

## Letter

# Constraining the $p\Lambda$ interaction from a combined analysis of scattering data and correlation functions

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## ABSTRACT

This work provides the first combined analysis of low-energy  $p\Lambda$  scattering, considering both cross section and correlation data. The obtained results establish the most stringent constraints to date on the two-body  $p\Lambda$  interaction, pointing to a weaker attraction than so far accepted. The best set of scattering lengths for the spin singlet and triplet are found to range from  $f_0, f_1 = (2.1, 1.56)$  to  $(3.34, 1.18)$  fm. With a chiral NY potential fine-tuned to those scattering parameters, the in-medium properties of the  $\Lambda$  are explored and a potential depth of  $U_\Lambda = -36.3 \pm 1.3(\text{stat})_{-6.2}^{+2.5}(\text{syst})$  MeV is found at nuclear matter saturation density.

## 1. Introduction

The strong interaction between nucleons (N) and hyperons ( $Y = \Lambda, \Sigma, \Xi$ ) plays a significant role in various aspects of nuclear and hadronic physics, ranging from the structure and properties of hypernuclei to the Equation of State (EoS) of neutron star (NS) matter [1,2]. The recent observations of gravitational waves emitted from NS mergers [3,4] and precise constraints on NS radii provided by the NICER collaboration [5–8] triggered a renewed interest in the presence of strange degrees of freedom in these compact objects [9,10].

Specifically, the  $N\Lambda$  system represents an important pillar for our understanding of the low-energy QCD dynamics between ordinary matter and strange particles [11]. Chiral effective field theory ( $\chi$ EFT) [12–15] is an excellent tool to study the  $N\Lambda$  interaction, since it offers the possibility to systematically improve the results by considering higher-order terms in the Lagrangian. These effective approaches rely on the availability of experimental data to determine the a priori unknown low-energy constants (LECs) associated with the contact interactions included in the Lagrangian. Until recently, the experimental constraints on the  $N\Lambda$  interaction, and, in general, on the strangeness  $S = -1$  baryon-baryon interaction, consisted primarily of scattering data [16–18] and measurements of  $\Lambda$ -hypernuclei binding energies [1,19]. Elastic and inelastic cross section data, probing the transition  $N\Lambda \leftrightarrow N\Sigma$ , are relatively scarce and not available down to the threshold. Results from the COSY experiment delivered input on

the  $N\Lambda - N\Sigma$  dynamics by studying the  $pp \rightarrow pK^+\Lambda$  reaction [20,21]. New scattering measurements on both  $N\Lambda$  and  $N\Sigma$  were reported by the CLAS [22] and E40 [23–25] collaborations, adding constraints at higher momenta. Additionally, measured binding energies and lifetimes of light  $\Lambda$ -hypernuclei [1] provide complementary information on the strength of the  $N\Lambda$  interaction, for example with regard to the hypertriton [26,27] specifically on the singlet state [14].

Data on hypernuclei in the medium and heavy mass regime have been employed to deduce the depth of the  $\Lambda$  single-particle potential  $U_\Lambda$  in infinite nuclear matter at nuclear saturation density  $\rho_0 = 0.166 \text{ fm}^{-3}$ . An overall attraction of  $-27 \sim -30$  MeV is typically reported [1,28–30], and this benchmark eventually serves as input for studies aiming to infer the behavior of  $\Lambda$  hyperons at NS core densities, reaching few times  $\rho_0$ . Specifically, in microscopic investigations that commence with NY potentials describing  $N\Lambda$  and  $N\Sigma$  scattering data, the generally somewhat too attractive contribution from the two-body interaction is counterbalanced by an appropriate repulsive three-body NNA component to meet the  $\approx -30$  MeV constraint [31,32]. The interplay between two- and three-body contributions is also considered in a recent phenomenological analysis of  $\Lambda$ -hypernuclei [30].

In the last years, novel data based on two-particle correlations, involving strange hadrons, have become available and offer high-precision experimental insight into the  $S = -1, -2, -3$  baryon-baryon interaction [33–39]. The recent measurement of the  $p\Lambda$  correlation function in  $pp$  collisions at  $\sqrt{s} = 13$  TeV by the ALICE Collabora-

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tion [34] provided the most precise data on this system down to threshold, accompanied by the first experimental observation of the opening of the  $N\Sigma$  channel in a two-body final state. Ongoing and future experimental efforts are posed to advance our understanding of the  $N\Lambda$  interaction and the  $N\Lambda \leftrightarrow N\Sigma$  dynamics. These efforts include the utilization of polarized  $\Lambda$  beams and high-precision hypernuclear spectroscopy [40], as well as statistically improved correlation functions during the ongoing LHC Run 3 data taking [41].

In this work, we, for the first time, perform a combined analysis of available  $N\Lambda$  scattering and correlation data to constrain the corresponding  $p\Lambda$  scattering parameters. The present study utilizes an Usmani-type potential and an interaction based on  $\chi$ EFT. Anticipating our main finding, the analysis suggests an overall less attractive  $N\Lambda$  interaction compared to what has formed the basis for theoretical investigations so far. To explore the possible implications for the  $N\Sigma$  scenarios [31,32], appropriately re-adjusted chiral potentials are employed to evaluate the single-particle potential  $U_\Lambda$  at  $\rho_0$ .

## 2. $p\Lambda$ interaction

For the analysis of the  $p\Lambda$  correlation data at low momenta, we employ wave functions generated from two different types of potentials. To thoroughly explore the sensitivity of the effective range parameters to the measured  $p\Lambda$  correlation functions, we use the Usmani potential [42], which includes spin dependence but lacks coupling to the  $N\Sigma$  channel. This allows for a realistic description of the  $N\Lambda$  interaction below the  $N\Sigma$  threshold, which is relevant for determining the effective range parameters. We use the expression for the potential given in Ref. [43]:

$$V_{p\Lambda}(r) = V_C(r) - \left( \bar{V} - \frac{1}{4} V_\sigma \sigma_\Lambda \cdot \sigma_p \right) T_\pi^2(r). \quad (1)$$

The short range part of the interaction is dominated by a Woods-Saxon-type repulsive core  $V_C$ , while the long-range part of the interaction is modeled by a two-pion exchange tail constructed from a modified one-pion exchange tensor potential [43],

$$T_\pi(r) = \left( 1 + \frac{3}{x} + \frac{3}{x^2} \right) \frac{e^{-x}}{x} \left( 1 - e^{-cr^2} \right)^2, \quad (2)$$

where  $x = m_\pi r \approx 0.7r$ . We take over the parameters from [43], i.e. we use  $c = 2 \text{ fm}^{-2}$  together with  $\bar{V} = 6.2 \text{ MeV}$  and  $V_\sigma = 0.25 \text{ MeV}$ , for the spin-independent part of the attractive potential and the spin-dependent part respectively. The expression for the repulsive core is

$$V_C(r) = W_C \left[ 1 + \exp \left( \frac{r - R_C}{d_C} \right) \right]^{-1}. \quad (3)$$

Its parameters ( $W_C$ ,  $R_C$ ,  $d_C$ ) are phenomenological in nature, and thus, we will adjust them in accordance with the analyzed data. Specifically, we will vary them independently for the two  $N\Lambda$  spin states when exploring the spin dependence in detail, see below.

In addition, we employ a modern NY potential derived within SU(3)  $\chi$ EFT [13,14], specifically, we utilize the NY potential NLO19 established in Ref. [14]. This potential incorporates contributions up to next-to-leading order (NLO) in the chiral expansion, in particular it includes contributions from one- and two-pseudoscalar-meson exchange diagrams, involving the Goldstone bosons  $\pi$ ,  $K$ ,  $\eta$ , and from four-baryon contact terms (without and with two derivatives), where the latter encode the unresolved short-distance dynamics. The LECs associated with these contact terms are free parameters and have been established by a global fit to a set of 36  $p\Lambda$  and  $N\Sigma$  low energy scattering data points [14], available since the 1960s. SU(3) flavor symmetry has been imposed which reduces the number of independent contact terms or LECs, respectively. Then, in the two  $S$ -wave states  $^1S_0$  and  $^3S_0$ , which dominate the scattering observables at low energies, there are 10 LECs [14], with two of them inferred from the NN sector via the imposed SU(3) symmetry.

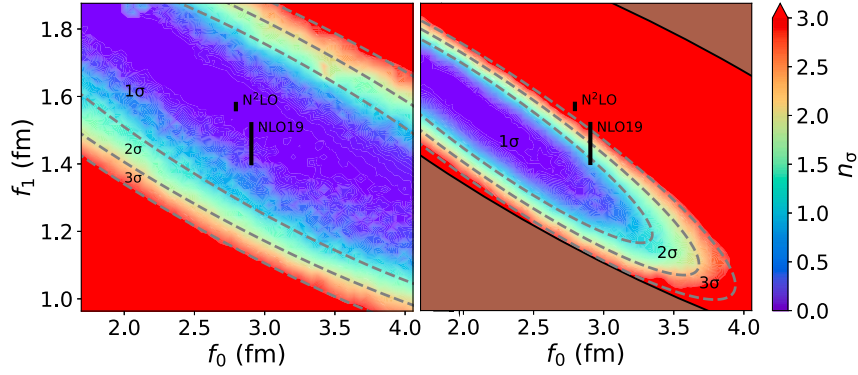
The present work incorporates the  $p\Lambda$  correlation data measured by ALICE as an additional experimental constraint [44]. To accommodate this, some of the LECs have to be varied in the search for the optimal strength of the  $N\Lambda$  interaction. Thereby, we aim at preserving the good description of the  $p\Sigma^+$  and  $p\Sigma^-$  data, as well as the  $p\Sigma^- \rightarrow n\Lambda$  transition cross section provided by the original potential [14]. The simplest and most efficient way to guarantee this is to relax the strict SU(3) symmetry for the contact interactions in the  $N\Lambda$  and  $N\Sigma$  forces [13,14]. Therefore, following the procedure in [45], we introduce an SU(3) symmetry breaking in the leading-order contact terms that contribute to the  $N\Lambda$  interaction in the relevant  $^1S_0$  and  $^3S_1$  partial waves. We emphasize that such an SU(3) symmetry breaking at NLO is well in line with  $\chi$ EFT and the associated power counting [13,46].

## 3. Analysis

The combined analysis of scattering and femtoscopic data is based on 12 data points for the  $p\Lambda$  elastic cross section, as well as six  $p\Lambda$  correlation functions measured in different ranges of pair transverse mass  $m_T$  in pp collisions at 13 TeV. In particular, six points of the cross section stem from the work of Alexander et al. [17], where we opt for those from the second choice of binning described in the corresponding work, while the remaining six data points are taken from the work of Sechi-Zorn et al. [16]. The femtoscopia data originates from the ALICE measurement of the  $p\Lambda$  correlation function in high-multiplicity (HM) pp collisions at 13 TeV [44]. When analyzed below the  $N\Sigma$  threshold, the  $S$ -waves are sufficient to account for the interaction. The parameters of the repulsive core  $V_C(r)$  in Eq. (3) are fitted independently for the spin singlet ( $S=0$ ) and triplet ( $S=1$ ) states, resulting in a total of 6 free parameters. The Usmani potential has been integrated into the CATS framework [47], which is capable of evaluating the corresponding cross section and correlation function by solving the Schrödinger equation. While this is sufficient to describe the cross section data, femtoscopic data necessitates additional knowledge of the two-particle emission source  $S(m_T, r)$ , as demanded by the Koonin-Pratt equation [48]

$$C(k) = \int S(m_T, r) \left| \Psi(\vec{k}, \vec{r}) \right|^2 d^3r. \quad (4)$$

Here,  $C(k)$  represents the correlation as a function of the single-particle momentum  $k$  in the pair rest frame, while  $\Psi(\vec{k}, \vec{r})$  is the wave function of the relative motion of the pair. The source  $S(m_T, r)$  is provided as a function of the relative distance between the particles  $r$  at the moment of their effective emission. The modeling of the source in small collision systems at the LHC has been extensively studied in several recent works [44,49,50], which provide compatible results on the source properties. In the present analysis, we adopt the CECA model [49], which operates based on a common emission source for all primordial particles. It accounts for particle production through the decay of short-lived resonances and incorporates an intrinsic  $m_T$  scaling of the source size, as observed in the data. The CECA framework utilizes three fit parameters to describe an effective hadronization surface on which the primordial particles are emitted. These particles are all moving radially away from the collision point, with their momentum distributions based on experimental measurements. The simulated primordial particles include protons,  $\Lambda$  hyperons, or resonances that decay into one of these species via the strong force. After the decay of the resonances, all final state particles of interest are grouped into  $p\Lambda$  pairs. Those satisfying the low-momentum condition  $k < 100 \text{ MeV}/c$  are used to construct a distribution in  $r$  and  $m_T$ , which, when normalized, corresponds to the source function  $S(m_T, r)$ . The resulting source is non-Gaussian, however, an effective Gaussian parameterization yields very similar results for  $C(k)$ . The main benefit of using the CECA framework is its ability to simultaneously model the pp as well as the  $p\Lambda$  source to reproduce the experimentally observed decreasing source size as a function of  $m_T$ . Consequently, this allows to calibrate the  $p\Lambda$  source to the pp correlation, which has been measured differentially in  $m_T$  by ALICE [44,51],



**Fig. 1.** Exclusion plots for the singlet ( $f_0$ ) and triplet ( $f_1$ )  $p\Lambda$  scattering lengths based on the analysis of the cross section data (left panel) and on the combined analysis of cross section and correlation data (right panel). See text for details.

significantly improving the sensitivity of the correlation function to the interaction potential. In the present analysis, we perform a pre-fit of the pp correlations using the Argonne  $v_{18}$  potential [52], following the same procedure as described in [49]. However, out of the seven available  $m_T$  bins, we have omitted the last two due to issues with convergence at very low  $k$ . To eliminate any bias related to the assumption of a common source, the extracted source parameters from the pre-fit of the pp correlations are used as an initial guess for the  $p\Lambda$  system, after which they are re-fitted alongside the six interaction parameters, allowing a variation of 3 standard deviations ( $\sigma$ ). Finally, we verify that the parameters converge to a proper local minimum. The remaining details on both the pp and  $p\Lambda$  fits, such as the inclusion of momentum resolution, feed-down, non-femtoscopic baseline, etc., are mirrored from the analysis of the same data described in [49].

The first objective of the present analysis is to quantify the allowed scattering lengths in the spin singlet/triplet channels ( $f_0$ ,  $f_1$ ), which can be accomplished by considering potentials of varying strengths in the CATS framework. Note that we use the sign convention where attractive/repulsive interactions are characterized by positive/negative scattering lengths. Both the cross section and the correlation function are composed of a weighted sum of the two channels, with respective weights of 1/4 and 3/4. The interactions in the two spin states are attractive and exhibit similar correlation shapes that differ in magnitude. Due to this similarity, the present analysis is not particularly sensitive to the individual scattering lengths of each spin channel, and a unique solution is not expected. Nevertheless, requiring that the two-body forces alone produce a bound hypertriton puts a lower limit on the strength of the interaction in the spin singlet channel. A concrete estimate is difficult to provide, however, judging from results for the hypertriton separation energy from Faddeev calculations employing modern YN potentials [14,15], values of  $f_0 \lesssim 2.0$  fm are not realistic. Assuming that the hypertriton is solely bound by three-body forces is likewise unrealistic given the present estimates [53] and explicit calculations [54] of their possible contribution. In view of this the scan is performed for  $f_0 > 1.6$  fm. The lack of a unique solution leads to convergence issues in the fit procedure. To address this problem, multiple fits are performed, each constrained within a specific small region of  $f_0$  and  $f_1$  values. The procedure is repeated until the entire desired parameter space is scanned. The best  $\chi^2$  of each individual step is saved, allowing the creation of an exclusion plot for  $f_0$  and  $f_1$ . The estimator for the exclusion is the total  $\chi^2 = \chi^2_{\text{scattering}} + \chi^2_{\text{femtoscopic}}$ . The  $\chi^2$  is converted into a number of standard deviations ( $n\sigma$ ) with respect to the best solution, accounting for a total of 9 degrees of freedom [55].

#### 4. Results and discussion

The exclusion plot based on results with the Usmani potential is shown in Fig. 1. The axes correspond to the scattering lengths in the singlet  $f_0$  and triplet  $f_1$  channel, while the color code contains infor-

mation on the compatibility with the data. The left panel is based on the analysis of only the cross section, while the right panel is the final result based on the combined analysis of femtoscopic and scattering data. The gray dashed lines mark the 1, 2 and 3 $\sigma$  exclusion regions. The black solid line, in the right panel, marks the border of a 3 $\sigma$  deviation with respect to the scattering data alone and is identical to the outer most dashed line from the left panel, while the shaded area depicts the region of even worse compatibility. As expected, there is a strong correlation between  $f_0$  and  $f_1$ , and the inclusion of femtoscopic data into the analysis leads to a significant decrease in uncertainties. Values of  $f_0 > 3.34$  fm or  $f_1 < 1.18$  fm are disfavored by the data. The lower (upper) bound of  $f_0$  ( $f_1$ ) cannot be constrained within the investigated parameter space. Fig. 1 contains two vertical bars depicting the values of the scattering parameters based on the NLO19 [14] and the next-to-next-to-leading order N<sup>2</sup>LO [15] potentials. The size of the markers represents the uncertainties related to the employed regulator (cutoff  $\Lambda$ ) in the chiral NY potentials. Both of these values are located approximately in the middle of the phase space region allowed by the scattering data alone, which is not surprising, as the LECs of those potentials have, up to now, been fitted to that data. Nevertheless, the enhanced sensitivity of the combined analysis shows that the predicted scattering lengths are disfavored by as much as 4.8 $\sigma$  in the case of N<sup>2</sup>LO. The NLO19 interaction is overall better in line with the present analysis, nevertheless, a systematic deviation of ca. 1-3  $\sigma$  is observed, depending on the cutoff value. Indeed, the predictions by the potential with cutoff  $\Lambda = 600$  MeV of  $f_0 = 2.91$  fm and  $f_1 = 1.41$  fm are in relatively good agreement, resulting in a deviation from the best solution of 1.1 $\sigma$ . On the other hand, a best fit of  $f_1$ , keeping  $f_0 = 2.91$  fm fixed, yields  $f_1 = 1.32 \pm 0.08$  fm. Clearly, due to the strong correlation between the two parameters, changing the value of  $f_0$  will influence the outcome for  $f_1$ . For example, fixing  $f_0 = 2.1$  fm implies the value  $f_1 = 1.56 \pm 0.11$  fm. Considering the combined analysis (right panel in Fig. 1), the best set of solutions can be approximated by the relation

$$f_1 \approx 2.2 \text{ fm} - 0.3 f_0 (\pm 0.1 \text{ fm}) \quad (5)$$

for  $f_0 \in (2.0, 2.9)$  fm. Table 1 in the Appendix provides multiple examples for scattering parameters and their compatibility to the data. These results indicate an overall less attractive interaction compared to the published chiral potentials.

As a next step we explore how this less attractive NA interaction affects predictions for the single-particle potential  $U_\Lambda$  at nuclear saturation density  $\rho_0$  and its density dependence in general, considering the relevance of this quantity for the role of the  $\Lambda$  hyperon in neutron stars [9,10]. In Fig. 2, we present results for the single-particle potential  $U_\Lambda(k_\Lambda = 0)$  as a function of the nuclear matter density  $\rho$ , evaluated self-consistently within a conventional  $G$ -matrix calculation. We employ the formalism described in detail in Refs. [31,56], where the so-called continuous choice is taken for the intermediate states, and the N<sup>3</sup>LO

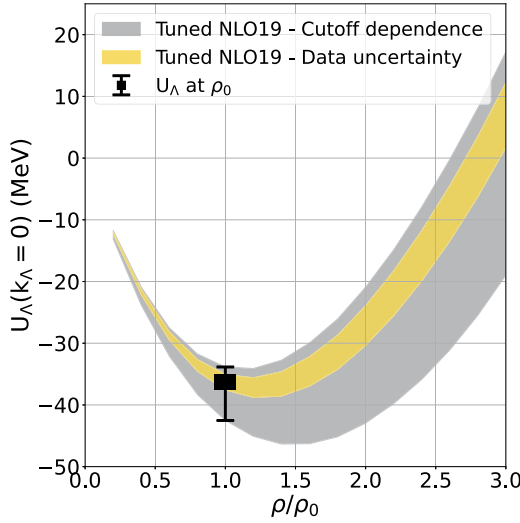


Fig. 2.  $\Lambda$  single-particle potential  $U_\Lambda$  as a function of the nuclear-matter density  $\rho$  with  $\rho_0 = 0.166 \text{ fm}^{-3}$  being the nuclear-matter saturation density.

potential from [57] is used for the NN interaction. The NLO19(600) potential is chosen as a starting point from which, by readjusting some of its LECs to reproduce 8 combinations of the  $\Lambda\Lambda$  spin singlet and triplet scattering lengths within the  $1\sigma$  region (points i to viii Table 1), we estimate the corresponding  $U_\Lambda(\rho_0)$  given by the black square in Fig. 2. The vertical error bar represents the theoretical uncertainty estimated by considering the NLO19 potentials with different cutoffs (500 – 650 MeV), all re-fitted to describe the same set of scattering parameters. The final result is  $U_\Lambda(\rho_0) = -36.3 \pm 1.3(\text{stat})^{+2.5}_{-6.2}(\text{syst})$  MeV, where the statistical uncertainty is associated with the data on the scattering parameters (right panel in Fig. 1) and the systematic with the cut-off dependence from the theory. The resulting theoretical uncertainty is large, as likewise reported in standard nuclear matter calculations with chiral nucleon-nucleon potentials [58,59]. Additionally, for the behavior of the potential depth as a function of  $\rho$ , we show in Fig. 2 the theoretical uncertainty (grey band) and the uncertainty from the combined data (yellow band). The predicted values for  $U_\Lambda(\rho)$  are similar to the result for the original NLO19 potential. Our results at  $\rho_0$  lie below the usually cited semi-empirical value of  $U_\Lambda = -27 \sim -30$  MeV obtained from hypernuclei constraints [1,30]. This is in line with comparable  $G$ -matrix calculations where a similar overbinding feature has been observed when two-body-only contributions are taken into account, see, for example, [14,60]. In two recent works [31,32] an overall repulsion from a chiral NNY three-body force has been incorporated in the form of an effective density-dependent NY two-body potential [61]. This addition allows the authors to satisfy the  $\approx -30$  MeV hypernuclear constraint and, at the same time, suppresses the appearance of  $\Lambda$  hyperons for densities as realized in NS, i.e. offers a solution to the so-called “hyperon-puzzle” [2,9]. Our results are compatible with such a strategy. Quantitative constraints on this effective three-body force might become available in future correlation studies [62,63].

In conclusion, in this work we have presented the first combined analysis of low-energy femtoscopic and scattering data to constrain the  $S$ -wave scattering parameters of the  $p\Lambda$  interaction, resulting in the tightest limits available for future theoretical studies. The  $p\Lambda$  interaction is found to be overall less attractive than what has been indicated by the scattering data from the 1960s. We observe a strong, approximately linear (Eq. (5)), correlation between the values of the scattering lengths in the spin singlet and triplet states. The best solution, if  $f_0$  is fixed to 2.1 fm, is  $f_1 = 1.56 \pm 0.08$  fm. Lower  $f_0$  values will eventually prohibit a hypertriton bound by two-body forces. The maximum (minimum) allowed values for  $f_0$  ( $f_1$ ) are 3.34 (1.18) fm.

Clearly, the accurate reproduction of low-energy  $\Lambda\Lambda$  data, like scattering cross sections and femtoscopic two-particle correlation functions, is an important requirement for realistic predictions of many-body systems. Thus, we have fine-tuned the chiral YN potential NLO19 to match the established scattering parameters in order to explore the impact on the in-medium properties of the  $\Lambda$  hyperon. The result with those NLO19 variants for  $U_\Lambda(\rho_0)$  is  $\sim -36$  MeV, which implies an overbinding with regard to the nominal  $\Lambda$  binding energy in infinite nuclear matter. This is consistent with the current notion of an additional repulsion acting on the  $\Lambda$  within the medium, attributed to three-body forces. The presented results can serve as a state-of-the-art guideline for the contribution to be expected from two-body  $p\Lambda$  interactions.

### Declaration of competing interest

The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

### Data availability

In this work, we have only used previously measured and publicly available data, which can be accessed by following the references in the manuscript.

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### Appendix A

Table 1 provides details on the 8 different selected sets of  $\{f_0, f_1\}$  values, chosen to represent the  $1\sigma$  region of best compatibility to the combined data, as well as 3 points anchored to existing parameterizations of the chiral effective field theory [13–15]. The compatibility is estimated using the number of standard deviations, denoted as  $n\sigma$ , with respect to the best possible fit. We consider three scenarios: firstly, only the femtoscopia data is taken into account, resulting in  $n\sigma_{\text{fnt}}$ ; secondly, only the scattering data is considered ( $n\sigma_{\text{scf}}$ ); and thirdly,  $n\sigma_{\text{tot}}$  corresponds to the combined analysis presented in this work. It is essential to note that these three scenarios represent independent analyses, each having a different best solution as a baseline. Consequently, there is no straightforward relation between the three estimators.

Table 1

Summary table showing the compatibility of different scattering parameters to the femtoscopia data ( $n\sigma_{\text{fnt}}$ ), scattering data ( $n\sigma_{\text{scf}}$ ) as well as the combined analysis from the present work ( $n\sigma_{\text{tot}}$ ). If the combined estimator  $n\sigma_{\text{tot}}$  is considered, solutions ii, v and vii represent a set of “best” solutions.

Usmani parameterization	$f_0$ (fm)	$f_1$ (fm)	$n\sigma_{\text{fnt}}$	$n\sigma_{\text{scf}}$	$n\sigma_{\text{tot}}$
NLO13(600)	2.91	1.54	5.2	0.0	4.6
NLO19(600)	2.91	1.41	1.7	0.4	1.1
N <sup>2</sup> LO(550)	2.79	1.58	5.4	0.0	4.8
i	2.10	1.44	0.2	2.1	1.0
ii	2.10	1.56	0.0	0.9	0.0
iii	2.10	1.66	1.8	0.2	1.0
iv	2.50	1.32	0.2	2.2	1.1
v	2.50	1.46	0.2	0.8	0.0
vi	2.50	1.55	1.8	0.2	1.0
vii	2.91	1.32	0.1	1.5	0.3
viii	3.34	1.18	1.2	0.9	1.0



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