

High-temperature multiferroicity and strong magnetocrystalline anisotropy in 3d-5d double perovskites

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Using density functional calculations we explore the properties of as-yet-unsynthesized 3d-5d ordered double perovskites ($A_2BB'O_6$) with highly polarizable Bi^{3+} ions on the A site. We find that the $\text{Bi}_2\text{NiReO}_6$ and $\text{Bi}_2\text{MnReO}_6$ compounds are insulating and exhibit a robust net magnetization that persists above room temperature. When the in-plane lattice vectors of the pseudocubic unit cell are constrained to be orthogonal (for example, by coherent heteroepitaxy), the ground states are ferroelectric with large polarization and a very large uniaxial magnetocrystalline anisotropy with easy axis along the ferroelectric polarization direction. Our results suggest a route to multiferroism and electrically controlled magnetization orientation at room temperature.

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I. INTRODUCTION

There is increasing current interest in developing multiferroic materials with ferromagnetic and ferroelectric order in the same phase for future spintronic or magnetoelectronic devices.^{1–4} Although new multiferroics are being predicted and synthesized at an accelerating pace, a major obstacle for their adoption in applications remains their low magnetic ordering temperatures, which are generally far below room temperature. The problem more generally lies in the scarcity of insulators with any net magnetization—either ferro- or ferrimagnetic—at room temperature, even before the additional requirement of polarization is included. Most work on novel multiferroics has been restricted to 3d transition metal oxides (see, for example, Refs. 5–12), motivated by the expectation that 4d or 5d compounds would likely be metallic. However, recent work on new 3d-5d double perovskites^{13,14} showed this to be a misconception and identified a ferrimagnetic insulator, $\text{Sr}_2\text{CrOsO}_6$, with magnetic ordering temperature well above room temperature. First-principles calculations have been shown to accurately reproduce the measured magnetic ordering temperatures^{15,16} in the Sr_2CrMO_6 series ($M = \text{W}, \text{Re}, \text{Os}$)¹⁷ and have been invaluable in explaining the origin of the robust ferrimagnetic ordering.^{18–21}

We build here on these recent developments to propose a route to achieving multiferroics with higher magnetic ordering temperatures. We use 3d-5d double perovskites to achieve high-temperature magnetism combined with insulating behavior and introduce lone-pair active cations on the A sites to induce polarizability.^{22,23} The heavy Bi and 5d elements provide an additional desirable feature: The spin-orbit interaction strongly couples the magnetic easy axis to the ferroelectric polarization direction. Specifically, we explore two compounds, $\text{Bi}_2\text{MnReO}_6$ and $\text{Bi}_2\text{NiReO}_6$. We use density functional theory to calculate their zero Kelvin structure and magnetic ordering, and we use Monte Carlo simulations with parameters extracted from the first-principles calculations to calculate their magnetic ordering temperatures. We find that both materials are magnetic insulators, with ordering temperatures well above room temperature. While the global ground state in both materials is antipolar, we show that when the in-plane lattice vectors form an angle close to 90°

a ferroelectric phase results. In practice this could be achieved using coherent heteroepitaxy and the resulting ferroelectricity could be manipulated using strain. We show that the magnetic behavior results from an antiferromagnetic superexchange^{17,24} and the ferroelectricity from the Bi^{3+} lone pairs, reminiscent of other Bi-based multiferroics. Finally, we investigate the effect of strong spin-orbit coupling (SOC) due to the presence of heavy Bi^{3+} and Re^{4+} cations on the structural, magnetic, and ferroelectric properties of these compounds.

II. METHOD OF CALCULATION

Structural optimizations were performed using the Vienna *ab initio* Simulation Package (VASP) with projector augmented potentials (PAW) potentials;²⁵ the semicore p states of Mn, Ni, and Re and the d states of Bi were included in the valence. We used an energy cutoff of 500 eV and $6 \times 6 \times 6$, $4 \times 4 \times 6$, and $4 \times 4 \times 4$ Γ -point centered k -point meshes for unit cells containing 10, 20, and 40 atoms, respectively. The exchange-correlation functional was treated within the generalized gradient approximation (GGA);²⁶ while extension to the GGA + U method had only a small influence on the electronic properties, we discuss later its effect on the structural behavior. Magnetic ordering temperatures were obtained using a finite-temperature Monte Carlo scheme within a Heisenberg Hamiltonian $H = -\frac{1}{2} \sum_{i,j} J_{i,j} \mathbf{M}_i \cdot \mathbf{M}_j$, where $\mathbf{M}_i$ and $\mathbf{M}_j$ are the magnetic moments on sites i and j of the crystal lattice. The exchange constants $J_{i,j}$ were calculated in the frozen-magnon scheme²⁷ using the all-electron full-potential linearized augmented plane-wave code FLEUR,²⁸ with a plane-wave cutoff of 4.2 hartrees and $15 \times 15 \times 15$ k -points and a $6 \times 6 \times 6$ spin-spiral grid in a 10-atom unit cell. Ferroelectric polarizations were extracted from the shifts of the centers of Wannier functions.²⁹ The magnetocrystalline anisotropy energy was extracted from the self-consistent total-energy calculations within the FLEUR code, on a $13 \times 13 \times 13$ k -point grid.

First, we calculate the lowest-energy structure for both $\text{Bi}_2\text{MnReO}_6$ and $\text{Bi}_2\text{NiReO}_6$ within the GGA approximation. We proceed by successively freezing in the 12 centrosymmetric combinations of tilts and rotations of the oxygen octahedra

that can occur in ordered double perovskites.³⁰ We then further reduce the symmetry of these lowest-energy tilt systems by displacing the anions and cations relative to each other in the manner of a polar displacement. Next we optimize the atomic positions (by minimizing the Hellmann–Feynman forces), as well as the unit cell shape and volume within each symmetry. In this first series of optimizations we assume ferrimagnetic ordering and do not include SOC; the influence of SOC on the lowest-energy structures is examined later.

III. GROUND-STATE STRUCTURE AND INFLUENCE OF EPITAXIAL CONSTRAINTS

Our calculations yield the same monoclinic, centrosymmetric $P2_1/n$ symmetry ground state for both compounds. It is characterized by an $a^-a^-c^+$ tilt pattern of the oxygen octahedra. Two lattice vectors are identical with angles of 93.6° and 93.5° between them in the Mn and Ni compounds, respectively (in the following we refer to these as the “in-plane” lattice vectors); the third lattice vector is perpendicular to the first two and of different length. Importantly, in both compounds there is a slightly higher energy ferroelectric (FE) structure with rhombohedral $R\bar{3}$ symmetry (see Table I). The $R\bar{3}$ structure corresponds to an $a^-a^-a^-$ tilt pattern yielding lattice vectors of equal length and rhombohedral angles of 60° and 61° for the Mn and Ni compounds, respectively, combined with polar relative displacements of anions and cations along the $[111]$ rhombohedral axis induced by the well-established stereochemically active Bi lone pair²² (see Fig. 1). The energy of the FE phase is significantly lower than that of the corresponding centrosymmetric $R\bar{3}$ phase, suggesting a high ferroelectric ordering temperature if this symmetry could be stabilized. For comparison, in the prototypical multiferroic BiFeO_3 with T_C of 1103 K, we obtain a difference of 515 meV per two formula units between the corresponding states. The calculated polarization in both cases is along the $[111]$ direction and comparable in size to that of BiFeO_3 (see Table II).

While the ground state $P2_1/n$ phase is of interest in its own right as a possible high-temperature magnetic insulator, we next explore whether it is possible to identify conditions that stabilize the $R\bar{3}$ ferroelectric phase. We use the fact that in the FE $R\bar{3}$ phase all three lattice vectors have equal length, and the rhombohedral angle is equal or close to the ideal value of 60° . In contrast, in the $P2_1/n$ phase, only the lengths of the two in-plane lattice vectors are equal, and the inter-in-plane angles deviate strongly from the ideal 90° . Motivated by these observations, we first constrain all three lattice parameters to be

TABLE I. Total energies (per formula unit) of the lowest-energy phases of $\text{Bi}_2\text{MnReO}_6$ and $\text{Bi}_2\text{NiReO}_6$ and the cubic $Fm\bar{3}m$ phase with respect to their ground-state $P2_1/n$ phase.

Symmetry	Tilt system (in Glazer notation ³¹)	Total energy	
		$\text{Bi}_2\text{MnReO}_6$	$\text{Bi}_2\text{NiReO}_6$
$Fm\bar{3}m$	$a^0a^0a^0$	1.86 eV	2.02 eV
$R\bar{3}$	$a^-a^-a^-$	248 meV	333 meV
$R\bar{3}$	$a^-a^-a^-$ + FE shift	32 meV	18 meV

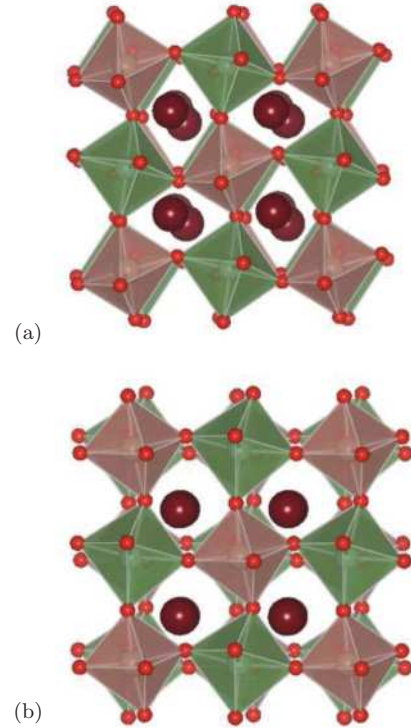


FIG. 1. (Color online) (a) Ground-state $P2_1/n$ structure and (b) the ferroelectric $R\bar{3}$ structure of the double perovskites $\text{Bi}_2\text{MnReO}_6$ and $\text{Bi}_2\text{NiReO}_6$. Bi^{3+} cations are depicted as the large (brown) spheres and O^{2-} as the small (red) spheres. Re^{4+} and Mn^{2+} (Ni^{2+}) are alternating in the shaded octahedra, in a three-dimensional checkerboard manner (this is indicated by the color of the octahedra). While in the $P2_1/n$ symmetry the Bi^{3+} cations form an “antipolar” pattern, their coherent shift along the $[111]$ direction can be clearly seen in the $R\bar{3}$ structure.

equal in length and indeed find that this constraint stabilizes the FE phase. Next we enforce that only two of the three lattice parameters are equal in length, but constrain them to be perpendicular to each other and again find that the FE phase is the lowest energy.³² Such a constraint could be achieved in practice through coherent heteroepitaxy between a thin film and a substrate and is often described as a biaxial strain state in the literature. In Fig. 2(a), we show the calculated energies of the previously $R\bar{3}$ and $P2_1/n$ structure types subject to this additional constraint, with the in-plane lattice parameters varied over a range of realistic substrate strains corresponding

TABLE II. Properties of the bulk ferroelectric $R\bar{3}$ phase in $\text{Bi}_2\text{MnReO}_6$ and $\text{Bi}_2\text{NiReO}_6$ with and without the SOC included: band gap, ferroelectric polarization P and the total magnetic moment M (spin + orbital in case of SOC) per formula unit (f.u.).

SOC	Compound	Band gap (eV)	P ($\mu\text{C}/\text{cm}^2$)	M ($\mu_B/\text{f.u.}$)
Off	$\text{Bi}_2\text{MnReO}_6$	0.7	84	2
	$\text{Bi}_2\text{NiReO}_6$	0.3	78	1
On	$\text{Bi}_2\text{MnReO}_6$	0.4	86	2.34
	$\text{Bi}_2\text{NiReO}_6$	0.2	80	0.58

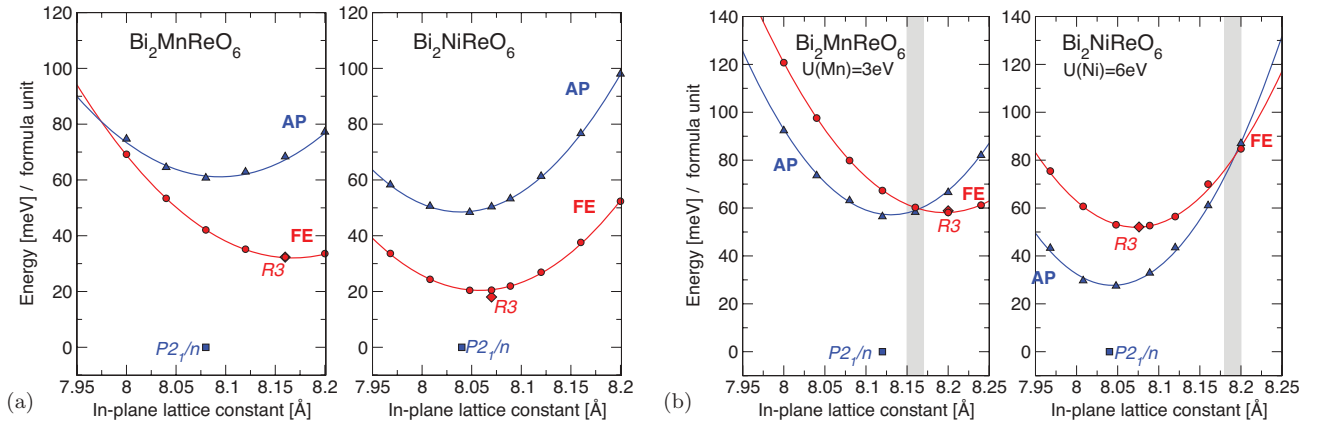


FIG. 2. (Color online) (a) Distorted Bi₂MnReO₆ and Bi₂NiReO₆ obtained from the R3 (red circles) and P₂₁/n (blue triangles) structure by constraining the two in-plane lattice vectors to be equal and the angle between them to 90°. The out-of-plane parameter and the ionic positions were relaxed. The energies are positioned with respect to the bulk unconstrained P₂₁/n ground state (blue squares). The red diamonds show the energies for the unconstrained R3 structure. A crossover between the antipolar (AP) and the ferroelectric (FE) state occurs at 1.8% (with respect to the minimum of the FE curve) of compressive strain in Bi₂MnReO₆. Note that the energy of the R3 state lies on the strain curve for Bi₂MnReO₆, but is somewhat lower for Bi₂NiReO₆, due to the choice of a square in-plane lattice: the rhombohedral angle in R3 phase of Bi₂MnReO₆ is 60°, while in Bi₂NiReO₆ it is 61°. (b) Similar to (a), with an addition of a Hubbard U on Mn (3 eV) and Ni (6 eV) 3d states. The shaded area shows the AP-FE crossover region.

to (001) epitaxial growth. For each in-plane lattice parameter we allow the length and angle of the out-of-plane lattice parameter and atomic positions to relax to their lowest-energy configurations. Our main finding is that, under the investigated constraint, the FE phase is lower in energy than the antipolar (AP) phase. At the optimized value of the in-plane lattice parameter (8.16 Å for Bi₂MnReO₆ and 8.07 Å for Bi₂NiReO₆) the energy differences between the FE and AP phases are 36 and 30 meV per formula unit, respectively. The FE phases are robustly insulating with calculated band gaps of 0.7 and 0.3 eV, respectively, and have large polarizations of 84 $\mu\text{C}/\text{cm}^2$ (Bi₂MnReO₆) and 81 $\mu\text{C}/\text{cm}^2$ (Bi₂NiReO₆) along the pseudocubic [111] direction. Notice, however, that as the in-plane compressive strain is applied, the differences in energies reduce, and in fact in Bi₂MnReO₆ a crossover is reached at a compressive strain value of 1.8%. We therefore expect that both compounds, although AP in bulk, will in fact be ferroelectric and hence multiferroic in thin-film form, over a range of experimentally accessible strains. We see later that SOC tips the scale toward the FE phase, while electron correlations favor the AP phase.

IV. ELECTRONIC AND MAGNETIC PROPERTIES OF THE FERROELECTRIC PHASE

Next, we analyze the magnetic behavior of the two ferroelectric compounds. We find that in both cases the lowest-energy ordering is ferrimagnetic, with the moments on the 3d and 5d transition metal ions antialigned (see Fig. 3). In both compounds, Re is in formal oxidation state 4⁺ corresponding to a filled $d - t_{2g}$ manifold in the minority spin-channel. The oxidation states of Mn in Bi₂MnReO₆ and of Ni in Bi₂NiReO₆ are 2⁺: $t_{2g}^3 e_g^2$ (high spin) for Mn and $t_{2g}^6 e_g^2$ for Ni. Due to these specific configurations of the outer electronic shells, and the nearly 150° Mn-O-Re (Ni-O-Re) angle, the magnetic moments on Re and Mn/Ni are coupled

via an antiferromagnetic superexchange mechanism.^{34–36} The result is a ferrimagnetic configuration with a total spin moment of $2 \mu_B$ in Bi₂MnReO₆ and $1 \mu_B$ in Bi₂NiReO₆.

Our calculated magnetic ordering temperatures in the ferroelectric phase are 330 K for Bi₂MnReO₆ and 360 K for Bi₂NiReO₆, both significantly above room temperature. As a comparison, using the same method, we calculate a magnetic ordering temperature of 670 K for Sr₂CrOsO₆ (the experimental value is 725 K). Note that if growth can only

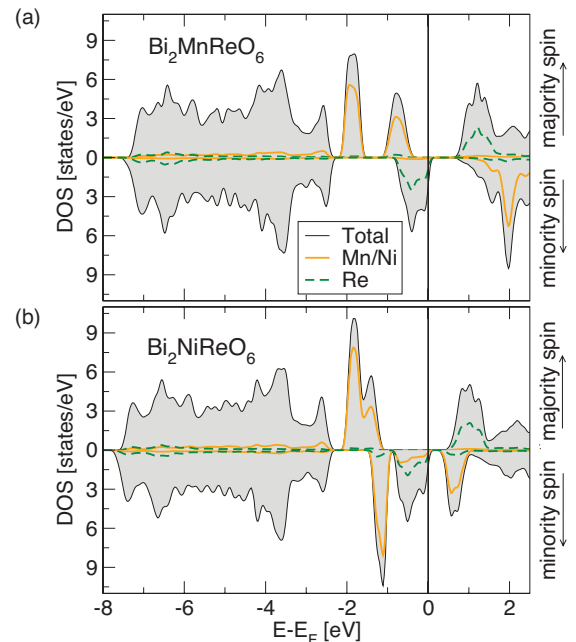


FIG. 3. (Color online) Density of states (DOS) of the ferroelectric phase of Bi₂MnReO₆ (a) and Bi₂NiReO₆ (b). The local magnetic moments on Mn/Ni and Re are antialigned. Thin black line, total DOS; green dashed line, Re; orange solid line, Mn/Ni.

be achieved in the form of ultrathin films, the ordering temperatures will likely be reduced.

V. SPIN-ORBIT COUPLING AND CORRELATIONS EFFECTS

Since the heavy Re and Bi atoms in our double perovskites are also likely to exhibit strong SOC, and consequently significant magnetostructural coupling,¹⁸ we repeat our calculations with SOC explicitly included. We find that the ground state remains $P2_1/n$ AP, but now its energy difference from the FE state with $R3$ symmetry is reduced to 10 meV in $\text{Bi}_2\text{MnReO}_6$ and only 2 meV in $\text{Bi}_2\text{NiReO}_6$. Both compounds still have semiconducting gaps which are now somewhat reduced while the ferroelectric polarization of the $R3$ phase is slightly increased (see Table II). The total magnetic moments (spin + orbital) amount to 2.34 and 0.58 μ_B , respectively. Note that, in contrast to half-metallic ferromagnets where the SOC introduces states in the minority-spin gap yielding a noninteger total magnetic moment, here the noninteger moment is the consequence of the mixing of spin-up and spin-down states (spin is no longer a good quantum number with SOC included), while the gap is preserved.

In both compounds the magnetic easy axis lies along the ferroelectric polarization direction. The associated anisotropy energy is large and comparable to that in current magnetic recording media: it amounts to 7 and 5.5 meV per formula unit in $\text{Bi}_2\text{MnReO}_6$ and $\text{Bi}_2\text{NiReO}_6$, respectively. This suggests an exciting possibility of electrical control of the magnetization direction.

Finally, we investigate the influence of electronic correlations by adding a Hubbard U on the d states of Mn and Ni. In order to reduce the computational effort, we do not include the SOC. We keep in mind, however, that a consequence of its inclusion, as we have seen, is a reduction in the energy of the FE state with respect to the AP one. Introduction of Hubbard U corrections (on Mn $U = 3$ eV and $J = 0.87$ eV, and on Ni $U = 6$ eV and $J = 0.90$ eV) does not change the ground-state structure ($P2_1/n$ still has the lowest energy). Interesting quantitative changes occur in the strain dependence however [Fig. 2(b)]. While within the GGA the ferroelectricity was robust to the choice of substrate lattice parameters over a likely range of accessible strains provided that the in-plane

lattice parameters were constrained to be perpendicular to each other, in GGA + U we find a crossover between the FE and AP states at moderate strain values. This suggests the intriguing possibility that an external strain, for example, from a piezoelectric substrate,³⁷ could induce a “dipole-flop” transition from a nonpolar structure in which the dipoles are antialigned to a ferroelectric one. For the assumed value of U , the crossover region [shaded area in Fig 2(b)] in $\text{Bi}_2\text{MnReO}_6$ is within less than 1% from either of the two minima: a small compressive strain will push the system toward the AP state, while a small tensile strain will favor a FE state. In $\text{Bi}_2\text{NiReO}_6$ the applied U pushes the AP state lower in energy, but the crossover region to the FE state is still within an experimentally accessible range of 1.5% tensile strain. While we cannot make a quantitative prediction, since the relative energies of the AP and the FE state depend strongly on the value of the applied U correction, within a reasonable range of U the crossover region lies within 2% strain from the ground-state structure.

VI. CONCLUSION

In summary, we predict from first-principles calculations that the $3d$ - $5d$ double-perovskite compounds $\text{Bi}_2\text{MnReO}_6$ and $\text{Bi}_2\text{NiReO}_6$ are high- T_C ferrimagnetic insulators. Moreover, it is likely possible to stabilize them in thin-film form in a ferroelectric phase with high polarization along the $[111]$ direction. The magnetic easy axis lies along the ferroelectric polarization direction with a very large associated anisotropy energy. The different sizes and charges of the $3d$ and $5d$ transition metal ions suggest that the required B -site ordering should be experimentally feasible; we hope that our findings will initiate experimental efforts to synthesize these novel multiferroic compounds.

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