

Nanosecond spin lifetimes in single- and few-layer graphene-hBN heterostructures at room temperature

Marc Drögeler,[†] Frank Volmer,[†] Maik Wolter,[†] Bernat Terrés,^{†,‡} Kenji Watanabe,[¶]
Takashi Taniguchi,[¶] Gernot Güntherodt,[†] Christoph Stampfer,^{†,‡} and Bernd
Beschoten^{*,†}

*2nd Institute of Physics and JARA-FIT, RWTH Aachen University, 52074 Aachen, Germany, EU,
Peter Grünberg Institute (PGI-9), Forschungszentrum Jülich, 52425 Jülich, Germany, EU, and
National Institute for Materials Science, 1-1 Namiki, Tsukuba, 305-0044, Japan*

E-mail: bernd.beschoten@physik.rwth-aachen.de

Phone: +49 (0)241 8027096. Fax: +49 (0)241 8022306

Abstract

We present a new fabrication method of graphene spin-valve devices which yields enhanced spin and charge transport properties by improving both the electrode-to-graphene and graphene-to-substrate interface. First, we prepare Co/MgO spin injection electrodes onto Si⁺⁺/SiO₂. Thereafter, we mechanically transfer a graphene-hBN heterostructure onto the prepatterned electrodes. We show that room temperature spin transport in single-, bi- and tri-layer graphene devices exhibit nanosecond spin lifetimes with spin diffusion lengths reaching 10 μm combined with carrier mobilities exceeding 20,000 cm²/Vs.

*To whom correspondence should be addressed

[†]RWTH Aachen University

[‡]FZ Jülich

[¶]NIMS

In recent years, graphene has drawn strong attention because of measured spin-diffusion lengths of several microns at room temperature. Typical non-local spin-valve devices on Si/SiO₂ substrates with charge carrier mobilities of several thousand cm²/Vs exhibit spin lifetimes below 1 ns.¹⁻¹⁰ In contrast, room temperature spin lifetimes above 1 ns have only been observed for epitaxial graphene on SiC¹¹ and for bilayer graphene devices (BLG) with low carrier mobility of 300 cm²/Vs (Ref. 2) or after post-processing of as-fabricated devices either by hydrogenation¹² or by oxygen treatment¹³ which both, however, result in a decrease of the mobility. In graphene-based spintronics there is a device-oriented quest for combining long spin lifetimes with large carrier mobilities. While large carrier mobilities have been achieved in suspended structures¹⁴ and spin-valves on hexagonal boron nitride (hBN) crystals,¹⁵ the respective spin lifetimes only exhibit several 100ps. Recent studies indicate that the overall short spin lifetimes are most likely not a result of intrinsic spin scattering mechanisms in graphene but are rather caused and limited by the contact and interface properties of spin injection and detection electrodes.^{4,9,16,17} This notion is supported by the observed increase of the spin lifetime with the contact-resistance-area products ($R_c A$) of both single-layer (SLG) and BLG devices.^{4,13} In this context, it is important to note that the oxide barrier, which is needed for spin injection and detection, usually does not grow epitaxially on the graphene surface. MgO, for example, grows in a Volmer-Weber mode (island formation) if no additional wetting layer is used.¹⁸ This island growth yields rather rough surfaces and additionally favors the formation of conducting pinholes between the overlaying ferromagnetic metal which is subsequently deposited and the underlying graphene sheet. It has been suggested that these conducting pinhole states may be the bottleneck for spin transport when hybridizing with the graphene layer.⁴

In this Letter, we present a new pathway for fabricating graphene spin-valves which diminishes some of the aforementioned shortcomings of the spin injection and detection contacts. In our approach, we first pattern MgO/Co electrodes which are deposited onto a silicon substrate. We emphasize that in contrast to all previous methods our MgO barrier is not deposited onto graphene but rather on top of the ferromagnetic Co layer. Thereafter, we mechanically press a graphene

flake, which was previously transferred on hBN, onto the MgO surface of the electrodes. We show that this transfer technique allows for (1) nanosecond spin lifetimes with values up to 3.7 ns in trilayer graphene (TLG) devices which result from large (R_{cA}) values of the contacts and at the same time for (2) high carrier mobilities according to the enhanced charge transport properties by the mechanical contact of graphene to the overlaying flattening hBN layer.

The new sample fabrication consists of two main steps (see Figures 1a and 1b) quite in contrast to the previously used top-down process. In a first step we prepare Co/MgO electrodes on a $\text{Si}^{++}/\text{SiO}_2$ substrate, where the Si^{++} can be used as a back gate. The electrodes are defined by standard electron beam lithography and metallized by molecular beam epitaxy. We use 40 nm thick Co for spin injection and detection. Afterwards, we deposit 1 nm of MgO on top of the Co. This layer acts as an injection barrier to allow for efficient spin injection and detection. A scanning force microscopy (SFM) image of the prepared electrodes is shown in Figure 1b. The electrodes exhibit smooth surfaces and do not show fencing at their edges. Both is essential for a plane graphene to electrode interface.

The second step is illustrated in Figure 1a. We use exfoliated hBN which was transferred onto a glass slide covered by a polymer to pick up exfoliated graphene from a second $\text{Si}^{++}/\text{SiO}_2$ substrate (similar technique as described by Wang et al.¹⁹). The thickness of the hBN varies between 60 – 80 nm. Subsequently, the graphene-hBN heterostructure is mechanically transferred on top of the electrodes and the glass slide is thereafter removed by dissolving the polymer in acetone. A top-view optical image of the finished device is shown in Figure 1c.

As illustrated by the cross-section of our device (Figure 1d), the graphene-hBN heterostructure is suspended for small electrode spacings while it may bend down to the underlying SiO_2 surface (non-suspended) for larger spacings. The bending can easily be seen in the optical image in Figure 2a of a different SLG device where the optical contrast is encoded into a false-color scheme (orange for suspended and green for non-suspended), which even allows to visualize the underlying graphene flake. An additional SFM line scan (Figure 2c) perpendicular to the electrodes in Figure 2d confirms this assignment.

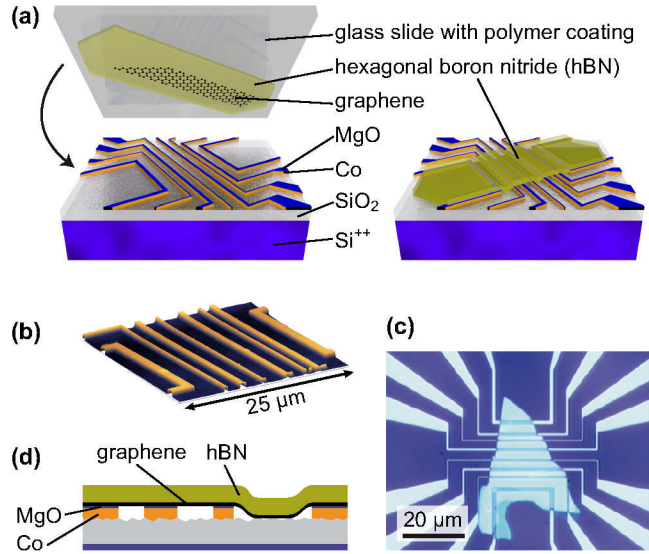


Figure 1: (a) Transfer technique for fabricating non-local graphene spin-valves (similar to Ref. 19). (b) Scanning force microscope image of the prepared ferromagnetic electrodes. (c) Optical micrograph of a transferred graphene-hBN heterostructure onto MgO/Co electrodes. (d) Schematic cross section of the final device.

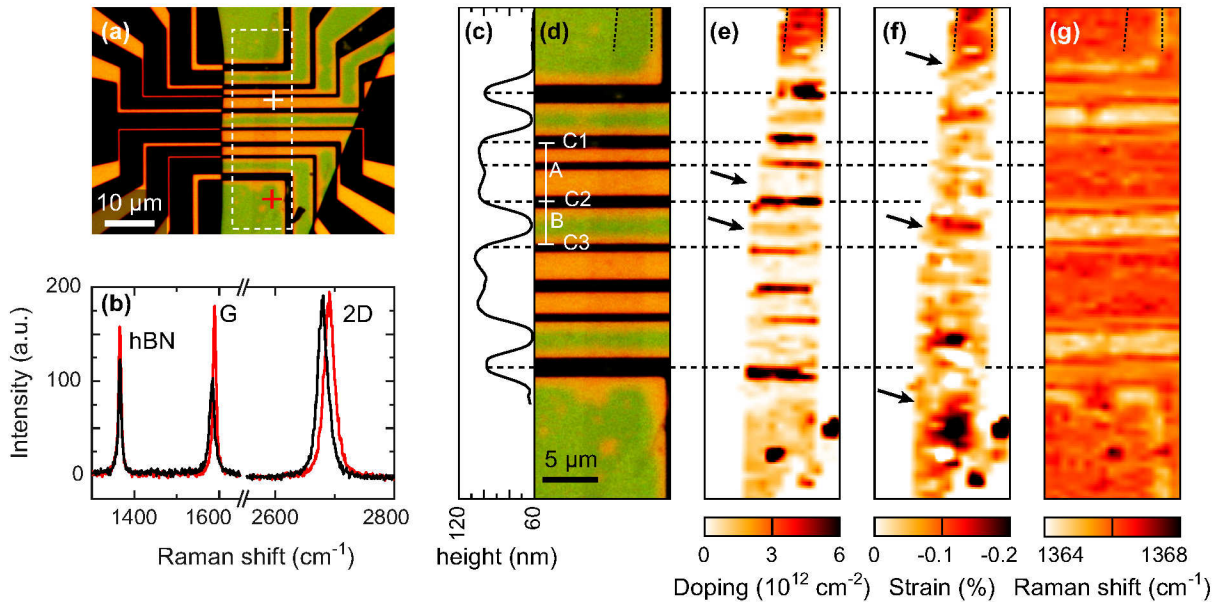


Figure 2: (a) Top view optical image of a Co/MgO/SLG-hBN device. (b) Raman spectra taken at the white and red crosses in panel (a). (c) SFM height profile scan showing the bending of the SLG-hBN. (d) Close up of white rectangular image detail in panel (a). (e) Doping and (f) strain distribution of the graphene flake. Values are extracted from the G and 2D-line positions of the Raman maps following Ref. 20. (g) Spatial image of the Raman hBN peak position (see panel (b)).

To further analyze the quality of our transferred SLG-hBN heterostructure, we use micro-Raman spectroscopy to compare suspended with non-suspended regions. The respective spectra in Figure 2b have been taken at the positions of the white and red cross in Figure 2a. We observe three distinct peaks which can be attributed to hBN and the G- and 2D-line of graphene. For suspended graphene (red curve) we get peak positions (G-peak at 1583 cm^{-1} and 2D-peak at 2679 cm^{-1}) which are very close to the values for pristine, freestanding graphene.²⁰ For the non-suspended graphene regions, however, we find a strong shift of both peak positions to larger wave numbers. This shift can be explained by local changes in doping and strain.²⁰

We therefore recorded a Raman map over the device area shown in Figure 2d and use a vector decomposition of the G- and the 2D-peak shift²⁰ to estimate doping and strain distributions in the graphene which are plotted in Figures 2e and 2f, respectively. We note that this method only allows to determine the carrier density but not its type.^{20,21} For the suspended parts of the graphene flake there are only minor charge fluctuations ($< 5 \times 10^{-11}\text{ cm}^{-2}$) visible while rather high doping is observed in all areas which are in direct contact with the electrodes. Moreover, doping occurs in the non-suspended regions which are in direct contact to the SiO_2 substrate. The doping may result from vacancies or charged defects in the MgO/Co electrodes and in the substrate exhibiting local electric fields which cause local doping.^{22,23}

The local strain distribution is shown in Figure 2f. There is only small strain in suspended regions and in regions which are supported by the electrodes. As expected, we find larger strain in all non-suspended regions showing that the bending causes local strain. It is thus interesting to explore whether the local strain has any influence on the spin transport properties.²⁴ Furthermore, we note that the largest strain is measured in areas where graphene has direct contact to the SiO_2 surface (see arrows in Figure 2f). These findings are in agreement with previous results by Lee et al. for graphene on SiO_2 ,²⁰ demonstrating that graphene exhibits less strain on hBN compared to SiO_2 substrates. The bending of the graphene-hBN heterostructure can also be seen as a peak shift of the hBN Raman line (Figure 2g) which can also be explained by local strain.²⁵

We next focus on spin and charge transport measurements on the SLG device presented in Fig-

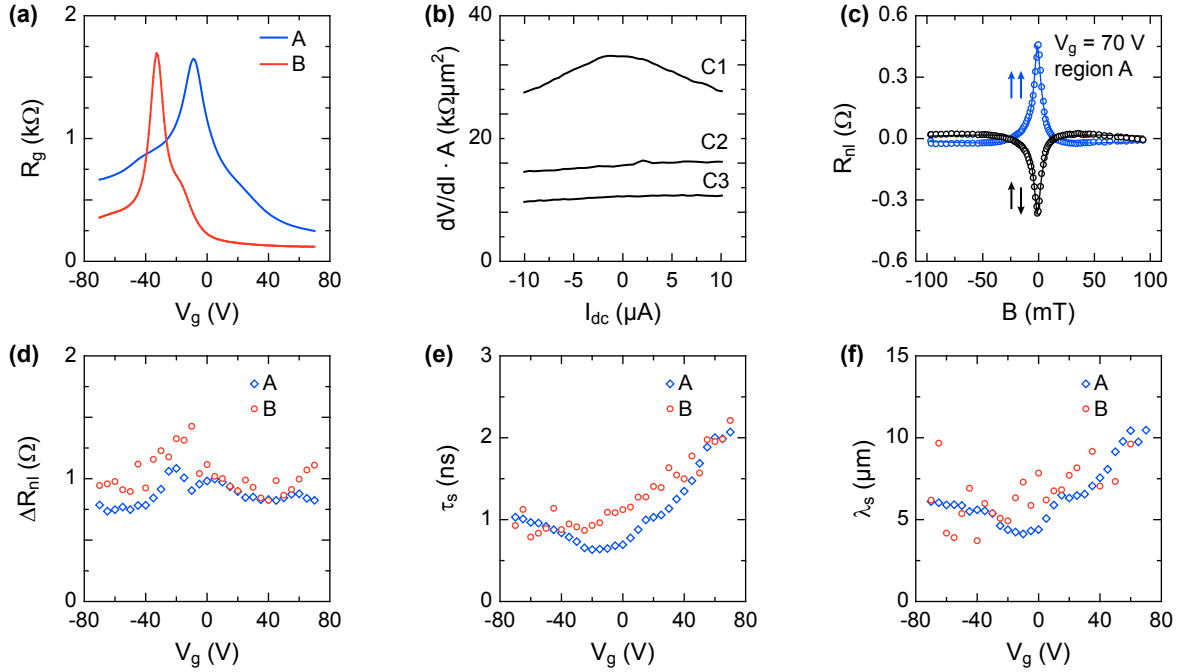


Figure 3: (a) Gate dependent graphene resistance of the SLG device from Figure 2 for suspended region A (blue curve) and non-suspended region B (red curve). (b) $dV/dI \cdot A$ curves of contacts C1, C2 and C3 labeled in Figure 2d. (c) Hanle spin precession curves taken at $V_g = 70$ V in region A. (d) Gate dependent spin signal for region A (blue data points) and region B (red data points). Respective gate dependent spin lifetimes are shown in panel (e) and spin diffusion lengths in panel (f).

ure 2. All transport measurements were performed at room temperature under vacuum conditions using a standard low frequency lock-in technique.²⁶ In Figure 3a we show the four-terminal back gate dependent resistance of the suspended region A (blue curve) and the non-suspended region B (red trace) (for assignment see Figure 2d). The charge neutrality point (CNP) of the suspended region is close to zero gate voltage while it is shifted to $V_g = -34$ V for the non-suspended region. The shift of the latter results from a strong n -doping by the substrate whereas the suspended region A is only slightly doped which is both in accordance to the Raman analysis in Figure 2e.

We extract the carrier density by $n = \alpha(V_g - V_g^0)$ with V_g being the back gate voltage and V_g^0 being the voltage to reach the CNP. The capacitive coupling constant α is different for suspended and non-suspended regions with respective values of $\alpha_A = 3.5 \times 10^{10} \text{ V}^{-1} \text{ cm}^{-2}$ and $\alpha_B = 4.8 \times 10^{10} \text{ V}^{-1} \text{ cm}^{-2}$.²⁷

The electron mobilities μ are determined from the gate dependent conductance σ using $\mu = 1/e \cdot \Delta\sigma/\Delta n$. We obtain mobilities of $23,000 \text{ cm}^2/\text{Vs}$ for the suspended region A and $20,000 \text{ cm}^2/\text{Vs}$ for the non-suspended region B near the CNP. Compared to all previous room temperature carrier mobilities in graphene spin-valve devices on Si/SiO₂ substrates these values are more than a factor of 2 larger which highlights the high quality of our devices.² We note that the given analysis is oversimplified as the graphene parts which are residing on top of the electrodes cannot be tuned by the gate voltage due to shielding of the back gate fields by the electrodes. The respective graphene resistance is thus a gate independent contribution to the total graphene resistance. This results in a smaller slope of σ and thereby yield smaller mobilities when using the above conservative estimate.

We characterize all spin injection and detection electrodes (C1 to C3) of regions A and B (see Figure 3d) by their differential contact resistances ($dV/dI \cdot A$) with A being the respective contact area.⁴ We observe large values for all contacts (Figure 3b). Only contact C1 exhibits the typical cusp-like dependence indicating tunneling behavior while the other contacts show a flat $dV/dI \cdot A$ curve which indicates transparent barriers. Interestingly, in previous studies transparent contacts could only be observed for contact resistance area products below $1 \text{ k}\Omega\mu\text{m}^2$ for devices with a

rather thick MgO layer (2 – 3 nm) which was directly deposited onto graphene.⁴ We thus conclude that our thinner MgO barriers (1 nm) have better contact properties which might be explained by the weaker coupling to the graphene layer after the mechanical transfer of the graphene-hBN heterostructure onto the MgO surface.

Spin transport properties were measured in the standard four-terminal non-local Hanle geometry.^{1,28,29} A typical measurement is shown in Figure 3c for region A at $V_g = 70$ V for parallel and antiparallel alignments of the Co magnetizations of the respective injector and detector electrodes after background subtraction. The spin signal ΔR_{nl} is given by the resistance difference at $B = 0$ T. The Hanle depolarization curves are fitted by a simplified solution of the steady-state Bloch-Torrey equation,^{30–32}

$$\frac{\partial \vec{s}}{\partial t} = \vec{s} \times \vec{\omega}_0 + D_s \nabla^2 \vec{s} - \frac{\vec{s}}{\tau_s} = 0, \quad (1)$$

where \vec{s} is the net spin vector, D_s is the spin diffusion constant and τ_s is the spin lifetime. Additionally, $\vec{\omega}_0 = g\mu_B \vec{B}/\hbar$ represents the Larmor frequency, where μ_B is the Bohr magneton, $\vec{B} = \vec{B}_\perp$ is the out-of-plane magnetic field and $g = 2$ is the gyromagnetic factor. The spin diffusion length λ_s is given by $\lambda_s = \sqrt{D_s \tau_s}$.

In Figure 3d we show ΔR_{nl} as a function of V_g for the suspended region A (blue diamonds) and the non-suspended region B (red circles). For both regions the spin signal is on the order of 1 Ω and shows a slight increase near the CNP. According to Han et al. this increase is characteristic for tunneling contacts.⁹ As discussed above, two of the three electrodes show a flat dV/dI -curve (see Figure 3b), which indicates either transparent or intermediate contacts. We thus find that even intermediate contacts can exhibit the largest spin signal at the CNP.

In Figure 3e we plot the respective gate dependent spin lifetimes τ_s . Most strikingly, we observe a strong increase of τ_s towards electron doping for $V_g > 0$ V with maximum values exceeding 2 ns. The enhanced spin transport properties are also seen in the spin diffusion lengths which exceed 10 μm in both suspended and non-suspended regions (see Figure 3f). The latter values are larger than in all previous measurements on non-local spin valves including results on hBN (4.5 μm)¹⁵

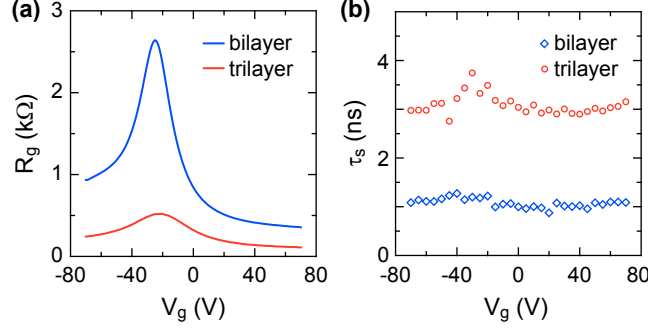


Figure 4: (a) Graphene resistance as a function of gate voltage for non-suspended BLG (blue curve) and TLG (red curve) devices. (b) Room temperature spin lifetime vs back gate voltage for BLG (blue diamonds) and TLG device (red circles).

and hydrogenated graphene ($7 \mu\text{m}$).¹² The enhanced spin transport properties for increased doping values have also been observed in most previous experiments,^{2,3,6,7,10,15,33} but their origin is not completely understood.^{34–36} Surprisingly, there is no distinct difference in τ_s and λ_s between the suspended and the non-suspended region indicating that even in our new devices the spin lifetime is still limited by contact-induced spin dephasing which hinders to explore relevant spin dephasing and spin relaxation mechanisms in the graphene layer itself.

It is interesting to compare these SLG results to few-layer graphene devices. By the same fabrication method we therefore additionally prepared BLG and TLG devices and show results on charge transport and spin lifetimes in Figures 4a and 4b, respectively. The data were taken on non-suspended regions which again result in a shift of the CNP towards negative gate voltages (see Figure 4a). We estimate electron carrier mobilities of $9,000 \text{cm}^2/\text{Vs}$ for BLG and $10,000 \text{cm}^2/\text{Vs}$ for TLG where we used $\alpha = 4.9 \times 10^{10} \text{V}^{-1} \text{cm}^{-2}$ for both. As discussed above, these values should be taken as a lower limit estimate. In contrast to the SLG device, we observe a completely different density dependence of the respective spin lifetimes (Figure 4b). While τ_s depends only weakly on gate voltage it becomes largest at the CNP reaching 3.7 ns for the TLG device, which is the largest room temperature value in graphene-based non-local spin transport to date. A similar gate voltage dependence was previously also observed in other graphene spin-valve devices^{7,10,12,15} including SLG. We therefore do not attribute this behavior to the number of graphene layers.

Figure 5 summarizes our results. It shows the dependence of τ_s on the electron mobility on

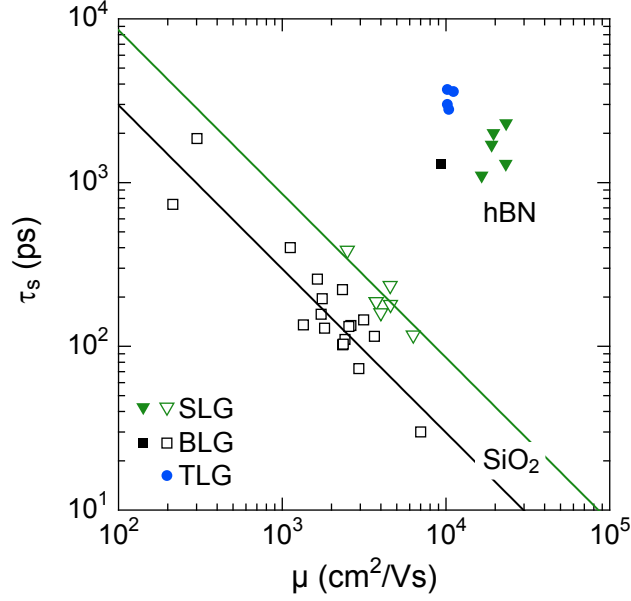


Figure 5: Room temperature spin lifetime as a function on carrier mobility obtained on single- and few-layer graphene non-local spin-valve devices for Co/MgO spin injection and detection electrodes. Results from the present study are depicted by the filled symbols while previous results on single and bilayer graphene (open symbols) are taken from Ref. 2 and 4.

a log-log scale. Data points from the present study are shown by filled symbols. In total we measured 10 regions of 5 devices. In 9 regions we obtain maximum spin lifetimes above 2 ns and mobilities above $10,000 \text{ cm}^2/\text{Vs}$ which demonstrates the reproducibility of the device performance by our fabrication method. For easier comparison we include results on SLG and BLG which some of us had previously measured.^{2,4} All latter devices were prepared on Si/SiO₂ by a conventional top-down fabrication method in which the MgO barriers are directly evaporated onto graphene. The overall improvements of the performances of our new devices are striking. These new devices exhibit spin lifetimes which are two orders of magnitude longer than the previous BLG devices (squares) with the largest mobility of $8,000 \text{ cm}^2/\text{Vs}$ that only yielded $\tau_s = 30 \text{ ps}$.² While a nanosecond spin lifetime was obtained in BLG devices with mobilities as low as $300 \text{ cm}^2/\text{Vs}$ we now obtain nanosecond spin lifetimes with mobilities which are almost two order of magnitude larger. We clearly attribute the increase in the mobilities to the hBN substrate while we relate the increase of the spin lifetimes to improved contact (i.e. electrode interface) properties according to our advanced transfer technique onto prepatterned electrodes which has several advantages over

previous methods. Firstly, the contact region of the graphene is never exposed to an electron beam, which most likely lead to a smaller number of spin-scattering centers in graphene.³⁷ Secondly, the interface between graphene and MgO is expected to be of higher quality, since more aggressive cleaning procedures can be used for removing resist residues from the lithography step. Furthermore, there is an island growth of MgO on graphene¹⁸ whereas it can grow fully epitaxial on Co.³⁸ Although our present MgO layers do not grow epitaxially they exhibit more homogeneous barriers as in previous studies. The homogeneity of the MgO layer does not only lead to an improved spin injection efficiency but also prohibits direct contact of Co atoms to graphene which is known to induce 3d-like hybridized states in graphene and can yield strong spin scattering.³⁹

In summary, we presented a new way of fabricating graphene-hBN spin-valve devices where we mechanically transfer the graphene onto predefined Co/MgO electrodes. All single-layer, bi-layer and trilayer graphene devices exhibit nanosecond spin lifetimes up to 3.7 ns with carrier mobilities exceeding $20,000 \text{ cm}^2/\text{Vs}$ and spin diffusion lengths above $10 \mu\text{m}$. Our presented transfer method can be applied to epitaxial oxide barriers, which are expected to yield even longer spin lifetimes. This ultimately paves the way to explore intrinsic spin transport properties and to realize promising devices in highest mobility graphene.

Acknowledgement

We thank S. Göbbels for helpful discussions and S. Engels for help with the transfer process. The research leading to these results has received funding from the DFG through FOR-912, the People Programme (Marie Curie Actions) of the European Union's Seventh Framework Programme FP7/2007-2013/ under REA grant agreement nÂ°607904-13 and the Graphene Flagship (contract no. NECT-ICT-604391).

References

- (1) Tombros, N.; Jozsa, C.; Popinciuc, M.; Jonkman, H. T.; van Wees, B. J. *Nature* **2007**, *448*, 571–574.

- (2) Yang, T.-Y.; Balakrishnan, J.; Volmer, F.; Avsar, A.; Jaiswal, M.; Samm, J.; Ali, S. R.; Pachoud, A.; Zeng, M.; Popinciuc, M.; Güntherodt, G.; Beschoten, B.; Özyilmaz, B. *Phys. Rev. Lett.* **2011**, *107*, 047206.
- (3) Avsar, A.; Yang, T.-Y.; Bae, S.; Balakrishnan, J.; Volmer, F.; Jaiswal, M.; Yi, Z.; Ali, S. R.; Güntherodt, G.; Hong, B. H.; Beschoten, B.; Özyilmaz, B. *Nano Letters* **2011**, *11*, 2363–2368.
- (4) Volmer, F.; Drögeler, M.; Maynicke, E.; von den Driesch, N.; Boschen, M. L.; Güntherodt, G.; Beschoten, B. *Phys. Rev. B* **2013**, *88*, 161405.
- (5) Popinciuc, M.; Józsa, C.; Zomer, P. J.; Tombros, N.; Veligura, A.; Jonkman, H. T.; van Wees, B. J. *Phys. Rev. B* **2009**, *80*, 214427.
- (6) Józsa, C.; Maassen, T.; Popinciuc, M.; Zomer, P. J.; Veligura, A.; Jonkman, H. T.; van Wees, B. J. *Phys. Rev. B* **2009**, *80*, 241403.
- (7) Maassen, T.; Dejene, F. K.; Guimarães, M. H. D.; Józsa, C.; van Wees, B. J. *Phys. Rev. B* **2011**, *83*, 115410.
- (8) Han, W.; Pi, K.; Bao, W.; McCreary, K. M.; Li, Y.; Wang, W. H.; Lau, C. N.; Kawakami, R. K. *Applied Physics Letters* **2009**, *94*, 222109.
- (9) Han, W.; Pi, K.; McCreary, K. M.; Li, Y.; Wong, J. J. I.; Swartz, A. G.; Kawakami, R. K. *Phys. Rev. Lett.* **2010**, *105*, 167202.
- (10) Han, W.; Kawakami, R. K. *Phys. Rev. Lett.* **2011**, *107*, 047207.
- (11) Maassen, T.; van den Berg, J. J.; IJbema, N.; Fromm, F.; Seyller, T.; Yakimova, R.; van Wees, B. J. *Nano Letters* **2012**, *12*, 1498–1502.
- (12) Wojtaszek, M.; Vera-Marun, I. J.; Maassen, T.; van Wees, B. J. *Phys. Rev. B* **2013**, *87*, 081402.

- (13) Volmer, F.; Drögeler, M.; Maynicke, E.; von den Driesch, N.; Boschen, M.; Güntherodt, G.; Beschoten, B. *in preparation* **2014**,
- (14) Guimaraes, M. H. D.; Veligura, A.; Zomer, P. J.; Maassen, T.; Vera-Marun, I. J.; Tombros, N.; van Wees, B. J. *Nano Letters* **2012**, *12*, 3512–3517.
- (15) Zomer, P. J.; Guimarães, M. H. D.; Tombros, N.; van Wees, B. J. *Phys. Rev. B* **2012**, *86*, 161416.
- (16) Maassen, T.; Vera-Marun, I. J.; Guimarães, M. H. D.; van Wees, B. J. *Phys. Rev. B* **2012**, *86*, 235408.
- (17) Dlubak, B.; Martin, M.-B.; Deranlot, C.; Servet, B.; Xavier, S.; Mattana, R.; Sprinkle, M.; Berger, C.; De Heer, W. A.; Petroff, F.; Anane, A.; Seneor, P.; Fert, A. *Nat. Phys.* **2012**, *8*, 557–561.
- (18) Wang, W. H.; Han, W.; Pi, K.; McCreary, K. M.; Miao, F.; Bao, W.; Lau, C. N.; Kawakami, R. K. *Applied Physics Letters* **2008**, *93*, 183107.
- (19) Wang, L.; Meric, I.; Huang, P. Y.; Gao, Q.; Gao, Y.; Tran, H.; Taniguchi, T.; Watanabe, K.; Campos, L. M.; Muller, D. A.; Guo, J.; Kim, P.; Hone, J.; Shepard, K. L.; Dean, C. R. *Science* **2013**, *342*, 614–617.
- (20) Lee, J. E.; Ahn, G.; Shim, J.; Lee, Y. S.; Ryu, S. *Nat. Commun.* **2012**, *3*, 1024.
- (21) Stampfer, C.; Molitor, F.; Graf, D.; Ensslin, K.; Jungen, A.; Hierold, C.; Wirtz, L. *Applied Physics Letters* **2007**, *91*, 241907.
- (22) Peres, N. M. R. *Rev. Mod. Phys.* **2010**, *82*, 2673–2700.
- (23) Das Sarma, S.; Adam, S.; Hwang, E. H.; Rossi, E. *Rev. Mod. Phys.* **2011**, *83*, 407–470.
- (24) Huertas-Hernando, D.; Guinea, F.; Brataas, A. *Phys. Rev. Lett.* **2009**, *103*, 146801.

- (25) Gorbachev, R. V.; Riaz, I.; Nair, R. R.; Jalil, R.; Britnell, L.; Belle, B. D.; Hill, E. W.; Novoselov, K. S.; Watanabe, K.; Taniguchi, T.; Geim, A. K.; Blake, P. *Small* **2011**, *7*, 465–468.
- (26) Details on the measurement technique can be found in Ref. 4.
- (27) In contrast to graphene which was directly deposited onto Si/SiO₂ we have to consider an additional dielectric (air) between the graphene and the surface of the substrate as well as the partial shielding of the electric field by the nearby electrodes. We therefore simulate the capacitive coupling of our devices using COMSOL for both suspended and non-suspended regions with different electrode spacings which gives an estimate for α .
- (28) Jedema, F. J.; Heersche, H. B.; Filip, A. T.; Baselmans, J. J. A.; van Wees, B. J. *Nature* **2002**, *416*, 713–716.
- (29) Lou, X.; Adelman, C.; Crooker, S. A.; Garlid, E. S.; Zhang, J.; Reddy, K. S. M.; Flexner, S. D.; Palmstrom, C. J.; Crowell, P. A. *Nat. Phys.* **2007**, *3*, 197–202.
- (30) Torrey, H. C. *Phys. Rev.* **1956**, *104*, 563–565.
- (31) Johnson, M.; Silsbee, R. H. *Phys. Rev. B* **1988**, *37*, 5312–5325.
- (32) Fabian, J.; Matos-Abiague, A.; Ertler, C.; Stano, P.; Žutić, I. *ACTA PHYSICA SLOVACA* **2007**, *57*, 565–907.
- (33) Han, W.; Chen, J.-R.; Wang, D.; McCreary, K. M.; Wen, H.; Swartz, A. G.; Shi, J.; Kawakami, R. K. *Nano Letters* **2012**, *12*, 3443–3447.
- (34) Zhang, P.; Wu, M. W. *Phys. Rev. B* **2011**, *84*, 045304.
- (35) Zhang, P.; Wu, M. W. *New Journal of Physics* **2012**, *14*, 033015.
- (36) Diez, M.; Burkard, G. *Phys. Rev. B* **2012**, *85*, 195412.

- (37) Childres, I.; Jauregui, L. A.; Foxe, M.; Tian, J.; Jalilian, R.; Jovanovic, I.; Chen, Y. P. *Applied Physics Letters* **2010**, *97*, 173109.
- (38) Yuasa, S.; Fukushima, A.; Kubota, H.; Suzuki, Y.; Ando, K. *Applied Physics Letters* **2006**, *89*, 042505.
- (39) Varykhalov, A.; Marchenko, D.; Sánchez-Barriga, J.; Scholz, M. R.; Verberck, B.; Trauzettel, B.; Wehling, T. O.; Carbone, C.; Rader, O. *Phys. Rev. X* **2012**, *2*, 041017.