

# ADAPTIVE-PRECISION POTENTIALS FOR LARGE-SCALE ATOMISTIC SIMULATIONS

2024-03-18 | David Immel, Ralf Drautz, Godehard Sutmann |

# INTERATOMIC POTENTIALS

## Atomic Cluster Expansion (ACE)<sup>1</sup>

modern and precise ML potential

$$E = \text{[diagram of atom with 2 neighbors]} + \dots + \text{[diagram of atom with 3 neighbors]} + \dots + \text{[diagram of atom with 4 neighbors]} + \dots + \text{[diagram of atom with 5 neighbors]} + \dots$$

| Cu potential     | nanoindentation |       | single force call <sup>2</sup> |       |
|------------------|-----------------|-------|--------------------------------|-------|
|                  | core-h          | cores | μs                             | cores |
| ACE <sup>2</sup> | 66243           | 640   | 320.0                          | 1     |
| EAM <sup>3</sup> | 83              | 128   | 1.5                            | 1     |

EAM is **200-800 times faster** than ACE

<sup>1</sup> Drautz, Ralf. *Physical Review B*. 2019

<sup>2</sup> Lysogorskiy, Yury et al. *npj computational materials*. 2021

<sup>3</sup> Mishin, Yuri et al. *Physical Review B*. 2001

## Embedded Atom Model (EAM)

traditional and fast potential

$$E = \frac{1}{2} \sum_j V(r_{ij}) + F \left( \sum_{j \neq i} \rho(r_{ij}) \right)$$

combine precise and fast

$$E = \lambda E_{\text{EAM}} + (1 - \lambda) E_{\text{ACE}}$$

- ACE for most interesting atoms
- EAM for remaining atoms

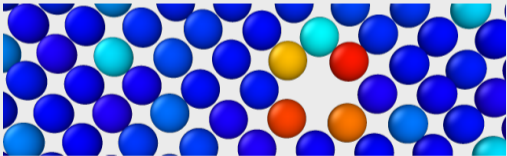
# DETECTING INTERESTING ATOMS

## centro-symmetry parameter<sup>4</sup> (CSP)

- detects defects, surfaces

⇒ interesting atoms

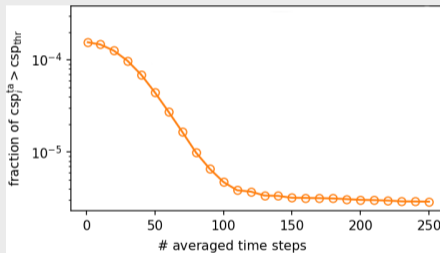
$$\text{CSP}_i = \sum_{j=1}^{N/2} |\vec{r}_{i,j} + \vec{r}_{i,j+N/2}|^2$$



all atomistic visualisations with ovito<sup>5</sup>

## time averaging

- slow change of CSP
- prevents detection of thermal fluctuations



<sup>4</sup>Kelchner, Cynthia L, Plimpton, SJ, and Hamilton, JC. *Physical review B*. 1998

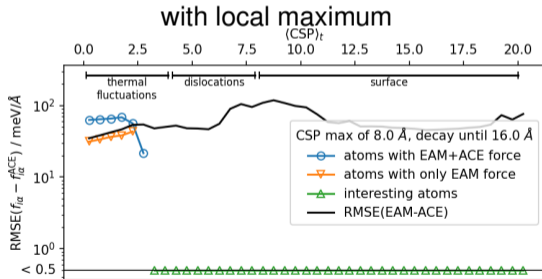
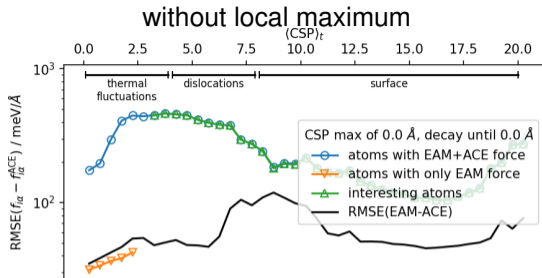
<sup>5</sup>Stukowski, Alexander. *Modelling and simulation in materials science and engineering*. 2009

# FORCES IN (100) COPPER

$$F_i = \sum_k \left( \underbrace{-\cancel{(\nabla_i \lambda_k)} (\cancel{E_k^{EAM}} - \cancel{E_k^{ACE}})}_{\text{next slide}} - \underbrace{\lambda_k (\nabla_i E_k^{EAM}) - (1 - \lambda_k) (\nabla_i E_k^{ACE})}_{\text{all } \lambda_k \text{ influence } F_i} \right)$$

## local maximum of CSP

- use  $\max(\{\langle \text{CSP}_j \rangle_t f(r_{ij})\})$  to calculate  $\lambda_i$
- ⇒ less EAM influence on interesting atoms



# ENERGY CONSERVATION

- one cannot calculate  $\nabla_i \lambda_k$
- potential is conservative for constant  $\{\lambda_k\}$

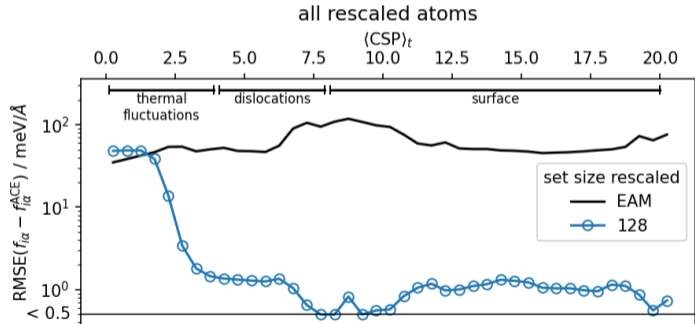
velocity change by integrator

$$\Delta v = \frac{F}{m} \Delta t$$

⇒ comparison with forces possible

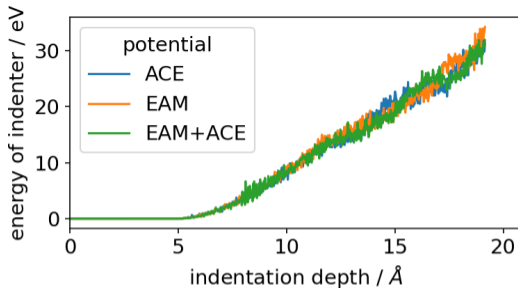
## local thermostat per atom

- 1 calculate energy difference compared to constant  $\{\lambda_k\}$  case
  - 2 rescale velocities of random local atoms
- ⇒ energy & momentum conservation



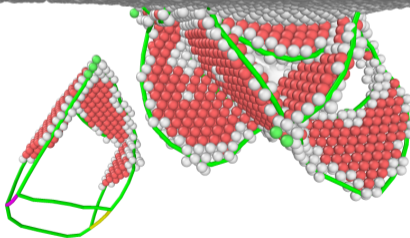
# NANOINDENTATION

- simulated with LAMMPS<sup>6</sup>
- $68^3$  unit cells  $\approx$  1.25 million atoms
- temperature: 292 K
- velocity controlled nanoindentation
- imaginary, spherical, repulsive indenter



Dislocation type

- $1/6\langle 112 \rangle$  (Shockley)
- $1/6\langle 110 \rangle$  (Stair-rod)
- $1/3\langle 100 \rangle$  (Hirth)



Structure types

- Other
- FCC
- HCP

<sup>6</sup>Thompson, Aidan P et al. *Computer Physics Communications*. 2022

# ADAPTIVE-PRECISION POTENTIALS

## Summary

$$E_i = \lambda_i E_{i,\text{EAM}} + (1 - \lambda_i) E_{i,\text{ACE}}$$

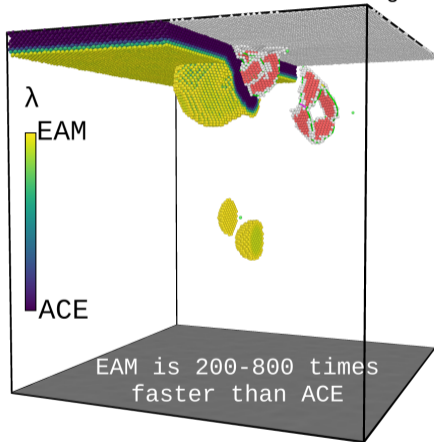
- detect interesting atoms with CSP
- ⇒ precise and fast potential

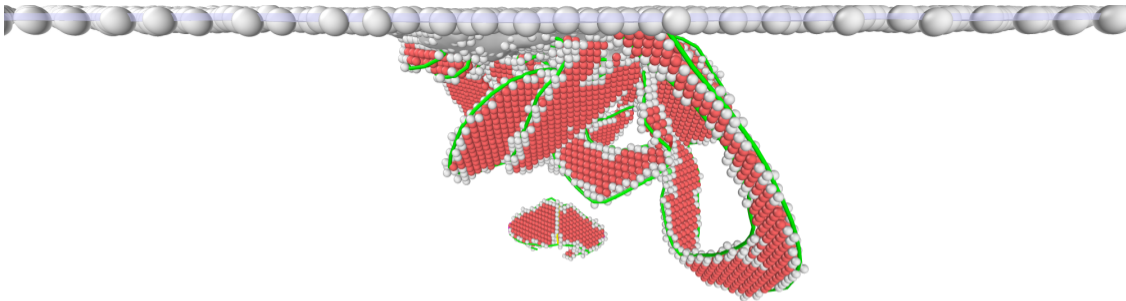
## Outlook

- bcc metal: Tungsten

left  
ACE calculations

right  
interesting atoms

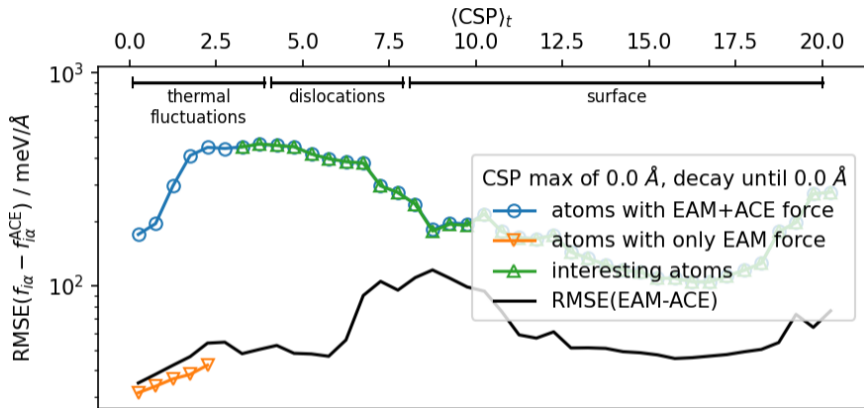




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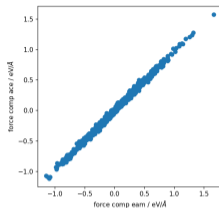
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# EAM + ACE FORCES



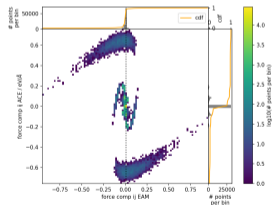
$$F_i^{\text{EAM}} \approx F_i^{\text{FACE}}$$

correlation 1.00

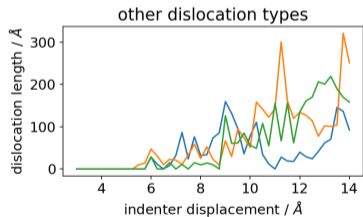
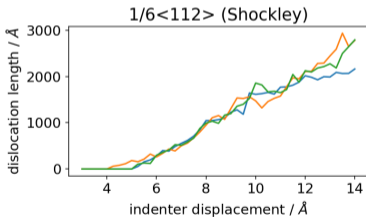
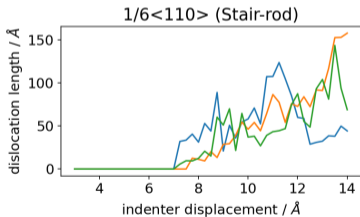
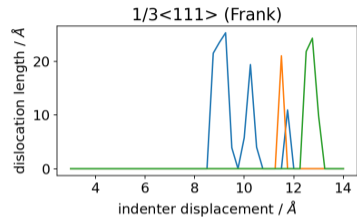
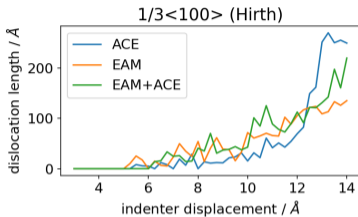
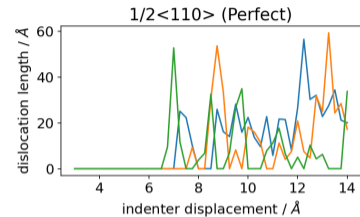


$$F_{i \rightarrow j}^{\text{EAM}} \not\approx F_{i \rightarrow j}^{\text{FACE}}$$

correlation -0.52



# DISLOCATIONS



EAM+ACE generates the same dislocations types like ACE.

# DYNAMIC LOAD BALANCING

## load per domain

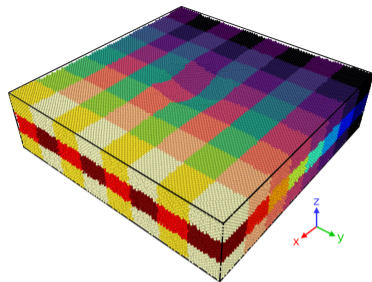
- load = force calculation time  $\tau_p$
- one potential:  $\tau_p = \tau_p^{\text{pot}}$
- EAM+ACE:  $\tau_p = n_p^{\text{EAM}} \tau_p^{\text{EAM}} + n_p^{\text{ACE}} \tau_p^{\text{ACE}} + n_p^{\text{CSP}} \tau_p^{\text{CSP}}$

## staggered grid

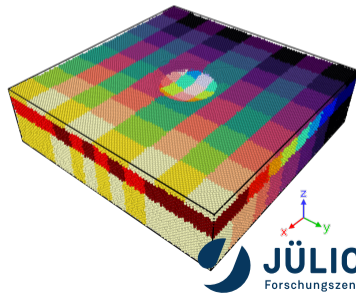
- cut box into layers, cut layer into rows, cut row into cells
- calculate domain boundaries with ALL<sup>a</sup>

<sup>a</sup>R. Halver, S. Schulz, and G. Sutmann.

<https://gitlab.version.fz-juelich.de/SLMS/loadbalancing/-/releases>. 2023.



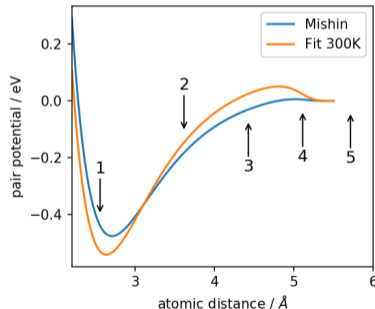
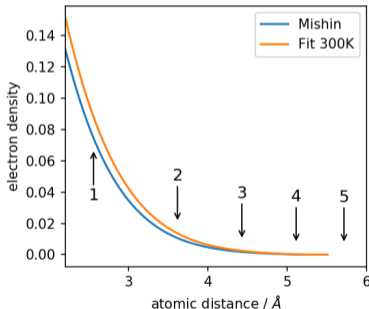
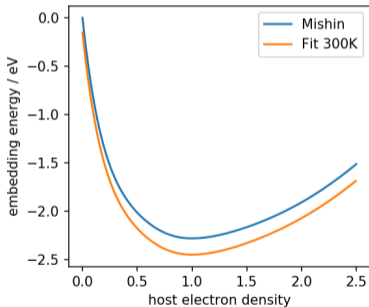
adjust domains to balance load



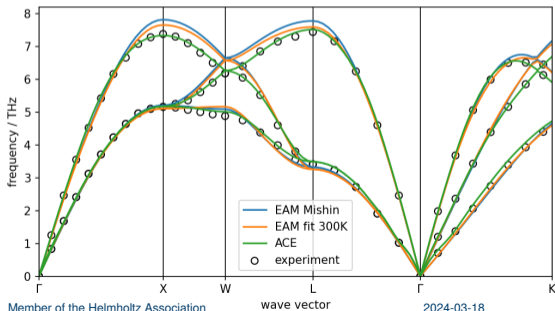
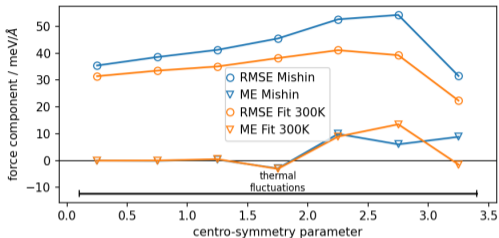
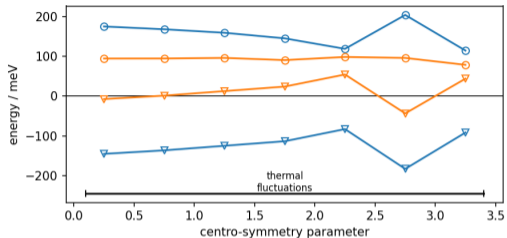
# UPFITTING EAM WITH ATOMICREX<sup>7</sup>

$$\mathcal{L}(A) = \sum_{o \in \mathcal{O}} \left( \frac{A_o^{\text{targ}} - A_o^{\text{pred}}}{\delta_o^{\text{tol}}} \right)^2 + \sum_{s \in \mathcal{S}} \frac{1}{N_s} \left( \sum_{i=1}^{N_s} \left( \frac{E_{s,i}^{\text{targ}} - E_{s,i}^{\text{pred}}}{\delta_{E_{\text{md}}}^{\text{tol}}} \right)^2 + \sum_{i=1}^{N_s} \left( \frac{\|F_{s,i}^{\text{targ}} - F_{s,i}^{\text{pred}}\|_{L_2}}{\delta_{F_{\text{md}}}^{\text{tol}}} \right)^2 \right)$$

- fitted scalar properties  $\mathcal{O}$ :  $a_0^{\text{FCC}}$ ,  $E_{\text{coh}}$ ,  $B$ ,  $C_{11}$ ,  $C_{12}$ ,  $C_{44}$
- fitted structures  $\mathcal{S}$ : snapshots of MD simulation of bulk with ACE at  $T$



# UPFITTED EAM PROPERTIES



|                                 | ACE     | EAM fit | EAM ref |
|---------------------------------|---------|---------|---------|
| $E_{\text{coh}} / \text{eV}$    | -3.6994 | -3.6956 | -3.5579 |
| $a_0^{\text{FCC}} / \text{\AA}$ | 3.6309  | 3.6304  | 3.6149  |
| $C_{11} / \text{GPa}$           | 173     | 171     | 171     |
| $C_{12} / \text{GPa}$           | 120     | 120     | 124     |
| $C_{44} / \text{GPa}$           | 77      | 80      | 76      |
| $B / \text{GPa}$                | 138     | 137     | 139     |