Crystal Thermal Transport in Altermagnetic RuO₂

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We demonstrate the emergence of a pronounced thermal transport in the recently discovered class of magnetic materials—altermagnets. From symmetry arguments and first-principles calculations performed for the showcase altermagnet, RuO₂, we uncover that crystal Nernst and crystal thermal Hall effects in this material are very large and strongly anisotropic with respect to the Néel vector. We find the large crystal thermal transport to originate from three sources of Berry's curvature in momentum space: the Weyl fermions due to crossings between well-separated bands, the strong spin-flip pseudonodal surfaces, and the weak spin-flip ladder transitions, defined by transitions among very weakly spin-split states of similar dispersion crossing the Fermi surface. Moreover, we reveal that the anomalous thermal and electrical transport coefficients in RuO₂ are linked by an extended Wiedemann-Franz law in a temperature range much wider than expected for conventional magnets. Our results suggest that altermagnets may assume a leading role in realizing concepts in spin caloritronics not achievable with ferromagnets or antiferromagnets.

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The anomalous Nernst effect (ANE) [1] and anomalous thermal Hall effect (ATHE) (or anomalous Righi-Leduc effect) [2]—the thermoelectric and thermal analogs of the anomalous Hall effect (AHE)—are the two fundamental anomalous thermal transport manifestations in spin caloritronics [3,4]. They describe separately the appearance of a transverse electrical current density J_j and a transverse thermal current density J_j^Q induced by a longitudinal temperature gradient $-\nabla_i T$ in the absence of an external magnetic field [Figs. 1(a) and 1(b)]. The ANE and ATHE are usually expressed as [5]

$$J_j = \alpha_{ji}(-\nabla_i T), \tag{1}$$

$$J_i^Q = \kappa_{ji}(-\nabla_i T), \tag{2}$$

where α_{ji} is the anomalous Nernst conductivity (ANC) and κ_{ji} is the anomalous thermal Hall conductivity (ATHC). The transverse thermal and electrical transport are related by the Lorenz ratio, $L_{ij} = \kappa_{ij}/(\sigma_{ij}T)$, where σ_{ij} is the anomalous Hall conductivity (AHC). In the zero-temperature limit, the Wiedemann-Franz (WF) law,

 $L_{ij}(T \to 0) = \pi^2 k_B^2/3e^2 = L_0$ (Sommerfeld constant), has been witnessed in conventional ferromagnets [6–8].

The ANE and ATHE have been investigated extensively in ferromagnets, and they are generally proportional to the spontaneous magnetization [6–13]. The antiferromagnets (AFMs) are long presumed to have vanishing anomalous thermal transport due to vanishing macroscopic magnetization. However, this assumption has been challenged in certain noncollinear AFMs hosting nonvanishing flavors of spin chirality. For example, the ANE and ATHE are predicted theoretically and/or observed experimentally in coplanar noncollinear AFMs Mn_3Y (Y = Ge, Sn) [14–18] and Mn_3XN (X = Ga, Zn, Ag, Ni) [19,20], where the vector spin chirality plays a crucial role [20]. The ANE and ATHE are also found in noncoplanar AFMs or skyrmions [21–25], in which the scalar spin chirality generates a realspace Berry phase of propagating electrons. The ANE and ATHE can emerge in noncoplanar magnets even without spin-orbit coupling (SOC), like the (quantum) topological Hall and topological magneto-optical effects [26–28].

While the ANE and ATHE in noncollinear AFMs were explored in the recent past, much less is known about their properties in collinear AFMs. Conventional collinear AFMs host time-reversal-like degenerate electronic bands

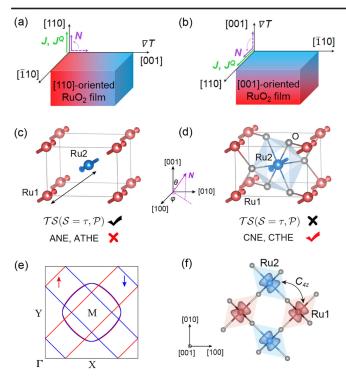


FIG. 1. (a),(b) Schematics of anomalous Nernst and anomalous thermal Hall effects in [110]- and [001]-oriented RuO₂ films. N denotes the Néel vector rotating from the [001] to [110] axis on the $(\bar{1}10)$ plane. J and J^Q are detectable electrical and thermal currents, respectively, induced by a temperature gradient ∇T . (c), (d) Magnetic unit cell of RuO2 without and with O atoms. Red and blue balls represent two Ru atoms with antiparallel spin magnetic moments, and gray balls represent nonmagnetic O atoms. The anomalous thermal transport is prohibited by the TS symmetry of the magnetic lattice alone; however, this symmetry is broken when taking into account the cage of O atoms, which gives rise to crystal thermal transport. Inset: parametrization of the Néel vector $N(\varphi, \theta)$ in spherical coordinates. (e) Reciprocal space Fermi surface featured by strong (cigar shaped) and weak (circular) spin-splitting states. (f) Realspace alternating spin density related by fourfold crystal rotation.

through a combined \mathcal{TS} symmetry (\mathcal{S} being spatial inversion \mathcal{P} or translation τ , \mathcal{T} being time reversal), prohibiting ANE and ATHE [Fig. 1(c)]. The \mathcal{TS} symmetry breaking by nonmagnetic atoms can have a drastic effect, as it, e.g., activates the "crystal" Hall effect in RuO₂ [29,30] by virtue of crystal time-reversal symmetry breaking. Respectively, from rigorous spin symmetry analysis, RuO₂ is recognized as a representative of a distinct flavor of magnetism beyond ferromagnetism and antiferromagnetism, termed altermagnetism [31,32]. Altermagnets are characterized by spin polarization in both reciprocal and real spaces [31–33] [Figs. 1(e) and 1(f)]. Thus, the question arises whether analogous crystal thermal effects [Fig. 1(d)] emerge in altermagnets due to a nontrivial interplay of spin and crystal symmetries.

Here, based on symmetry analysis and state-of-the-art first-principles calculations, we answer this question

positively. Taking RuO₂ as a showcase representative of altermagnetism, we reveal a novel class of anomalous thermal transport effects, namely, the crystal Nernst effect (CNE) and crystal thermal Hall effect (CTHE), to emerge in altermagnetic materials. The crystal thermal transport in RuO₂ is strongly anisotropic with respect to the orientation of the Néel vector and can be observed experimentally in [110]- or [001]-oriented films. We elucidate that large crystal thermal transport is microscopically related to Weyl fermions, pseudonodal surfaces, and ladder transitions. Moreover, we find that the anomalous Lorenz ratio is in accordance with the Sommerfeld constant in a rather wide temperature range of 0-150 K. Our results suggest a promising altermagnetic spin-caloritronics platform for the realization of room-temperature crystal thermal transport.

The material under study, RuO_2 , has a rutile structure with a space group $P4_2/mnm$ [Fig. 1(d)]. Several recent studies reveal room-temperature collinear antiparallel magnetic order in both RuO_2 thin films and bulk crystals [30,34–36], which promotes exciting applications in spintronics, such as the crystal Hall effect [29,30], spin-polarized currents [37,38], spin-splitter torque [37,39–41], giant tunneling magnetoresistance [38,42], magneto-optical effect [43,44], and tunneling AHE [42,45].

The Néel vector of RuO₂, $N = S_1 - S_2$ ($S_{1,2}$ are antiparallel spin moments on two Ru atoms) was shown to exhibit a dominant projection along the [001] axis [34,35]. For convenience, we introduce the spherical coordinates to describe the orientation of the Néel vector $N(\varphi, \theta)$ (see Fig. 1), with the experimentally observed direction of $N(\varphi = 107.2^{\circ}, \theta = 22.7^{\circ})$ [35]. Such a low-symmetry orientation is very susceptible to experimental conditions, and it can be changed by an external magnetic field or by the effects of spin-orbit torque [46–48]. Notably, a recent experiment has realized the crystal AHE in RuO₂ films utilizing the magnetic field-tunable reorientation of the spin-quantization axis [30]. Here we focus on the crystal thermal transport in RuO2 assuming that the Néel vector can rotate from the [001] to [110] axis on the $(\bar{1}10)$ plane, i.e., $N(\varphi = 45^{\circ}, 0^{\circ} \le \theta \le 360^{\circ})$.

We assess the anomalous transport coefficients as [49–51]

$$R_{ij}^{(n)} = \int_{-\infty}^{\infty} (\varepsilon - \mu)^n \left(-\frac{\partial f}{\partial \varepsilon} \right) \sigma_{ij}^{T=0}(\varepsilon) d\varepsilon, \tag{3}$$

where μ is the chemical potential, $f=1/\{\exp[(\varepsilon-\mu)/k_BT]+1\}$ is the Fermi-Dirac distribution function, and $\sigma_{ij}^{T=0}(\varepsilon)$ is the zero-temperature intrinsic AHC (see Supplemental Material [52]). Then, the temperature-dependent AHC σ , ANC α , and ATHC κ , respectively, read

$$\sigma_{ij} = R_{ij}^{(0)}, \quad \alpha_{ij} = -R_{ij}^{(1)}/eT, \quad \kappa_{ij} = R_{ij}^{(2)}/e^2T.$$
 (4)

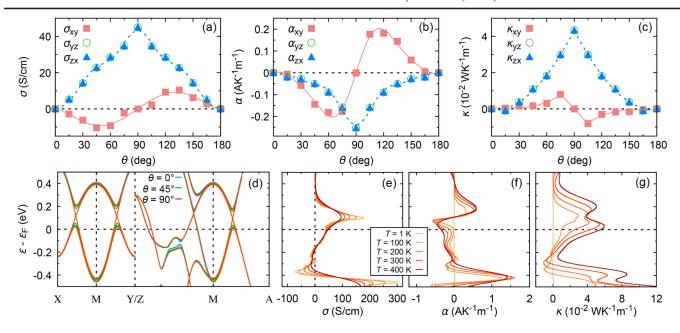


FIG. 2. (a)–(c) Components of the anomalous Hall conductivity σ , anomalous Nernst conductivity α , and anomalous thermal Hall conductivity κ at T=300 K as a function of polar angle θ when the Néel vector rotates within the $(\bar{1}10)$ plane. The lines are guides to the eye. The conductivity at $\theta+\pi$ is not plotted as it is opposite in sign to that at θ due to time-reversal symmetry. (d) Relativistic band structures of RuO₂ for $N(\varphi=45^\circ,\theta=0^\circ,45^\circ,90^\circ)$. (e)–(g) σ , α , and κ as a function of Fermi energy at $N(\varphi=45^\circ,\theta=90^\circ)$ for different temperatures. The color scheme from light to dark corresponds to "warming" from 1 to 400 K.

The computed three crystal thermal transport coefficients of RuO₂, shown in Figs. 2(a)–2(c), are remarkably all nonzero except for $N(\varphi=45^{\circ},\theta=\mathbb{N}\pi)$. For the orientation of the Néel vector along the [001] axis $(\theta=\mathbb{N}\pi)$, the effects are prohibited by the presence of multiple mirror planes: the glide mirror $\mathcal{M}_{[010]}\tau_{1/2}$ and $\mathcal{M}_{[100]}\tau_{1/2}$ (here \mathcal{M} and τ denote mirror and translation operations, respectively) from the $P4_{2'}/mnm'$ magnetic space group. The vanishing value of the xy component of transport coefficients for $\theta=(\mathbb{N}+1/2)\pi$ is due to the $\mathcal{TM}_{[001]}$ symmetry from the Cmm'm' magnetic space group.

Figures 2(a)–2(c) depict three prominent features of crystal thermal transport. First, zx and yz components are nearly identical. This is ensured by the symmetry constraint $TC_{2x\bar{y}}R_{yz} = R_{zx}$ [see Eq. (3)]; here, $C_{2x\bar{y}}$ forces R_{yz} to $-R_{zx}$, and R_{zx} is odd under \mathcal{T} . Second, all components show an oscillatory behavior with θ : while the zx and yz components exhibit a period of 2π , σ_{xy} is π periodic. This can be understood from realizing that the z component of the spins at $\pi - \theta$ is the time-reversed counterpart of the ones at θ with x and y components staying the same, which results in the fact that $R_{zx,yz}(\pi-\theta) = R_{zx,yz}(\theta)$ but $R_{xy}(\pi-\theta) = -R_{xy}(\theta)$. Finally, σ , α , and κ are strongly anisotropic in the direction of the Néel vector. For example, zx and yz components gradually increase with increasing θ from 0° to 90°, which can be explained from the evolution of Berry curvature (Supplemental Material, Fig. S1 [52]).

We now illustrate three distinct types of geometrical Berry curvature contributions that shape the crystal electronic and thermal transport properties in altermagnets: Weyl fermions, pseudonodal surfaces, and ladder transitions [Figs. 3(a)–3(c)]. As θ increases, the band splitting magnitude at specific k points diminishes, and gaps along X-M-Y and Z-M-A paths progressively close [Fig. 2(d)], signaling the emergence of Néel-order-dependent topological Weyl nodal features [29,59,60]. Without SOC, we identify two spin-up nodal lines on the (001) and (110) planes and two spin-down nodal lines on the (001) and ($\bar{1}10$) planes, connected by C_{4z} rotation symmetry (Fig. S2 [52]). Upon incorporating SOC, for $N \parallel [110]$, the nodal line on the (110) plane is preserved, protected by $\mathcal{M}_{[110]}$ symmetry, while those on the (001) plane disperse into three pairs of Weyl points [Fig. 3(d) and Supplemental Material [52], Fig. S2]. In Figs. 3(e) and S3(a) [52], we show how large Berry curvature emerges in regions of Weyl points due to interband transitions within bands of the same spin (spin-conserved parts, $\uparrow \uparrow$ or $\downarrow \downarrow$), schematically depicted in Fig. 3(a). The Weyl point contribution becomes more pronounced at the Fermi energy $\varepsilon = \varepsilon_F \pm 0.19 \text{ eV}$ [Figs. S3(b) and S3(c) [52]].

On the other hand, due to spin group symmetries \mathcal{TS}_{2x} and \mathcal{TS}_{2y} ($\mathcal{S}_{2x,2y}$ being twofold screw rotations), the degeneracy of spin-up and spin-down states on the $k_x = 0, \pi$ and $k_y = 0, \pi$ planes is enforced [e.g., ΓY and ΓX paths in Fig. 1(e)], creating four nodal planes [Fig. S3(d) [52]], as also observed for FeSb₂ [61] and CaFeO₃ [62]. This degeneracy is lifted by SOC, resulting in substantial Berry curvature near these pseudonodal surfaces

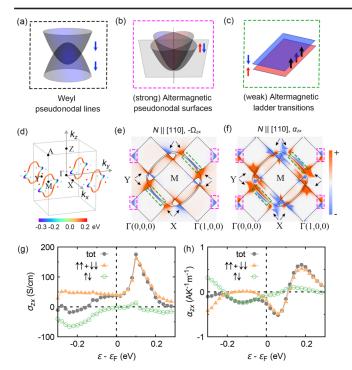


FIG. 3. Three distinct types of interband transitions in altermagnetic RuO₂: (a) pseudonodal lines forming among the bands of the same spin, (b) altermagnetic pseudonodal surfaces forming among the bands of opposite spin driven by crystal symmetry, and (c) ladder transitions among weakly split bands of opposite spin with similar dispersion. (d) Momentum and energy distribution of topological nodal lines and Weyl points. (e) Relativistic Fermi surface (black lines) and Berry curvature Ω_{zx} (color maps, in atomic units) on the (001) plane at the true Fermi energy. The contributions from gapped nodal lines, pseudonodal surfaces, and ladder transitions are indicated by black arrows and pink and green dashed rectangles, respectively. (f) Similar to (e) but for the anomalous Nernst conductivity α_{zx} . (g),(h) Total σ_{zx} and α_{zx} and their decompositions to spin-conserved ($\uparrow\uparrow+\downarrow\downarrow$) and spin-flip ($\uparrow\downarrow$) parts. In (d)–(h), the Néel vector points to $N(\varphi = 45^{\circ}, \theta = 90^{\circ})$.

[Figs. 3(e) and S3(a)]. The Berry curvature's origin here is tied to interband transitions between states of opposite spin, activated near high-symmetry nodal planes, Fig. 3(b). Remarkably, the Berry curvature also arises from regions where a very small gap between spin-up and spin-down bands exists without SOC [63]. This stems from spin-flip transitions between two spin-polarized bands exhibiting similar dispersion across the Fermi energy [Fig. 3(c)], visible as rings centered at the M point in Fig. 1(e). Such "ladder" transitions have been observed in the anomalous Hall effect of ferromagnetic FePt alloys [64]. The distribution of the Berry curvature from ladder transitions in RuO₂ appears asymmetric along different ΓM paths when $N \parallel [110]$ [Figs. 3(e) and S3(a) [52]], while symmetric patterns emerge when $N \parallel [100]$ or [010] (Fig. S4).

We emphasize that among the three types of Berry curvature we considered, the latter two exhibit a distinctive feature of altermagnetism. These are generated by crystal symmetry-driven (quasi)degeneracies between states with opposite spin, which foster the spin-flip $(\uparrow\downarrow)$ transitions. Specifically, at the true Fermi energy, the k-resolved distribution of Nernst conductivity showcases significant contributions from Weyl points [Figs. 3(f) and Supplemental Material [52], Figs S5(c) and S5(d)]. However, with a slight adjustment to the position of the Fermi energy, the Nernst and Hall conductivities display substantial spinflip contributions [Figs. 3(g) and 3(h)]. Notably, in the regime of hole doping (e.g., $-0.2 \sim 0.0$ eV), the ANE is entirely dominated by the spin-flip process. This starkly contrasts with conventional collinear antiferromagnets with TS symmetry, such as bilayer MnBi₂Te₄, in which the contributions from spin-conserved parts ($\uparrow \uparrow$ and $\downarrow \downarrow$) tend to cancel each other, and the impact of the spin-flip part is negligible (Fig. S6 [52]).

Next, we turn our attention to the magnitude of crystal thermal transport coefficients. Figures 2(e)–2(g) show σ , α , and κ as a function of the Fermi energy for different temperatures. At the true Fermi energy ($\varepsilon = \varepsilon_F$), σ stays nearly constant with the increasing of temperature, while α and κ change drastically upon heating. In addition, although σ is rather small, α and κ can reach as much as $-0.35~{\rm AK^{-1}~m^{-1}}$ and $5.5\times10^{-2}~{\rm WK^{-1}~m^{-1}}$ [65]. These values can be further substantially enhanced by engineering the degree of band filling via electron or hole doping.

In understanding the temperature dependence of thermal transport, let us first turn to the low-temperature limit. Here, σ , α , and κ [Eq. (4)] are reduced to the first-order correction in the Sommerfeld expansion [49],

$$\sigma_{ij} \approx \sigma_{ij}^{T=0}(\mu),$$
 (5)

$$\alpha_{ij} \approx -\frac{\pi^2 k_B^2 T}{3e} \frac{\mathrm{d}\sigma_{ij}^{T=0}(\varepsilon)}{\mathrm{d}\varepsilon} \bigg|_{\varepsilon=\mu},$$
 (6)

$$\kappa_{ij} \approx \frac{\pi^2 k_B^2 T}{3e^2} \sigma_{ij}^{T=0}(\mu), \tag{7}$$

where e is the elementary charge and k_B is the Boltzmann constant. Relations (6) and (7) reflect two well-known expressions: one is the Mott relation, linking the ANC to the energy derivative of AHC; the other is the WF law, which introduces the anomalous Lorenz ratio $L_{ij} = \kappa_{ij}/(\sigma_{ij}T)$, converging to the Sommerfeld constant $[L_0 = \pi^2 k_B^2/(3e^2) = 2.44 \times 10^{-8} \ \Omega W K^{-2}]$ in the low-temperature limit.

The variation of σ , κ , and L with temperature for different Fermi energies is shown in Fig. 4. When $\varepsilon = \varepsilon_F$, the anomalous Lorenz ratio L is close to the Sommerfeld constant L_0 for T < 100 K [Fig. 4(c)]. This is because, in the low-temperature region, L is dominated by σ due to the linear dependence of κ on temperature

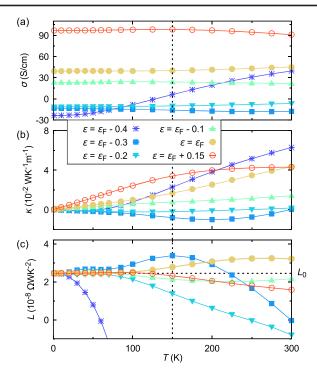


FIG. 4. Temperature dependence of (a) anomalous Hall conductivity σ , (b) anomalous thermal Hall conductivity κ , and (c) anomalous Lorenz ratio L for $N(\varphi=45^\circ,\theta=90^\circ)$ with different Fermi energies ε . The horizontal dashed line in (c) denotes the Sommerfeld constant L_0 . The vertical dashed line denotes the allowed maximal temperature range of the Wiedemann-Franz law.

[Fig. 4(b)], and σ is nearly constant below 100 K [Fig. 4(a)]. The WF law is valid in the energy range of the nodal line (-0.2-0.2 eV), and its robustness gradually weakens when going away from this energy range. Particularly, with the energy approaching the crossing points at about $\varepsilon = \varepsilon_F + 0.15$ eV [Fig. 2(d)], the WF law is valid even up to 150 K. Hence, the robust validity of the WF law in RuO₂ at relatively high temperatures is likely related to its Weyl nodal properties, which have a topological origin. The underlying physics presents a stark contrast to the expectations based on typical experiences with conventional ferromagnets [6–8].

Here, we do not consider the effect of inelastic scattering due to phonons [66,67], magnons [68], and their interactions [69], which usually break the validity of anomalous WF law for finite temperatures, as observed in traditional ferromagnets [6–8]. Recently, the anomalous WF law is found to be valid in a wide temperature range for noncollinear AFMs, promoting the unique role of the intrinsic mechanism for thermal properties [15,17,18]. The intrinsic contribution can be further significantly enhanced by tuning the Fermi energy to lie at the position of magnetic topological (quasi)degeneracies. It strongly indicates that the dominant intrinsic mechanism in RuO₂ comes from its novel topological nodal features. We suggest that the unconventional anomalous thermal effects in RuO₂ can

be observed experimentally in the [110]- or [001]-oriented films [Figs. 1(a) and 1(b)], as in the case of previously reported anomalous Hall measurements [30].

In this study, we have employed RuO₂ as a prototype to explore the crystal thermal transport of altermagnets, while our findings hold broader relevance across a diverse spectrum of altermagnets. For instance, the presence of a nonzero spin-flip process, a key feature of crystal thermal transport, is distinctly observable in another altermagnet, MnTe [70] (Supplemental Material, Fig. S7 [52]). Overall, the unexpected crystal thermal properties in room-temperature altermagnets, RuO₂ and MnTe, are poised to generate significant interest in the field of altermagnetic spin caloritronics.

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