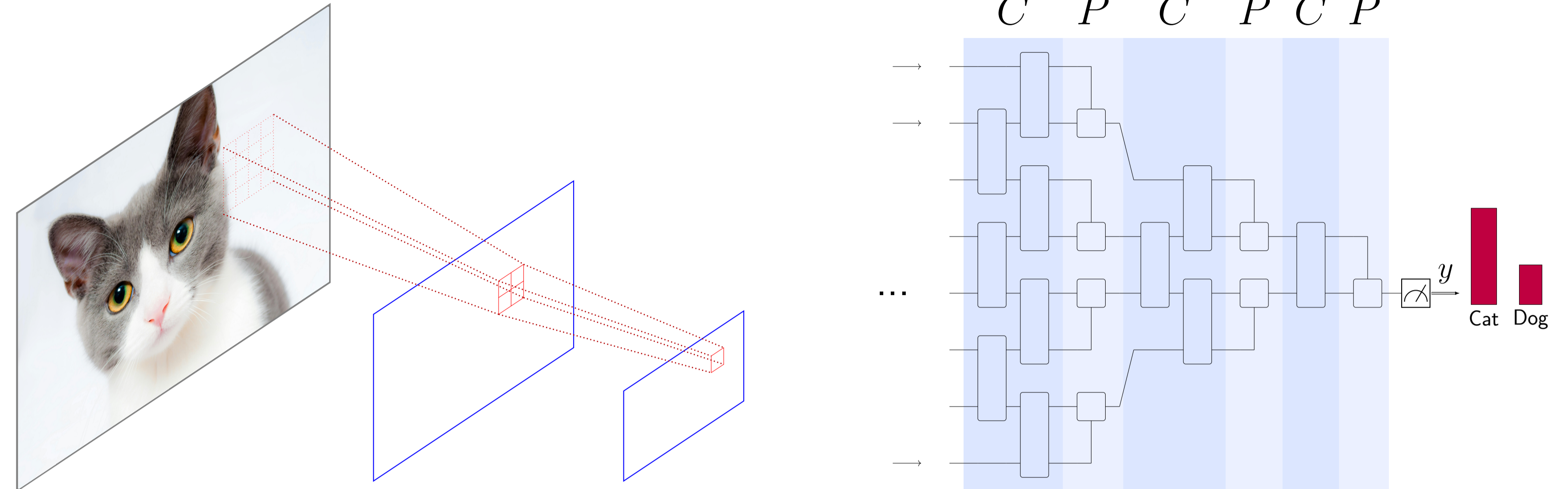


## Background

Quantum convolutional neural networks (QCNNS) extend classical CNN concepts to parameterized quantum circuits (PQCs), but their deployment on NISQ devices is challenging [1, 2]. To fit QCNNS on current hardware, often dimensionality-reduction techniques (e.g. PCA, autoencoders) are applied, which can lead to:

- Loss of fine details
- Disrupt spatial structure that CNNs exploit
- Obscuring whether the QCNN or the pre-processing do the classification
- Limiting generalization to more complex architectures



## Fragment encoding

We encode image fragments into a compact quantum representation, where each qubit sequentially processes a fragment analogous to multiple convolutional layers.

- Classical convolution:

$$x_{i,j}^{(l+1)} = \sum_{a=1}^k \sum_{b=1}^k w_{a,b} x_{i+a,j+b}^{(l)} \quad (1)$$

- Fragment encoding:

$$U(\phi_0)E(x_0) \dots U(\phi_k)E(x_k) = (U(\phi_0)E(x_0)) \dots (U(\phi_k)E(x_k)), \quad (2)$$

$$E(x_{i,j}^{(l+1)}) = \prod_{a=1}^k \prod_{b=1}^k U(\phi_{a,b}^{(l)}) E(x_{i+a,j+b}^{(l)}). \quad (3)$$

## Proposition

The depth of fragment encoding scales as  $O(1)$ .

## Scaling

We evaluate QCNN architectures across different qubit counts. In the Best Model column, the sequence before '→' denotes the fragment-encoding gates, and the sequence after '→' refers to the QCNN circuit blocks from [3]. Models are read left to right in layer order.

Number of Qubits	Best Model	Accuracy
1	$R_x - R_y - R_z - R_x - R_y \rightarrow U3$	51.35
4	$U3 - U3 - U3 - U3 \rightarrow C5$	61.37
16	$U3 - U3 - U3 \rightarrow Pool - C2$	71.79

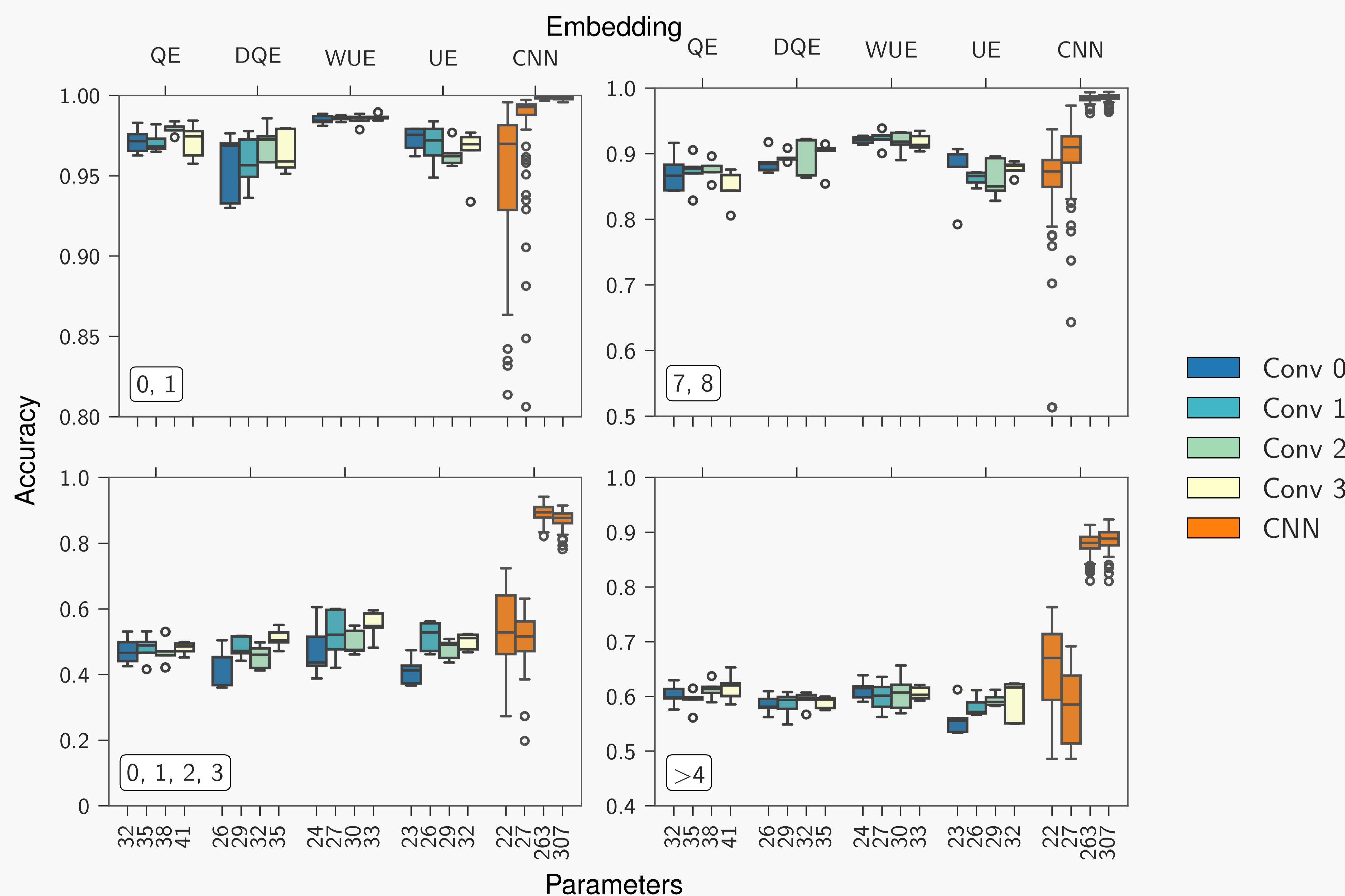
## CNN baseline

To ensure a fair comparison, we optimize the classical CNN baseline using Bayesian optimization [4, 5] over 50,000 sampled architectures (100-run averaged performance). The objective encourages high accuracy while penalizing overly large models:

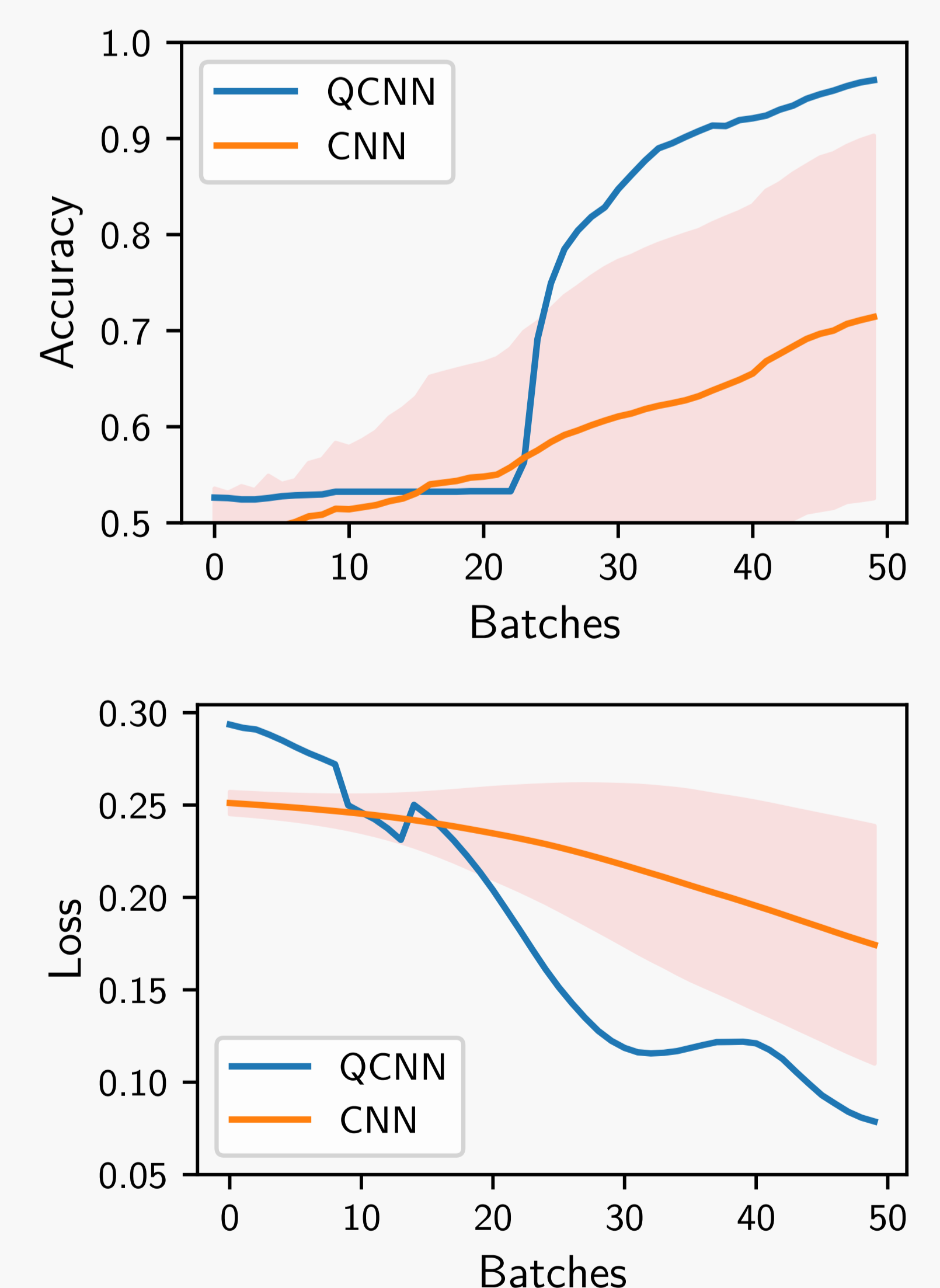
$$\mathcal{L}_{CNN} = \begin{cases} 1.9 - \text{acc}, & \text{if } \text{acc} \leq 0.9 \\ \frac{\text{params}}{100,000}, & \text{otherwise} \end{cases} \quad (4)$$

## Subset MNIST 49 qubit classification

### Simulation



### IBM Heron r2 (0 vs. 1)



## Conclusion & limitations

- QCNN accuracy improves with more qubits
- QCNNS converge faster than classical models
- Trainable encoding sequences hint at efficient quantum feature maps
- Tasks were simple (subsets MNIST)
- QCNNS are classically simulatable if not carefully designed [6]

## References

- [1] GRANT, Edward *et al.* Hierarchical quantum classifiers. **npj Quantum Information**, Nature Publishing Group UK London, v. 4, n. 1, p. 65, 2018.
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