \sigma_f(E^*)/\sigma_{\text{inel}}(E^*)$. The evolution of $P_f$ with $E^*$ is shown in Fig. 3 for Au (○), Bi (●), and U (▼).

The figure shows that the evolution of $P_f(E^*)$ with $E^*$ is quite different for the three targets. At the low excitation of about 150 MeV, the fission probability of a U-like nucleus is close to 90%, while for the less fissile Bi-like nucleus it is 25% and only 5% for Au-like nuclei. At such low $E^*$, the excited nuclei are still similar in $A$ and $Z$ to the target nucleus since only a few nucleons are removed during the INC stage, and the different behavior of $P_f(E^*)$ is still dominated by the different initial fissility. At higher $E^*$, considerably more nucleons are emitted during the INC (at

![FIG. 1. Measured inelastic or inclusive (○) and fission (▲) differential cross sections $d\sigma/dE^*$ as a function of $E^*$ for $p(2.5 \text{ GeV}) + U, Bi, \text{ and } Au$. The histograms show the result of INC2.0 [10] calculations of the inclusive cross sections.](image)

![FIG. 2. Logarithmic contour plots used for the selection of fission fragments from the reaction $p + Bi$. (a) Correlation between the two heaviest fragments $A_1$ and $A_2$, (b) Total kinetic energy (TKE) of the two FFs as a function of their sum mass $A_1 + A_2$, (c) Distributions of the folding angle $\theta_{\text{fold}}$ between the FFs (in arbitrary units/rad) as a function of $E^*$.](image)
\[ E^* = 1000 \text{ MeV} \] about \( \Delta A = 12 \) mass and \( \Delta Z = 4-5 \) charge units according to the INCL2.0 model [10], very similar for Au, Bi, and U. Consequently, the fissionality of the thus produced nuclei is considerably lowered. This results in a strong decline of \( P_f(E^*) \) in the case of U from the high value of about 90\% at 150 MeV down to 35\% at 900 MeV, while for the Au target a continuous increase of \( P_f(E^*) \) with \( E^* \) is observed. For the Bi target one notices an intermediate behavior, with an almost constant value of about 25\% between 200 and 600 MeV, followed by a further increase to 30\%. Obviously, in the flat region of \( P_f(E^*) \) for Bi the loss in fissility from the A, Z depopulation is compensated by an enhancement of fission due to the increase of \( E^* \), while from then on the effect of an increasing \( E^* \) dominates.

Despite the large differences in fissionality and fission barriers \( B_t = 5, 12, \) and 21 MeV (finite-range fission barriers [14] used in the calculations discussed below) of the initial nuclei U, Bi, and Au, respectively, one observes that \( P_f(E^*) \) assumes the same value of about 30\% for all three target nuclei at the highest excitations.

After this empirical discussion we confront now the observed evolution of \( P_f \) with \( E^* \) with statistical-model calculations applying the transition-state model to fission. To this purpose we have used the population of nuclei as a function of \( E^* \) predicted by the INCL2.0 code [10] as input to the statistical-model code GEMINI by Charity et al. [15]. The angular momentum imparted during the INC (up to 20 units of \( h \) at the highest \( E^* \)) is likewise taken into account. For the level density parameters we assumed \( a_n = (A/10) \text{ MeV}^{-1} \) and for their ratio at the transition state and at ground state deformation \( a_i/a_n = 1.000, 1.017, \) and 1.022 for U, Bi, and Au, respectively. For U and Au these values are the same as in [3], while for Bi we have chosen an intermediate value. No extra transient time for fission is applied. The result of these calculations is shown in Fig. 3 for the three targets by the dashed (U), dotted (Bi), and solid (Au) histograms. It is obvious that the calculations reproduce the characteristically different trends in \( P_f \) at lower \( E^* \), as well as the almost equal \( P_f \) at the highest \( E^* \) nearly quantitatively, and, most importantly, they do so without the use of any additional transient time.

What can be learned from this agreement for the understanding of fission? From the calculations we can identify the range of multiple-chance fission steps or the range in excitation energy \( E^*_\text{fis} \) when fission is decided upon. At \( E^* = 800 \text{ MeV} \) of initial excitation, for example, fission occurs at a mean excitation energy of \( \langle E^*_\text{fis} \rangle = 700 \text{ MeV} \) for Au and Bi with a width of \( \sigma_{E^*_\text{fis}} = 110 \text{ MeV} \), while for U the corresponding values are 600 and 180 MeV. This implies that fission occurs rather early in the long deexcitation chain at these high initial excitation energies. For U, because of its lower fission barriers, fission is spread over a larger range of deexcitation steps and thus comes on average on a lower energy \( \langle E^*_\text{fis} \rangle \).

These conclusions are at variance with the findings of Jurado et al. [6] reporting a maximum excitation energy for the decision to fission of less than 300 MeV in the reaction U (1A GeV) on (CH2)\_n. Also, Benlliure et al. [5] concluded from a similar inverse-kinematics experiment [Au (0.8A GeV) + p] on a mean energy for fission of \( \langle E^*_\text{fis} \rangle = 128 \pm 20 \text{ MeV} \) for Au-like nuclei. These relatively low excitation energies were accounted for [5,6] in the calculations by a dynamical fission hindrance or a transient time of \( \tau_d = 2 \times 10^{-21} \frac{\text{s}}{} \), which suppresses fission at higher \( E^* \), and the resulting losses in \( \sigma_i \) were then compensated for by a relatively large value of the level density at saddle of \( a_i/a_n = 1.05 \).

In order to confront our data with these parameters, we show the thus calculated fission probability \( P_f(E^*) \) for Au, as an example, by the dot-dashed line in Fig. 3. Clearly, this calculation fails to describe the actual Au fission data. It also fails in the case of Bi and U fission. This example also demonstrates the decisive advantage of the differential observation of \( dP_f(E^*)/dE^* \) over other methods [5,6] in that it allows an independent determination of \( a_i/a_n \) and \( \tau_d \), \( a_i/a_n \) accounts for the rise of \( P_f \) at low \( E^* \leq 200 \text{ MeV} \), while \( \tau_d \) becomes all the more effective the higher \( E^* \) is in excess of \( \approx 300 \text{ MeV} \), i.e., the range which is fully covered with the present incident energy of 2.5 GeV, but much less so at 0.8 or 1 GeV [5,6].

The reason for the significant deviation of the present conclusions from those reported in Refs. [5,6] is not due to different model calculations. The INC/statistical-model calculations agree quite well when fed with the same parameters. Rather, the discard arises from the experiment. Since it is hardly possible to determine \( E^* \) in inverse kinematics directly from the number of evaporated particles, \( E^* \) is, instead, deduced [5,6] from the FFs’ charges \( Z_{1,2} \) and their distributions. There are, however, question-
FIG. 4. Energy spectra of α particles that are emitted into 3 angular domains relative to the motion of the light fission fragment: $\Theta_{\alpha-LF} = 10^\circ$ to $40^\circ$, $70^\circ$ to $100^\circ$, and $140^\circ$ to $170^\circ$. Three calculated components are fitted to the experimental distribution (circles): the contribution from the compound nucleus prior to scission (thick continuous lines) and from the light (dashed lines) and the heavy (dotted lines) fission fragment. At $70^\circ$ to $100^\circ$ a further component for the neck emission is added (thin line). The total calculated spectrum is shown by the histogram. Example from 2.5 GeV $p + Au$ at $E^* = 600–900$ MeV.

able assumptions and uncertain parameters involved in this delicate relation between $Z_{1,2}$ and $E^*$ that shed serious doubts on the precision of the thus deduced $E^*$ required for a convincing conclusion about $\tau_d$.

The first part of the present investigation has shown that fission is initiated on a fast time scale and, hence, at high excitation. If this conclusion is correct, the large amount of remaining excitation must be carried off, either during the descent from saddle to scission or after scission. Indeed, the correctly calculated components are fitted to the experimental distribution (histograms) provides a good approximation at least to the lower-energy ($E_\alpha \leq 35$ MeV) part, i.e., to the evacuation part of the spectra. This is, in particular, true for their low-energy shoulders visible near $E_\alpha = 5$ MeV due to the emission from the heavy ($10^\circ$–$40^\circ$) or the light ($140^\circ$–$170^\circ$) FF. The high-energy tails in the measured spectra, instead, originate partly from preequilibrium $\alpha$ emission. From the good fit in the evaporation regime one concludes that as much as about 80% of the total evaporation yield stems from the compound nucleus prior to scission, while only $(20 \pm 10\%)$ originates from the separated FFs. Hence, this observation corroborates the general findings that the fission process is relatively slow [1], which so far are based mostly on heavy-ion reactions and much lower $E^*$.

In summary, we have studied the excitation energy dependence of the fission probability in 2.5 GeV proton-induced reactions on Au, Bi, and U. Simulations with the combined intranuclear-cascade–statistical model provide a very satisfying reproduction of the observed evolution of $P_f(E^*)$ with $E^*$. Prerequisite for this good agreement is that no additional transient delay time is allowed for the fission dynamics at the saddle. Fission thus seems to be decided upon very fast and early in the long deexcitation chain from the highest initial excitations—a conclusion which is, however, at variance with recent conclusions from other provenience [5,6]. The finding of a fast decision to fission is supplemented by the observation that the major part (about 80% at $E^* = 600–900$ MeV) of all alpha particles is evaporated prior to scission or that the entire fission process is, indeed, relatively slow.

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