

# Internal and external magnetic-field engineering of negative magnetization and exchange bias in $\text{La}_{1-x}\text{Pr}_x\text{CrO}_3$ ( $0.8 \leq x \leq 0.9$ )

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The negative magnetization and exchange bias phenomena have been the subject of interest due to their promising applications in spintronic devices. In this study, we have comprehensively investigated these two intertwined magnetic phenomena in  $\text{La}_{1-x}\text{Pr}_x\text{CrO}_3$  ( $x = 0.8-0.9$ ) compounds. The Cooke's model fit to dc magnetization data infers negative internal magnetic field for  $x = 0.8, 0.85$ , and  $0.87$  and positive for  $x = 0.9$ . The crossover of internal magnetic field from negative to positive across  $x = 0.87$  and its dominance over the external applied magnetic field leads to the magnetization switching from negative to positive. The internal magnetic field behavior also explains the anomalous magnetization behavior involving reduced magnetization for  $x = 0.87$ , despite having higher  $\text{Pr}^{3+}$  concentration than that for  $x = 0.8$  and  $0.85$ . The anomalous magnetization is corroborated well by the neutron depolarization experiments, where no depolarization is observed for  $x = 0.87$  owing to nearly compensated domain magnetization. Remarkably, a switching of the exchange bias from inverse (with positive  $H_{\text{EB}}$ ) to conventional (with negative  $H_{\text{EB}}$ ) due to a competition of external and internal magnetic fields is found in  $x = 0.8$  and  $0.85$  compounds. The  $x = 0.87$  and  $0.9$  compounds, on the other hand, show only conventional exchange bias at all measured magnetic fields. Using the Cooke's model, we show that the antiferromagnetic coupling between polarized  $\text{Pr}^{3+}$  and weak ferromagnetic component of canted  $\text{Cr}^{3+}$  moments explain not only the inverse exchange bias but the conventional exchange bias as well, however, the moment orientations are different for both types of exchange bias. Moreover, our study demonstrates that the ferromagnetic coupling between the two moments can also lead to conventional exchange bias, similar to that observed in interfacial heterostructure systems.

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## I. INTRODUCTION

In the recent years, the study of exchange bias (EB) and unusual negative magnetization (NM) phenomena has gained intense research interest due to their significance in fundamental physics as well as potential technological importance in thermomagnetic switches [1], spin valves [2], high-density magnetic storage [3], voltage-mediated magnetic switching [4], and various spintronic devices [5]. In the NM phenomenon, the order parameter, magnetization ( $M$ ) changes its sign from positive to negative during decrease of temperature under some external magnetic field ( $H$ ) and the temperature

at which magnetization becomes zero is called compensation temperature ( $T_{\text{COMP}}$ ) [1]. The EB, on the other side, is manifested by shifting of the hysteresis loop and is characterized by the exchange bias shift parameters  $H_{\text{EB}}$  (and  $M_{\text{EB}}$ ). Following its discovery in Co/CoO core-shell nanoparticles by Meiklejohn and Bean [6], EB was mainly studied in core-shell nanoparticles [7–9] and in various magnetic heterostructures involving different phases like ferromagnetic (FM), antiferromagnetic (AFM), and spin glass [10,11]. In most of these systems, only conventional EB with negative  $H_{\text{EB}}$  was reported [7–11], however, inverse EB with positive  $H_{\text{EB}}$  was reported in few systems only [12,13]. The AFM and FM exchange coupling at the interface between two magnetic phases causes a pinning effect and this was understood to be a cause of positive and negative  $H_{\text{EB}}$ , respectively [13,14]. From the last two decades, research of EB is extended to homogeneous magnetic compounds (without any real interface), where similar to interfacial systems, conventional EB was reported [15–17]. However, the origin of EB in these systems is found to be different and is related to the intrinsic exchange coupling between magnetic sublattices present.

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Recently, attention has been given to study EB in magnetic compounds showing the NM phenomenon [18,19]. Interestingly, in these compounds, similar to NM, EB also shows sign reversal across the  $T_{\text{COMP}}$  leading to both inverse and conventional EB below and above the  $T_{\text{COMP}}$ , respectively [20–23]. Such concurrent occurrences of inverse and conventional EB are quite appealing, rendering these compounds further useful for thermal-assisted magnetic random access memory devices [24]. Literature studies show that NM-based perovskite compounds, particularly  $R\text{BO}_3$  [with magnetic  $R$  (rare earth) and  $B = \text{Cr, Fe}$ ], show such a remarkable  $H_{\text{EB}}$  reversal with temperature [20,21,23,25]. However, the sign reversal of  $H_{\text{EB}}$  with magnetic field in these compounds is seldom observed [26]. Among various studied  $R\text{BO}_3$  compounds,  $\text{La}_{1-x}\text{Pr}_x\text{CrO}_3$  are found particularly interesting. Our recent study on  $\text{La}_{1-x}\text{Pr}_x\text{CrO}_3$  ( $x = 0, 0.25, 0.5, 0.75$ , and  $1$ ) [27,28] compounds show a correlation among NM, EB, and electrical properties. The study also demonstrated the sign reversal of  $H_{\text{EB}}$  from positive to negative across  $x = 0.75$ . The  $T_{\text{COMP}}$  was found to increase with increasing  $x$ , became maximum for the  $x = 0.75$  followed by a decrease [28]. The electrical conduction mechanism also changed across  $x = 0.75$ . In these compounds, it is also reported that the NM phenomenon disappears at  $x > 0.85$  [29,30]. However, the physics behind the mysterious disappearance of NM in these compounds is not known so far. Further, Yoshi *et al.* [30] reported positive and negative  $H_{\text{EB}}$  in  $\text{La}_{1-x}\text{Pr}_x\text{CrO}_3$  ( $x = 0.75$  and  $0.85$ ) compounds under the conditions of cooling magnetic field ( $H_{\text{COOL}} < \text{internal magnetic field } (H_{\text{I}})$  and  $H_{\text{COOL}} > H_{\text{I}}$ , respectively). They explained the positive and negative  $H_{\text{EB}}$  based on the AFM and FM coupling between  $\text{Pr}^{3+}$  and weak ferromagnetic  $\text{Cr}^{3+}$  moments, respectively, as explained in the literature for the heterostructure systems [13,14]. However, an in-depth or detailed explanation of the experimental EB results was not provided. Therefore, to shed light on the unusual NM disappearance and EB behavior with  $H_{\text{COOL}}$ , in this study, we have investigated  $\text{La}_{1-x}\text{Pr}_x\text{CrO}_3$  ( $x = 0.8$  to  $0.9$ ) compounds using comprehensive dc magnetization, neutron diffraction, and neutron depolarization studies.

Our dc magnetization data analysis using the Cooke's model reveals that the polarized  $\text{Pr}^{3+}$  ( $M_{\text{Pr}}$ ) and FM component of canted  $\text{Cr}^{3+}$  ( $M_{\text{Cr}}$ ) moments are coupled in various configurations like  $M_{\text{Cr}}$  up ( $\uparrow$ ),  $M_{\text{Pr}}$  down ( $\downarrow$ );  $M_{\text{Cr}}$  down ( $\downarrow$ ),  $M_{\text{Pr}}$  up ( $\uparrow$ );  $M_{\text{Cr}}$  up ( $\uparrow$ ),  $M_{\text{Pr}}$  down ( $\downarrow$ ) depending upon the applied magnetic field. These  $M_{\text{Cr}}$  and  $M_{\text{Pr}}$  spin orientations not only explain the NM and its disappearance but also explain the anomalous magnetization behavior in these compounds involving decreasing magnetization upto  $x = 0.87$  followed by an increase. Interestingly, the changing orientation of  $M_{\text{Pr}}$  and  $M_{\text{Cr}}$  moments with magnetic field also explains the inverse ( $x = 0.8$  and  $0.85$ ) and conventional ( $x = 0.8, 0.85, 0.87$ , and  $0.9$ ) EB in these compounds. This study also reveals that NM and EB have the same underlying physics origin and these two magnetic phenomena are indeed intertwined with each other.

## II. EXPERIMENTAL DETAILS

The polycrystalline powder samples of  $\text{La}_{1-x}\text{Pr}_x\text{CrO}_3$  were prepared by the solid-state reaction method, as de-

scribed in Refs. [27,28]. The single phase of the samples was confirmed using a laboratory source-based x-ray diffraction data recorded at room temperature (see Sec. S1 in the Supplemental Material (SM) [31]). The dc magnetization  $M(T)$  measurements were carried out on all powder samples in the temperature range of 5–300 K under various magnetic fields in field-cooled-cooling (FCC) and field-cooling-warming (FCW) modes. In the FCC mode, the dc magnetization was measured while cooling the sample under a magnetic field, while in the FCW mode, the dc magnetization was measured in the warming cycle under the same magnetic field applied for the FCC measurement. For EB measurements, the  $M(H)$  hysteresis loops were recorded at various temperatures by sweeping the magnetic field over  $\pm 50$  kOe in field-cooled (FC) mode. In field-cooled (FC) hysteresis loop measurements, each sample was cooled from room temperature down to a measuring temperature under a given magnetic field, and then hysteresis loop was recorded. After every hysteresis loop measurement, the sample was heated to room temperature (above the magnetic ordering temperature) for demagnetization. For both types of the dc magnetization measurements, the Physical Property Measurement System (PPMS) DynaCool 14 of the Physics Lab at the Heinz Maier-Leibnitz Zentrum (MLZ) and the SQUID magnetometer at the Institute of Physics (IOP) were used. The neutron depolarization experiments using polarized neutrons were carried out on all powder samples in the temperature range of 5–300 K under a magnetic field of 50 Oe using the Polarized Neutron Spectrometer ( $\lambda = 1.201 \text{ \AA}$ ) at Dhruva reactor, Bhabha Atomic Research Centre (BARC), Mumbai, India. The neutron powder diffraction experiments over the temperature range of 5 to 300 K under zero magnetic field were carried out using the position-sensitive detector-based powder diffractometer-I ( $\lambda = 1.094 \text{ \AA}$ ) at Dhruva reactor, BARC, Mumbai, India. The x-ray and neutron diffraction data were analyzed by the Rietveld refinement technique [32] using FULLPROF software package [33].

## III. RESULTS

### A. dc magnetization

Figure 1 shows the temperature-dependent dc magnetization of  $\text{La}_{1-x}\text{Pr}_x\text{CrO}_3$  ( $x = 0.8, 0.85, 0.87$ , and  $0.9$ ) compounds in  $H = 100$  Oe recorded in field-cooled-cooling (FCC) mode. The  $x = 0.8, 0.85$ , and  $0.87$  compounds show the interesting phenomenon of NM with the compensation temperatures ( $T_{\text{COMP}}$ ) of 216, 222, and 198 K, respectively [Figs. 1(a)–1(c)]. The NM phenomenon disappears for  $x > 0.87$  and thus the  $x = 0.9$  compound shows only positive  $M$  in the entire magnetic ordering state (below  $T_{\text{N}}$ ) [Fig. 1(d)]. The magnetization behaviors align well with the literature findings [29,30]. The magnetic ordering temperature ( $T_{\text{N}}$ ) is found to be decreasing from 250 K for  $x = 0.8$  to 242 K for  $x = 0.9$ , which is also consistent with the decreasing trend of  $T_{\text{N}}$  with increasing  $x$  in  $\text{La}_{1-x}\text{Pr}_x\text{CrO}_3$  compounds [28,34]. Further, the  $M$  data under  $H = 100$  Oe as a function of  $x$  at some selected temperatures are plotted in Fig. 1(e). The  $M$  values for  $x = 0.25, 0.5, 0.75$ , and  $1$  compounds, taken from our previous study [28], are also plotted in Fig. 1(e) to see complete  $x$  dependence of  $M$  in  $\text{La}_{1-x}\text{Pr}_x\text{CrO}_3$  series.

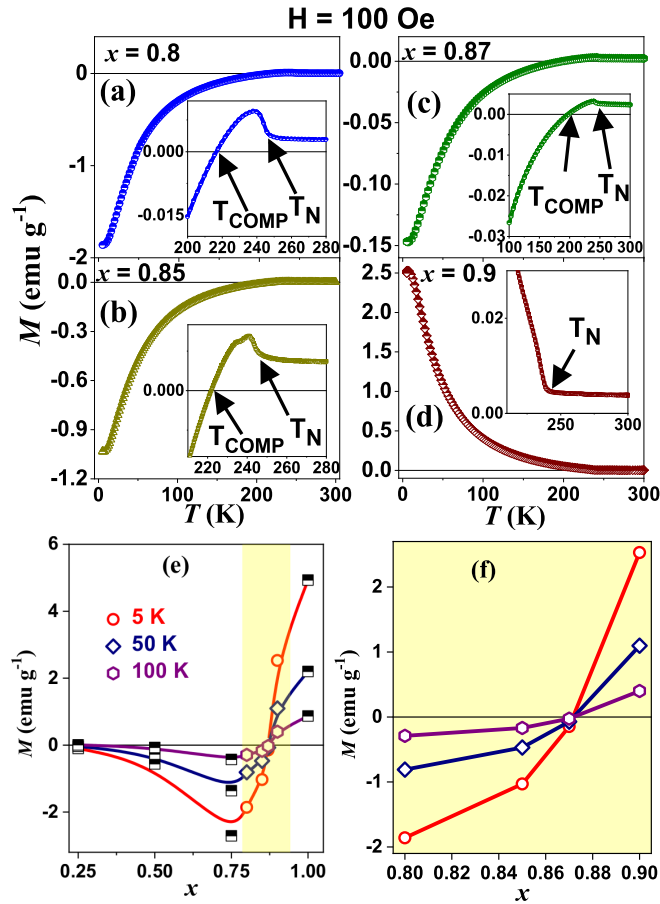


FIG. 1. (a)–(d) The dc magnetization ( $M$ ) vs temperature ( $T$ ) curves of  $\text{La}_{1-x}\text{Pr}_x\text{CrO}_3$  ( $x = 0.8, 0.85, 0.87$ , and  $0.9$ ) compounds recorded in field-cooled-cooling (FCC) mode under  $H = 100$  Oe. Insets show the zoomed view of  $M$  near the transition temperatures ( $T_{\text{COMP}}$  and  $T_N$ ). (e) The  $x$  dependence of  $M$  at some selected temperatures. The half-filled black squared symbol data are taken from Ref. [28]. (f) Enlarged view of highlighted yellow region of  $M$  vs  $x$  curves in (e).

As shown in Fig. 1(e), the  $x = 0.75$  compound exhibits the higher negative  $M$  than that for all other NM compounds of this series. It is also evident that with increasing  $x$  from 0.75, negative  $M$  value at a given  $T$  starts to decrease, changes sign from negative to positive across  $x = 0.87$  with minimum negative  $M$ , and then remains positive with increasing  $M$ , thus indicating an anomalous  $M$  behavior [Figs. 1(e) and 1(f)] in the compounds of  $\text{La}_{1-x}\text{Pr}_x\text{CrO}_3$  series. Here it should be noted that the initial increase in  $M$  up to  $x = 0.75$  is consistent with the increasing  $\text{Pr}^{3+}$  concentration in  $\text{La}_{1-x}\text{Pr}_x\text{CrO}_3$  as  $\text{Pr}^{3+}$  is a magnetic ion with an effective magnetic moment of  $\sim 3.58 \mu_B$ . However, a decrease in  $M$  for  $x > 0.75$  and the lowest  $M$  observed for  $x = 0.87$  are totally unusual as these compounds have higher magnetic  $\text{Pr}^{3+}$  concentration than that of  $x \leq 0.75$ . This nonmonotonic  $M$  behavior should be related with the different orientations of  $\text{Pr}^{3+}$  and  $\text{Cr}^{3+}$  moments with changing  $x$ . The mesoscopic and domain-level understanding of the anomalous  $M$  behavior has been obtained by neutron depolarization experiments performed using polarized neutrons (see next section). Moreover, we have fitted

the dc magnetization data using the Cooke's model to get an insight into the anomalous  $M$  behavior in these compounds (see Discussion section).

To get a detailed understanding of the NM in  $x = 0.8, 0.85$ , and  $0.87$  compounds, the  $M$  vs  $T$  data have been recorded under various magnetic fields and the results are displayed in Figs. 2(a)–2(c). The  $x = 0.8$  compound shows the NM phenomenon up to a magnetic field of 5 kOe [Fig. 2(a)]. Interestingly, for  $H = 5$  kOe, a sharp upturn at low temperature is observed in the  $M$  vs  $T$  curve, leading to a further change in  $M$  sign from negative to positive, i.e., two  $T_{\text{COMP}}$  for the compound. A similar sharp upturn is also observed for  $H > 5$  kOe  $M$  vs  $T$  curves, however,  $M$  remains positive throughout the measured temperature range. The  $x = 0.85$  compound shows the  $M$  behavior under various  $H$  similar to the  $x = 0.8$ , except that the  $H$  is decreased from 5 to 2 kOe to observe the NM phenomenon [Fig. 2(b)]. In contrast to  $x = 0.8$  and  $0.85$ , the NM phenomenon disappears at a relatively small  $H$  ( $> 200$  Oe) for  $x = 0.87$  [Fig. 2(c)]. The variation of  $T_{\text{COMP}}$  with  $H$  for  $x = 0.8$  and  $0.85$  compounds is shown in Fig. 2(d). The  $T_{\text{COMP}}$  is found to be decreasing with increasing  $H$ . The  $T_{\text{COMP}}$  also decreases with increasing  $x$ . The  $x = 0.9$  shows only positive magnetization at all applied  $H$ , for instance, see  $M$  vs  $T$  curves under  $H = 1$  and 5 kOe [Fig. S2 in SM [31]]. Similar to  $M$  behavior, interesting EB results (presented later) are also found for these compounds. In the EB section; we see that  $x = 0.8$  and  $0.85$  compounds show inverse and conventional EB, i.e., sign reversal of  $H_{\text{EB}}$  from positive to negative with variation of cooling magnetic field ( $H_{\text{COOL}}$ ). While the  $x = 0.87$  and  $0.9$  compounds show only conventional EB for all measured  $H_{\text{COOL}}$ .

## B. Neutron depolarization

To understand the anomalous  $M$  behavior of  $\text{La}_{1-x}\text{Pr}_x\text{CrO}_3$  compounds at the mesoscopic or domain-level length scales, the one-dimensional ( $z$ - $z$ ) neutron depolarization experiments are carried out over the temperature range of 5–300 K under  $H = 50$  Oe. In these experiments, polarized neutrons (with polarization  $\sim 98.8\%$  along the  $z$  direction) are incident on the sample under study, and final neutron beam polarization ( $P_f$ ) is measured. It should be noted that paramagnets, collinear antiferromagnets, and canonical spin-glass systems, having average zero magnetization at the mesoscopic length scales, do not cause any depolarization of the polarized neutron beam. The other details of the instrument are given elsewhere [35,36]. The  $P_f$  for  $\text{La}_{1-x}\text{Pr}_x\text{CrO}_3$  ( $x = 0.8, 0.85, 0.87$ , and  $0.9$ ) compounds as a function of the temperature (5–300 K) is shown in Fig. 3(a). It is evident that  $P_f$  shows a monotonic decrease right below  $\sim 120$  and  $100$  K for  $x = 0.8/0.9$  and  $0.85$  compounds, respectively, indicating an increase in domain magnetization with decreasing temperature. On the other hand, no neutron beam depolarization for  $x = 0.87$  in the whole measured temperature range represents the almost compensated magnetic state with nearly zero-domain magnetization. The  $P_f$  as a function of  $x$  at 5 and 50 K are plotted in Fig. 3(b). Interestingly, the  $P_f$  data reflect the  $M$  behavior shown in Fig. 1(f), thus providing a mesoscopic understanding of the anomalous  $M$  behavior over the magnetic domain length scale.

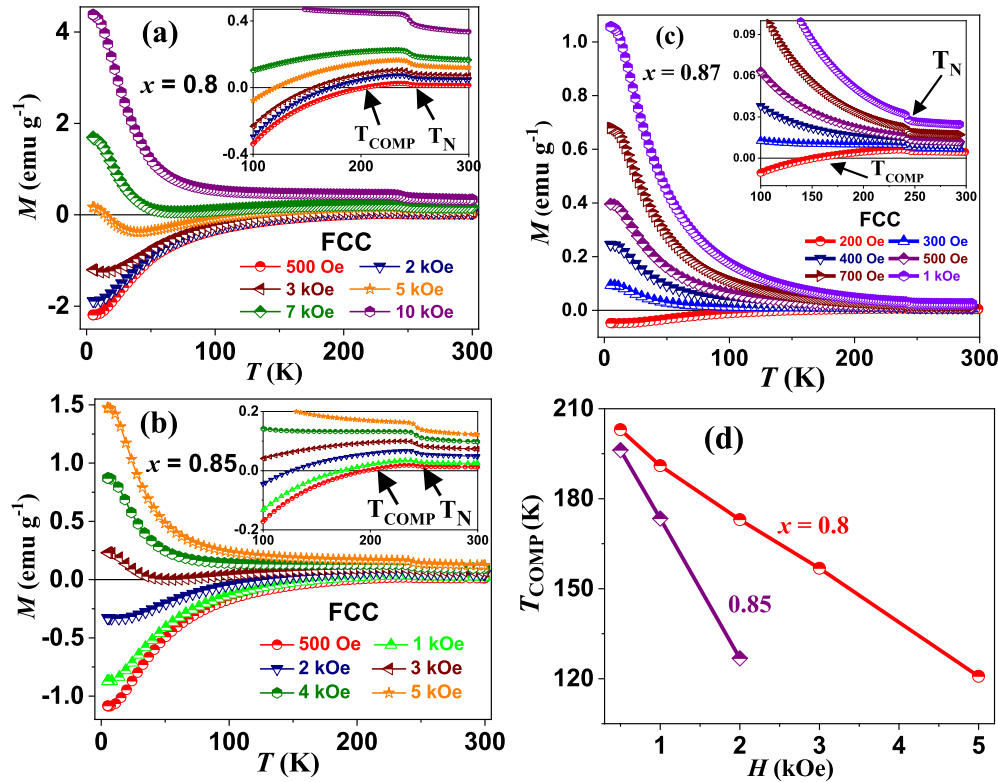


FIG. 2. FCC  $M$  vs  $T$  curves for (a)  $x = 0.8$ , (b)  $x = 0.85$ , and (c) 0.87 recorded under various  $H$ . Insets show the zoomed view of  $M$  vs  $T$  curves near the  $T_{\text{COMP}}$  and  $T_N$ . (d) Variation of  $T_{\text{COMP}}$  with  $H$ .

Since  $\text{La}_{1-x}\text{Pr}_x\text{CrO}_3$  ( $x = 0.8, 0.85$ , and  $0.9$ ) compounds show finite depolarization of incident polarized neutron beam, therefore we have estimated the average domain size of these compounds using the following equation [35,36]:

$$P_f = P_i \exp \left[ -\alpha \left( \frac{d}{\delta} \right) \langle \Phi_\delta \rangle^2 \right], \quad (1)$$

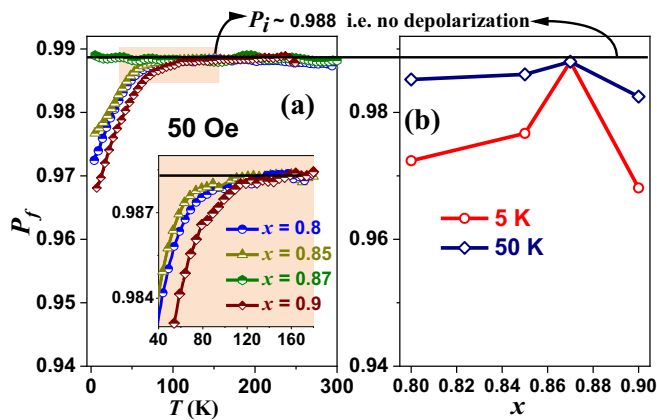


FIG. 3. (a) The transmitted neutron beam polarization ( $P_f$ ) vs temperature ( $T$ ) curves for  $\text{La}_{1-x}\text{Pr}_x\text{CrO}_3$  ( $x = 0.8, 0.85, 0.87$ , and  $0.9$ ) compounds recorded under  $H = 50$  Oe. The zoomed-view of highlighted  $P_f$  curves is shown in the inset displaying the onset of neutron depolarization below  $\sim 100$  and  $\sim 120$  K for  $x = 0.85$  and  $0.8/0.9$ , respectively. (b) The  $x$  dependence of  $P_f$  for  $x = 0.8$  to  $0.9$  at  $5$  and  $50$  K. The black line in both figures at  $P_f \sim 0.988$  indicates the zero neutron depolarization line.

where  $P_i/P_f$  is the initial/final neutron beam polarization,  $\alpha$  ( $\sim 1/3$ ) is a dimensionless parameter,  $d$  ( $\sim 4.4$  mm) is the effective thickness of the samples, and  $\Phi_\delta = (4.63 \times 10^{-10} \text{ G}^{-1} \text{ \AA}^{-2}) \lambda B \delta$  is the precession angle for a neutron of wavelength  $\lambda$  ( $= 1.201 \text{ \AA}$ ) traveling a distance  $\delta$  (average domain size) inside a domain of magnetization  $B$  ( $= 4\pi M_s \rho$ ). Here,  $M_s$  and  $\rho$  are the saturation magnetization and density of the compounds in  $\text{emu g}^{-1}$  and  $\text{g cm}^{-3}$ , respectively. Using all these parameters in Eq. (1),  $\delta \sim 2(1), 1.54(10)$ , and  $4(2) \mu\text{m}$  at  $5$  K for  $x = 0.8, 0.85$ , and  $0.9$  compounds, respectively, are estimated. Thus, the  $x = 0.8, 0.85$ , and  $0.9$  compounds have almost same average domain size, at least within the certainty of our experimental resolution. It may be noted from Eq. (1) that neutron depolarization depends on the product of domain magnetization and domain size. Since the compounds have almost same average domain size, therefore, the depolarization is mainly governed by the domain magnetization in the samples.

### C. Exchange bias

To study the EB in  $\text{La}_{1-x}\text{Pr}_x\text{CrO}_3$  ( $x = 0.8, 0.85, 0.87$ , and  $0.9$ ) compounds, the hysteresis loops are recorded at various temperatures by cooling the compounds under  $5$  kOe magnetic field ( $H_{\text{COOL}}$ ). Figure 4(a) shows the hysteresis loops for all four compounds at  $100$  K. It is worth noting that for  $x = 0.8$  and  $0.85$ , the hysteresis loops shift towards the positive magnetic field axis, i.e., along  $+H$  with  $+H_{\text{COOL}}$ , indicating the presence of inverse EB. While the hysteresis loops are found to be shifted along the negative magnetic



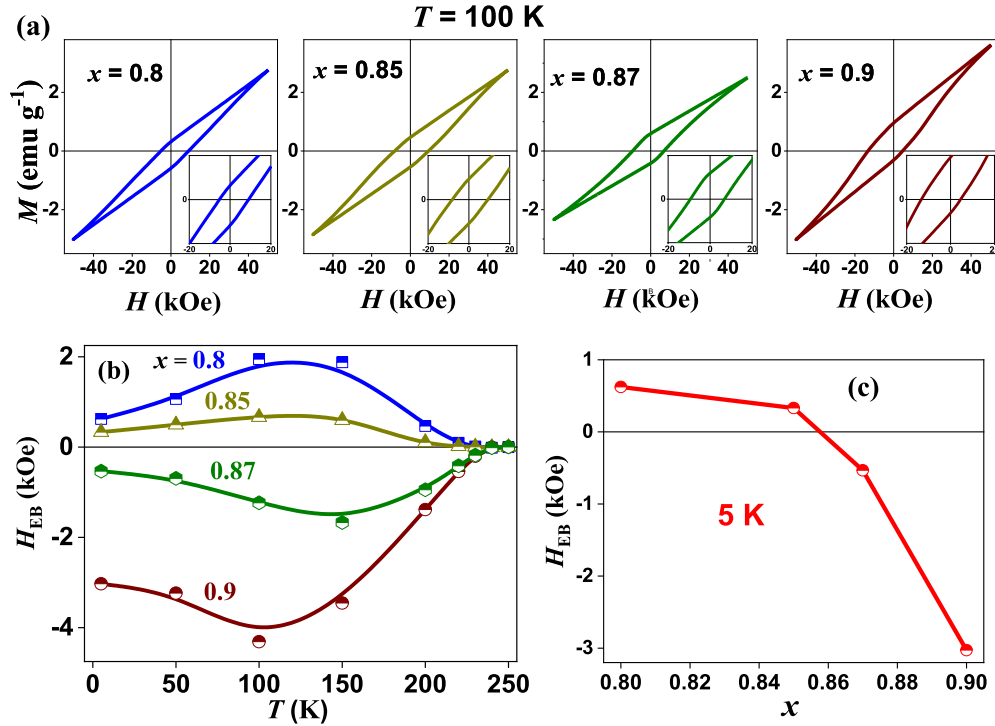


FIG. 4. (a) Field-cooled ( $H_{COOL} = 5$  kOe) hysteresis loops of  $\text{La}_{1-x}\text{Pr}_x\text{CrO}_3$  ( $x = 0.8, 0.85, 0.87$ , and  $0.9$ ) compounds at 100 K. Zoomed view of the hysteresis loops is shown in the inset for better clarity of EB. (b) Temperature dependence of  $H_{EB}$  for all compounds. (c) Variation of  $H_{EB}$  with  $x$  at 5 K.

field axis, i.e., along  $-H$  with  $+H_{COOL}$ , for  $x = 0.87$  and  $0.9$ , thus revealing conventional EB in these compounds. The EB field is defined as  $H_{EB} = \frac{H_{C1} + H_{C2}}{2}$ , here  $H_{C1}$  and  $H_{C2}$  are the coercive fields for the descending and ascending branches of  $M(H)$  hysteresis loop, respectively. The temperature dependence of  $H_{EB}$  is shown in Fig. 4(b). Interestingly, the NM compounds, i.e.,  $x = 0.8$  and  $0.85$  exhibit inverse EB with apparent positive  $H_{EB} > 50$ – $100$  Oe at all the temperatures below 220 K ( $\sim T_{COMP}$ ) and 200 K ( $< T_{COMP}$ ), respectively, while above these temperatures, a very small  $H_{EB} \sim -20$  Oe is observed. The positive  $H_{EB}$  is consistent with the literature reports on other Cr-based NM compounds [23,37–39] as well as matches with our previous studies on  $\text{YbCrO}_3$  [20] and  $\text{La}_{1-x}\text{Pr}_x\text{CrO}_3$  ( $0.25 \leq x \leq 0.75$ ) [27,28]. The non-NM compound (i.e.,  $x = 0.9$ ), on the other hand, exhibits usual negative  $H_{EB}$  throughout the  $T < T_N$  range, which is also consistent with the literature on other non-NM compounds [17,40]. However, for the critical composition,  $x = 0.87$  of  $\text{La}_{1-x}\text{Pr}_x\text{CrO}_3$ , the negative  $H_{EB}$  is found, which is indeed a fascinating observation. The remanence asymmetry ( $M_{EB}$ ) is also calculated using the expression  $M_{EB} = \frac{M_{R1} + M_{R2}}{2}$ , where  $M_{R1}$  and  $M_{R2}$  are the upper and lower remanent magnetizations of  $M(H)$  hysteresis loop, respectively. The  $M_{EB}$  exhibits the similar temperature dependence as that of  $H_{EB}$  except with the opposite sign, i.e., negative for  $x = 0.8, 0.85$  and positive for  $x = 0.87, 0.9$  compounds [Fig. S3(a) in SM [31]].

The  $H_{EB}$  as a function of  $x$  at 5 K is plotted in Fig. 4(c). It should be noted that similar to  $M$  behavior [Fig. 1(f)],  $H_{EB}$  is also changing its sign, however, from positive to negative

across  $x = 0.87$ , indicating that both NM and EB are correlated with each other and have the same underlying origin. Interestingly,  $H_{EB}$  vs  $x$  [Fig. 4(c)] variation is found similar to the  $M_{Cr}$  (FM  $\text{Cr}^{3+}$  moment) and  $H_I$  (internal field) vs  $x$  [see highlighted part of Figs. 7(b) and 7(c)], calculated from the Cooke's model fit (see Discussion section), demonstrating the role of orientations of coupled  $M_{Cr}$  and polarized  $\text{Pr}^{3+}$  ( $M_{Pr}$ ) moments in the sign reversal of  $H_{EB}$  in the present series of  $\text{La}_{1-x}\text{Pr}_x\text{CrO}_3$  compounds.

To understand the EB results for  $x = 0.8, 0.85$ , and  $0.87$  under  $H_{COOL} = 5$  kOe, we have further performed detailed EB experiments under various  $H_{COOL}$ . The calculated  $H_{EB}$  for these compounds are plotted in Fig. 5. Interestingly, both  $x = 0.8$  and  $0.85$  compounds show the sign reversal of  $H_{EB}$  from positive to negative across  $\sim 18$  kOe and  $\sim 7$  kOe, respectively [Figs. 5(a)–5(d)]. It is interesting to note that these values are close to their corresponding maximum  $|H_I|$  values, calculated from the Cooke's model fit (see Discussion section). On the other hand, the  $x = 0.87$  compound shows negative  $H_{EB}$  [Fig. 5(e)] at all  $H_{COOL}$ s. The  $M_{EB}$  is also calculated for these compounds and results are plotted in Figs. S3(b)–S3(d) in SM [31]. Similar to  $H_{EB}$ , the sign reversal of  $M_{EB}$ , however, with opposite polarity, is observed with  $H_{COOL}$  for  $x = 0.8$  and  $0.85$  compounds, while the  $x = 0.87$  shows only positive  $M_{EB}$ . Thus, our comprehensive investigation indicates that EB in these NM compounds can be tuned using both external and internal magnetic fields. In the Discussion section, we show how the coupled  $M_{Cr}$  and  $M_{Pr}$  moments with different orientations lead to the striking EB in these compounds.

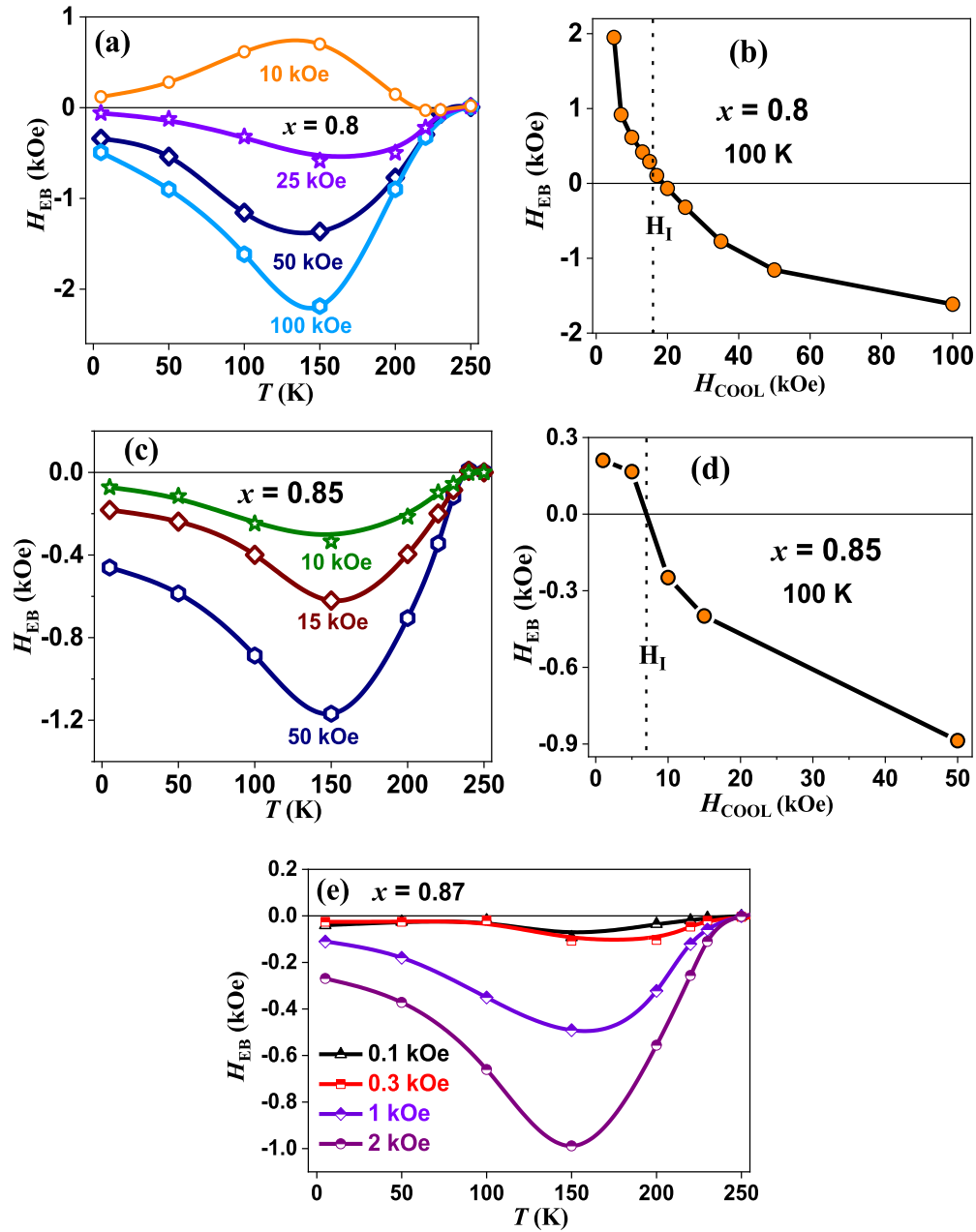


FIG. 5. Thermal variation of  $H_{EB}$  for (a)  $x = 0.8$ , (c)  $x = 0.85$ , and (e)  $x = 0.87$  under different  $H_{COOL}$ s. Variation of  $H_{EB}$  with  $H_{COOL}$  at 100 K for (b)  $x = 0.8$  and (d)  $x = 0.85$ .

#### D. Magnetic neutron diffraction

Since the  $\text{La}_{1-x}\text{Pr}_x\text{CrO}_3$  ( $x = 0.8 - 0.9$ ) compounds show the fascinating phenomena of NM and EB, so it is quite essential to investigate the magnetic ground state of these compounds using a microscopic neutron diffraction (ND) technique. The ND data for all compounds over the temperature range of 5–300 K under a zero magnetic field have been recorded. Since all compounds exhibit similar ND patterns, therefore, the ND data for only  $x = 0.8$  are shown in Fig. 6(a). It is evident from the ND patterns at  $T < T_N$  that  $\{(011)(110)\}$  Bragg peaks are purely magnetic, while  $\{(211)(031)$  and  $\{(132)(310)\}$  Bragg peaks have nuclear contribution also. All magnetic Bragg peaks are indexed with

the propagation vector  $\mathbf{k} = (000)$ . The Rietveld refinement on the ND data has been carried out by considering both nuclear (space group:  $Pnma$ ) and magnetic phases, and a good agreement has been obtained between the experimental and calculated data with a magnetic reliability factor ( $R_{\text{mag}} \sim 3$  [Fig. 6(b)]. The Rietveld refinement infers that the increment in the intensities of above-mentioned Bragg peaks is accounted by the  $G_y$  magnetic ordering of  $\text{Cr}^{3+}$  spins. Same magnetic model has been used for the Rietveld refinement of ND data of  $x = 0.85$ , 0.87, and 0.9 compounds (not shown) and the AFM ( $G_y$ ) component of  $\text{Cr}^{3+}$  has been estimated. Figure 6(c) shows the temperature variation of AFM  $\text{Cr}^{3+}$  moment which exhibits a Brillouin-function type dependence.

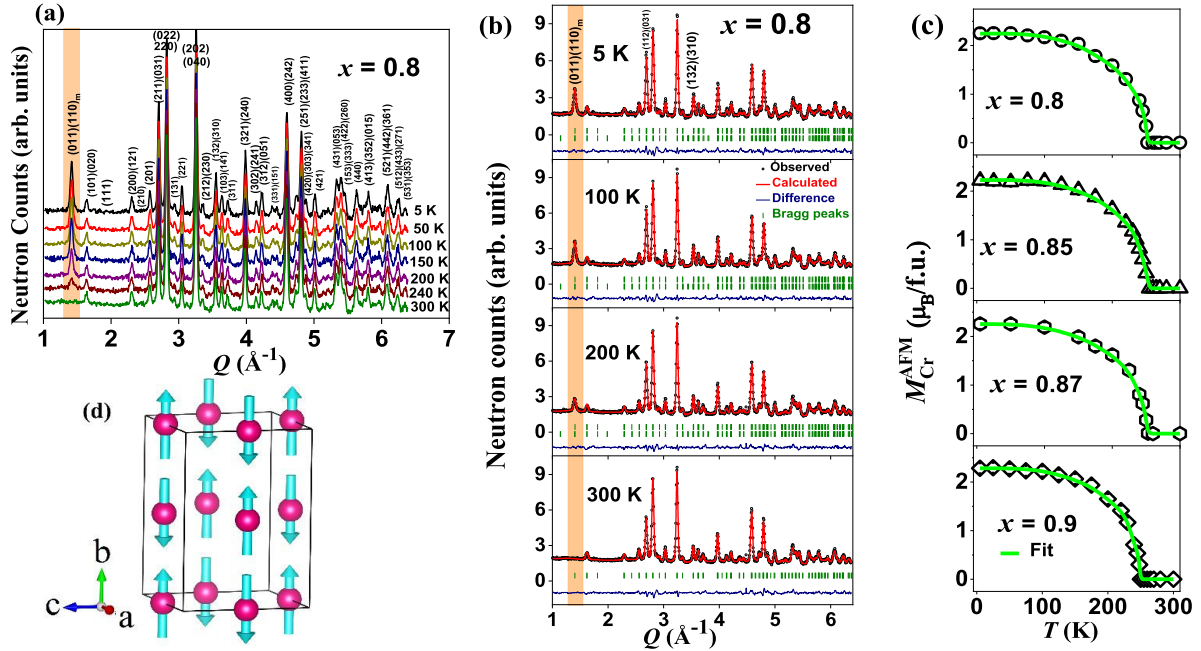


FIG. 6. (a) The ND data of  $x = 0.8$  compound at various temperatures plotted as a function of momentum transfer  $Q = 4\pi \sin\theta/\lambda$ . Here  $\theta$  is the Bragg angle and  $\lambda$  ( $=1.094 \text{ \AA}$ ) is the wavelength of incident neutrons. The neutron intensities are shifted vertically upward for clarity. All Bragg peaks are indexed by their respective  $hkl$  values. (b) Rietveld refined ND patterns of  $x = 0.8$  at some selected temperatures. The open (black) symbols show the experimental data, while the solid red line is a Rietveld fit. The difference of these two data is shown by a navy-blue line at the bottom. The vertical bars (olive), i.e., upper (lower) represent the positions of Bragg reflections. The purely magnetic  $\{(110)(011)\}$  Bragg peaks are highlighted by the orange color. (c) Thermal variation of the AFM ( $G_y$ )  $\text{Cr}^{3+}$  moment in  $\text{La}_{1-x}\text{Pr}_x\text{CrO}_3$  ( $x = 0.8, 0.85, 0.87$ , and  $0.9$ ) compounds. The solid green line shows a fit using molecular-field approach as described in the text. (d) Magnetic structure of these compounds consisting of AFM  $G_y$   $\text{Cr}^{3+}$  spins.

The temperature-dependent AFM  $\text{Cr}^{3+}$  moment has been analyzed using the molecular-field approach. According to this approach, the magnetic moment data can be fitted with the following equation,  $M_{\text{Cr}}^{\text{AFM}}(T) = M_S B_S(x)$ , where  $M_S(T)$  is the saturation magnetization and  $B_S(x)$  is the Brillouin function which can be expressed as  $B_S(x) = \frac{(2J+1)}{2J} \coth(\frac{2J+1}{2J}x) - \frac{1}{2J} \coth(\frac{1}{2J}x)$ , where  $x = \frac{gJ\mu_B H}{k_B T}$ . The above equation successfully fits the experimental AFM  $\text{Cr}^{3+}$  moment [solid green line in Fig. 6(c)] and the estimated  $M_S$  lies between  $\sim 2.2(1)$  to  $2.3(1) \mu_B$  for the present  $\text{La}_{1-x}\text{Pr}_x\text{CrO}_3$  compounds, which are close to the free-ion spin-only  $\text{Cr}^{3+}$  moment ( $3 \mu_B$ ). The magnetic structure of the compounds with AFM  $G_y$  ordering of  $\text{Cr}^{3+}$  spins is shown in Fig. 6(d). Further, it is known that the FM ( $M_{\text{Cr}}$ ) component of the  $\text{Cr}^{3+}$  is generally very small ( $\sim 10^{-2}$ – $10^{-5} \mu_B$ ) in  $\text{RCrO}_3$  compounds [27,41], therefore, it could not be detected in the present ND experiments. On the other hand, despite having theoretically large  $\text{Pr}^{3+}$  magnetic moment ( $gJ \sim 2.6$ – $2.9 \mu_B$  for  $x = 0.8$ – $0.9$ ), it could also not be detected in our zero-field ND experiments. It indicates that the  $\text{Pr}^{3+}$  moment ( $M_{\text{Pr}}$ ) in these compounds is very small and is below the detection limit of the instrument. We may expect the small  $\text{Pr}^{3+}$  moment if the  $\text{Pr}^{3+}$  spins are weakly polarized under the  $\text{Cr}^{3+}$  internal field. However, these small moments are indeed present and an atomistic coupling between them is responsible for the remarkable NM and EB phenomena in the compounds as discussed in the next section.

#### IV. DISCUSSION

For  $\text{RCrO}_3$  systems, it is known that the  $\text{Cr}^{3+}$  atom exhibits canted AFM ordering with both AFM and weak FM ( $M_{\text{Cr}}$ ) moments, and  $\text{R}^{3+}$  polarizes under the internal field of ordered  $\text{Cr}^{3+}$  atoms [42]. In this study, we have probed AFM  $\text{Cr}^{3+}$  moment using a microscopic neutron diffraction technique (Sec. III D), while  $M_{\text{Cr}}$ , which arises from the canting of AFM ordered  $\text{Cr}^{3+}$  moments due to the Dzyaloshinskii-Moriya interaction [41,43] and polarized  $\text{Pr}^{3+}$  moment ( $M_{\text{Pr}}$ ) are estimated using the Cooke's model fit [44] to dc magnetization data. The polarized nature of  $\text{Pr}^{3+}$  in the present compounds is evident from the neutron depolarization experiments (Sec. III B). Interestingly, the estimated  $M_{\text{Cr}}$  and  $M_{\text{Pr}}$  moments and their orientations with respect to internal ( $H_1$ ) and external ( $H$ ) applied magnetic fields not only explain the NM, its elusive disappearance for  $x > 0.87$  and anomalous  $M$  behavior but also provide an insight into the remarkable inverse and conventional EB results.

The dc magnetization data of  $\text{La}_{1-x}\text{Pr}_x\text{CrO}_3$  ( $x = 0.8, 0.85, 0.87$ , and  $0.9$ ) compounds under  $H = 100 \text{ Oe}$  [Fig. 7(a)] are fitted using the following expression of the Cooke's model:

$$M = M_{\text{Cr}} + \frac{C(H + H_1)}{T + \theta} \quad (2)$$

and the parameters  $M_{\text{Cr}}$ ,  $H_1$ , and  $\theta$  are estimated. In the above expression, the second term corresponds to  $M_{\text{Pr}}$ ;  $C = xC_{\text{Pr}}$  is

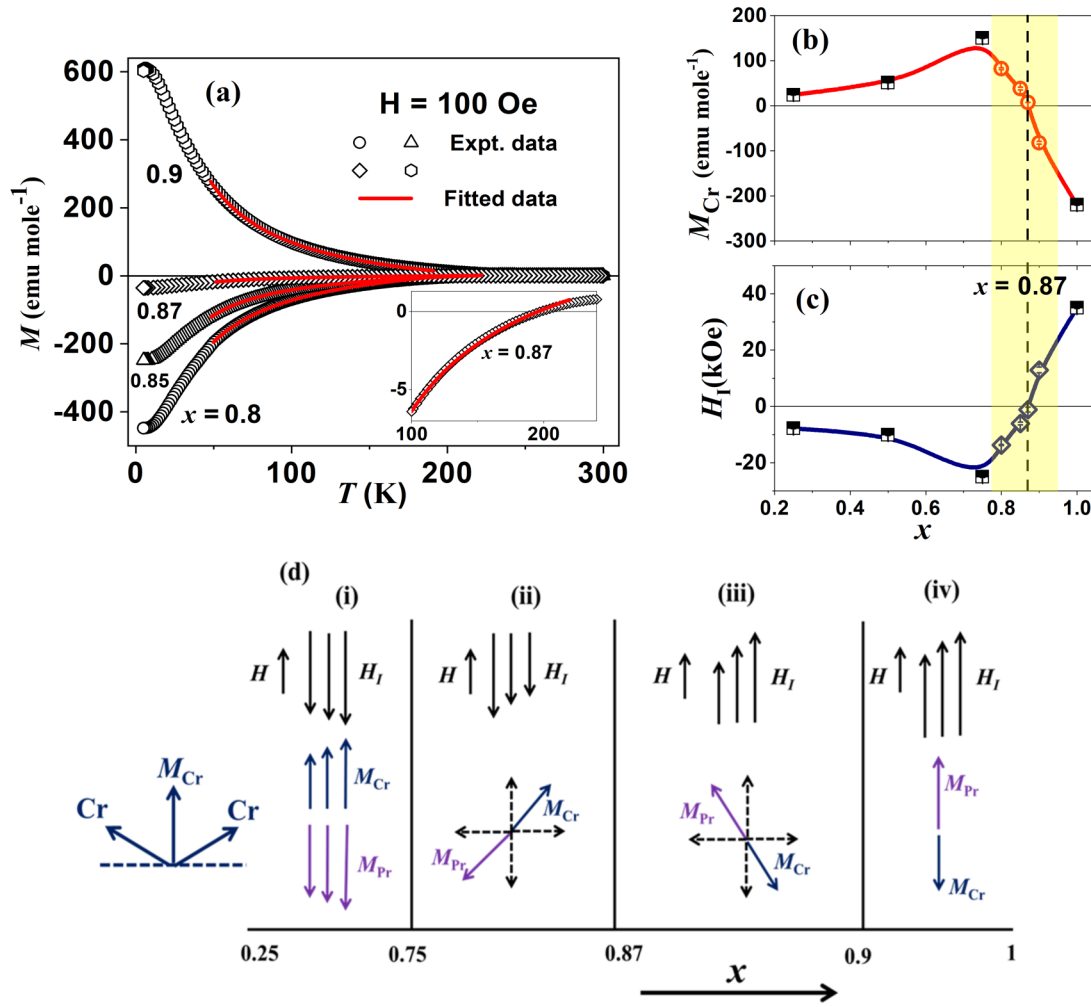


FIG. 7. (a) The  $M$  vs  $T$  data (open symbols) under  $H = 100$  Oe for  $x = 0.8, 0.85, 0.87, 0.9$  compounds and fitted curves (red) using the Cooke's model [Eq. (2)]. Inset shows the zoomed view for  $x = 0.87$ . The  $x$  dependence of (b)  $M_{Cr}$  and (c)  $H_I$ , derived from the Cooke's model. The  $0.8 \leq x \leq 0.9$  range is yellow highlighted. Black squared symbol data are taken from Ref. [28]. (d) Schematic depicts the orientations of  $M_{Cr}$  and  $M_{Pr}$  moments with respect to the external ( $H$ ) and internal ( $H_I$ ) magnetic fields for different  $x$  in  $\text{La}_{1-x}\text{Pr}_x\text{CrO}_3$  compounds. The dotted arrows in (d) serve as a reference for  $M_{Cr}$  and  $M_{Pr}$  moments with respect to  $H$  and  $H_I$ . The drawn moments and magnetic fields in (d) are not shown to scale.

the Curie constant with  $C_{Pr} = 1.602$  emu-K/mole-Oe [27],  $H$  and  $H_I$  are the externally applied and internal magnetic fields, respectively, and  $\theta$  is the Weiss constant. The derived  $\theta$ 's  $\sim 4.9$  (9), 3.2 (1), 7.7 (1), and 4.3 (1) K for the respective compounds indicate the dominant antiferromagnetic interactions. The variation of the derived  $M_{Cr}$  and  $H_I$  as a function of  $x$  is shown in Figs. 7(b) and 7(c). The  $M_{Cr}$  and  $H_I$  for  $x = 0.25, 0.5, 0.75$ , and 1 compounds are also shown, taken from Ref. [28]. Similar to maximum  $|M|$  for  $x = 0.75$  [Fig. 1(e)], the compound also shows the highest positive  $M_{Cr}$  and negative  $H_I$  compared to  $x = 0.25$  and 0.5 compounds. However, it is worthy to note from Figs. 7(b) and 7(c) that for  $x > 0.75$ ,  $M_{Cr}$  ( $|H_I|$ ) start to decrease, changes its sign from positive (negative) to negative (positive) across  $x = 0.87$ , consistent with the  $M$  data shown in Fig. 1(e). Similar to the  $x = 0.8$  and 0.85, positive  $M_{Cr}$  and negative  $H_I$ , however small, are found for  $x = 0.87$ . The positive and negative  $M_{Cr}$  indicate the FM  $\text{Cr}^{3+}$  alignment in the same and opposite direction, respectively, relative to the  $H$ . The negative  $H_I$  ( $> H$ ) for  $x = 0.8$ ,

0.85, and 0.87 compounds make  $M_{Pr}$  negative indicating its alignment opposite to  $H$  as well as  $M_{Cr}$  (aligned along  $H$ ). The dominance of  $M_{Pr}$  over  $M_{Cr}$  (aligned along  $H$ ) below  $T_{\text{COMP}}$  results in the NM in  $x = 0.8, 0.85$ , and 0.87 compounds. On the other hand, for the  $x = 0.9$  compound, the positive  $H_I$  indicates that the positive magnetization in these compounds is dominated by  $M_{Pr}$  polarized along  $H$ , while (negative)  $M_{Cr}$  is opposite to both.

Now we explain the disappearance of NM for  $x > 0.87$  and anomalous  $M$  behavior in  $\text{La}_{1-x}\text{Pr}_x\text{CrO}_3$  compounds. Fig. 7(d)(i–iv) depicts a schematic showing the orientations of  $M_{Cr}$  and  $M_{Pr}$  as a function of  $x$ . For  $0.25 \leq x \leq 0.75$ ,  $|M_{Cr}|$  increases with  $x$  leading to the increase in  $|H_I|$  [Figs. 7(b) and 7(c)] which in turn increases the  $|M_{Pr}|$ . As  $|M_{Pr}|$  is larger than  $|M_{Cr}|$ , it causes the net  $|M| (= |M_{Pr}| - |M_{Cr}|)$  to increase with  $x$  [Fig. 1(e)]. For  $0.75 < x < 0.87$ , a decrease in  $|H_I|$  [Fig. 7(c)] causes some of the  $M_{Pr}$  spins to rotate along the direction of  $H$ . However, both  $M_{Cr}$  and  $M_{Pr}$  are antiferromagnetically coupled by a large  $|H_I|$  of the order of



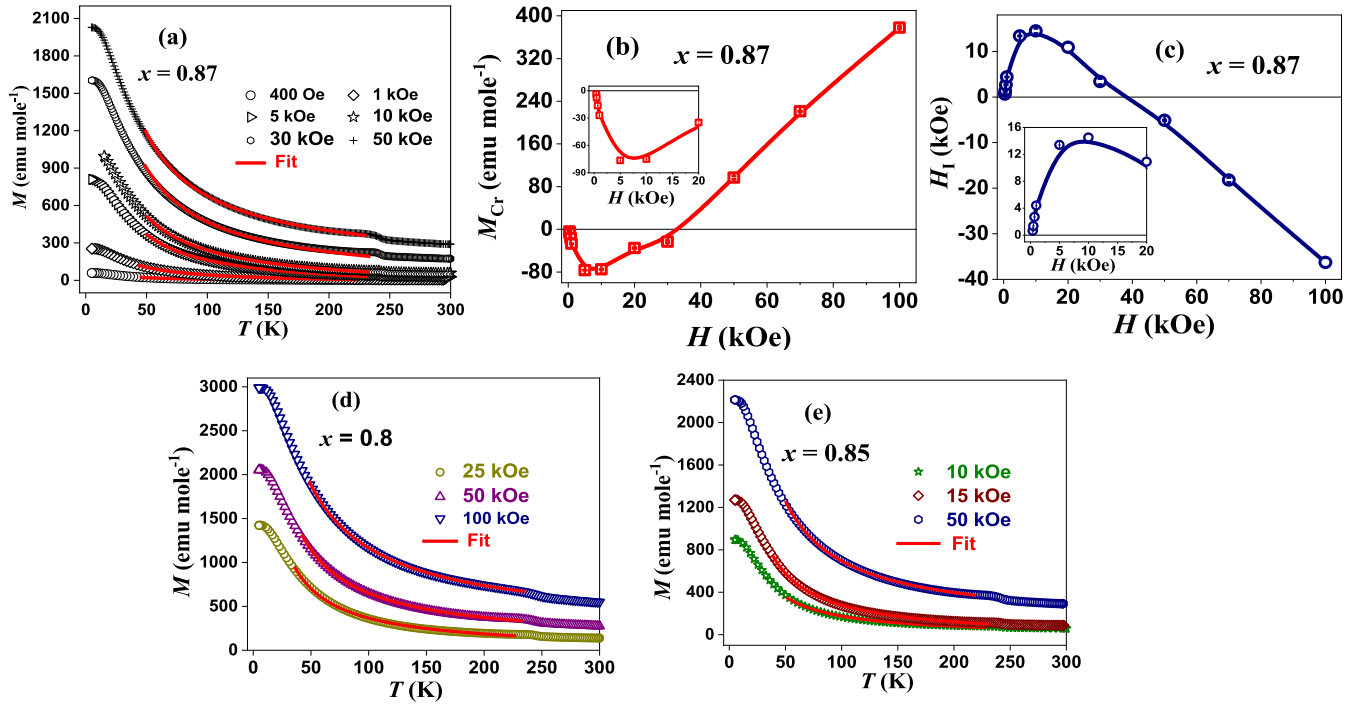


FIG. 8. Fitted (red line)  $M$  vs  $T$  data (open symbols) for (a)  $x = 0.87$ , (d)  $x = 0.8$ , and (e)  $x = 0.85$  compounds using the Cooke's model. The  $H$  variation of (b)  $M_{Cr}$  and (c)  $H_1$  for the  $x = 0.87$  compound. Insets show the enlarged view of  $M_{Cr}$  and  $H_1$  in the low- $H$  region.

$\sim$ kOe, therefore, the coupled sublattices will rotate simultaneously. Consequently, the net ( $M_{Cr}$  and  $M_{Pr}$ ) moment in the direction of  $H$  decreases, which in turn decreases the  $|M|$  [see Fig. 1(e) for  $M$  behavior and Fig. 7(d)(ii) for schematic]. For  $x = 0.87$ ,  $M_{Pr}$  and  $M_{Cr}$  moment orientations are such that they almost compensate each other, resulting in the smallest  $|M|$  for the compound. The almost compensated magnetic domains are also evident from the neutron depolarization experiments (Fig. 3). Further for  $x > 0.87$ , the positive  $H_1$  makes net effective magnetic field ( $H + H_1$ ) positive which causes more and more  $M_{Pr}$  spins to rotate further along the direction of  $H$  or equivalently along  $H_1 + H$ , leading to the disappearance of NM and hence positive  $M$  for  $x > 0.87$  [Fig. 1(e)]. The orientations of  $M_{Cr}$  and  $M_{Pr}$  for  $x > 0.87$  compounds are shown in Fig. 7(d) (iii and iv).

It is interesting to note here that the polarization of  $Pr^{3+}$  spins under the internal field of  $Cr^{3+}$  plays an important role not only in bringing the NM in these compounds but also in NM disappearance for  $x > 0.87$ . It is also interesting to compare the magnetization results of present  $La_{1-x}Pr_xCrO_3$  compounds with the literature reported  $La_{1-x}Ce_xCrO_3$  compounds [45]. These compounds show the NM phenomenon for  $0.8 \leq x \leq 1$  where it was explained by considering the dominant polarized  $Ce^{3+}$  moment, aligned opposite to the  $Cr^{3+}$  moment under its internal field. For the intermediate compositions ( $0.5 < x < 0.8$ ), only a downturn in the field-cooled magnetization data with decreasing temperature, without NM, was observed, also suggesting a finite contribution of polarized  $Ce^{3+}$  moment to the field-cooled magnetization. However, for  $x \leq 0.5$ ,  $La_{1-x}Ce_xCrO_3$  compounds show neither NM nor downturn in the field-cooled magnetization data, implying the effect of polarized  $Ce^{3+}$  moment to the field-

cooled magnetization is negligible. This comparison indicates that the polarized  $Pr^{3+}$  moment is indeed responsible in deciding the interesting magnetic behavior of all compounds of  $La_{1-x}Pr_xCrO_3$  series. Further, we have also fitted the present  $H$ -dependent  $M$  data for  $x = 0.8$  [Fig. 2(a)] and  $0.85$  [Fig. 2(b)] compounds below the  $T_{COMP}$  with the Cooke's model (fitted data are not shown) and parameters  $M_{Cr} \sim 70.54\text{--}98$ ,  $32.26\text{--}45.13$  emu mole<sup>-1</sup> and  $|H_1| \sim 11.5\text{--}15.7$ ,  $5.2\text{--}7$  kOe, respectively, are estimated. The  $\theta$ 's  $\sim 4.9$  and  $3.2$  K are kept fixed for the fitting.

Now we turn our attention to explain the interesting EB results in  $La_{1-x}Pr_xCrO_3$  ( $x = 0.8\text{--}0.9$ ) compounds (Figs. 4 and 5). To understand these EB results, it is necessary to understand the orientation of  $M_{Cr}$  and  $M_{Pr}$  moments with respect to  $H$  in these compounds. We first focus on EB results of  $x = 0.87$  compound. The  $M$  vs  $T$  curves under various  $H$  ( $\geq 300$  Oe) for this compound are fitted using the Cooke's model [Eq. (2)], while some of them are shown in Fig. 8(a), and the derived  $M_{Cr}$  and  $H_1$  are plotted in Figs. 8(b) and 8(c). The  $\theta \sim 7.7$  K is kept fixed for the fitting. The fitted results reveal negative values of  $M_{Cr}$  and positive values of  $H_1$ , similar to  $x = 0.9$ , for  $H \leq 30$  kOe, while reverse polarities are observed for  $H > 30$  kOe. We call this field as critical magnetic field ( $H_{ct}$ ). Since  $H_1$  is positive for  $H \leq H_{ct}$ ,  $M_{Pr}$  aligns along  $H_1$  (also along  $H$ ) and  $M_{Cr}$  opposite to it in the beginning to the  $M$ - $H$  cycle. Therefore, during the magnetic field cycle of  $+H_{max}$  to  $-H_{max}$  in a hysteresis loop, AFM coupling between  $M_{Cr}$  and  $M_{Pr}$  will hinder the rotation of dominant  $M_{Pr}$  along the negative direction of applied  $H$ . This occurs because a positive magnetization state is energetically favorable for the compound, resulting in higher  $H_{C1}$ . Whereas an easy switching of the  $M_{Pr}$  along the direction of positive magnetic field

while changing the magnetic field from  $-H_{\max}$  ( $=50$  kOe) to  $+H_{\max}$  ( $=50$  kOe) in a hysteresis loop makes  $H_{C2}$  smaller. Consequently, a conventional (negative  $H_{EB}$ ) EB is observed. Similar explanation also holds for explaining conventional EB in  $x = 0.9$  [Fig. 4(b)] owing to similar orientations of  $M_{Cr}$  and  $M_{Pr}$  in the compound. Now the question is what happens to the orientations of two spin moments in  $x = 0.87$  when measured under  $H$  ( $=50, 70$ , and  $100$  kOe)  $> H_{ct}$ , and what would be its consequences on the EB sign. It can be seen from Figs. 8(b) and 8(c) that for  $H = 50, 70$ , and  $100$  kOe, the derived  $M_{Cr}$  is positive and  $H_I$  is negative. Since for these field values,  $H$  is much larger than the  $|H_I|$ , it provides high Zeeman energy to  $M_{Pr}$  thus preventing it from aligning opposite to positive  $M_{Cr}$ . This leads to a FM coupling between these moments and hence resulting again a conventional (negative  $H_{EB}$ ) EB.

According to the literature [13,14], it is the only FM interfacial coupling which is responsible for the conventional EB in heterostructures. However, our study shows that it is not only the FM coupling between the moments which brings the conventional EB but AFM coupling can also be responsible for the same effect in single-phase homogeneous magnetic systems. In the next paragraph, we show that the AFM and FM couplings between  $M_{Cr}$  and  $M_{Pr}$  moments can also lead to conventional EB in  $x = 0.8$  and  $0.85$  compounds which supports the conventional EB results for  $x = 0.87$  compound.

Now we focus on the EB results of  $x = 0.8$  and  $0.85$  compounds. We recall from Figs. 4(b) and 5(a)–5(d) that these compounds exhibit the sign reversal of  $H_{EB}$  from positive ( $H_{COOL} < |H_I|$ ) to negative ( $H_{COOL} > |H_I|$ ). Similar tuned  $H_{EB}$  behavior is reported in the literature for  $x = 0.85$ , where authors explained positive and negative  $H_{EB}$  by considering the AFM and FM couplings between  $M_{Pr}$  and  $M_{Cr}$ , respectively [30]. Our results also infer that an AFM coupling leads to positive  $H_{EB}$  in both  $x = 0.8$  and  $0.85$  compounds, and it can be explained by the mechanism described above for  $x = 0.87$ . The only difference is that for  $x = 0.8$  and  $0.85$ , when  $H_{COOL} < |H_I|$  ( $\sim 15.7$  kOe for  $x = 0.8$  and  $\sim 7$  kOe for  $x = 0.85$ ), where NM state is favorable,  $M_{Cr}$  aligns along the direction of  $H$  and  $M_{Pr}$  opposite to it in the beginning of  $M$ - $H$  cycle [28]. This alignment leads to positive  $H_{EB}$  in both the compounds [Figs. 4(b) and 5(a)–5(d)]. Further, similar to the case of  $x = 0.87$ , both FM and AFM couplings between  $M_{Pr}$  and  $M_{Cr}$  moments can contribute to negative  $H_{EB}$  in  $x = 0.8$  and  $0.85$  compounds, rather than only FM coupling, as reported in the literature for  $x = 0.85$  [30]. To explain the present negative  $H_{EB}$  results for  $x = 0.8$  and  $0.85$  [Figs. 5(a)–5(d)], we have fitted their  $M$  vs  $T$  data recorded under  $H = 25, 50$ , and  $100$  kOe for  $x = 0.8$  [Fig. 8(d)], and  $H = 10, 15$ , and  $50$  kOe for  $x = 0.85$  [Fig. 8(e)], using the Cooke's model. Interestingly, for  $x = 0.8$  under  $H$  ( $= 50$  and  $100$  kOe) and  $0.85$  under  $H = 50$  kOe, the derived  $M_{Cr}$  and  $H_I$  results align well with those for  $x = 0.87$  under  $H$  ( $> H_{ct}$ ), revealing a FM coupling and resulting in negative  $H_{EB}$  in the compounds. While for  $x = 0.8$  under  $H = 25$  kOe and  $x = 0.85$  under  $H = 10$  and  $15$  kOe, an AFM coupling between dominant positive  $M_{Pr}$  and negative  $M_{Cr}$  is observed, consistent with  $x = 0.87$  for  $H < H_{ct}$ , again leads to a negative  $H_{EB}$ . Thus, our study reveals that both AFM and FM couplings between two moments can be responsible for the observed negative  $H_{EB}$  in  $x = 0.8, 0.85$ , and  $0.87$  compounds. We would like to mention

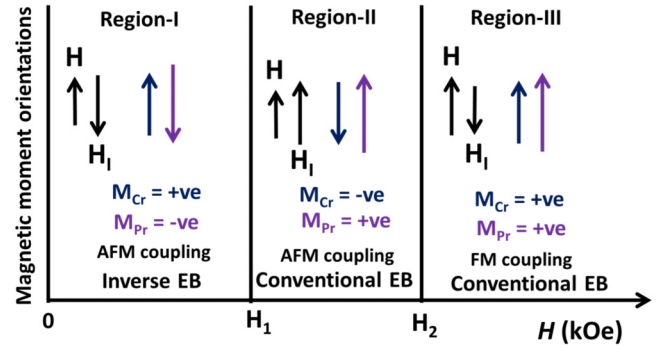


FIG. 9. Schematic diagram showing spin orientations of  $M_{Cr}$  (navy blue) and  $M_{Pr}$  (violet) moments with respect to  $H$  and  $H_I$  in the  $\text{La}_{1-x}\text{Pr}_x\text{CrO}_3$  ( $x = 0.8\text{--}0.9$ ) compounds. Here  $H_1$  and  $H_2$  denote the critical magnetic fields. The drawn variables *viz.* moments and magnetic fields are not on an absolute scale.

that the AFM coupling at high magnetic fields, where the rare-earth sublattice aligns along  $H$  and opposite to transition-metal sublattice, is unusual and rare but has also been reported in  $\text{ErFeO}_3$  single crystals [46,47], which are isostructural to the present compounds ( $H \sim 15$  kOe in Ref. [46] and  $H \sim 180$  kOe in Ref. [47]). Further, it may be noted that despite  $x = 0.87$  exhibits the NM like to  $x = 0.8$  and  $0.85$ , the compound does not show the inverse EB. It may also be noted that the  $H_I \sim -600$  Oe for  $x = 0.87$  in the NM state is significantly smaller than the  $x = 0.8$  ( $H_I \sim -15.7$  kOe) and  $0.85$  ( $H_I \sim -7$  kOe) compounds. This may change initial  $\text{Pr}^{3+}$ - $\text{Cr}^{3+}$  coupling [Figs. 7(b) and 7(c)], responsible for NM, during demagnetization process in the hysteresis loop measurements in such a way that results always conventional EB in the  $x = 0.87$  compound (as discussed earlier) even in the NM state.

Based on our comprehensive magnetization results, we propose a schematic depicting the orientations of  $M_{Cr}$  and  $M_{Pr}$  with  $H$  in  $\text{La}_{1-x}\text{Pr}_x\text{CrO}_3$  ( $x = 0.8\text{--}0.9$ ) compounds as shown in Fig. 9. In the low- $H$  region, the inverse EB (in the NM state) is favored with  $M_{Cr}$  and  $M_{Pr}$  orientations shown in region I. As  $H$  is increased (region II) and exceeds a certain critical field ( $H_1$ ), the  $M_{Cr}$  and  $M_{Pr}$  moments reorient themselves into a different spin configuration with AFM coupling responsible for conventional EB. Upon further increase of  $H$  and above  $H_2$  (region III), the AFM coupling between the moments weakens and it changes into FM coupling which also contributes to conventional EB.

In brief, our comprehensive EB study demonstrates that  $\text{La}_{1-x}\text{Pr}_x\text{CrO}_3$  compounds provide a unique platform to study concurrent occurrences of inverse and conventional EB, which are otherwise rarely observed, based on the AFM and FM/AFM coupling, respectively, between  $M_{Cr}$  and  $M_{Pr}$  moments. Since  $\text{La}_{1-x}\text{Pr}_x\text{CrO}_3$  compounds exhibit remarkable NM and EB phenomena, thus making these useful for thermomagnetic switches and thermal-assisted magnetic random access memory devices. However, an easy magnetization switching feature of critical composition  $x = 0.87$  makes this compound further promising for several advanced technological applications. For instance, the magnetization switching

at a much smaller field ( $\sim 300$  Oe) requires less energy for writing and erasing magnetic states, making this compound an ideal candidate for low-power spintronic memory devices. Furthermore, this feature may also have implications for highly sensitive magnetic sensors and ultrafast magnetic switching devices.

## V. COMMENT ON POLARIZED $\text{Pr}^{3+}$

We finally give a discussion on the polarization of  $\text{Pr}^{3+}$  spins under the internal field of  $\text{Cr}^{3+}$  in  $\text{La}_{1-x}\text{Pr}_x\text{CrO}_3$  compounds and its comparison with other  $R_{1-x}R'_x\text{TMO}_3$  ( $R$  and  $R'$  are two different rare earths and  $\text{TM}$  is a transition metal) [37,48,49] and  $\text{Pr}^{3+}$ -based compounds [50,51]. Barbosa *et al.* explained the NM phenomenon in  $\text{Nd}_{1-x}\text{Pr}_x\text{CrO}_3$  ( $x = 0.15$  to  $0.6$ ) compounds by considering the AFM coupling between FM  $\text{Cr}^{3+}$  and polarized  $\text{Nd}^{3+}$  spins [37]. They completely excluded the polarization of  $\text{Pr}^{3+}$  spins owing to the large crystal-field splitting  $\sim 48$  K between the ground state and first-excited energy levels of the  $\text{Pr}^{3+}$  ions in  $\text{PrCrO}_3$  and considered the  $\text{Pr}^{3+}$  spins in paramagnetic state. Contrary to  $\text{Nd}_{1-x}\text{Pr}_x\text{CrO}_3$ ,  $\text{Nd}_{1-x}\text{Dy}_x\text{CrO}_3$  ( $x = 0.2$  and  $0.33$ ) [16,40] compounds do not show the NM phenomenon indicating the crucial role of  $\text{Pr}^{3+}$  in bringing the NM in  $\text{Nd}_{1-x}\text{Pr}_x\text{CrO}_3$ . Further, in  $\text{Y}_{1-x}\text{Pr}_x\text{CrO}_3$  [48] and  $\text{Gd}_{0.5}\text{Pr}_{0.5}\text{MnO}_3$  [49] compounds, authors also considered the polarization of  $\text{Pr}^{3+}$  under the internal field of  $\text{Cr}^{3+}$  and  $\text{Mn}^{3+}$ , respectively, to explain the NM, consistent with our present study on  $\text{La}_{1-x}\text{Pr}_x\text{CrO}_3$ . Here it is worthy to note that both end members of  $\text{Y}_{1-x}\text{Pr}_x\text{CrO}_3$  and  $\text{Gd}_{0.5}\text{Pr}_{0.5}\text{MnO}_3$  compounds do not show the NM phenomenon further supporting the role of polarized  $\text{Pr}^{3+}$  in bringing the NM in these two compounds. Furthermore, in some Pr-based intermetallic compounds, the polarized or induced moment of Pr is observed, as indicated by the Schottky anomaly in heat capacity data, provided that the crystal field splitting between ground and first excited levels of Pr is large ( $\sim 90$  K) [50,51]. Therefore, more investigations are required on  $\text{Pr}^{3+}$ -based compounds to get insight of the exact cause of its polarization and hence its role in deciding the magnetic properties of a given magnetic material. At the same time, we cannot neglect the polarization of  $\text{Pr}^{3+}$  in the present non-NM  $\text{La}_{1-x}\text{Pr}_x\text{CrO}_3$  ( $x > 0.87$ ) compounds also. This is because if  $\text{Pr}^{3+}$  spins are in paramagnetic state without any polarization, then there would not be any depolarization of the polarized neutron beam (Fig. 3) as no significant change in the FM  $\text{Cr}^{3+}$  moment is expected with increasing  $\text{Pr}^{3+}$  concentration causing itself to depolarize the incident-polarized neutron beam [28]. Since the observed  $P_f$  variation [Fig. 3(b)] is similar to that of  $H_i$  [see highlighted part of Fig. 7(c)], it further suggests the polarization of  $\text{Pr}^{3+}$  in these  $\text{La}_{1-x}\text{Pr}_x\text{CrO}_3$  compounds. The polarization of  $\text{Pr}^{3+}$  under the internal field of  $\text{Cr}^{3+}$  or  $\text{Fe}^{3+}/\text{Cr}^{3+}$  is reported in other non-NM orthochromite compounds ( $\text{Gd}/\text{Pr}$ ) $\text{CrO}_3$ ,  $\text{Pr}_{0.5}\text{Eu}_{0.5}\text{CrO}_3$ ,  $\text{Pr}_{0.5}\text{Y}_{0.5}\text{CrO}_3$ , and  $\text{PrFe}_{0.5}\text{Cr}_{0.5}\text{O}_3$  [52,53].

## VI. SUMMARY AND CONCLUSIONS

The comprehensive investigations of two magnetic phenomena involving NM and EB have been carried out on  $\text{La}_{1-x}\text{Pr}_x\text{CrO}_3$  ( $x = 0.8 - 0.9$ ) compounds. Despite all compounds belonging to the same  $Pnma$  space group, notable and interesting magnetic behaviors are observed with varying  $\text{Pr}^{3+}$  composition, temperature, and, more importantly, with varying magnetic field. The dc magnetization study reveals several striking features: (i) NM phenomenon is observed in  $x = 0.8, 0.85, 0.87$  but not in  $x = 0.9$ . (ii) An anomalous magnetization behavior with a minimum magnetization for  $x = 0.87$  is noted, despite its higher  $\text{Pr}^{3+}$  concentration compared to  $x = 0.8$  and  $0.85$ . (iii) Remarkably, both inverse and conventional EB are observed in  $x = 0.8$  and  $0.85$ , while only conventional EB is present in  $x = 0.87$  and  $0.9$ . Interestingly, all these results are explained by considering the competition between the polarized  $\text{Pr}^{3+}$  ( $M_{\text{Pr}}$ ) and weak ferromagnetic component of canted  $\text{Cr}^{3+}$  ( $M_{\text{Cr}}$ ) moments derived from the Cooke's model fit, indicating that both phenomena share the same underlying physics origin. The AFM  $\text{Cr}^{3+}$  moments derived from the neutron diffraction for all compounds are fitted using the molecular-field approach. The most notable conclusion from this study is that AFM as well as FM coupling can lead to the conventional EB in the compounds, in contrast to the previously understood model, which only considered FM coupling. Furthermore, the detailed and comprehensive study also demonstrates that both NM and EB are indeed correlated with each other and thus strengthen the subject knowledge of these two fascinating phenomena in condensed matter physics research area. The intriguing features of NM and EB reversals with temperature and magnetic field in the present  $\text{La}_{1-x}\text{Pr}_x\text{CrO}_3$  compounds are reminiscent of similar manipulations of magnetization and EB with magnetic field, electric field, current, and strain in various heterostructures, facilitating their applications in spintronic devices [54–56].

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## DATA AVAILABILITY

The data that support the findings of this article are not publicly available. The data are available from the authors upon reasonable request.

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