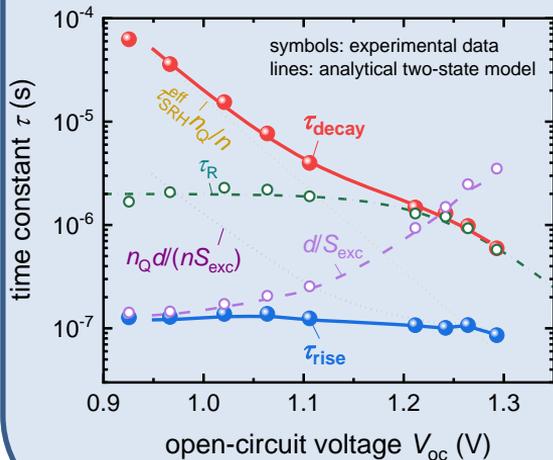


# USING TRANSIENT METHODS TO CHARACTERIZE RECOMBINATION AND EXTRACTION IN HALIDE PEROVSKITE SOLAR CELLS

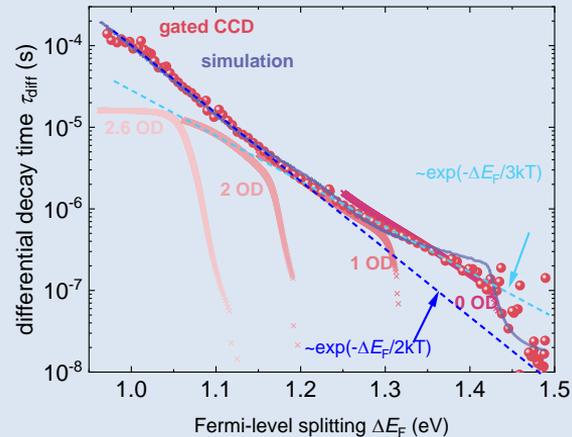
Thomas Kirchartz, Genghua Yan, Ye Yuan, Lisa Krückemeier, Uwe Rau

IEK-5 Photovoltaik, Forschungszentrum Jülich

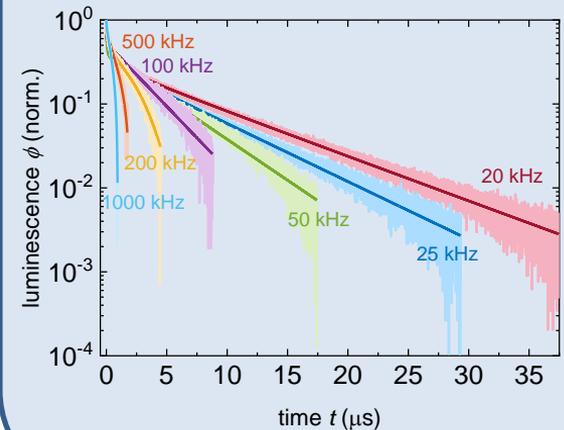
## 1) Charge separation vs. recombination

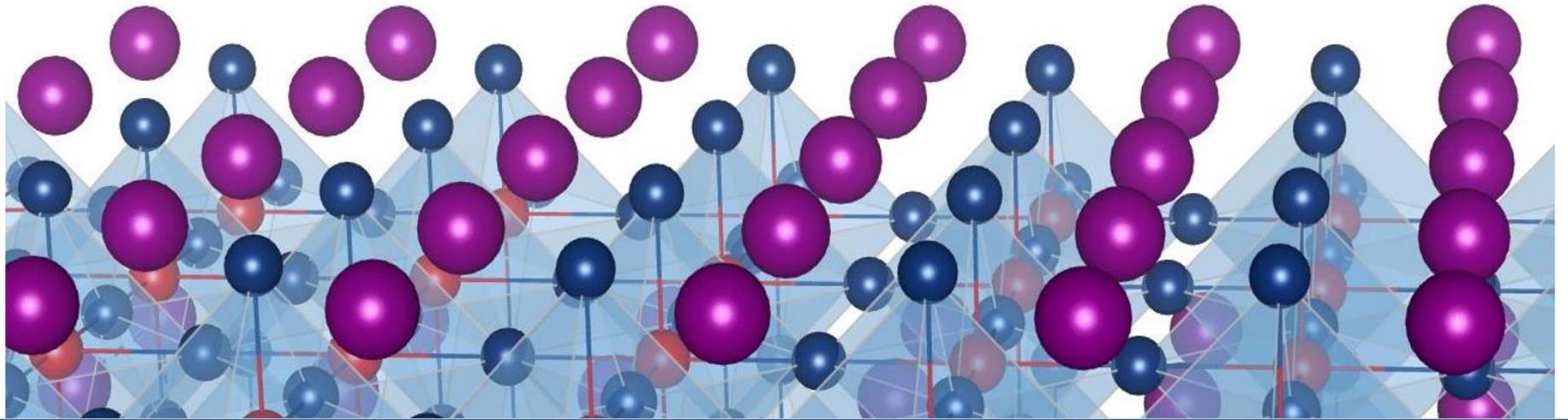


## 2) On the importance of shallow defects



## 3) On the importance of repetition rates



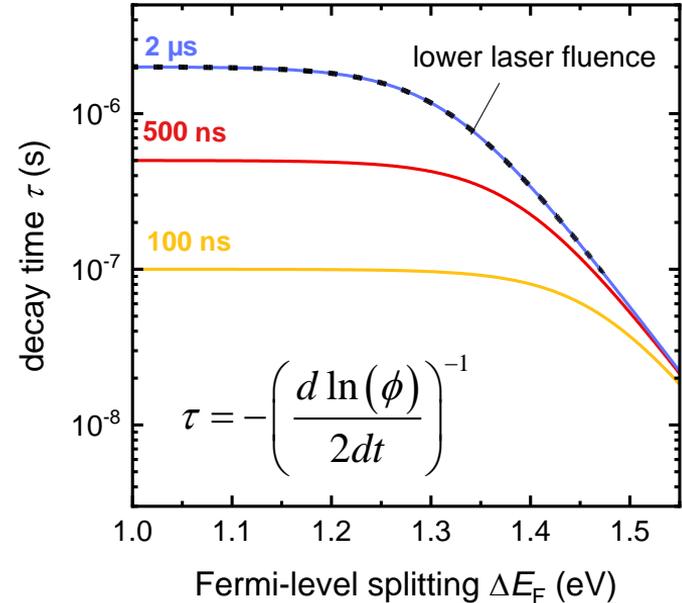
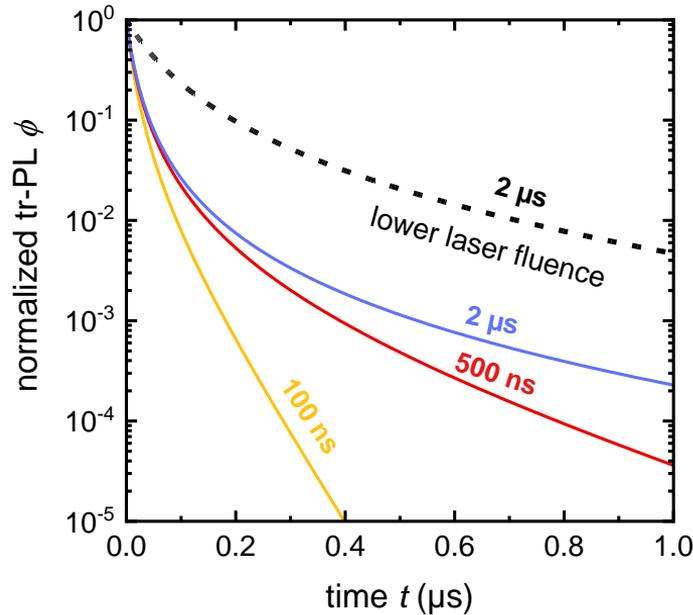
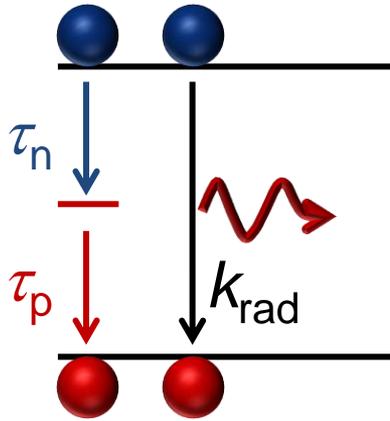
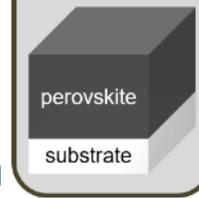


## PART 0: INTRODUCTION

# TRANSIENT PHOTOLUMINESCENCE AND LIFETIMES

# Transient Photoluminescence

## Layer on Glass – Bulk Recombination



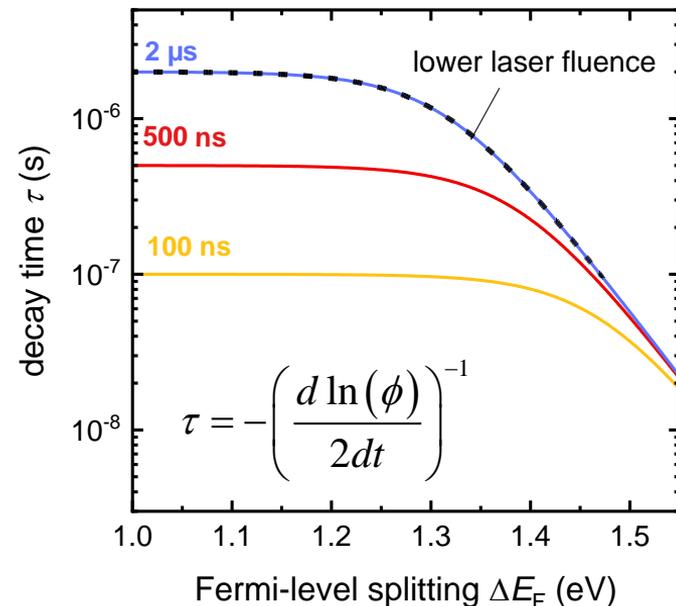
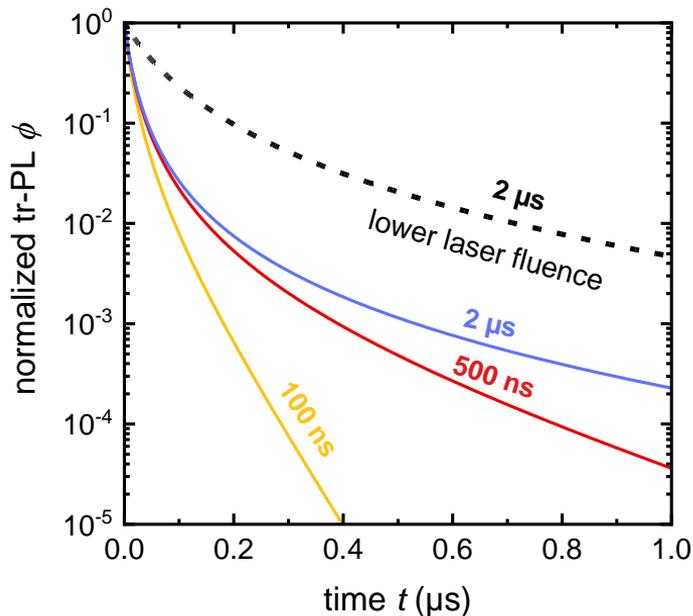
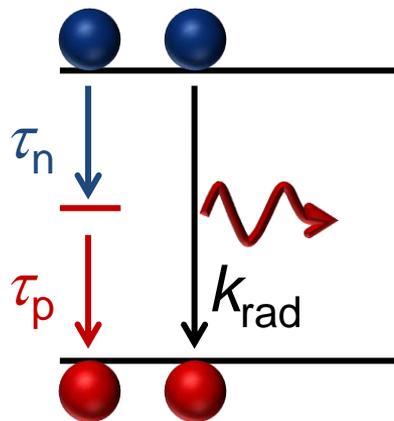
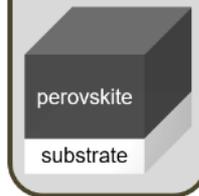
$$\frac{dn}{dt} = -k_{\text{rad}} n^2 - \frac{n}{\tau_p + \tau_n}$$

SRH + radiative recombination

← time

# Transient Photoluminescence

## Layer on Glass – Bulk Recombination

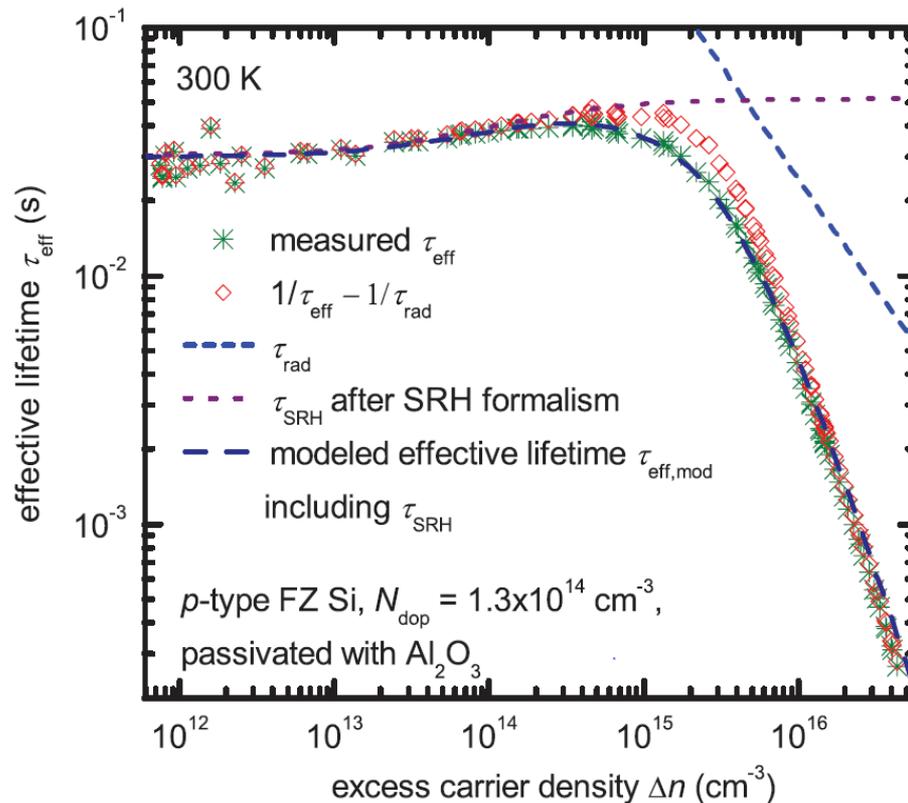
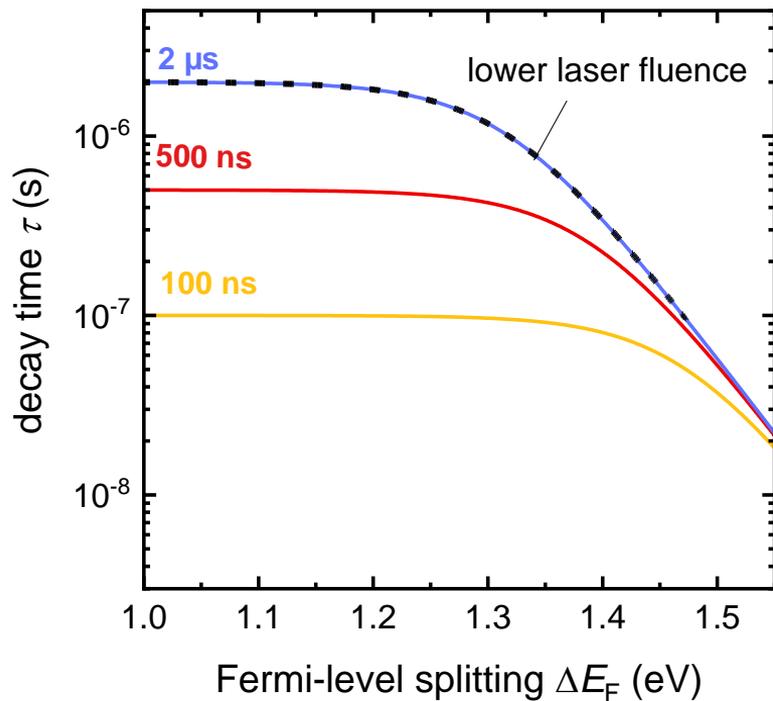


$$\tau_{\text{diff}} = -\frac{n}{dn/dt} = \frac{1}{k_{\text{rad}}n + \tau_p + \tau_n}$$

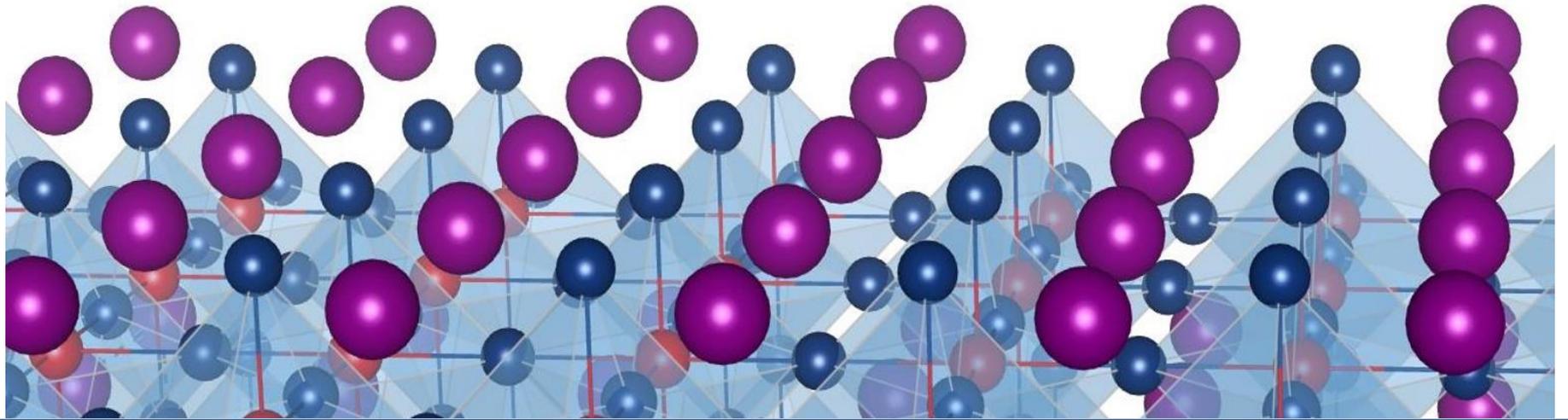
Decay Time

← time

# Differential decay times in passivated Si wafers



Richter et al. Phys. Rev. B **86**, 165202 (2012)



# PART 1: RECAP FROM HOPV 2022

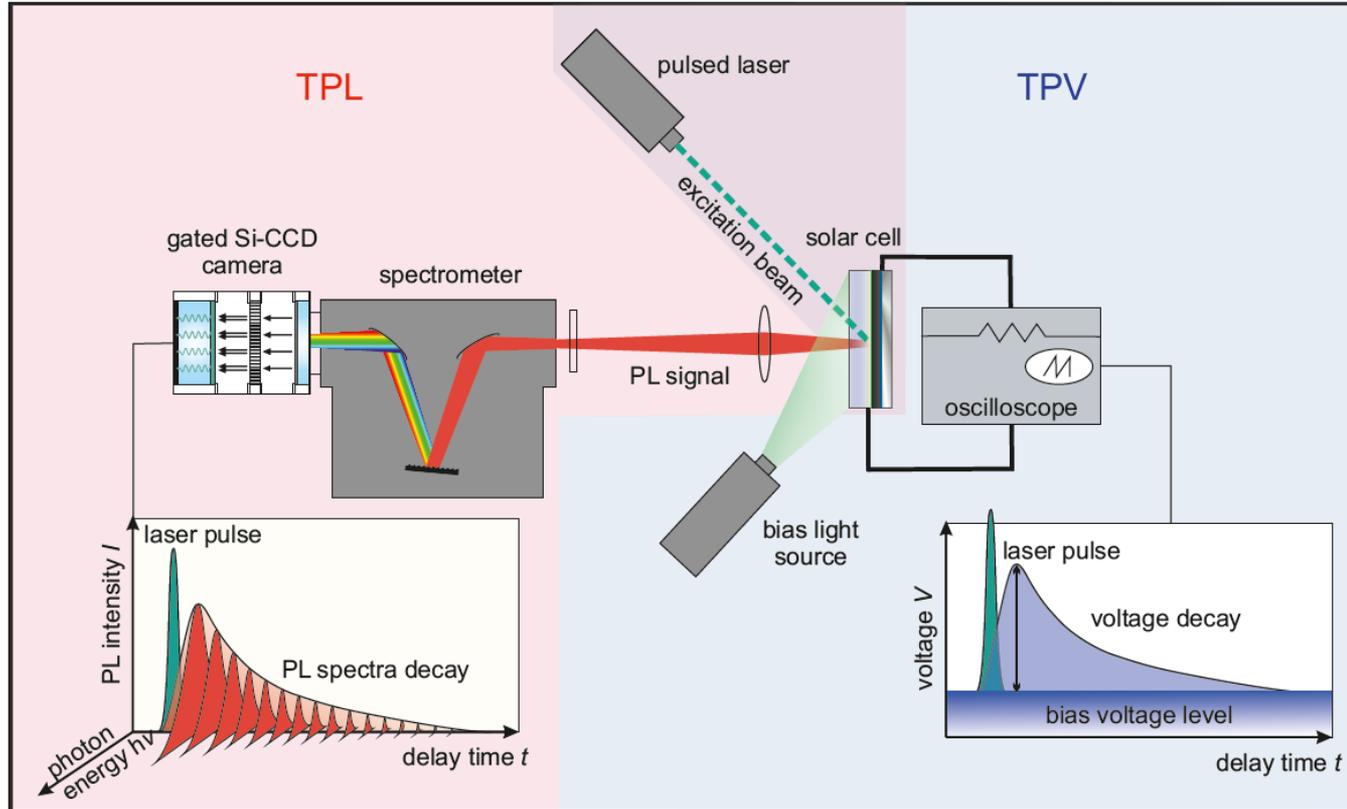
## TRANSIENT PHOTOVOLTAGE VS. PHOTOLUMINESCENCE

# Transient Photoluminescence (TPL)

# Transient Photovoltage (TPV)

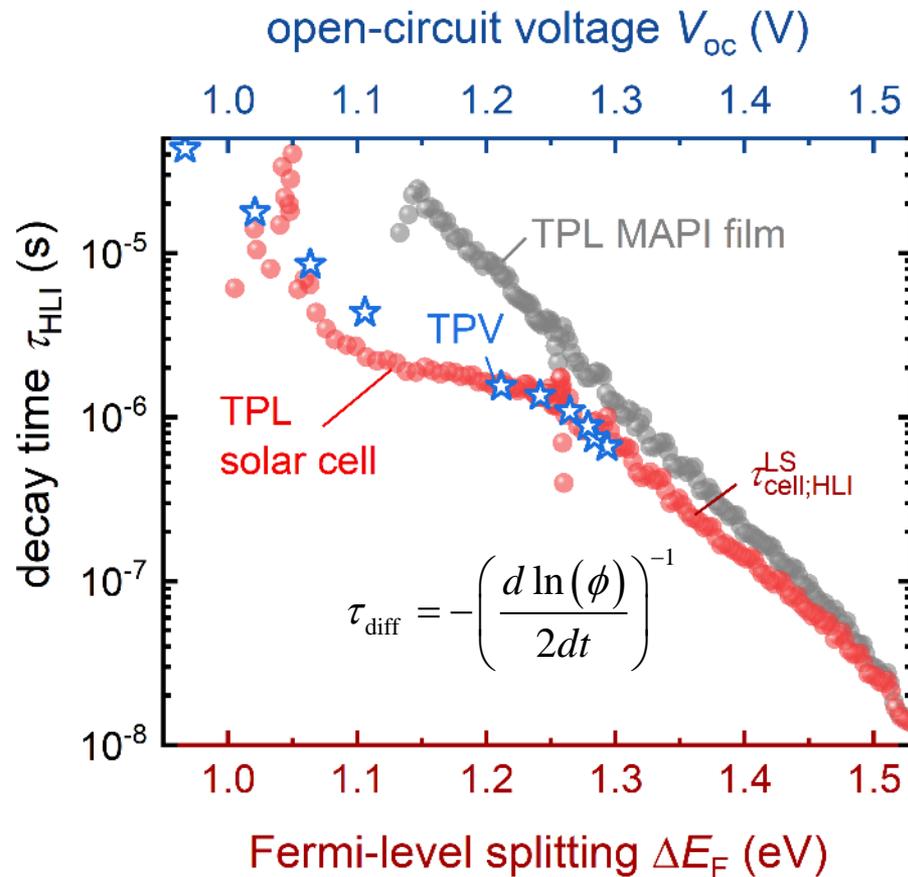
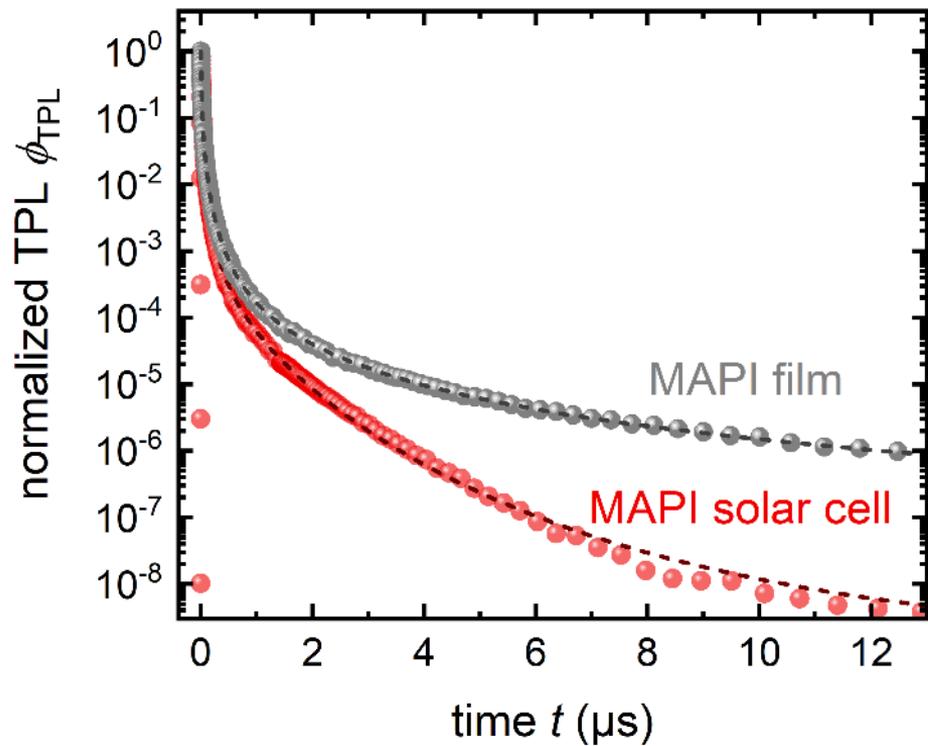
measures the luminescence decay

measures the decay of an external voltage

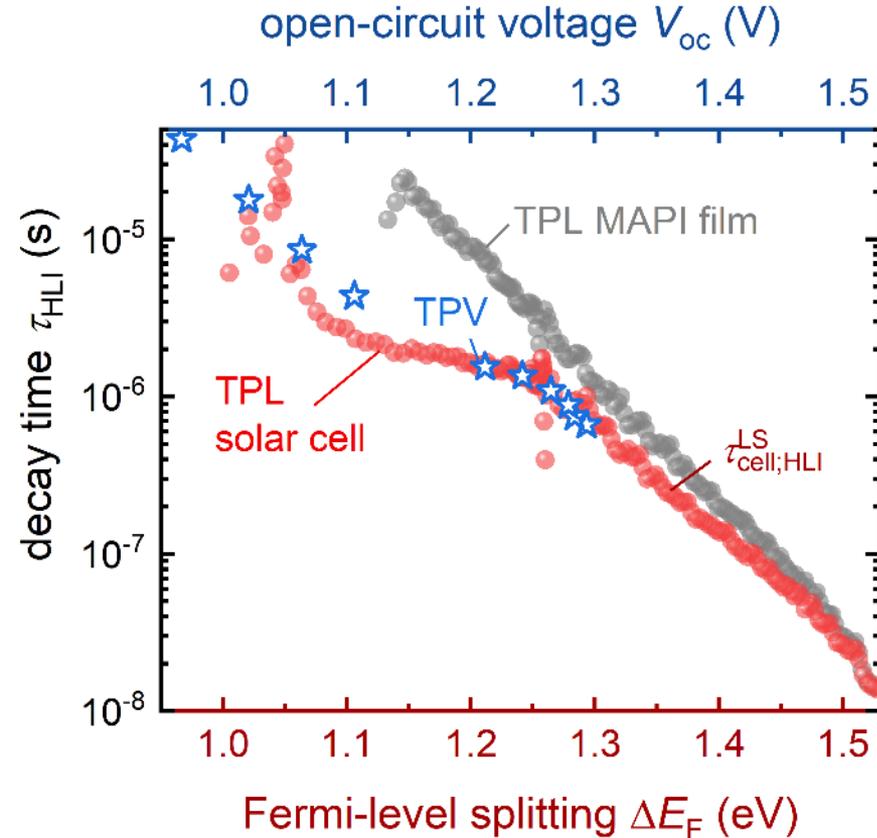


# Transient Photoluminescence

## Layer on Glass – Bulk Recombination



# How to make sense out of it

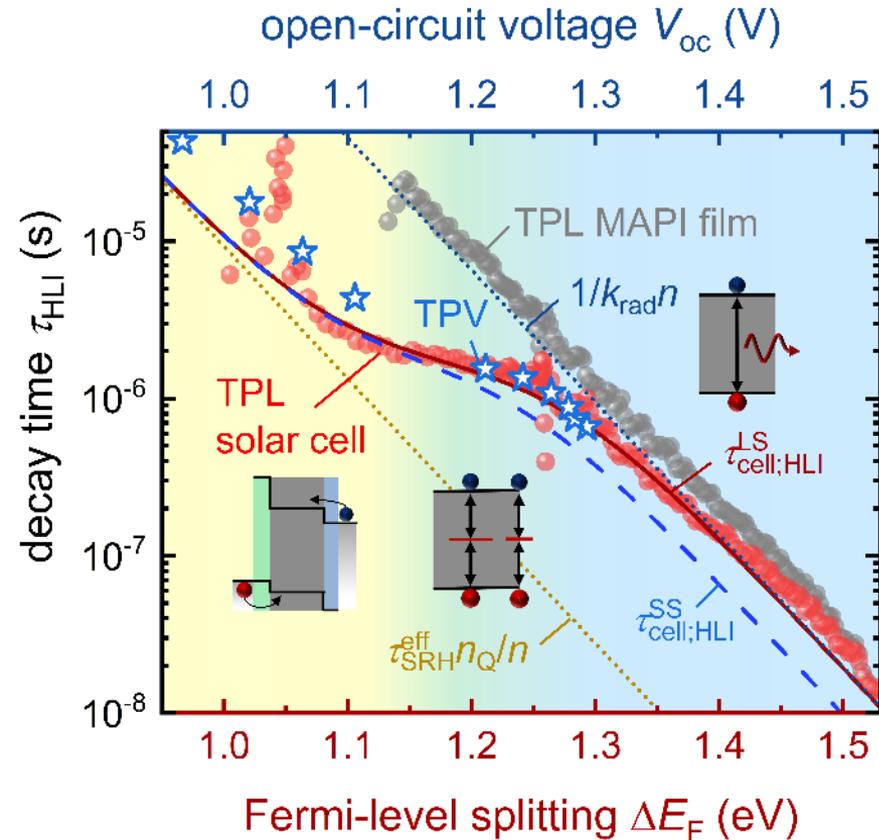


$$\frac{dn(t)}{dt} = -k_{rad}n(t)^2 - \frac{n(t)}{\tau_{SRH}^{bulk}} - \frac{C_{area}}{qd_{pero}} \frac{dV_{ext}(t)}{dt} + G$$

$$\tau_{cell,HLI}^{LS} = -\frac{n(t)}{dn(t)/dt} = \frac{n_Q/n(t)+1}{k_{rad}n(t)+1/\tau_{SRH}^{eff}}$$

$$n_Q = 2C_{area}k_B T / (q^2 d_{pero})$$

# How to make sense out of it

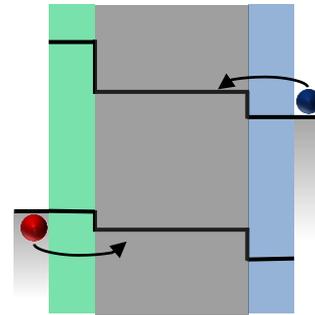


Capacitive discharging of the electrodes

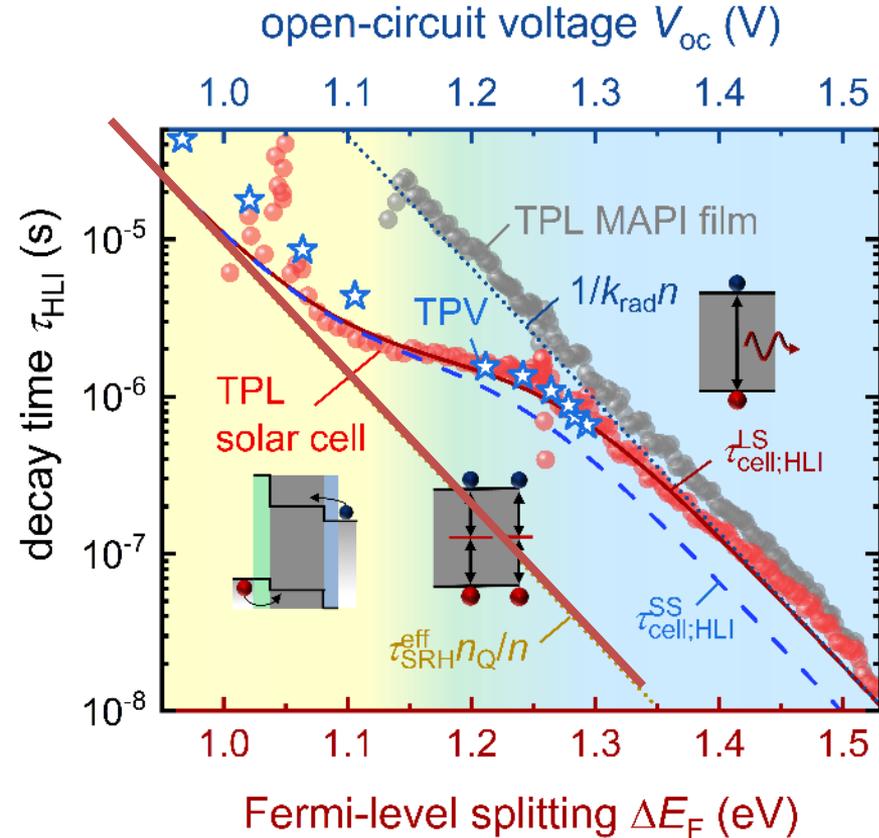
$$\frac{dn(t)}{dt} = -k_{rad}n(t)^2 - \frac{n(t)}{\tau_{SRH}^{bulk}} - \left[ \frac{C_{area}}{qd_{pero}} \frac{dV_{ext}(t)}{dt} \right] + G$$

$$\tau_{cell,HLI}^{LS} = -\frac{n(t)}{dn(t)/dt} = \frac{n_Q n(t) + 1}{k_{rad}n(t) + 1/\tau_{SRH}^{eff}}$$

$$n_Q = 2C_{area}k_B T / (q^2 d_{pero})$$



# How to make sense out of it

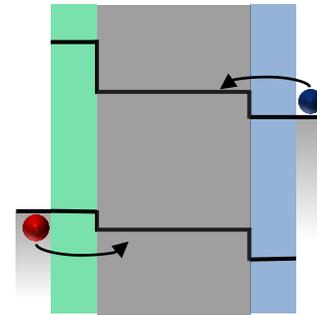


Capacitive discharging of the electrodes

$$\frac{dn(t)}{dt} = -k_{rad}n(t)^2 - \frac{n(t)}{\tau_{SRH}^{bulk}} - \frac{C_{area}}{qd_{pero}} \frac{dV_{ext}(t)}{dt} + G$$

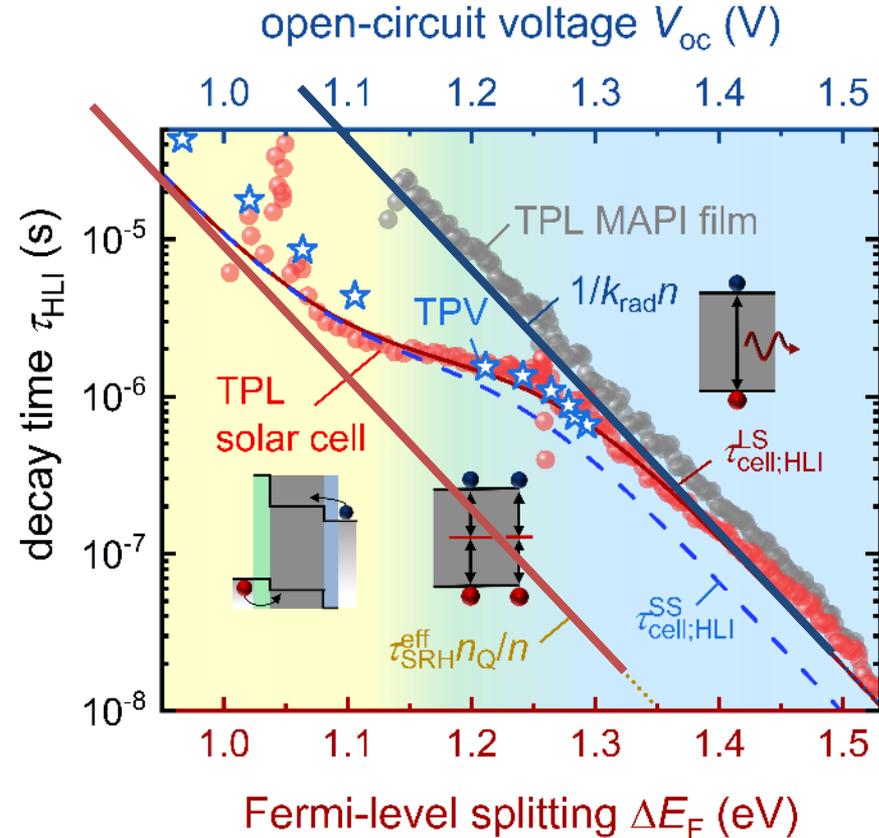
$$\tau_{cell,HLI}^{LS} = -\frac{n(t)}{dn(t)/dt} = \frac{n_Q n(t) + 1}{k_{rad}n(t) + 1/\tau_{SRH}^{eff}}$$

$$n_Q = 2C_{area}k_B T / (q^2 d_{pero})$$



Re-injection of carriers into the perovskite layer

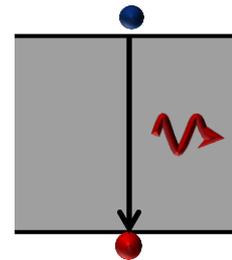
# How to make sense out of it



$$\frac{dn(t)}{dt} = -k_{rad}n(t)^2 - \frac{n(t)}{\tau_{SRH}^{bulk}} - \frac{C_{area}}{qd_{pero}} \frac{dV_{ext}(t)}{dt} + G$$

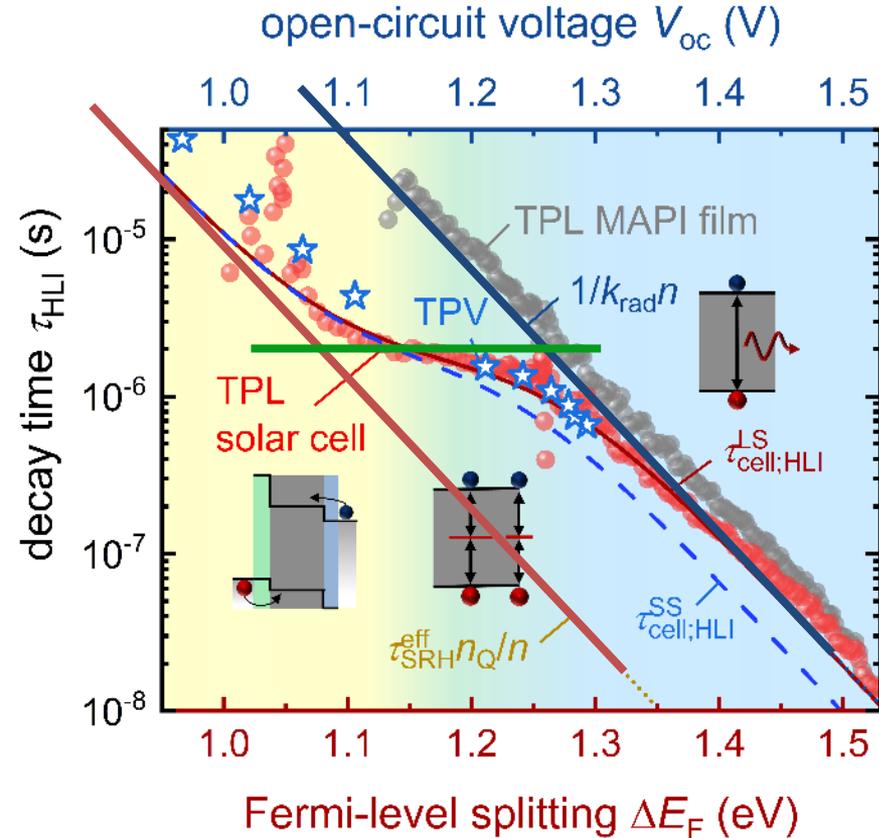
$$\tau_{cell,HLI}^{LS} = -\frac{n(t)}{dn(t)/dt} = \frac{n_Q n(t) + 1}{k_{rad}n(t) + 1/\tau_{SRH}^{eff}}$$

$$n_Q = 2C_{area}k_B T / (q^2 d_{pero})$$



Radiative recombination

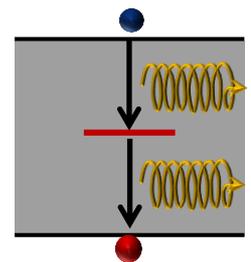
# How to make sense out of it



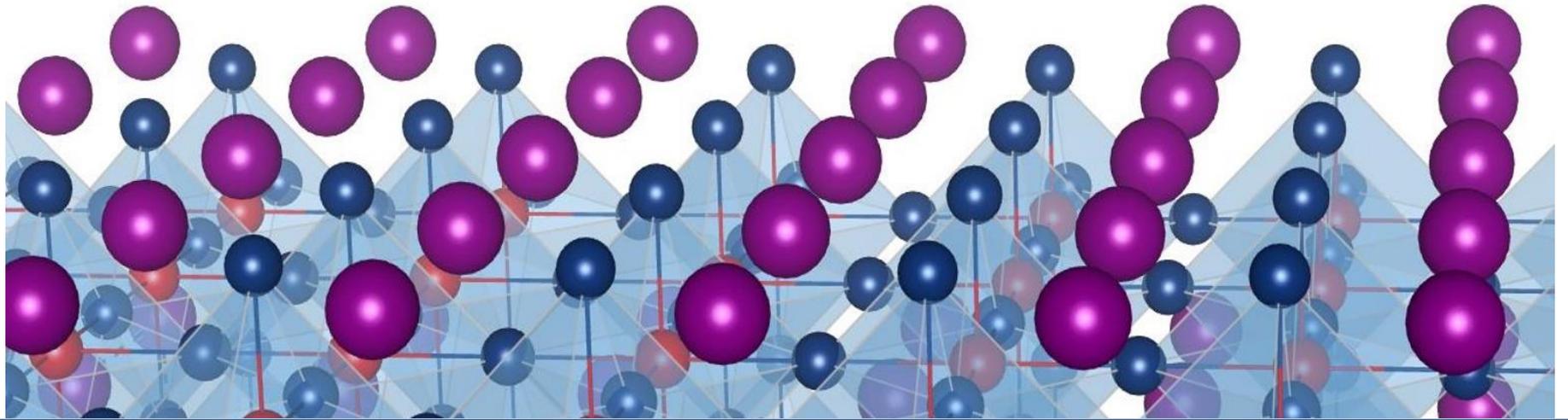
$$\frac{dn(t)}{dt} = -k_{rad}n(t)^2 - \frac{n(t)}{\tau_{SRH}^{bulk}} - \frac{C_{area}}{qd_{pero}} \frac{dV_{ext}(t)}{dt} + G$$

$$\tau_{cell,HLI}^{LS} = -\frac{n(t)}{dn(t)/dt} = \frac{n_Q/n(t)+1}{k_{rad}n(t)+1/\tau_{SRH}^{eff}}$$

$$n_Q = 2C_{area}k_B T / (q^2 d_{pero})$$



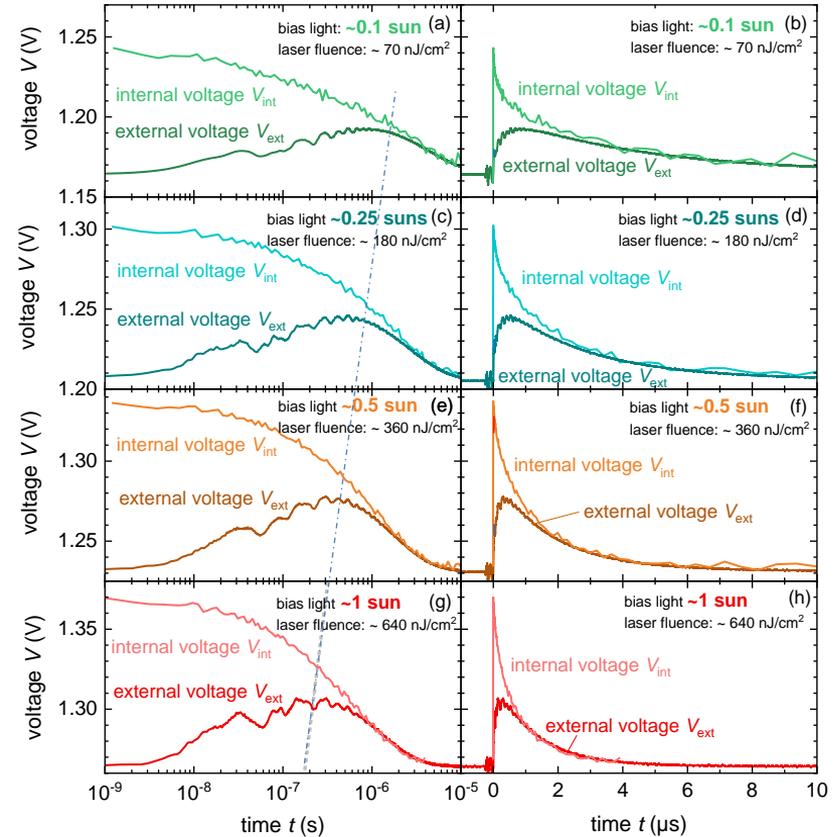
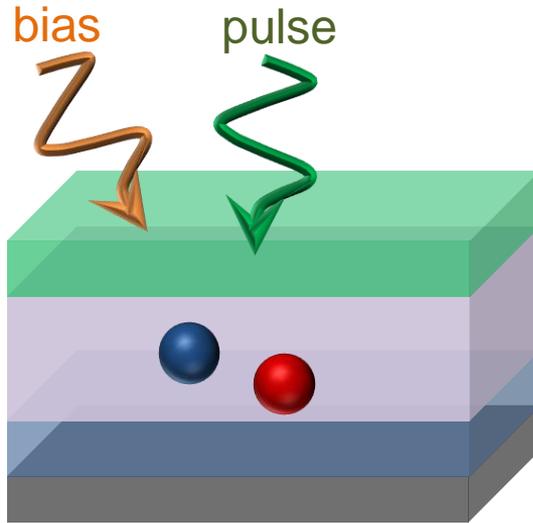
Shockley-Read-Hall recombination



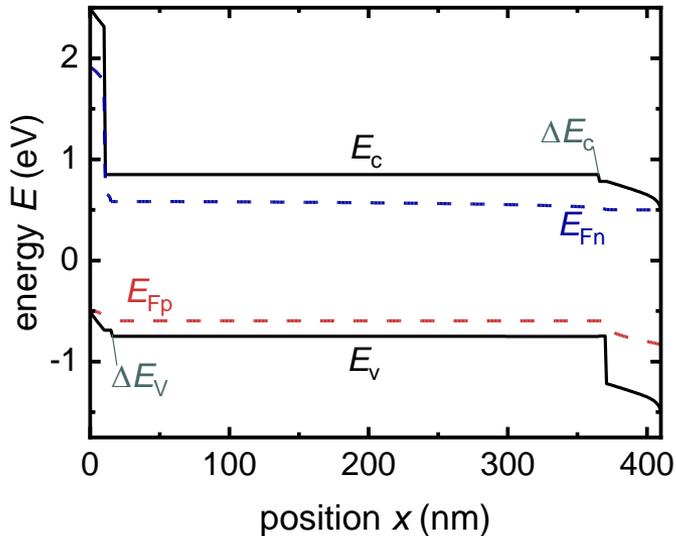
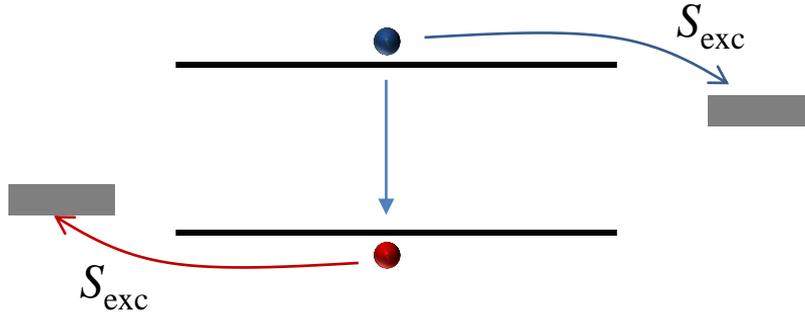
## PART 2: ANALYSIS OF SMALL SIGNAL MEASUREMENTS

### RECOMBINATION VS. EXTRACTION

# Experimental data – internal vs. external voltage



# Transient Methods – Recombination and Extraction



$$\frac{dn}{dt} = -k_{\text{rad}} n^2 - \frac{n}{\tau_{\text{SRH}}^{\text{eff}}} - \frac{S_{\text{exc}}}{d} \left( n - n_i \exp\left(\frac{qV_{\text{ext}}}{2kT}\right) \right) + G$$

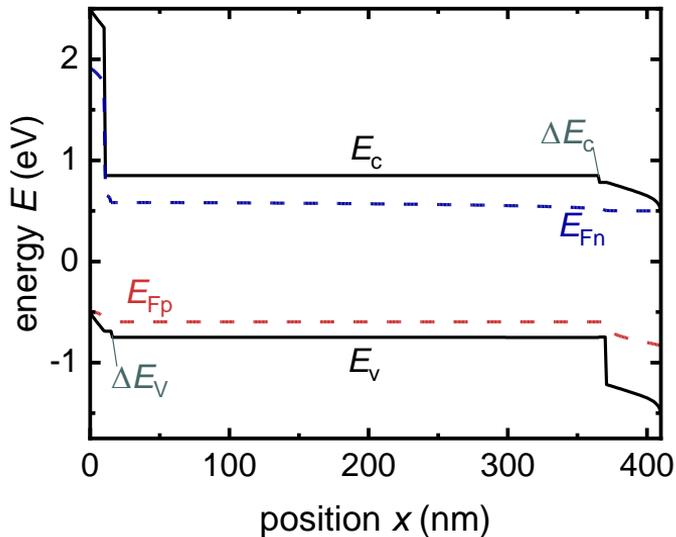
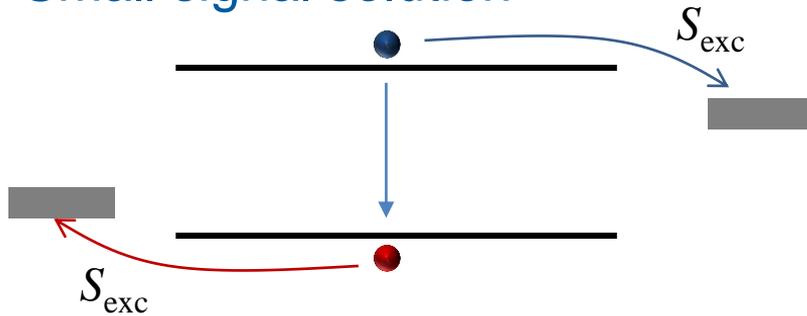
Recombination and extraction

$$\frac{dV_{\text{ext}}}{dt} = \frac{qS_{\text{exc}}}{C_{\text{area}}} \left( n - n_i \exp\left(\frac{qV_{\text{ext}}}{2kT}\right) \right)$$

Electrode (dis)charging

# Recombination and Extraction

## Small signal solution



$$\frac{d}{dt} \begin{pmatrix} \delta V_{\text{int}} \\ \delta V_{\text{ext}} \end{pmatrix} = \begin{pmatrix} -\left( \frac{1}{\tau_{\text{SRH}}^{\text{eff}}} + 2k_{\text{rad}} n_{\text{bias}} + \frac{S_{\text{exc}}}{d} \right) & \frac{S_{\text{exc}}}{d} \\ \frac{S_{\text{exc}} n_{\text{bias}}}{dn_Q} & -\frac{S_{\text{exc}} n_{\text{bias}}}{dn_Q} \end{pmatrix} \begin{pmatrix} \delta V_{\text{int}} \\ \delta V_{\text{ext}} \end{pmatrix}$$

$$\tau_{\text{rise}} = \frac{2}{k_1 + k_2 + k_3 + \sqrt{(k_1 + k_2 + k_3)^2 - 4k_1 k_3}}$$

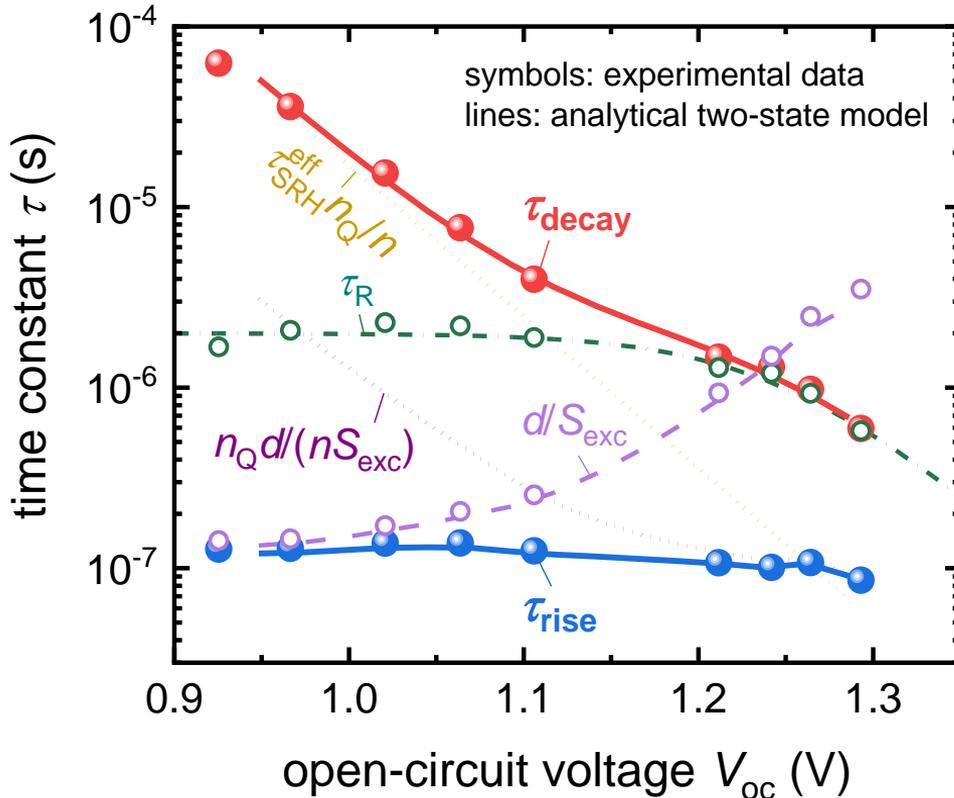
$$\tau_{\text{decay}} = \frac{2}{k_1 + k_2 + k_3 - \sqrt{(k_1 + k_2 + k_3)^2 - 4k_1 k_3}}$$

$$k_1 = \frac{1}{\tau_{\text{SRH}}^{\text{eff}}} + 2k_{\text{rad}} n_{\text{bias}}, \quad k_2 = \frac{S_{\text{exc}}}{d}, \quad k_3 = \frac{S_{\text{exc}} n_{\text{bias}}}{dn_Q}$$

Inverse Eigenvalues of Matrix

# Recombination and Extraction

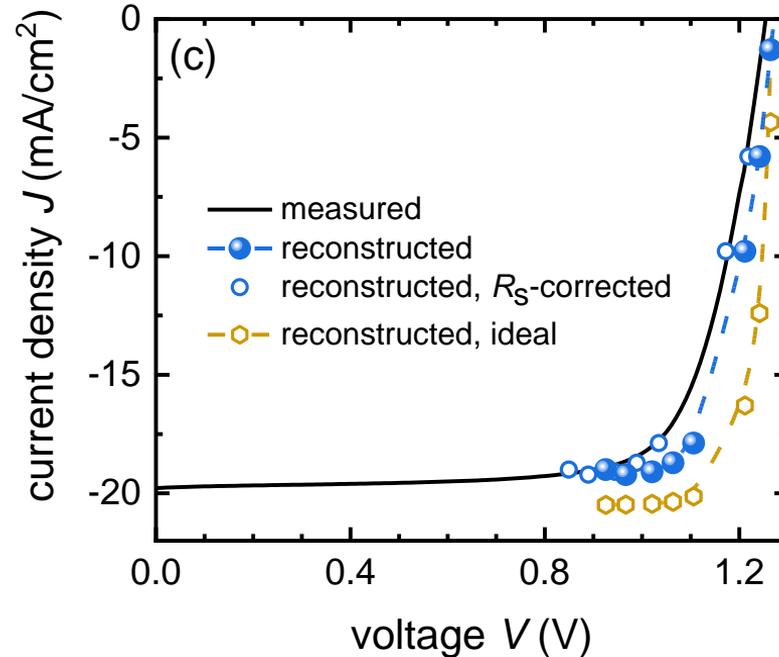
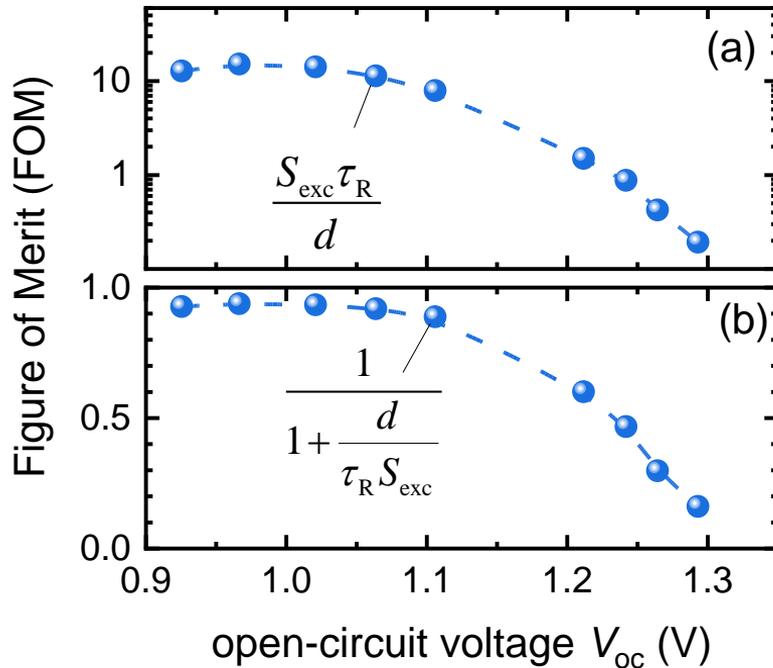
## Comparison with Experiment



$$\tau_{\text{decay}} \approx \frac{dn_{\text{Q}}}{S_{\text{exc}} n_{\text{bias}}} + \frac{\tau_{\text{R}} n_{\text{Q}}}{n_{\text{bias}}} + \tau_{\text{R}}$$

$$\tau_{\text{rise}} \approx \left( \frac{1}{\tau_{\text{R}}} + \frac{S_{\text{exc}}}{d} + \frac{S_{\text{exc}} n_{\text{bias}}}{dn_{\text{Q}}} \right)^{-1}$$

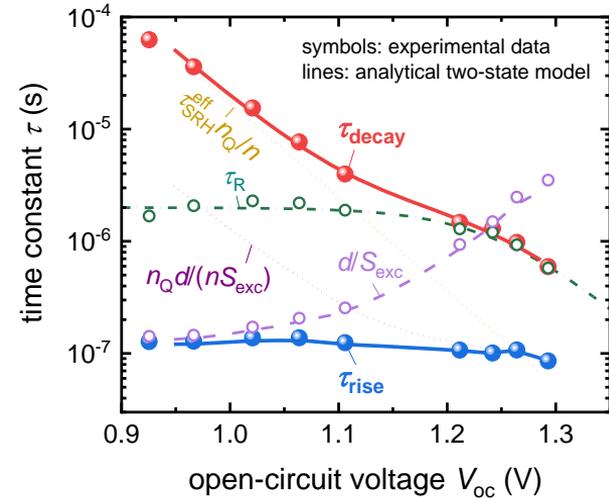
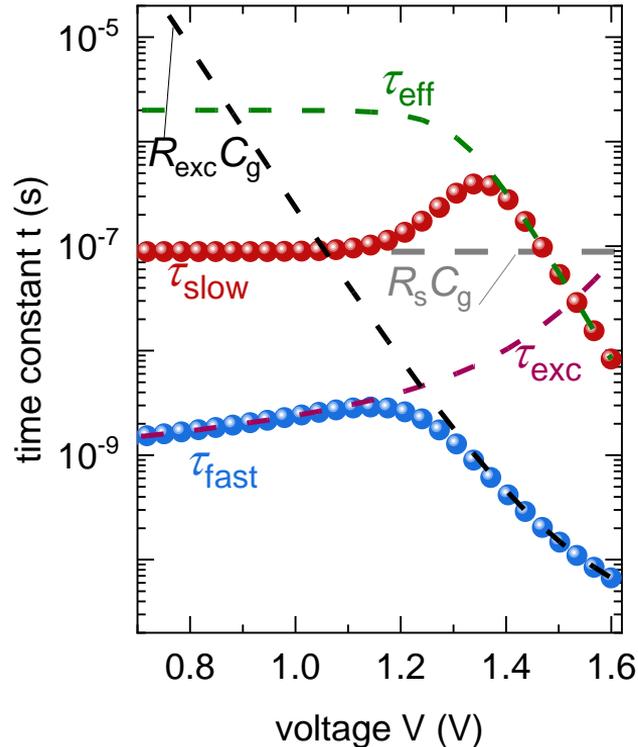
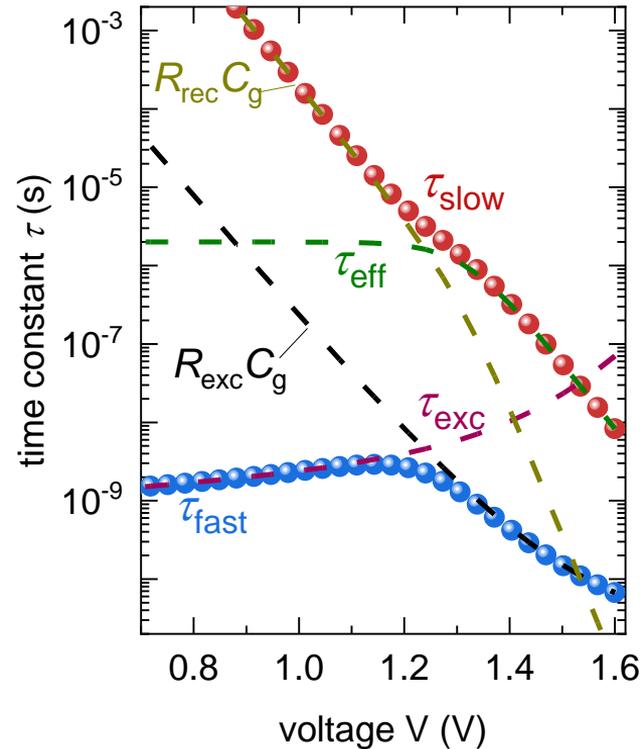
# Collection Efficiencies and Impact on $JV$ curves



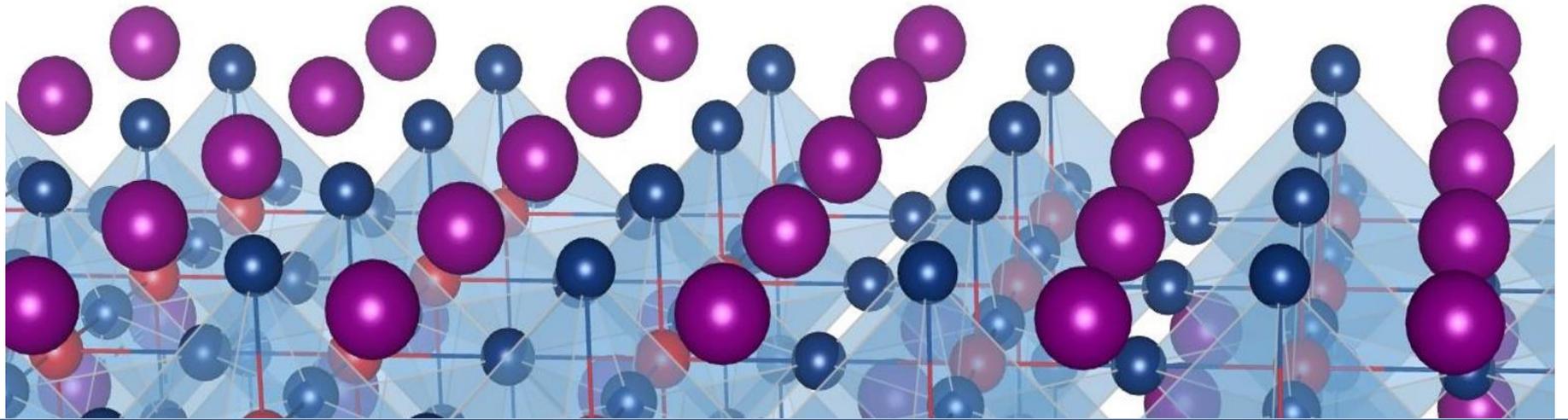
$$J = qd(R - G) = qd \left( \frac{1}{1 + d / (S_{exc} \tau_R)} \right) \left[ \frac{n_0}{\tau_R} \exp \left( \frac{qV_{ext}}{2k_B T} \right) - G \right]$$

# Frequency-Domain Methods

simulated data (freq. domain)

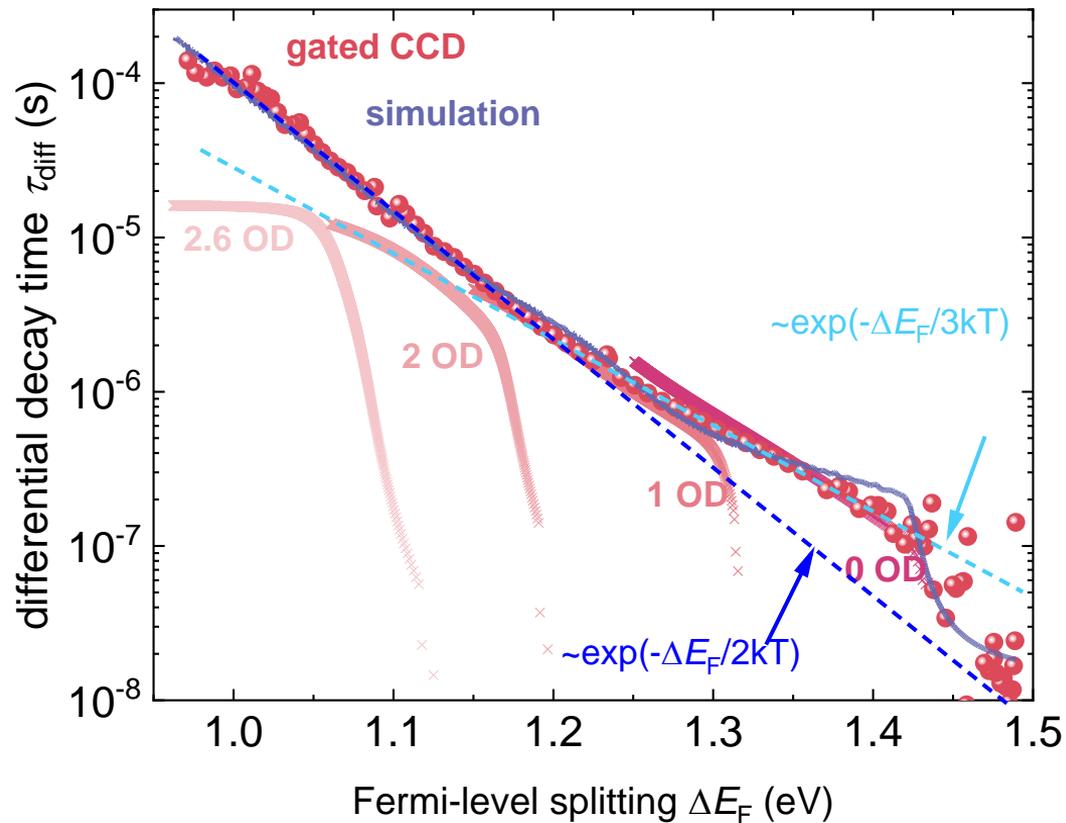
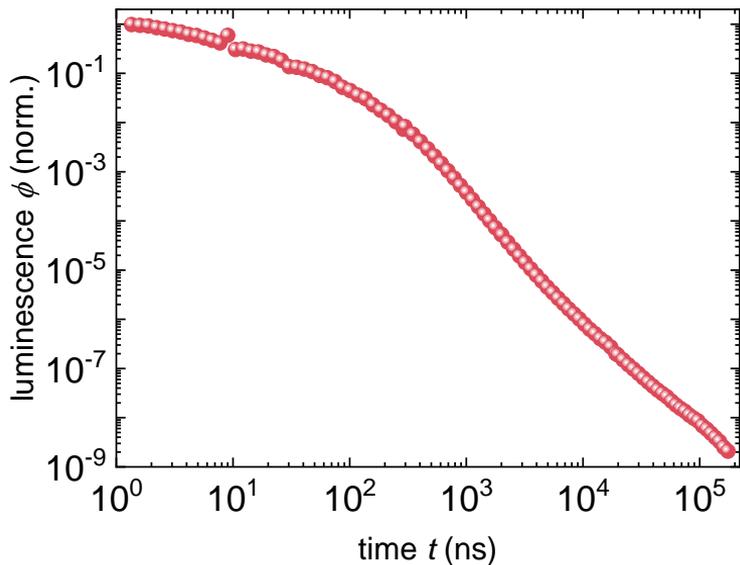


Experimental data  
(time domain)

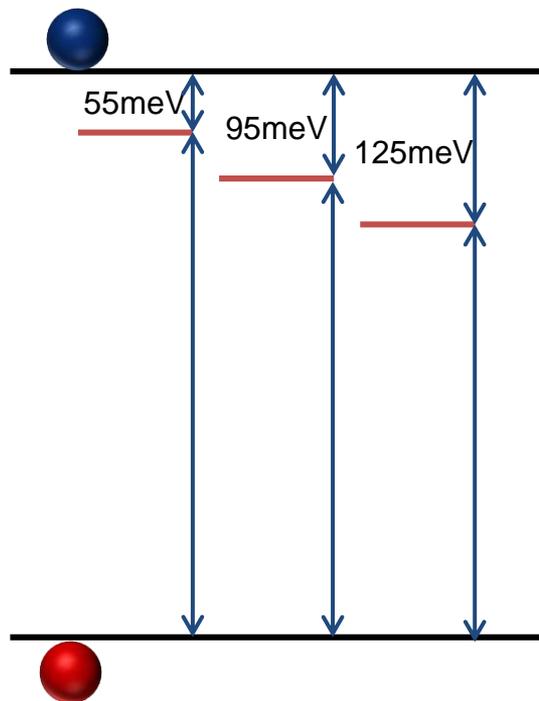


## PART 3: SHALLOW DEFECTS AND HOW THEY CHANGE THE SITUATION

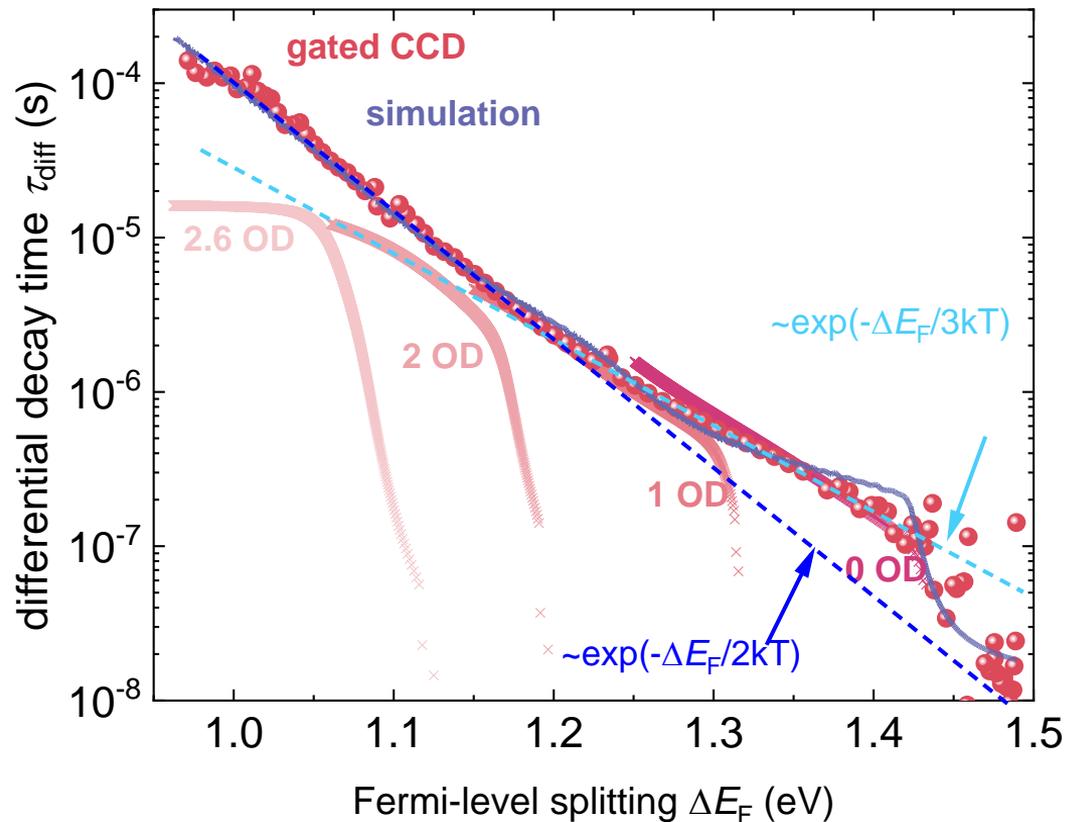
# High dynamic range tr-PL



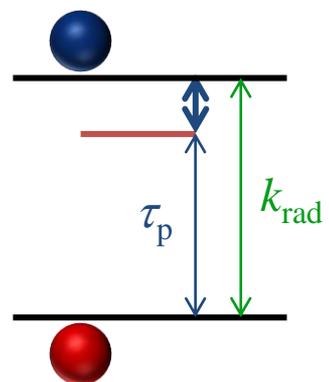
# Defect levels assumed in the modelling



schematic not quite to scale

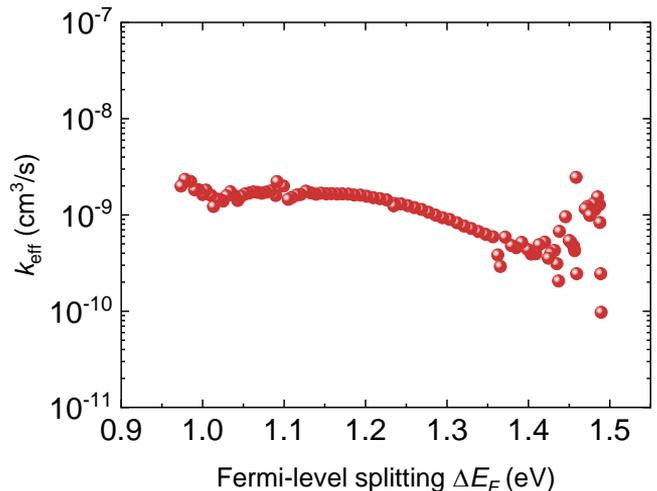
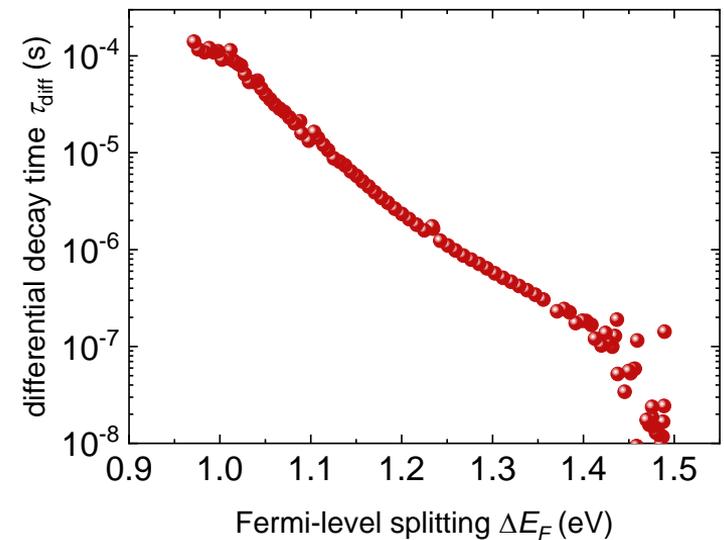


# On the presence or absence of deep defects

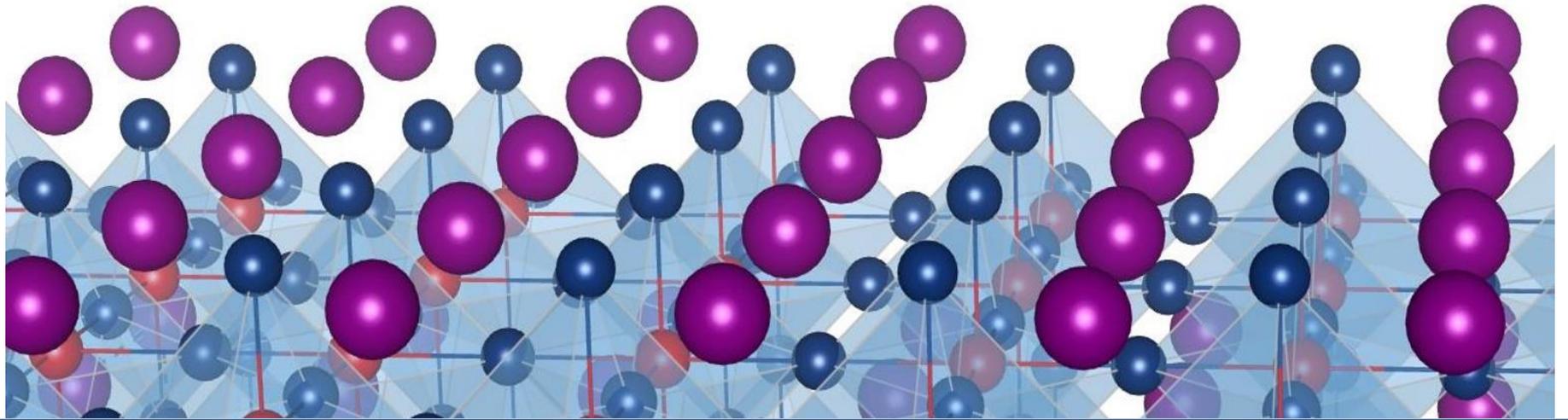


$$\tau_{\text{diff}} \approx \tau_p \sqrt{\frac{n_1 N_T}{np}} \frac{1}{1 + k_{\text{rad}} \tau_p n_1}$$

$$n_1 = N_C \exp\left(-\frac{E_C - E_T}{kT}\right)$$

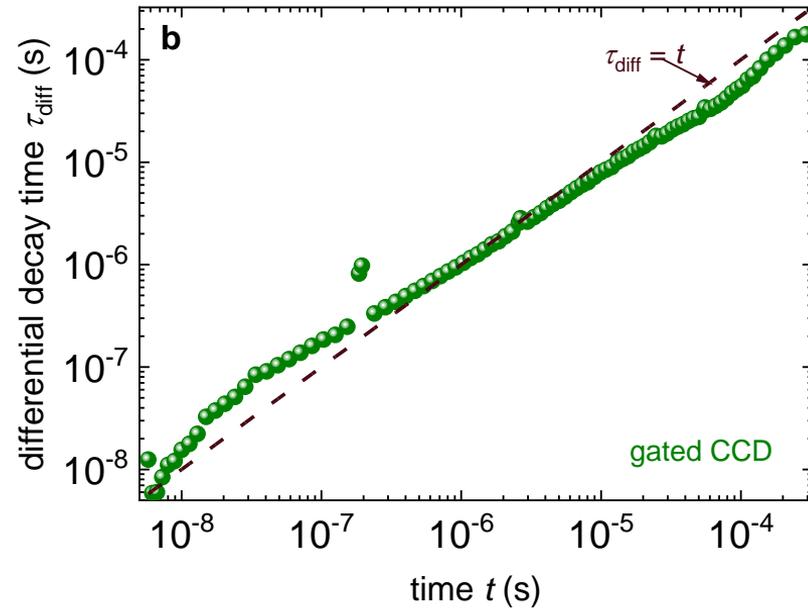
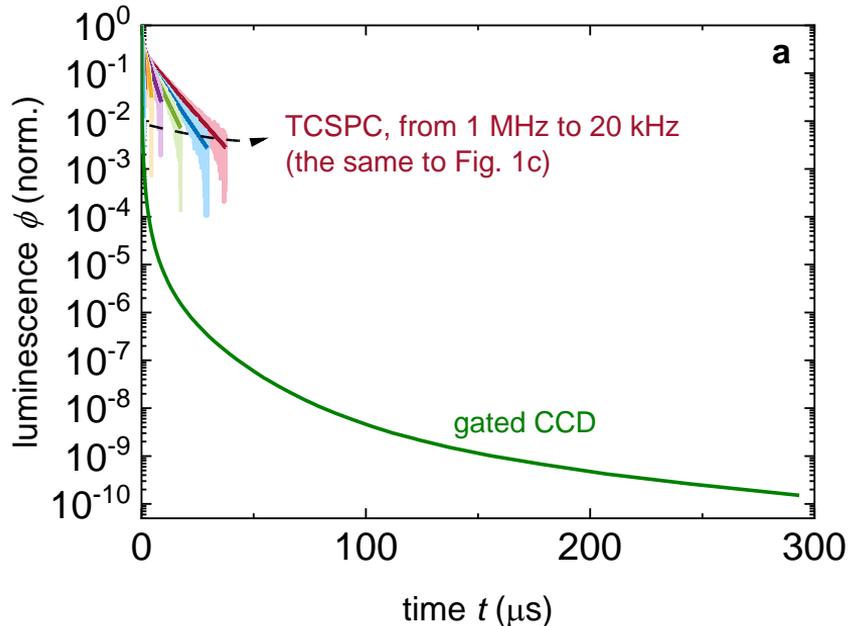


$$k_{\text{diff}} \approx \frac{1 + k_{\text{rad}} \tau_p n_1}{\tau_p \sqrt{n_1 N_T}}$$



## PART 4: REPETITION RATES AND HOW THEY AFFECT DECAY TIMES

# Why $\tau = t$ can be a decent approximation

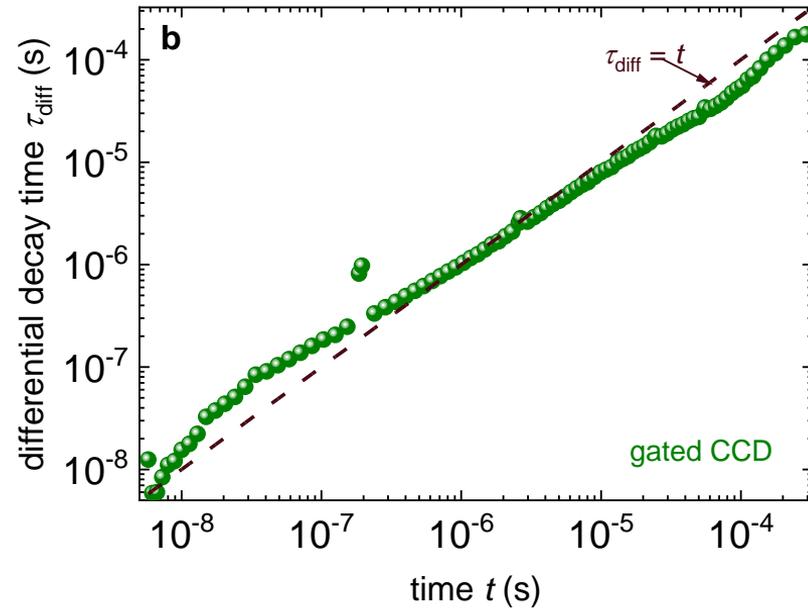
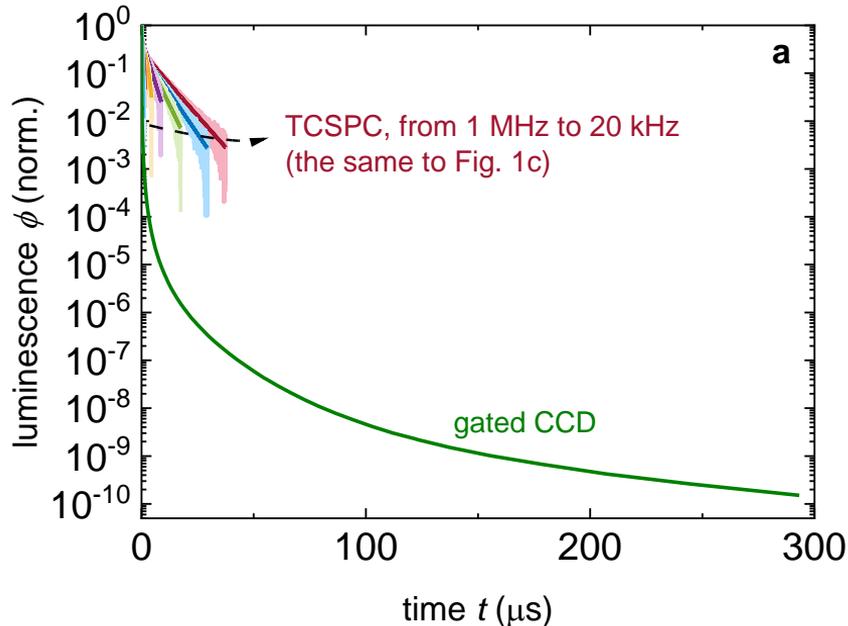


$$\frac{dn(t)}{dt} = -kn^2$$

$$\tau_{\text{diff}} = (kn(t))^{-1}$$

$$n(t) = \frac{n(0)}{1 + n(0)kt} \approx 1/(kt)$$

# Why $\tau = t$ can be a decent approximation



$$\frac{dn(t)}{dt} = -kn^2$$

$$\tau_{\text{diff}} = (kn(t))^{-1}$$

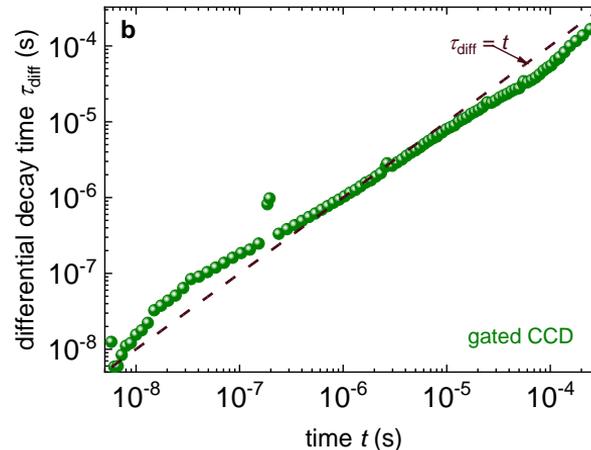
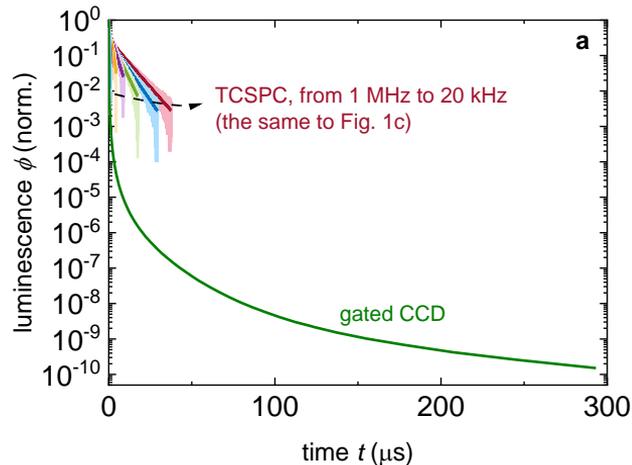
$$\tau_{\text{diff}} = t$$

$$n(t) = \frac{n(0)}{1 + n(0)kt} \approx 1/(kt)$$

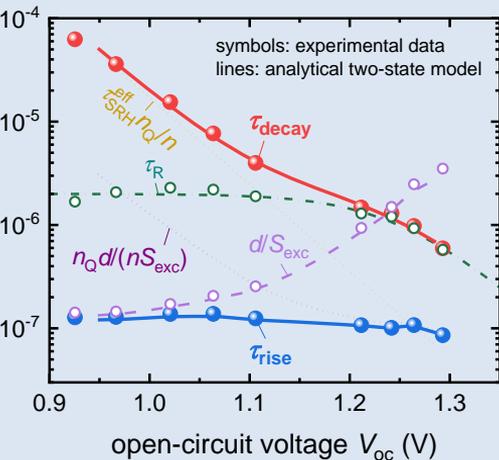
# Summary

If a sample is intrinsic, the following holds:

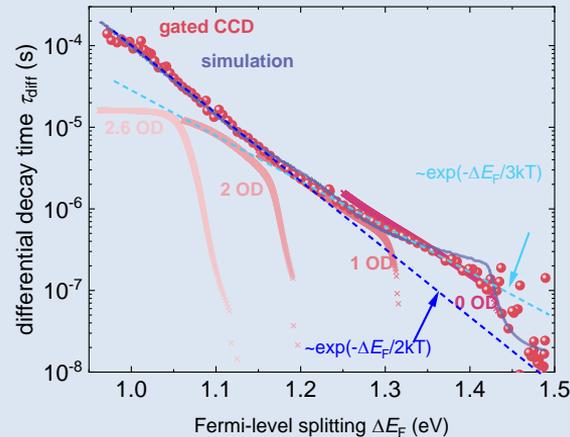
- Every decay not dominated by a deep defect will lead to non-exponential decays.
- Those are often similar to radiative recombination (even if they are not)
- They will automatically lead to  $\tau_{\text{diff}} \approx t$  implying that decay times determined towards the end of a decay are  $\sim$  the inverse repetition rate.



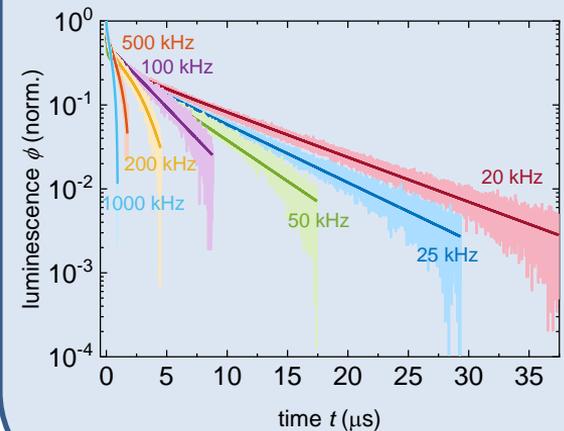
1) Rise and decay times  $\rightarrow$  recombination and extraction times



2) Lifetime loses meaning. Effective k might be more useful.



3)  $\tau \sim 1/f_{\text{rep}}$  is a risk to consider.

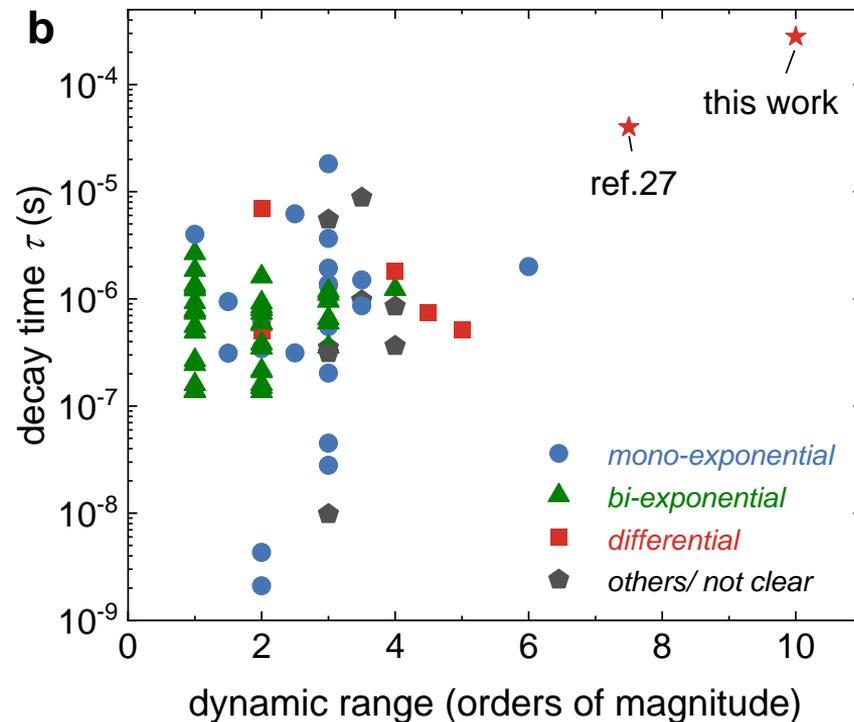
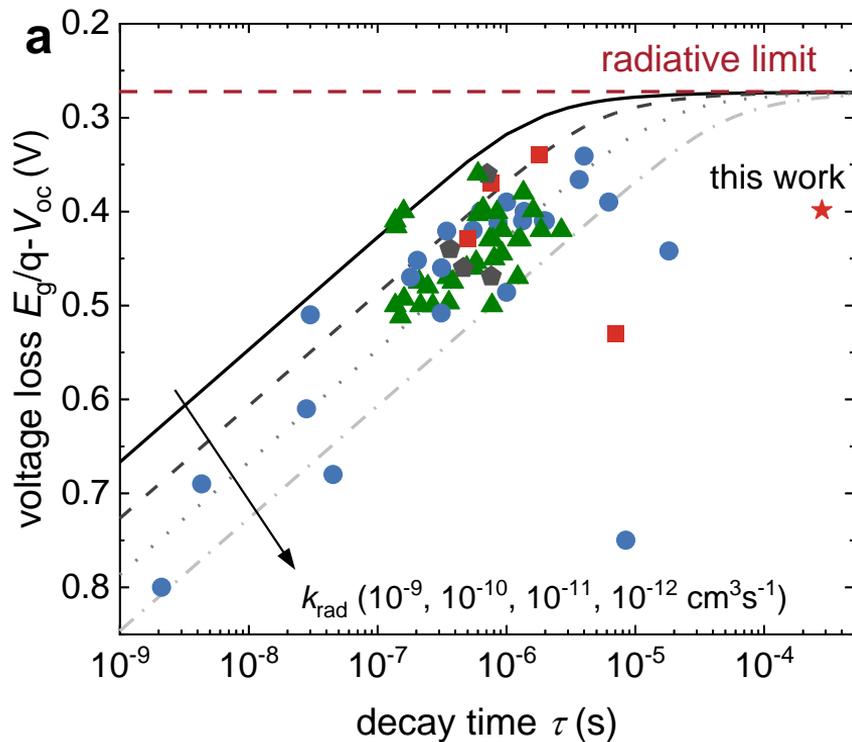




**Funding from**  
Helmholtz Association  
DFG  
OCPC Fellowships

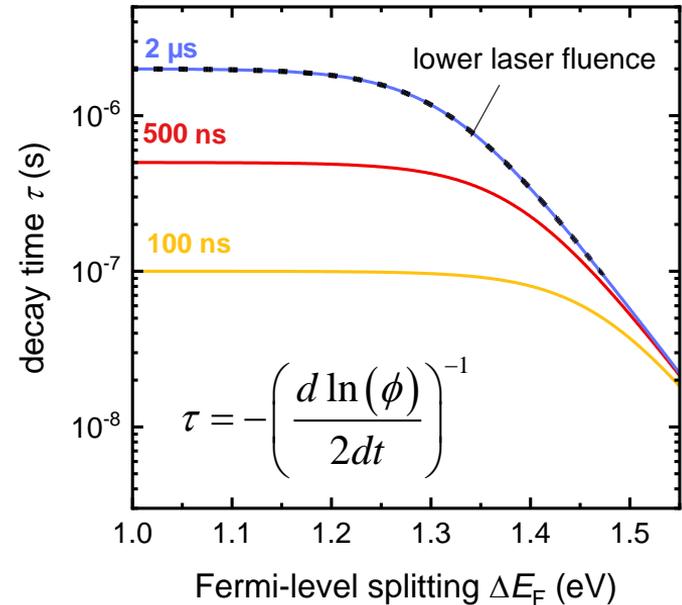
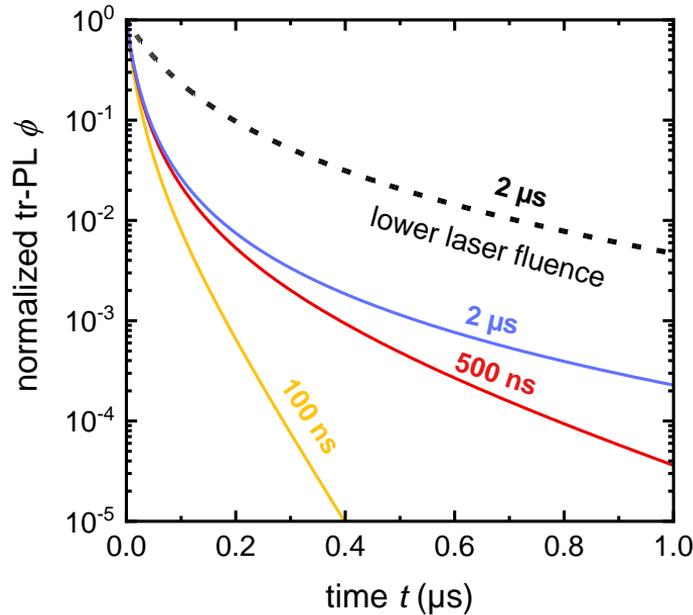
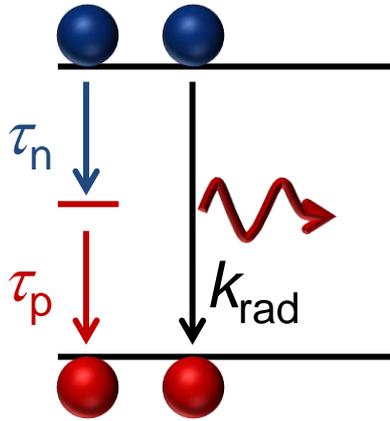
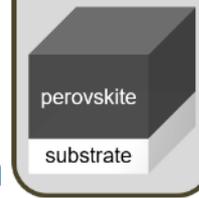
**Thank you for your attention**

# The importance of dynamic range



# Transient Photoluminescence

## Layer on Glass – Bulk Recombination



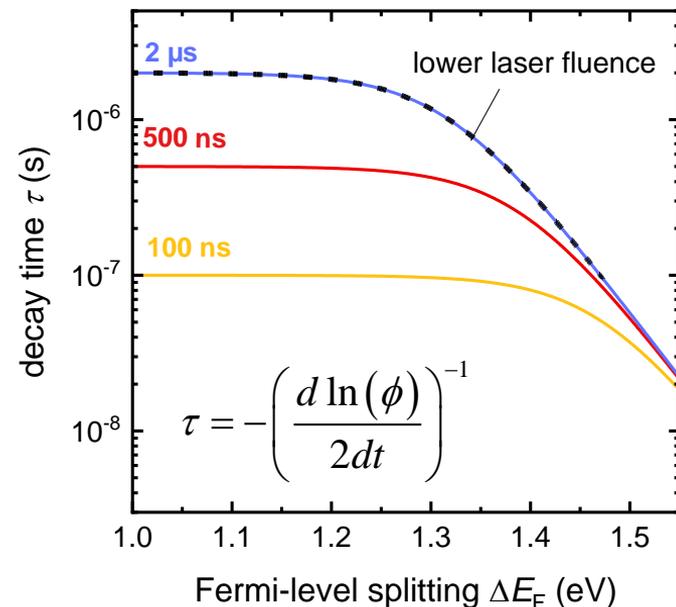
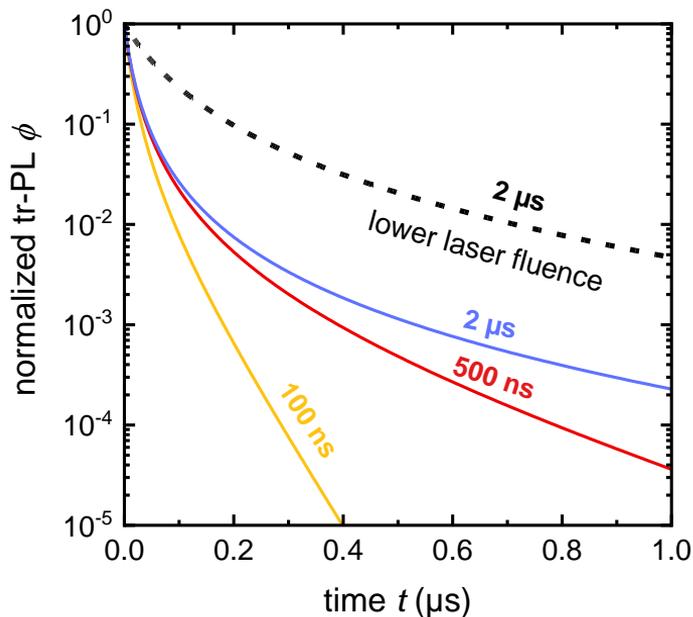
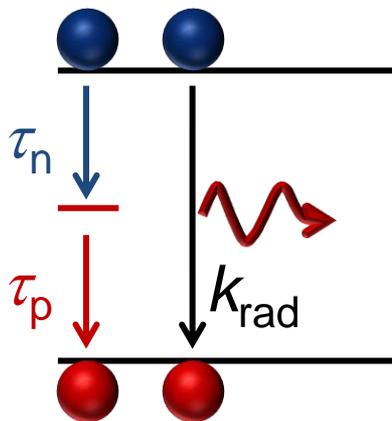
$$\frac{dn}{dt} = -k_{\text{rad}} n^2 - \frac{n}{\tau_p + \tau_n}$$

SRH + radiative recombination

← time

# Transient Photoluminescence

## Layer on Glass – Bulk Recombination



$$\tau_{\text{diff}} = -\frac{n}{dn/dt} = \frac{1}{k_{\text{rad}}n + \tau_p + \tau_n}$$

Decay Time

