Re-formation of chlorine reservoirs in southern hemisphere polar spring

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Abstract. This paper focuses on the recovery of chlorine reservoir species in the lower stratosphere in late Antarctic spring. The investigations are based on measurements from the Halogen Occultation Experiment (HALOE) on board the Upper Atmosphere Research Satellite (UARS) and calculations by the Mainz photochemical box model and the NASA Langley Research Center trajectory model. During late Antarctic spring 1994, HALOE observed high HCl mixing ratios up to 2.7 ppbv at 20 km altitude in the ozone-depleted air inside the polar vortex. These values correspond approximately to the sum of all available inorganic chlorine species. In the preceding period of chlorine activation on polar stratospheric clouds (PSCs), the observed HCl mixing ratios in some cases were below 0.3 ppby. This indicates a fast conversion of active chlorine species into the form of HCl after PSCs disappear with increasing stratospheric temperatures. Box model calculations are presented that assess the rate of HCl increase in late spring when heterogeneous chemistry on polar stratospheric clouds becomes insignificant. The calculations were performed along Lagrangian trajectories starting from HALOE measurements in September 1994. Sensitivity calculations are presented regarding uncertainties in input parameters of the calculations. In the vortex edge region, calculated HCl increase rates are significantly lower compared with HALOE observations. Introducing additional HCl-yielding branches of the reactions of ClO with OH and HO₂ helps to reduce this discrepancy.

Introduction

It is well established that chlorine compounds are an essential factor for catalytic ozone depletion that leads to the formation of the ozone hole in Antarctica. The understanding of conversions from the passive chlorine reservoirs (HCl, ClONO₂) into active forms (Cl, ClO, Cl₂O₂) and back is important to quantify the ozone depletion. In this paper, the reformation of the chlorine reservoirs is investigated. After the chlorine-activating polar stratospheric clouds (PSCs) have evaporated due to the temperature increase in the Antarctic spring, the conversion back to chlorine reservoirs takes place. For low ozone mixing ratios, typical of the Antarctic lower stratosphere in early spring, the rapid formation of HCl by the reaction Cl+CH₄ is favored over ClONO₂ formation via ClO+NO2, which is more typical in the northern hemisphere [Prather and Jaffe, 1990; Douglass et al., 1995]. This increase of HCl mixing ratios is observed by

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the Halogen Occultation Experiment (HALOE). For the 1994 Airborne Southern Hemisphere Ozone Experiment (ASHOE) campaign, calculations along middle latitude trajectories of airmasses observed by HALOE have been made and compared successfully with in situ measurements made on the ER-2 aircraft [*Pierce et al.*, this issue]. The same model and similar initialization method are used here to calculate the HCl increase rate within the Antarctic polar vortex in late spring compared with the increase measured by HALOE.

Observations

The HALOE instrument, launched in 1991 on the Upper Atmosphere Research Satellite (UARS), is designed to measure important atmospheric trace constituents involved in ozone chemistry. Observations of chemical compounds include ozone (O₃), water vapor (H₂O), methane (CH₄), hydrogen fluoride (HF), nitrogen oxides (NO and NO₂), and hydrogen chloride (HCl) at sunrise and sunset [Russell et al., 1993a]. The data presented here were obtained from software version 17 of the retrieval algorithm. The accuracy of the HALOE data as derived from correlative measurements at the altitude considered here (≈20 km) is typically 5-10% for ozone [Brühl et al., 1996] and 15-20% for HCl [Russell et al., 1996]. HALOE extensively sampled the Antarctic polar vortex during mid-September to mid-October 1994. To identify vortex air, CH₄ mixing ra-

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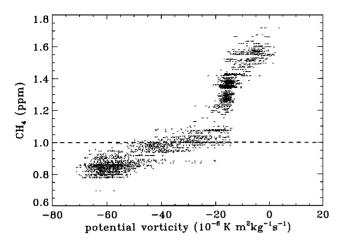


Figure 1. CH₄ as a function of UKMO potential vorticity on the 460 K potential temperature surface between September 24 and October 18, 1994. On this isentropic level, airmasses with a CH₄ mixing ratio below 1.0 ppmv (dashed line) are assumed to be inside the polar vortex.

tios measured by HALOE were used. Diabatic descent of air inside the polar vortex results in lower CH₄ mixing ratios on a specific isentropic surface than for air parcels outside, indicating their origin from higher altitudes [Russell et al., 1993b]. Figure 1 shows HALOE CH₄ mixing ratios in October as a function of potential vorticity (PV) on the 460 K isentropic surface, derived from United Kingdom Meteorological Office (UKMO) wind and temperature data. Airmasses with high negative PV, located inside the vortex, are correlated with low CH₄ mixing ratios. On the chosen potential temperature level of 460 K, airmasses with a CH₄ mixing ratio below 1.0 ppmv are assumed to be inside the vortex.

HALOE generally measured very low O₃ mixing ratios (down to 0.1 ppmv) and low mixing ratios of NO_x (:=NO+ NO₂) down to 0.15 ppbv inside the vortex. The re-formation of the chlorine reservoir HCl can be seen in the HALOE measurements. A time series of vortex HCl mixing ratios from September 11 to October 18 on the 460 K potential temperature level is displayed in Figure 2. Very low HCl mixing ratios below 0.3 ppbv are measured within the vortex in mid-September, increasing to 2.7 ppbv within 1 month. During this period, the HCl mixing ratio outside the vortex (CH₄>1.2 ppmv) stayed almost constant at about 1.0 ppby (not shown). This indicates the typical high chlorine activation within the vortex in early spring followed by an almost complete conversion of active chlorine species into HCl, because the observed final HCl mixing ratios correspond to the mixing ratio of total inorganic chlorine Cl_v (:=HCl+ClONO₂+HOCl+ Cl+ClO+2·Cl₂O₂) at this altitude. Thus, the other chlorine reservoir species ClONO₂ was also converted into HCl. In the figure, different ozone mixing ratios are plotted with different symbols indicating that the HCl mixing ratios increase faster for low ozone mixing ratios. The HCl increase rate is estimated by a linear fit to the HALOE data in each ozone mixing ratio bin (see legend in Figure 2). The time range of the fit (September 24

to October 18) corresponds to that of the fourth ASHOE deployment when trajectory calculations were available. Note however, that this is only an estimate of the increase rate of HCl mixing ratios since observations grouped within the same ozone mixing ratio bin do not represent the same air parcel but similar airmasses, yet the trend in the data is obvious. The fitting errors of the HCl increase rate lie between 10 and 15% (1 σ). The accuracy of the HALOE HCl data is about 15-20% at this altitude [Russell et al., 1996]. Although the latitude of the HALOE observations changes with time between 56°S and 73°S, the data are comparable since only vortex measurements were chosen. The systematic uncertainty that could arise from the latitude sampling of the HALOE instrument was estimated from simultaneously measured HF and derived Cl_v data. On an isentropic level, Cl_v generally increases with latitude. This may overestimate the HCl increase rate by up to 20%. On the other hand, if the data equatorward of 60°S (September 28 to October 1) were left out of the linear fit, the derived HCl increase rates rose by up to 12%. The overall uncertainty of the derived HCl increase rate due to data accuracy (20%), latitude sampling (20%) and line fitting error (15%) is of the order of 30-40%.

The observed HCl increase rate is unlikely to be caused by dynamical processes: The diabatic descent inside the vortex or at the vortex edge could transport HCl-rich air down to the θ =460 K level. However, in order to explain the observed HCl increase rate, diabatic cooling rates of about 6 K/d would be needed and the maximum cooling rates are lower by about a factor of 10, as estimated from calculations at 70 hPa on October 6, 1994 using the Shine radiative heating code [Shine, 1987] and UKMO assimilated temperatures. Furthermore, if one invokes vertical or horizontal transport or mixing as an explanation, one would expect similar trends for HCl and HF measurements, but there is

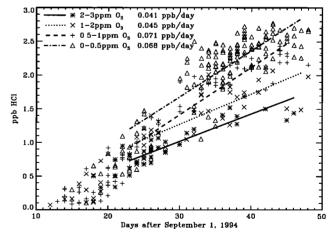


Figure 2. HCl mixing ratio as a function of time inside the polar vortex as it is measured by HALOE on the 460 K potential temperature level. The vortex is characterized by CH₄ values less than 1.0 ppmv for HALOE sunrise and sunset measurements south of 50°S. Different ozone mixing ratio intervals are indicated with different symbols. A linear fit to the data for days 23-47 (September 24 to October 18), is shown for each ozone interval.

no significant trend in the HF data over this time period (not shown). Therefore, the correlation between the HCl increase rate and ozone suggests a chemical cause.

The observed airmasses show a clear signature of dehydration. Typical H_2O mixing ratios in the ozone-depleted air ($O_3 < 1$ ppmv) are between 2 and 3 ppmv; a few observations are even slightly below 2 ppmv which is comparable with the observed dehydration in 1987 [Kelly et al., 1989].

Model Descriptions

Trajectories of the airmasses were calculated by the NASA Langley Research Center trajectory model which uses a fourth order Runge-Kutta scheme using linearly interpolated wind and temperature fields provided by the UKMO analysis [Pierce et al., 1994].

The Mainz photochemical box model uses an implicit numerical integration scheme developed by Gear [1971] with a self-adjusting time step, the commercial package FACSIM-ILE [Curtis and Sweetenham, 1987], to integrate the chemical equations. The model includes 38 chemical species, a standard reaction scheme with 69 gas phase reactions (8 termolecular, 57 bimolecular, 4 thermal decay) including the methane oxidation chain and 22 photolysis reactions. Heterogeneous chemistry on/in liquid ternary H₂SO₄/HNO₃/ H₂O solution aerosols is parametrized from results of a thermodynamic model [Carslaw et al., 1995a,b]. Also, heterogeneous chemistry on crystalline nitric acid trihydrate (NAT) and ice particles is incorporated. Heterogeneous chemistry on sulfuric acid tetrahydrate (SAT) is not incorporated, which is justified since uptake coefficients on SAT are significantly below those on the liquid aerosol [Ravishankara and Hanson, 1996]. Crystalline (ice, NAT, SAT) particles are assumed to form only as temperatures fall below the the ice frost point [Koop et al., 1995] and evaporate as temperatures rise above the corresponding thermodynamic equilibrium temperatures (T_{SAT} , T_{NAT} , T_{Ice}). The model uses currently recommended kinetic reaction rates [DeMore et al., 1994]. The photolysis rates are calculated by a spherical geometry scheme that was developed by Lary and Pyle [1991]. Integrations of the kinetic reaction equations are performed along an airmass trajectory using temperature, pressure and position information obtained from the trajectory model. For a more detailed description of the models see Pierce et al. [1994], Müller and Crutzen [1993], Müller et al. [1994] and K.S. Carslaw et al. (Uncertainties in reactive uptake coefficients for solid stratospheric particles, 2, Effect on modeled ozone depletion, submitted to Geophysical Research Letters, 1996).

Trajectory Calculations

Calculations were performed for an ensemble of 63 trajectories that start at the locations of HALOE sunrise measurements in the vortex on the 460 K potential temperature level around 60°S latitude between September 24 and 29, 1994, and that end on October 18, 1994. The error introduced by assuming isentropic trajectories was estimated by comparing the isentropic evolution of all HALOE airmasses between September 24 and October 18, 1994, with a three-dimensional model calculation over the same time interval. In these calculations, 95% of the trajectories stayed within a range of \sim 12° in longitude, \sim 2.5° in latitude, and \sim 5 K in potential temperature, respectively. Thus, diabatic descent is not a significant error source. Furthermore, the prediction of the exact location of the single air parcels is not critical to this study, since no coincidences with other data are used.

Initialization of Chemical Species

The initialization of all relevant chemical species is of critical importance to get reliable results in the box model calculations. The HALOE experiment provides measurements of O₃, H₂O, CH₄, NO, NO₂, HCl and HF that were used directly to initialize the box model. The remaining species were determined from a combination of HALOE data, correlations with other data, and monthly climatologies of the latitude-pressure distributions of chemical species obtained by the Mainz two-dimensional (2-D) photochemical model [Gidel et al., 1983; Brühl and Crutzen, 1993; Grooss et al., 1994]. A third-order polynomial fit between total inorganic chlorine Cl_v and HF as derived from the 2-D model was used to determine the initialization of Cl_v from HALOE HF observations [Müller et al., 1996] (e.g. for September 1994 and 65°S, $[Cl_y] = -0.344 + 6.22 \cdot [HF] - 2.36 \cdot [HF]^2 - 0.119 \cdot [HF]^3$, where [HF] and [Cl_v] are given in parts per billion by volume, [HF]<1.46 ppbv). At the 460 K level within the polar vortex, typical values of 2.7 ppbv Cl_v were derived from the HALOE data. The initial partitioning within the inorganic chlorine species was derived in the following way. The HCl mixing ratio was initialized directly from the HALOE measurement. The relative partitioning within ClOX (:=Cl_y-HCl), mainly ClO and ClONO2, that could not be derived from the HALOE measurements was taken from the 2-D model results for the given month at the closest latitude grid point. During Antarctic spring, this relative partitioning was very variable near the vortex edge, and some caution needs to be applied when using the 2-D model results for initialization in regions of large latitudinal gradients due to its coarse latitudinal resolution (10°). On September 15 on the 55 hPa level at 65°S, 92% of the ClOX was in the form of ClONO₂ corresponding to the ClONO2 collar that was observed in aircraft measurements [Toon et al., 1989], whereas at 75°S, the partitioning was opposite, only 6% of the ClOX being ClONO₂. Thus the exact partitioning of the ClOX species is not clear from the 2-D model and is likely to be between the two cases. To account for this problem, two extreme possibilities of initial partitioning within ClOX were selected: In the reference calculation, the partitioning ratio was taken from the corresponding 2-D latitude (vortex edge), which might be an overestimation of ClONO₂. In contrast, sensitivity calculations were performed in which all ClOX was initialized as CIO to simulate air inside the vortex core where most of the chlorine was in the active form ClO and its dimer. The possible range of solutions should lie in between those two extreme cases.

The odd nitrogen species were initialized using the correlation of CH₄ and NO_v (:=HNO₃ + NO + NO₂ + NO₃ + 2·N₂O₅ + HNO₄ + ClONO₂) obtained on ER-2 flights during the ASHOE campaign. However, NO_v inside the vortex cannot be derived directly from the CH₄/NO_y ER-2 correlation in this case, since denitrification has taken place in the vortex during the preceding cold period and the ER-2 measurements of CH₄ and NO_y were located outside the vortex. A rough approximation of the denitrification inside the vortex is an average NO_y reduction by 75% of the outsidevortex value, as observed in 1987 by Fahey et al. [1990]. Minimum temperatures in the 1987 and 1994 winters were similarly low, about 182 K in July, and also the observed minimum H₂O mixing ratios of 1.5-2 ppmv were comparable with those of 1987 [Kelly et al., 1989]. This estimate of 75% denitrification was used to initialize HNO₃ and the other unknown NO_v species inside the vortex. The relative partitioning between the unknown NO_v species was taken from the 2-D model. The sensitivity of the model results to this approximation is discussed below.

Radicals with short lifetimes such as O, O(¹D), OH, HO₂, Cl and Br were initialized with zero mixing ratio. This is justified since they adjust themselves to photochemical equilibrium with other species on short timescales, so their initialization does not significantly affect the model calculations. Total inorganic bromine Br_x was taken from the 2-D model. It was initialized as BrO because it undergoes fast redistribution within the Br_x family. All other chemical species that have minor importance and minor variability were initialized directly from the output of the 2-D model.

The overhead ozone profile that is needed for the calculation of radiative fluxes was held constant along the trajectory and was determined from the HALOE ozone profile at the beginning of the calculation. The method of initializing the model with HALOE data was tested in comparison with in situ measurements from the ER-2 aircraft and was shown to be successful [Pierce et al., this issue]. Due to the long lifetime and narrow data range of the HCl in middle latitudes, the predicted HCl by the HALOE initialized trajectories did not compare with the ER-2 data as well as the other species; a mean bias of 0.09 ppbv was found. This is, however, of minor relevance to this study, since the variability of HCl inside the polar vortex was much larger and a small mean bias in the HCl data does not contribute to the calculated increase rates.

Results

The calculations show an increase of HCl in almost all trajectories from the low initial mixing ratios resulting from earlier chlorine activation to values close to total inorganic chlorine in some cases, consistent with the HALOE HCl observations. Figure 3 displays the development in time of the key chemical species O₃, HCl, ClONO₂, ClO, HOCl and NO_x for a typical trajectory calculation inside the polar vortex. The HCl mixing ratio increases up to a maximum possible 2.7 ppbv (=Cl_y, derived from HALOE HF data) at the end of the trajectory. The trajectory starts with a low ozone

mixing ratio of 0.53 ppmv resulting from catalytic destruction in the ozone hole. It has a high initial ClONO₂ mixing ratio and a low ClO mixing ratio derived from the 2-D model partitioning of ClOX.

ClO is produced during daytime by ClONO₂ photolysis. During nighttime, ClONO₂ is formed due to recombination with NO₂. The conversion of ClOX species into HCl during the modeled time is clearly seen in the simultaneous ClONO₂ decrease and HCl increase. The decomposition of ClONO₂ also causes an increase in NO_x mixing ratios.

Due to low water vapor mixing ratios and higher temperatures, none of the trajectories in this study reached temperatures below the ice frost point (T_{ice}=183.3 K (185.6 K) for 50 hPa and 2.0 (3.0) ppmv H₂O), which are needed to form crystalline PSC particles (ice, NAT, SAT). However, heterogeneous chemistry on the ternary liquid aerosol is still important in some trajectories. In this example, a minor heterogeneous reactivation of chlorine on day 4 (September 28) is calculated at temperatures around 188 K. For the given gas phase mixing ratios in this example (1.9 ppmv H₂O, 1.7 ppbv HNO₃), the typical lifetime of HCl due to the fastest of the heterogeneous reactions, HCl+ClONO₂, is about 2 days at the minimum temperature T=188 K. This is not sufficient for a complete activation of chlorine. (A higher H₂O mixing ratio of 3 ppmv would decrease this lifetime by a factor 2.5.)

Very few of the trajectories show a further period of significant chlorine activation due to heterogeneous reactions on the liquid aerosols at this late period in the spring. Only two of the 63 trajectories got near the south pole, where there are low temperatures and continuous sunlit conditions. These conditions are suitable for the heterogeneous reaction $ClONO_2 + HCl \rightarrow Cl_2 + HNO_3$ on liquid ternary aerosol particles, and lead to a complete removal of HCl in these two trajectories. Despite these two exceptions, all other trajectories undergo only minor heterogeneous chlorine activation, such as on day 4 of Figure 3. The chlorine deactivation and a fast recovery of HCl during late September and early October dominate the photochemistry of the vortex airmasses considered.

In the absence of heterogeneous chlorine activation reactions, the HCl increase rate, d[HCl]/dt, is determined mainly by

(R1)
$$Cl + CH_4 \rightarrow HCl + CH_3$$
.

Other standard HCl-yielding reactions have a much smaller contribution to the HCl production. The time derivative of the HCl concentration due to this reaction is given by

$$\frac{d}{dt}[HCl] = k_1 \cdot [CH_4] \cdot [Cl] \tag{1}$$

where k_1 is the rate of reaction (R1). Thus, the HCl recovery is governed by the chlorine atom concentration, which itself is determined by its main production reaction

(R2)
$$ClO + NO \rightarrow Cl + NO_2$$

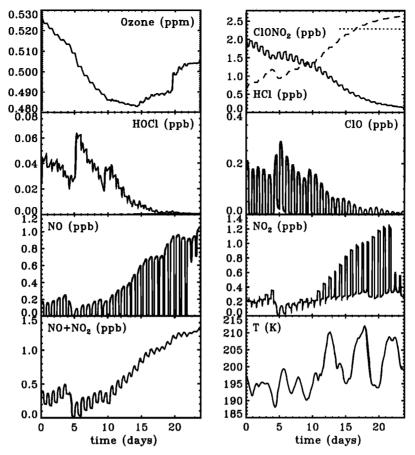


Figure 3. Development of the key chemical species of one example trajectory on the 460 K isentropic surface. The trajectory starts on September 24, 1994, at 67°S. The modeled airmass is strongly dehydrated (H₂O=1.9 ppmv) and considered denitrified (HNO₃=1.7 ppbv). The CH₄ mixing ratio is 0.86 ppmv. The dotted line in the HCl panel corresponds to the 2.3 ppbv level (85% of Cl_y), up to which the HCl increase rates contribute to the calculated average (see text).

and the sink reaction

(R3)
$$Cl + O_3 \rightarrow ClO + O_2$$
.

Thus, the chlorine atom concentration is given by

$$[Cl] = \frac{k_2[NO]}{k_3[O_3]} \cdot [ClO] . \tag{2}$$

Lower ozone values shift this ratio toward higher Cl concentrations due to slower formation of ClO.

The NO concentrations are determined by the available NO_x and the ratio between NO and NO₂. The NO_x mixing ratio increases as the ClONO₂ reservoir is decomposed, and the ratio between NO and NO₂ is given through a photochemical equilibrium of the reactions (R2) and

(R4)
$$NO_2 + h\nu \rightarrow NO + O$$

(R5)
$$NO + O_3 \rightarrow NO_2 + O_2$$
.

This leads to the equilibrium relation

[NO] =
$$\frac{J_4}{k_2[\text{ClO}] + k_5[\text{O}_3]} \cdot [\text{NO}_2]$$
. (3)

Since [ClO] \gg [Cl], the ClO concentration can be determined from the major source and sink reactions. The main ClO source is the photolysis of ClONO₂,

(R6)
$$ClONO_2 + h\nu \rightarrow Cl + NO_3$$

followed by reaction (R3) given above. With the sink reaction

(R7)
$$ClO + NO_2 + M \rightarrow ClONO_2 + M$$
,

the steady state ClO concentration is given approximately by

$$[ClO] \approx \frac{J_6[ClONO_2]}{k_7[NO_2]}$$
 (4)

A combination of the equations (1) to (4) yields

$$\frac{d}{dt}[HCl] = \frac{k_1 k_2 J_4 J_6[CH_4]}{k_3 k_7 [O_3]} \cdot \frac{[ClONO_2]}{k_2 [ClO] + k_5 [O_3]}$$
(5)

This equation contains reaction rates, photolysis rates and concentrations of slowly varying compounds CH₄, ClONO₂ and O₃, as well as the daily variable species ClO. Higher HCl increase rates are obtained for lower ozone concentra-

tions. With the increase of HCl, the ClONO₂ concentrations decrease since total inorganic chlorine is conserved. For low ozone mixing ratios, HCl concentrations can increase until saturation in which almost no ClOX is left and all the inorganic chlorine is in the form of HCl. The photolysis rates J_4 and J_6 in the numerator indicate that HCl recovery only takes place during sunlit hours.

To compare the results with the HALOE observations of Figure 2, the average HCl increase rates $\overline{d[\text{HCl}]/dt}$ are computed for all calculated vortex trajectories. In the trajectories starting with the lowest ozone mixing ratios, the HCl mixing ratio increases fast toward its maximum possible value, about 2.7 ppbv, and stays constant at this level over the remaining time of the trajectory. To look only at the periods of increasing HCl mixing ratios, the average of the HCl increase rate was taken over the time in which HCl is below 85% of the maximal value. This value (2.3 ppbv) is marked in the HCl panel of Figure 3 by a dotted line.

In Figure 4 the mean HCl increase rate $\overline{d[\text{HCl}]/dt}$ as a function of initial ozone mixing ratio for the calculated polar trajectories is shown (black circles). It is clearly larger for low ozone concentrations and reaches high values of the order of 0.1 to 1 ppbv/d for ozone mixing ratios lower than 0.4 ppmv. A few trajectories with slightly negative $\overline{d[\text{HCl}]/dt}$ due to heterogeneous chlorine activation are outside the plotted range.

However, there is a quantitative discrepancy between these calculations and the HCl increase rate derived from HALOE. The HCl time derivatives estimated from HALOE (see Figure 2) are plotted by large pluses in Figure 4. The calculated

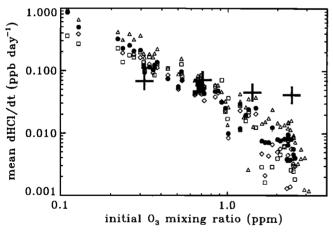


Figure 4. Mean HCl increase rate as a function of initial ozone mixing ratio for isentropic trajectories on the θ =460 K level starting from September 24 to 29, 1994, inside the polar vortex. The black circles indicate the mean HCl increase rate of the reference calculation for each single trajectory run. The large pluses correspond to HCl increase rates derived from HALOE data (see Figure 2). The symbols are the results of the different sensitivity calculations: triangles denote calculations with less denitrification inside the vortex $(NO_y=0.5\cdot NO_y^*)$ instead of $0.25\cdot NO_y^*$; diamonds denote calculations with double sulfuric acid amount; and squares denote calculations with maximum ClO initialization (ClO=ClOX).

HCl increase rate for ozone mixing ratios between 2 and 3 ppmv (corresponding to vortex edge) is lower by a factor of 4 or more compared with the HALOE observations. This discrepancy is subject to further investigation in the following section, in which the sensitivity of the model results to various model input parameters is investigated. In particular, the discrepancy between the model results and the HALOE observations of the HCl increase rate will be discussed. The HCl increase rate for very low ozone mixing ratios (below 0.2 ppmv) cannot be compared to the HALOE observations sufficiently because of limited data sampling.

Sensitivity Studies

The influence of many model input parameters and assumptions in this calculation was tested. The sensitivity of the calculations to the denitrification assumption, aerosol amount and partitioning within the ClOX species for initialization is described in this section. Furthermore, the influence of the additional HCl-yielding branches of the reactions of OH and HO₂ with ClO is discussed.

Denitrification

The denitrification of the polar vortex in Antarctic spring could not be derived from the ASHOE data, but was estimated based upon Antarctic NO_y measurements in 1987 [Fahey et al., 1990]. The measurements inside the vortex showed an average decrease of NO_y to about 0.25·NO_y*, where NO_y* is the expected NO_y mixing ratio derived from the outside-vortex N₂O tracer correlation. Although comparable dehydration was observed in 1987, the exact denitrification is not clear. In a sensitivity calculation, this factor 0.25 was replaced by 0.5. This causes an increase in the initialization of HNO₃ by more than a factor of 2, since the species NO, NO₂ and ClONO₂ are fixed by the initialization scheme. The results of the example trajectory are displayed in Figure 5 (thick lines/pluses) in comparison with the reference calculation described above.

The higher NO_v mixing ratios lead to faster chlorine deactivation because of the main part of NO_v is in the form of HNO₃. The higher HNO₃ concentration leads to enhanced NO_x production by HNO₃ photolysis, which causes an enhanced chlorine atom concentration due to the more effective reaction of ClO with NO (see equation (2)). The reaction of ClO with NO is favored over the reaction of ClO with NO₂, since the NO/NO₂ daytime ratio increases by a factor of about 2-3 due to lower ClO mixing ratios (compare equation (3)) and, secondly, the reaction ClO + NO being 3.5 times faster than the reaction ClO + NO₂ at 50 hPa and 200 K. Thus a faster HCl increase rate is calculated according to equation (1). This is illustrated in Figure 5: During the first 10 days of this sensitivity calculation, higher chlorine atom concentrations are seen compared with the reference calculation, leading to a faster HCl increase. At the end of the calculation, lower ClOX concentrations are calculated, because almost all inorganic chlorine is already converted into HCl, and ClONO₂ photolysis is less effective.

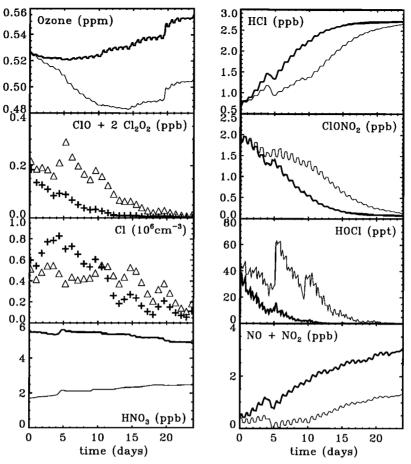


Figure 5. Development of chemical species for the test calculation with enlarged NO_y (less denitrified air) of the example trajectory on the 460 K potential temperature surface. Thick lines and pluses correspond to the test calculation and the thin lines and triangles to the reference (shown also in Figure 3). In the plots of the diurnally variable active chlorine species (Cl, ClO+2·Cl₂O₂), nighttime values are almost zero; therefore only the maximum diurnal values (local noontime) are displayed with a symbol instead of the complete diurnal cycle for better readability.

The HCl increase rates as a function of ozone mixing ratios for all trajectories of these sensitivity calculations are displayed as triangles in Figure 4. The calculated mean HCl increase rates are about 50% higher compared with the reference calculations, but the general behavior in the dependence on ozone mixing ratio does not change. The discrepancy between modeled and observed HCl increase rates cannot be solved by these calculations. In 1987, the most pronounced observed denitrification was 90%; however, a stronger denitrification would lead to lower HCl increase rates and is not probable in the vortex edge region.

Liquid Aerosol Abundance

The results of the calculations are sensitive to the aerosol loading since heterogeneous reaction rates are proportional to the aerosol surface area. The aerosol amount used in the reference calculation (0.25 ppbv $\rm H_2SO_4$ in the aerosol, particle density 10 cm⁻³) corresponds to background aerosol surface areas of about 1.5 $\mu \rm m^2/cm^3$ that are consistent with observed quantities during the ASHOE campaign (J.E. Dye, personal communication, 1996). Heterogeneous chemistry on the sulfate aerosol plays a key role in chlorine

activation, and it is important to look for renewed heterogeneous chlorine activation during the deactivation period. A sensitivity calculation was performed by doubling the total H_2SO_4 mixing ratio. The results are plotted in Figure 6 for the above example trajectory. In the case of enlarged aerosol amount, more HCl is converted back into active chlorine, which slows down the mean HCl increase. The higher ClO values lead to more ozone destruction through the catalytic chlorine cycles as well as to higher ClONO₂ concentrations. Lower NO_x values are calculated because of an increased reaction rate of NO_2 with ClO (R7).

The trajectories show a slower HCl increase for enlarged aerosol content. The mean HCl increase rate for all trajectories of this sensitivity calculation is plotted as diamond symbols in Figure 4. For most trajectories, the HCl increase rate decreases by up to 25% compared with the standard calculation.

Initial CIOX Partitioning

As discussed above, there is no information in the HALOE data about the initial partitioning of the ClOX species. In the standard calculation, the ClOX partitioning was taken from

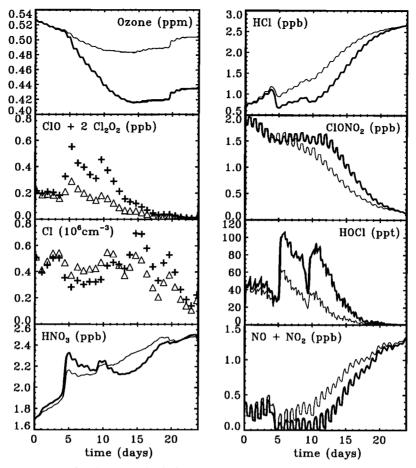


Figure 6. As Figure 5, but for the test calculation with doubled sulfuric acid amount. Note the different scales on the y axis.

the 2-D model output. At the latitudes of the HALOE occultations, from which the trajectories start, the 2-D model predicts almost all ClOX to be in the form of ClONO₂, corresponding to conditions on the vortex edge (65°S). However, it is likely that ClOX is still mostly in the form of active chlorine as the 2-D model output suggests inside the vortex (75°S). Therefore, the opposite extreme situation was calculated, in which all initial ClOX was initialized as ClO. Clearly, more ozone destruction is seen in these calculations due to higher concentration of active chlorine that is involved in catalytic destruction of ozone. Figure 7 shows the development of species for the two extreme initial conditions. After about 10 days, ClO and ClONO₂ levels have reached about equal values in both runs. After day 10, a faster recovery of HCl is seen in the high ClO case due to lower ozone mixing ratios. At the beginning of the trajectory, a fast complete titration of the available NO_x by ClO yielding ClONO₂ takes place.

Both effects compete against each other: In the beginning, higher ClO mixing ratios cause slower HCl recovery (see equation (5)), and later, faster HCl recovery is caused by lower ozone concentrations. The mean HCl increase rate for all trajectories of this sensitivity calculation is plotted with squares in Figure 4. The higher initial chlorine activation causes changes of $\pm 30\%$ in the HCl increase rate.

Heterogeneous Chemistry

Sensitivity calculations were carried out in which the scheme for heterogeneous chemistry was changed such that NAT particles form at 3 K below the NAT equilibrium temperature T_{NAT} [Molina et al., 1993] instead of being only formed as temperatures decrease below the ice frost point. In these calculations, the particles were initially solid (SAT). However, due to denitrification and dehydration, T_{NAT} is significantly lower than for typical stratospheric H₂O and HNO₃ mixing ratios (T_{NAT} =189.9 K for 2 ppmv H₂O and 2 ppbv HNO₃ at 50 hPa [Hanson and Mauersberger, 1988]), and NAT nucleation does not occur in any of the trajectories. Figure 8 shows the calculated HCl increase rates for the modified microphysics (crosses) and without heterogeneous chemistry (pluses) and for the reference calculation (open circles). The results of the calculation with solid SAT lie between the reference calculation (formation of liquid aerosol at $T > T_{\rm SAT} \approx 215$ K) and the calculation without heterogeneous chemistry ($T < T_{SAT}$).

So far, we conclude that the sensitivity of the HCl increase rate to the uncertain input parameters is small compared with the discrepancy between the model and HALOE data. However, the discrepancy between the observed and calculated HCl increase rate might be resolved by incorporating the additional reactions described now.

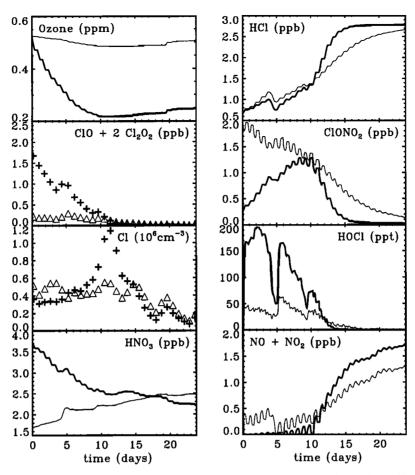


Figure 7. As Figure 5, but for the test calculation with maximum ClO initialization. The difference in HNO₃ initialization is due to conservation of NO_y and different ClONO₂ initialization. Note the different scales on the y axis.

Additional Reaction Branches

One important result of this study is the calculation of a much lower HCl increase rate than is derived from the HALOE occultation. This discrepancy could indicate that

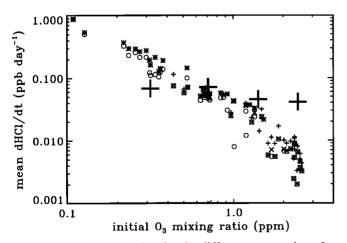


Figure 8. As Figure 4, but for the different assumptions for different microphysics assumptions. Open circles represent the reference calculations with liquid aerosol; also plotted are the results of calculations initialized with crystalline SAT (crosses), and without heterogeneous chemistry (pluses).

other reactions are occurring. There are two speculative reaction branches yielding HCl that are not in the standard box model version:

(R8)
$$ClO + OH \rightarrow HCl + O_2$$

(R9)
$$ClO + HO_2 \rightarrow HCl + O_3$$

The main products of these two reactions are Cl + HO₂ and HOCl + O₂, but small branching ratios yielding HCl are possible. The HCl-yielding branching ratios of both reactions are uncertain. Ab initio calculations suggest that the HCl-yielding branching ratio of the reaction ClO+OH (R8) is small (but not necessarily zero), because it involves spinforbidden curve crossings [Lee and Rendell, 1993]. Laboratory measurements indicate a branching ratio for this reaction between 0 and 14% [Poulet et al., 1986; DeMore et al., 1994]. The HCl-yielding branching ratio for the reaction CIO+HO₂ (R9) is dependent on temperature and pressure. At 900 hPa and 210 K, a branching ratio of 5±2% was measured, decreasing to 2±1% at 240 K [Finkbeiner et al., 1995]. A few measurements are also available at low temperature and low pressure. These measurements were made in a helium atmosphere with about 3 hPa pressure, corresponding to an atmospheric pressure of 0.5 hPa. An upper limit of 3% at 248 K [Leu, 1980] and an upper limit of 1% at 215 K (J. Crowley, unpublished results, 1995) were observed. In the intermediate pressure range between \approx 0.5 and 900 hPa and at temperatures below 210 K, no measurements of the HCl-yielding branching ratio of ClO + HO₂ are reported. Therefore the pressure and temperature dependence of this branching ratio in the stratosphere is still unclear.

The importance to ozone in the middle stratosphere of a possible branch of the reaction between ClO and OH yielding HCl (R8) has been already discussed [Brühl and Crutzen, 1988; McElroy and Salawitch, 1989; Toumi and Bekki, 1993; Eckman et al., 1995]. The incorporation of this reaction branch of the order of 5% improves agreement between model calculations and observations. Lary et al. [1995] show that incorporation of reaction (R8) into photochemical models causes a faster HCl recovery in the lower stratosphere. A detailed analysis based on simultaneously observed HO_x, NO_x and chlorine species between 20 and 40 km [Chance et al., 1996] concluded that a small HClyielding branching ratio for the reaction of ClO with HO₂ or OH is needed to bring the photochemical model calculations into agreement with the HALOE data. In that study, a branching ratio of 5% for reaction (R8) and 3% for reaction (R9) gives the best agreement between the observations and the model which is used here. Sensitivity calculations were performed in which the two reaction branches with the quoted branching ratios were added.

For this analysis the initialization of the ClOX species plays an important role, because the rate of HCl increase due to the reactions (R8) and (R9) depends on the ClO concentration. With these additional reaction branches, calculations were performed with the two extreme cases of initial ClOX partitioning as discussed before. The results of these calculations are shown in Figure 9 for both initial ClOX partitionings. For ozone mixing ratios above 1 ppmv, the calculated HCl increase is substantially faster compared with the reference calculation. The discrepancy between HALOE observations and the calculations for high ozone mixing ratios is much lower, but there are still differences. In the calculation with the initialization of high chlorine activation, the higher ClO concentrations cause a higher efficiency of the reactions (R8) and (R9). Therefore, an even faster increase of the HCl mixing ratios is seen, which gives the best agreement of all sensitivity calculations. However, the calculated HCl increase rates in both cases are still lower than the HALOE observations. This suggests that reactions (R8) and (R9) may indeed take place in the stratosphere and might even have larger partitionings than used here. A more exact determination of the branching ratios by laboratory measurements would reduce this uncertainty in model calculations.

There may also be other error sources which could cause part of the discrepancy. For example, the uncertainty of model input parameters as reaction rate coefficients influences the results. The reported uncertainties in k_1 (CH₄+Cl) and k_2 (NO+ClO) at 200 K are 40% and 35%, respectively [DeMore et al., 1994]; an increase of these rate coefficients to their maximum possible values could cause about 90% increase in the HCl increase rate (see equation (5)) and also

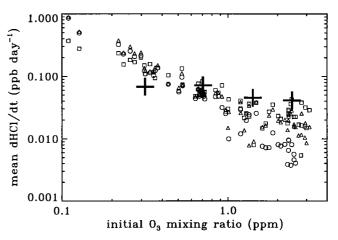


Figure 9. Mean HCl increase rate as a function of initial ozone mixing ratio with the additional reactions (R8) and (R9). The open circles indicate the mean HCl increase rate obtained by the reference calculation. The symbols are the results from the calculation with the branching ratios of 5% and 3% for the reactions (R8) and (R9). Large pluses correspond to the increase rate derived from the HALOE data. The calculations were performed with two different initial ClOX partitionings. Triangles denote ClOX partitioning from 2-D model (92% ClONO₂, 8% ClO) as in the reference run. Squares denote initialization with all ClOX set to ClO.

reduce the discrepancy. Similar consideration applies for a decrease in the reaction rates k_3 (Cl+O₃, 35%) and k_7 (ClO+NO₂, 35%). Together with the estimated uncertainty of 30-40% from the HALOE observations, most of the discrepancy at the vortex edge could also be explained without reactions (R8) and (R9), if these rate coefficients were assigned to their extreme possible values simultaneously. However, this case seems rather unlikely and may cause discrepancies for lower ozone mixing ratios, where in the current study reasonable agreement was found.

Summary

Calculations with the linked NASA Langley Research Center trajectory model and Mainz photochemical box model for a large set of trajectories in the Antarctic region have been presented. A method to derive the chemical initialization of box model calculations on the basis of HALOE data was introduced. The calculations were used to analyze stratospheric chemistry changes in the polar vortex at the end of the period of heterogeneous chlorine activation and chlorinecatalyzed ozone destruction; in particular, the observations and calculations of the HCl recovery were studied. The HCl increase rates depend on the ozone mixing ratios, with faster HCl increase at lower ozone mixing ratios. High HCl increase rates of more than 0.1 ppbv/d were found for ozone mixing ratios below 0.5 ppmv. A complete conversion of all available ClOX into HCl is seen in both the box model calculations and the HALOE observations. For ozone mixing ratios above 1 ppmv a quantitative discrepancy of the HCl increase rate between calculations and HALOE observations was found. The sensitivity of the box model results to the assumption of denitrification, to the sulfate aerosol amount, and to the ClOX initialization was investigated. None of the three could (completely) explain the discrepancy in HCl increase rate for high ozone mixing ratios. The discrepancy may be resolved by HCl-yielding branches in the reactions of OH and HO₂ with ClO.

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