

Thermophoresis of charged colloidal spheres and rods

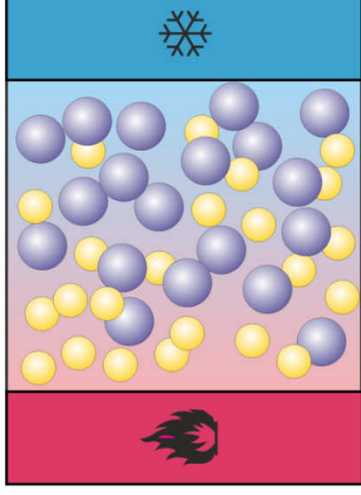
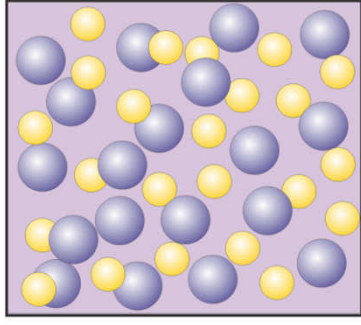
20. Mai 2015

| Simone Wiegand, Dzmitry Afanasenkau, Olga Syschchyk, Zilin Wang,
Johan Buitenhuis and Jan K.G. Dhont

Phenomenological equation

(..., thermodiffusion, Soret effect) –

Movement of particles driven by a temperature gradient



D - diffusion coefficient,

c - concentration,

D_T - thermodiffusion coefficient,

$\vec{j}$ - flux, T – temperature

S_T – Soret coefficient

$$\vec{j} = -D\vec{\nabla}c - c(1-c)D_T\vec{\nabla}T$$

Steady state $\vec{j}=0$

$$S_T = \frac{D_T}{D} \propto \frac{\Delta c}{\Delta T}$$

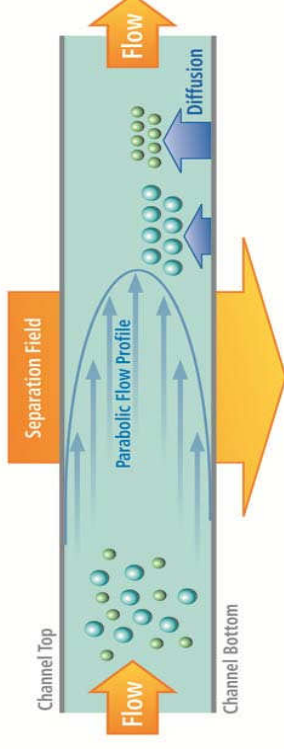
Thermophoresis: What ? Where is it used?

Application areas

- Characterization of macromolecules and colloids, e.g. TFFF (thermal field flow fractionation)
- Separation of mixtures, e.g. thermogravitational column
- Measuring equilibration constants of biochemical reactions
- Studying interaction and folding of macromolecules

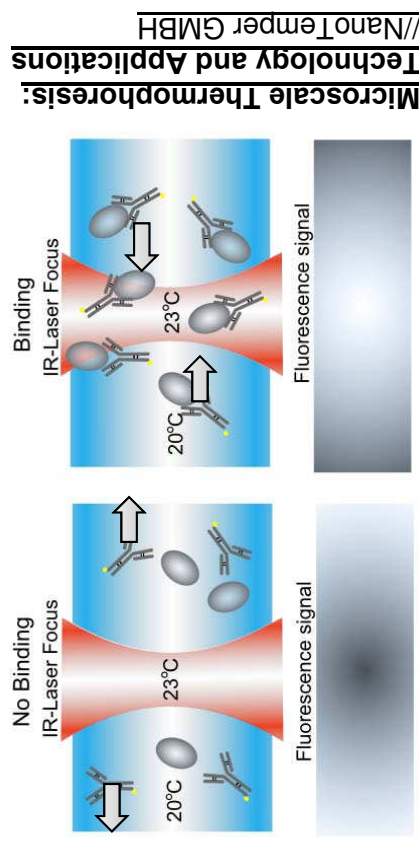
Application examples

- Thermal field flow fractionation



Separation of mixtures (TFFF) //Wikipedia

- Microscale thermophoresis



Microscale Thermophoresis: Technology and Applications: //NanoTemper GmbH

To the warm or to the cold?



mass

moment
of inertia

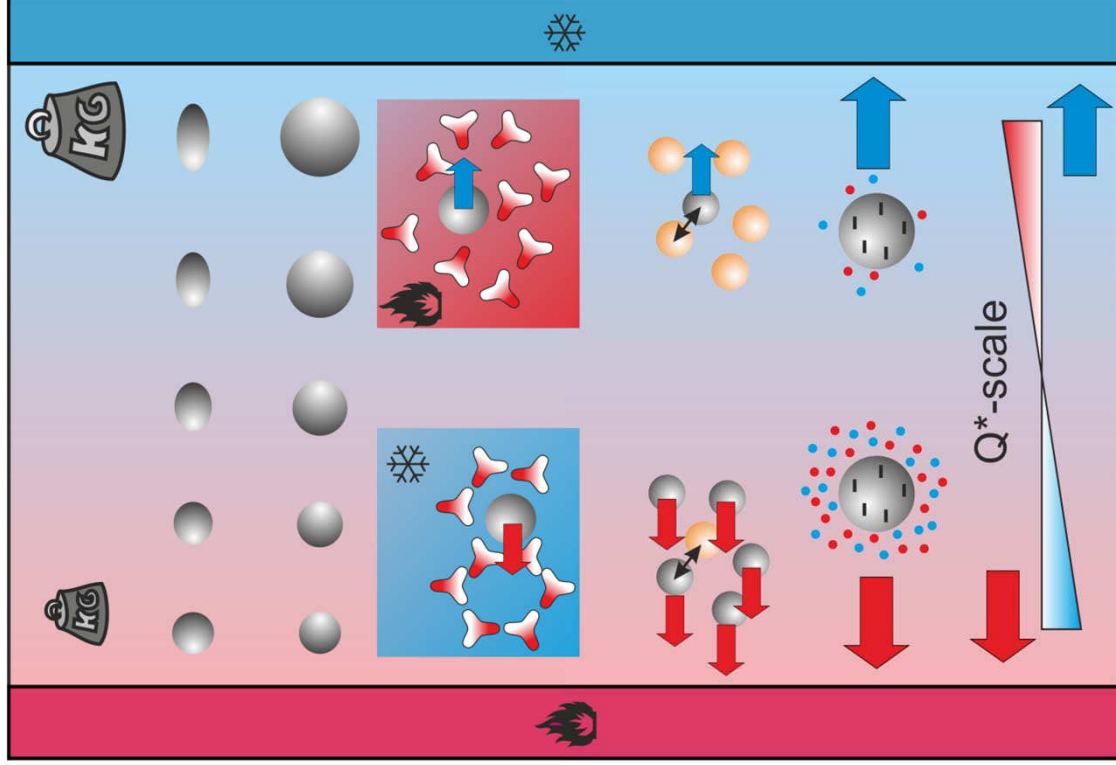
size

hydrogen
bond
network

strong
cross
interaction

ionic
strength

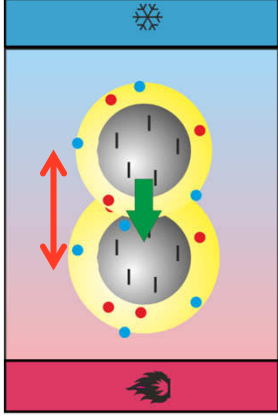
heat of
transfer



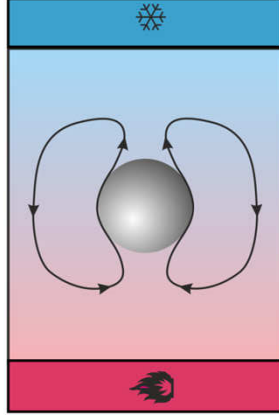
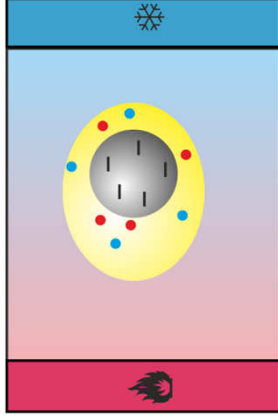
Influence of charges

$$\lambda_{\text{DH}} \propto \sqrt{\frac{T}{I}}$$

T .. temperature
 I .. ionic strength



/



... of minor
 importance in
 water, but
 relevant in
 solvents with
 low dielectric
 constant

$$\delta W_{\text{ev}} = - \int F \cdot dt$$

internal force F_w due to change
 of the double layer structure on
 displacement of the sphere

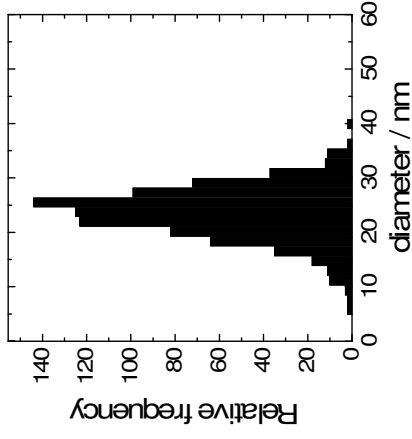
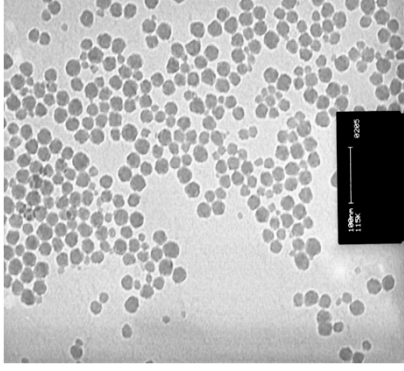
electric force F_{el} due to non-
 spherical symmetry of the
 double layer structure.

solvent-friction force F_{sol} due to
 solvent flow arising from the
 asymmetry of the double-layer
 structure.

[J. K. G. Dhont and W. J. Briels, Eur. Phys. J. E **25** (2008) 61–76]

Ionic strength effect

charged silica colloidal particles (Ludox)



valid for thin and thick double layers:

e ... elementary charge

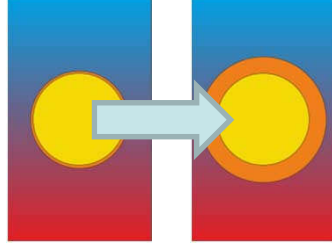
l_B .. Bjerrum length

σ .. surface charge density

$\kappa^{-1} = \lambda_{DH}$.. Debye length

ϵ .. dielectric constant

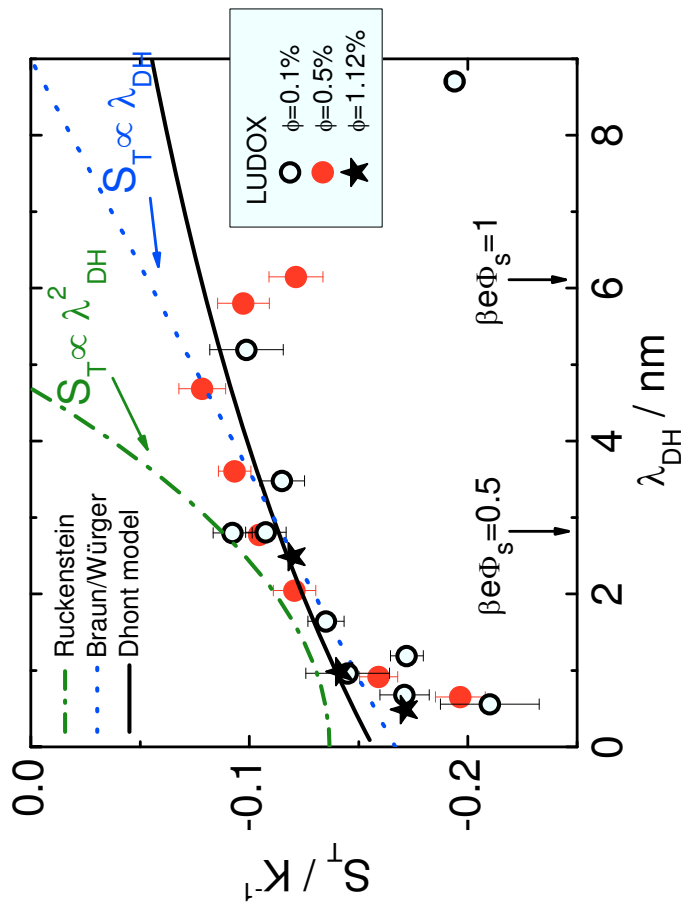
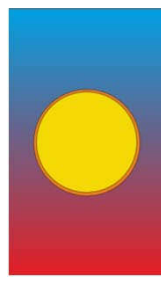
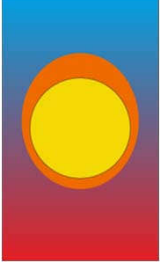
a .. radius of the colloid



$$S_T = \frac{1}{T} \left\{ 1 + \frac{1}{4} \left(\frac{4\pi l_B^2 \sigma}{e} \right)^2 \frac{1}{(1 + \kappa a)^2} \frac{\kappa a^4}{l_B^3} \left\{ 1 - \frac{d \ln \epsilon}{d \ln T} \left(1 + \frac{2}{\kappa a} \right) \right\} \right\} + A(T)$$



Hui Ning



[H. Ning, J.K.G. Dhont, SW, Langmuir, 24 (2008), 2426]
[Dhont, J. K. G.; SW; Duhr, S.; Braun, D. Langmuir, 23 (2007), 1674]

Model system for a charged rod: fd-virus

System: *wt* fd-virus

1 μm

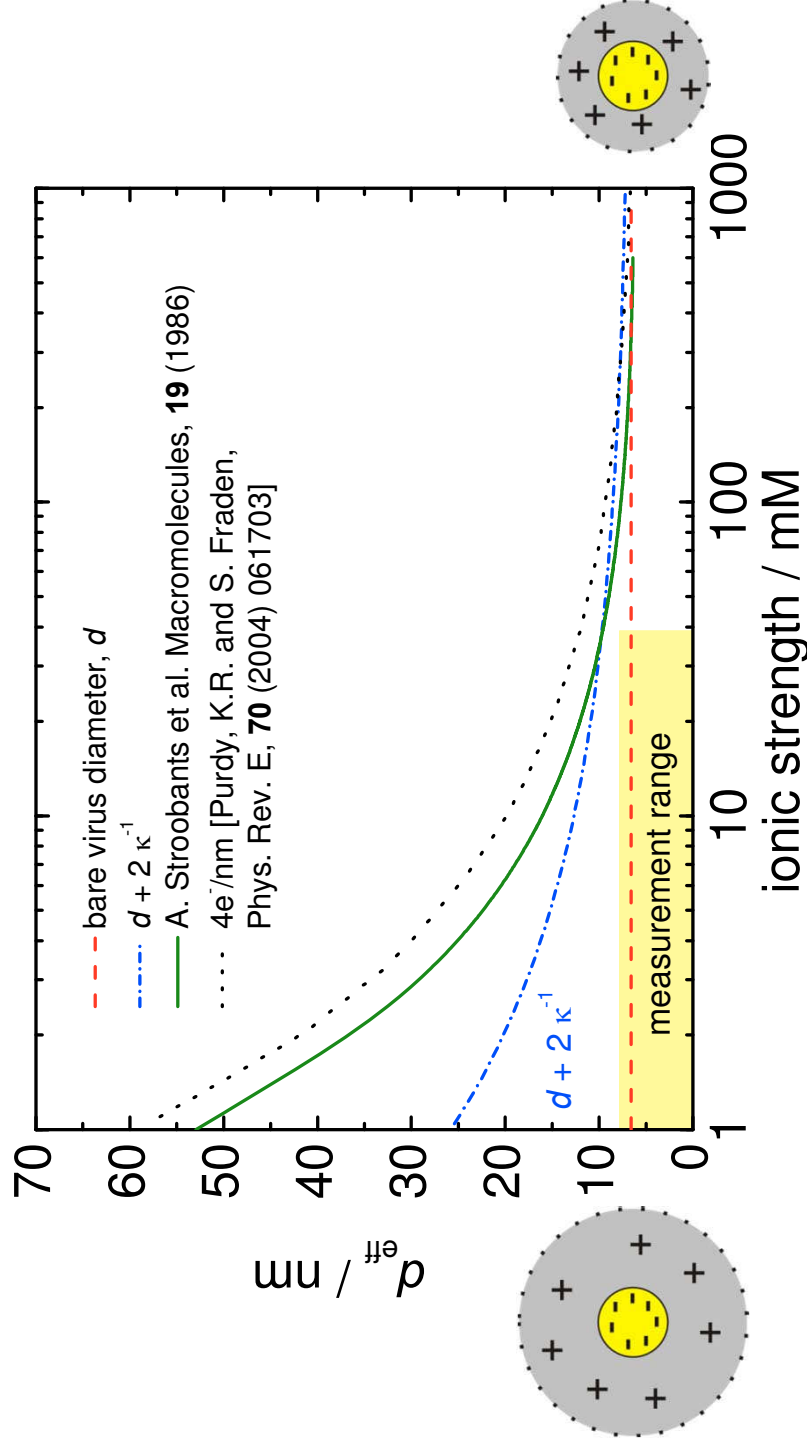


Diameter = 6.6 nm

Length = 880 nm

Molar mass = 1.64×10^7 g/mol

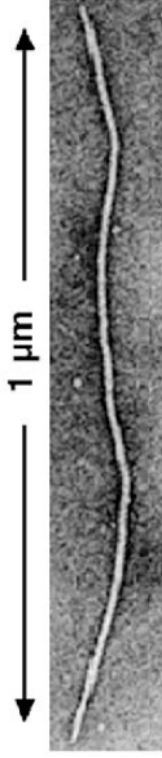
Effective diameter



Onsager, L., Ann. N.Y. Acad. Sci, **51**(1949) 627-659.

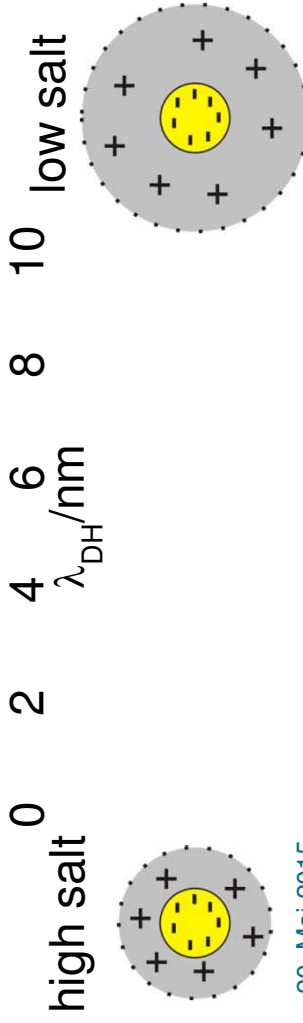
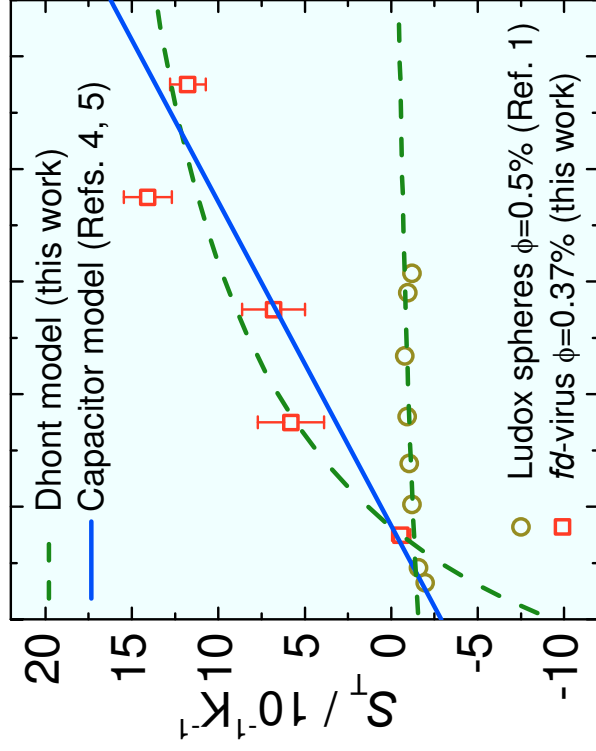
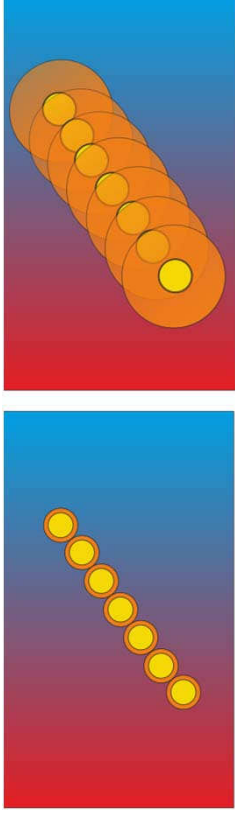
Single particle effects: charged colloidal rod

System: wt fd-virus



Theoretical description

Thin double layer Thick double layer



Model	σ/enm^{-2}	Offset
Dhont	0.050 ± 0.003	-1.39
Capacitor	0.016 ± 0.002	-0.74
Calculated bare charge	0.066	



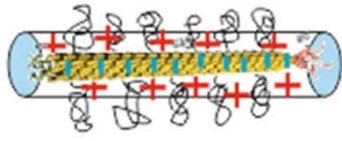
Zilin Wang
Folie 8

Charged colloidal rod with hairs



Johan Buitenhuis

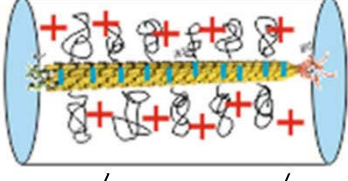
Ionic strength > 20mM



MPEG=5000g/mol

Electric double layer

Ionic strength < 20mM

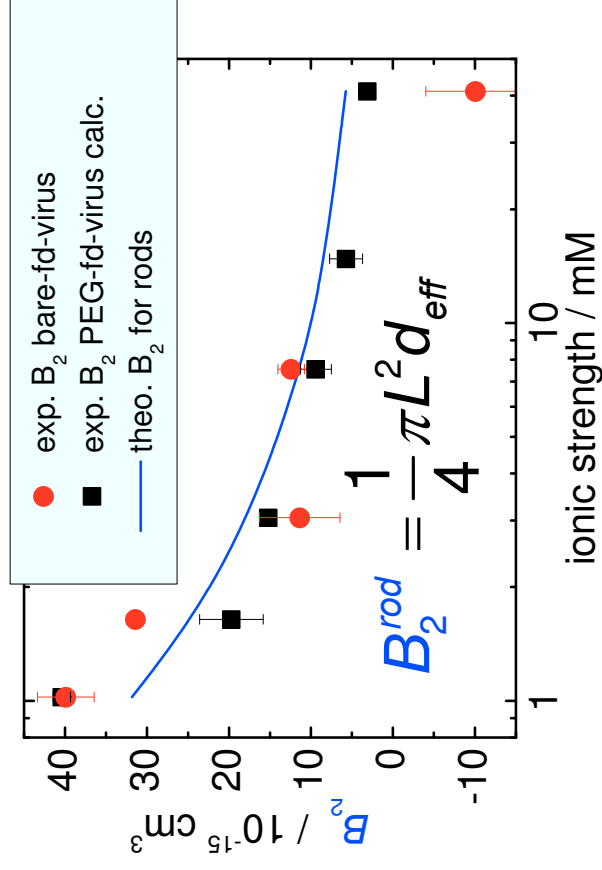
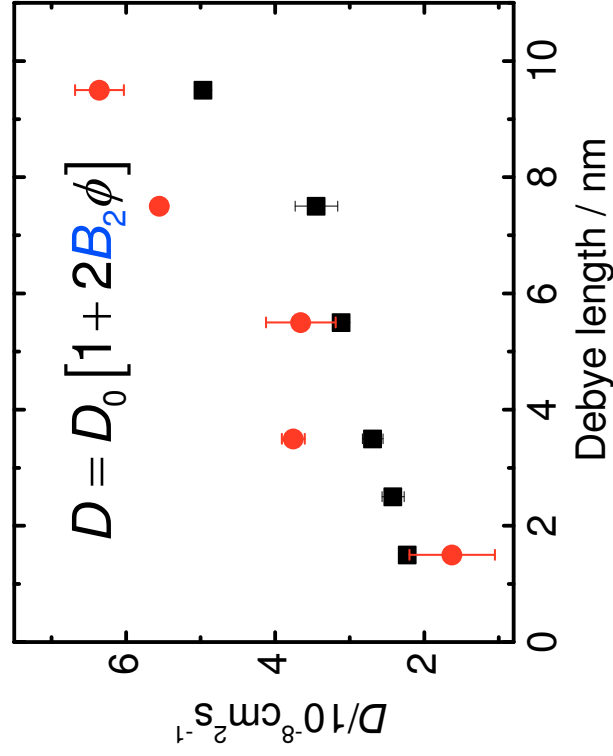


Steric vs. electric interaction



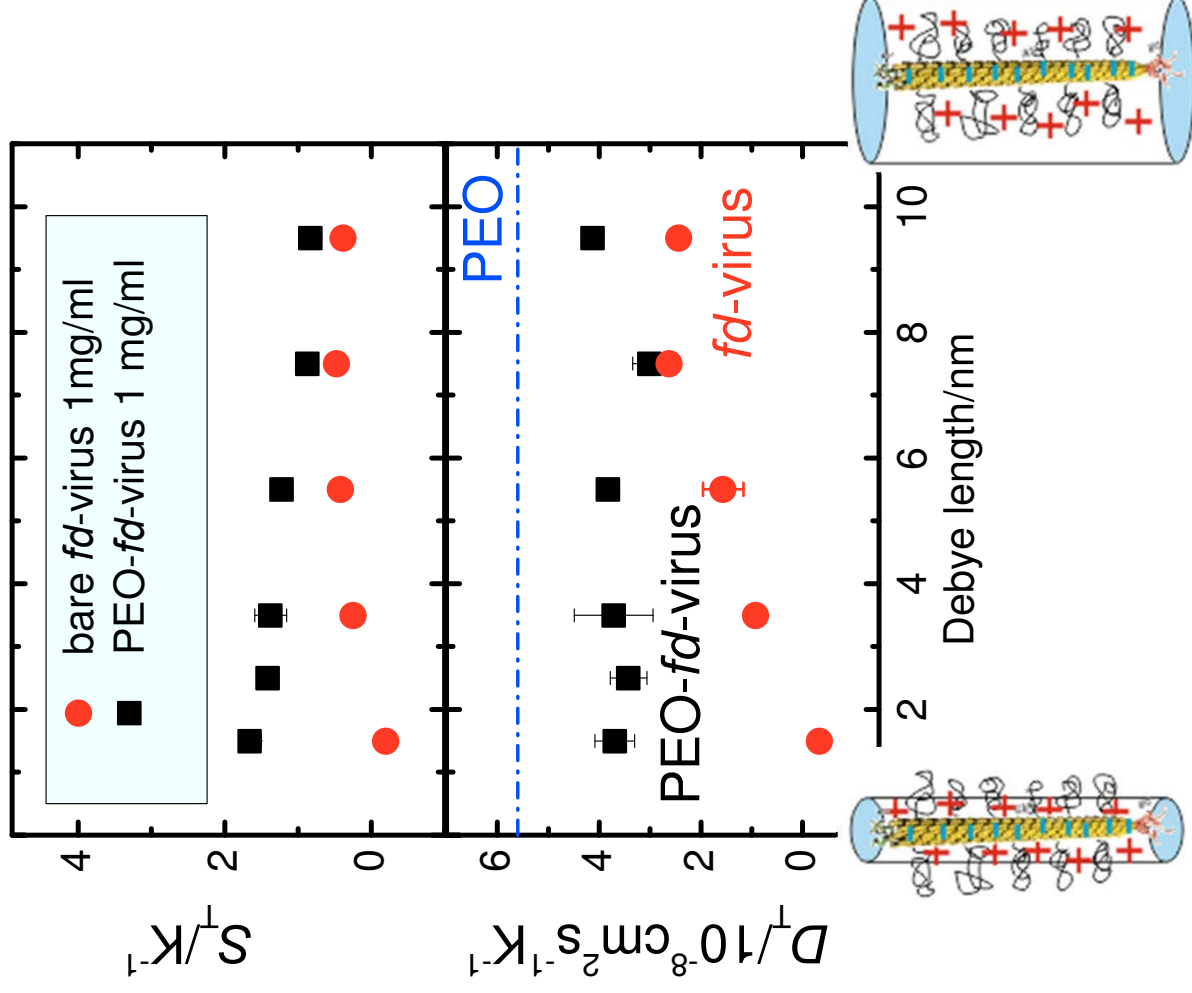
Zilin Wang

Onsager, L., Ann. N.Y. Acad. Sci, **51**(1949) 627-659.



Diffusion remains almost the same

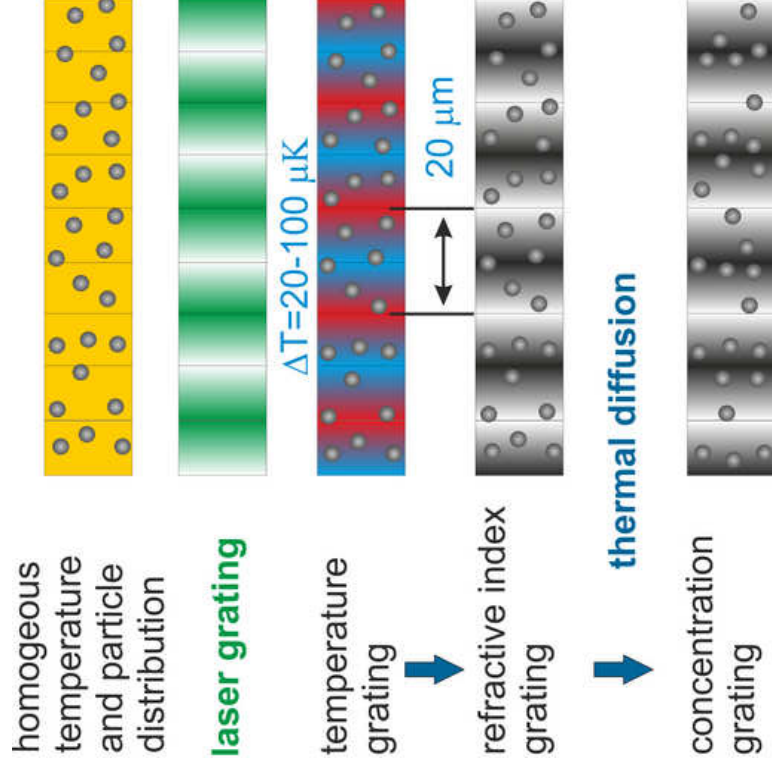
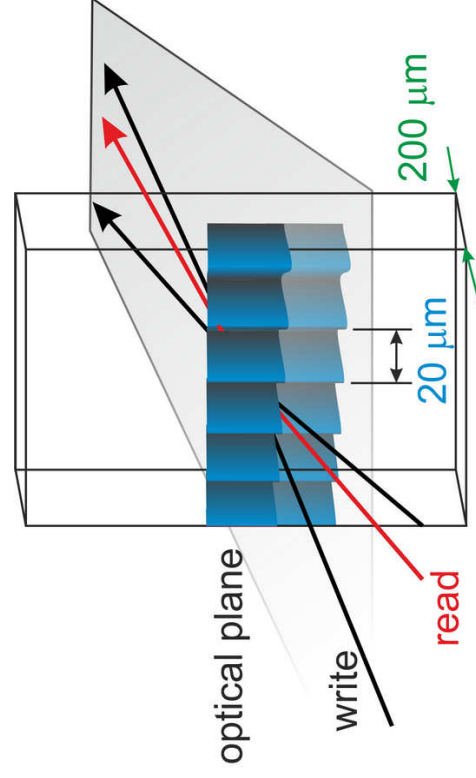
Charged colloidal rod with hairs



Thermal diffusion
more sensitive to
the grafting of
the polymers

... (more) projects in progress,

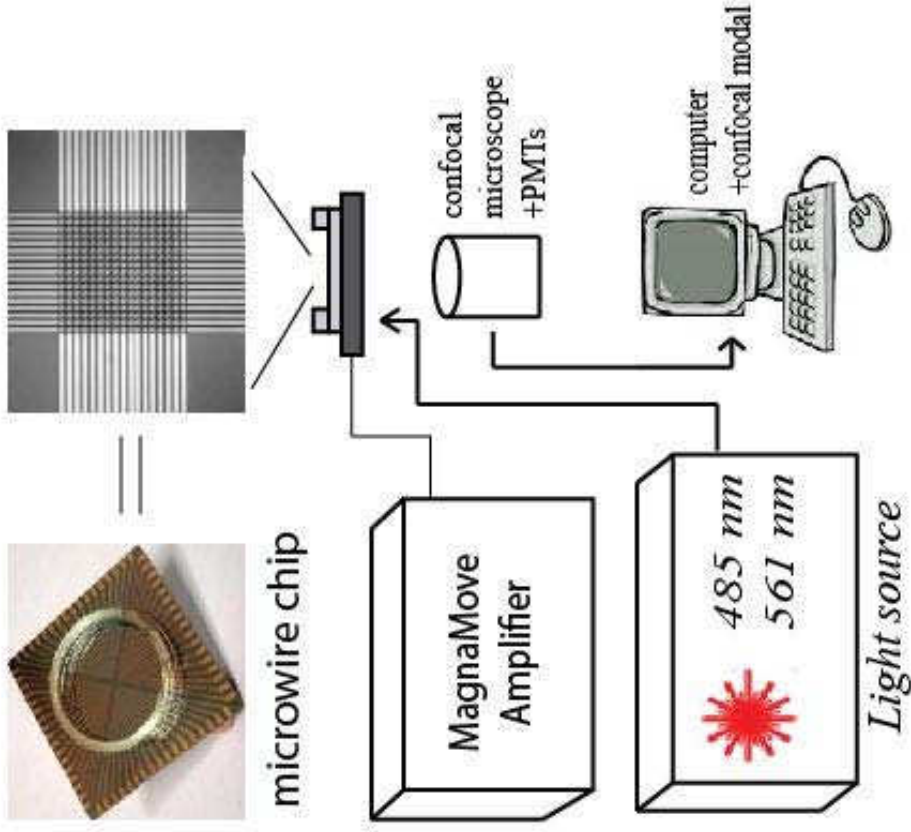
Measured quantity:
Intensity of the diffracted beam



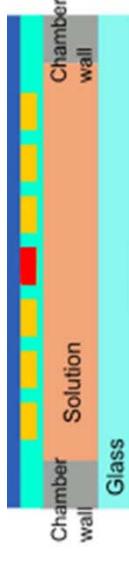
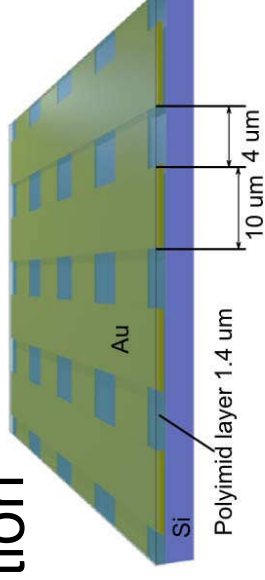
TDFRS
Thermal diffusion forced
Rayleigh scattering

[S. Wiegand *et al.*, J. Phys. Chem. B, **111**(2007) 14169]

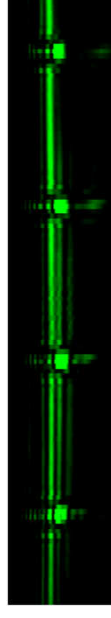
Thermophoretic microfluidic cells microwire chip



Objective: investigation of biomolecules in buffer solution



Confocal XZ slice
(scattered light)

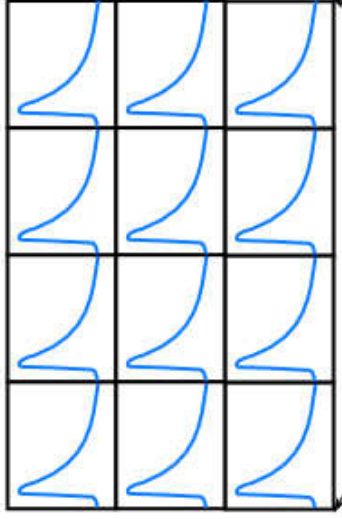


[Rinklin, P., D. Afanasyuk, SW, A. Offenhäuser, and B. Wolfrum,
Lab on a Chip, 15 (2015) 237-243]

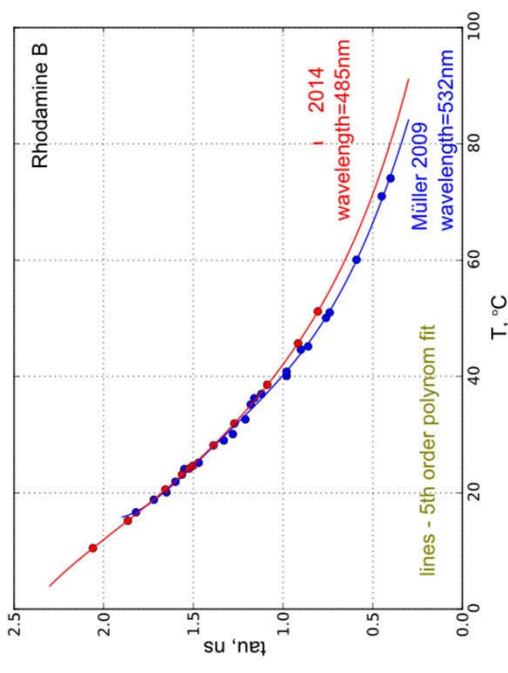
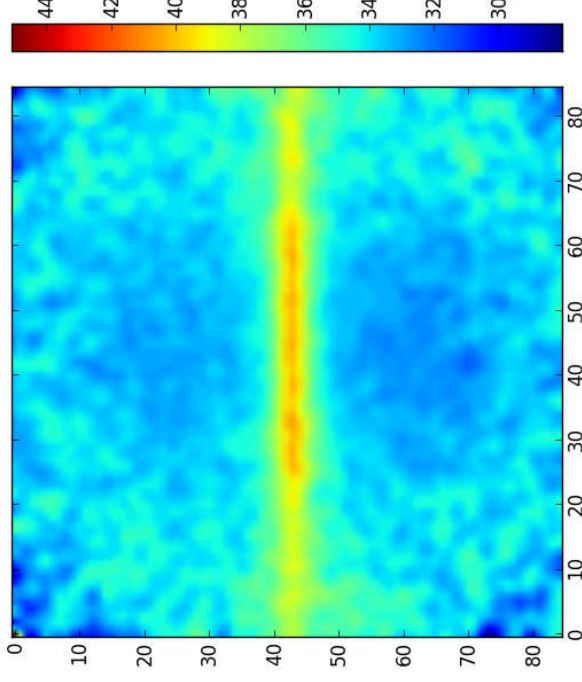
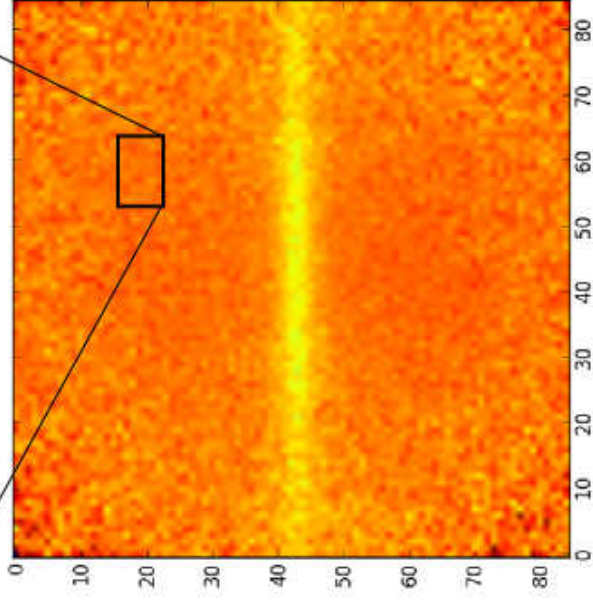
Thermophoretic microfluidic cells

FLIM –

Fluorescence Life-time Imaging Microscopy

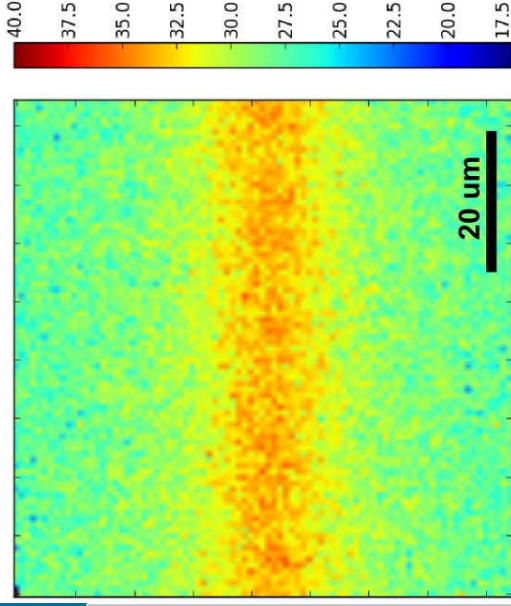


$$T=f(\tau)$$

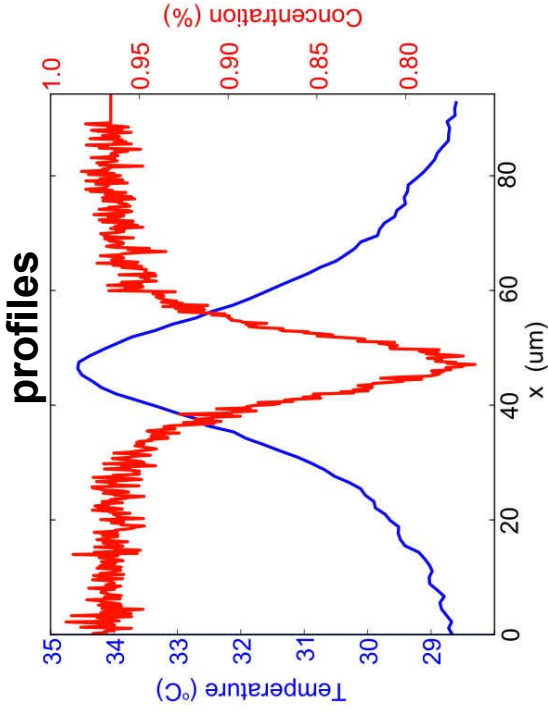


Thermophoretic microfluidic cells

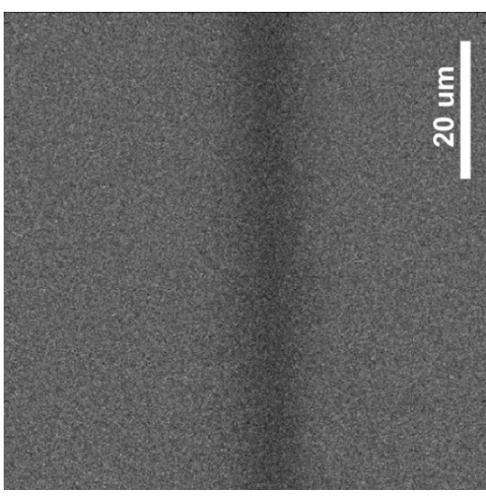
Temperature distribution



Temperature and concentration profiles



Intensity

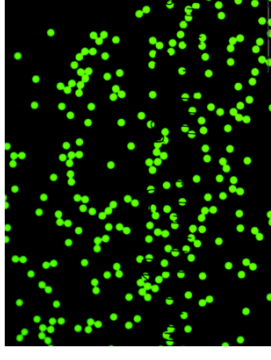


$$S_T = \frac{D}{D_T} = -\frac{1}{c} \frac{|\nabla c|}{|\nabla T|} = -\frac{1}{c} \frac{\left(\frac{dc}{dx} \right)}{\left(\frac{dT}{dx} \right)}$$

Preliminary thermophoresis results

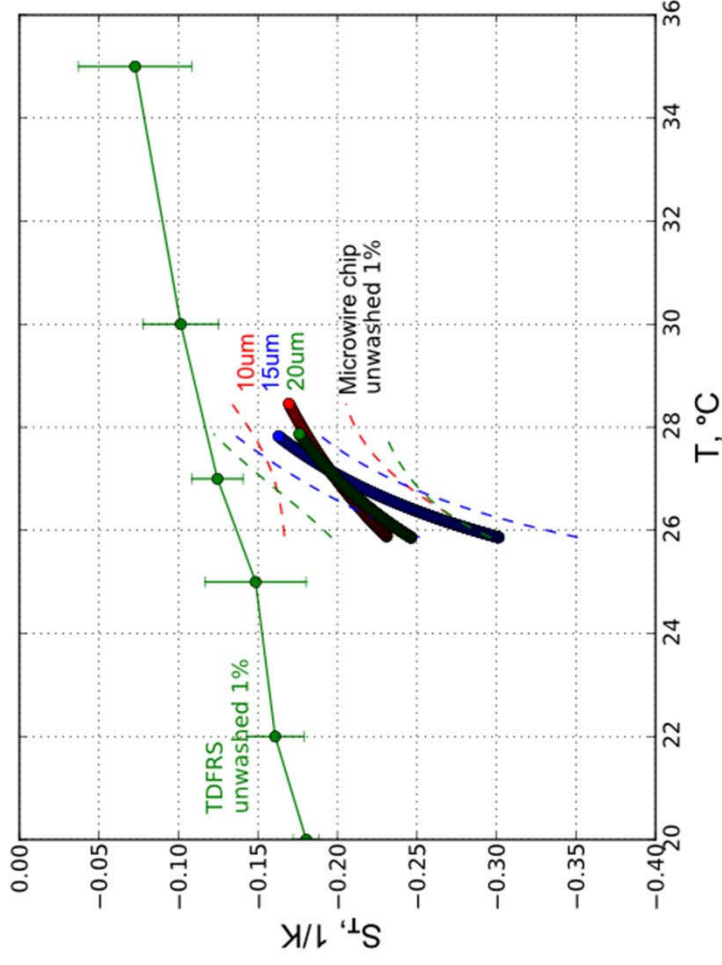
System:

Fluoro-Max Dyed Green
Aqueous Fluorescent Particles
(G25) from Thermo Scientific



<http://www.thermoscientific.com>

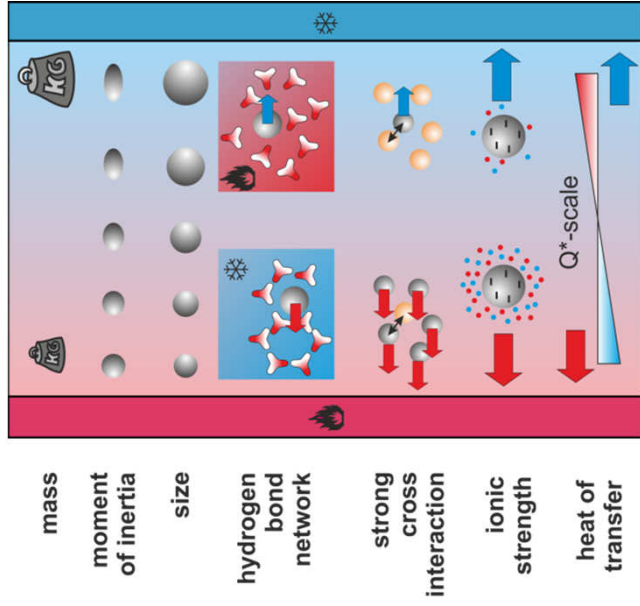
The surface of particles is carboxylated. Suspension contains traces of detergent and preservative agent. **SW1**



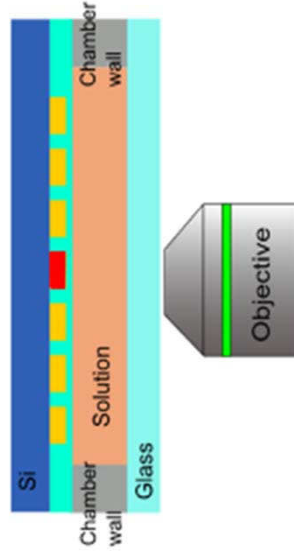
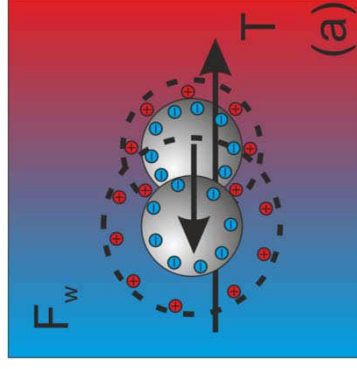
Technical problems

- Concentration changes
- Zero level
- Convection
- T measurements error (~20%)

Message to take home



Thermophoresis
in aqueous
systems is
complex



Thank you for your attention and thanks to...



Jan Dhont –
support &
theory



Hui Ning –
Ludox particles



Zilin Wang –
fd virus



Johan Buitenhuis –
synthesis



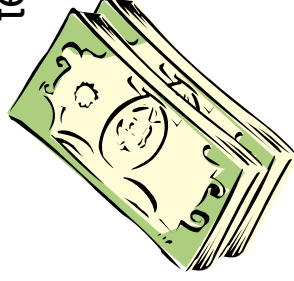
Hartmut Kriegs -
technical support



Dzmitry
Afanasev -
thermophoretic
microfluidic cell

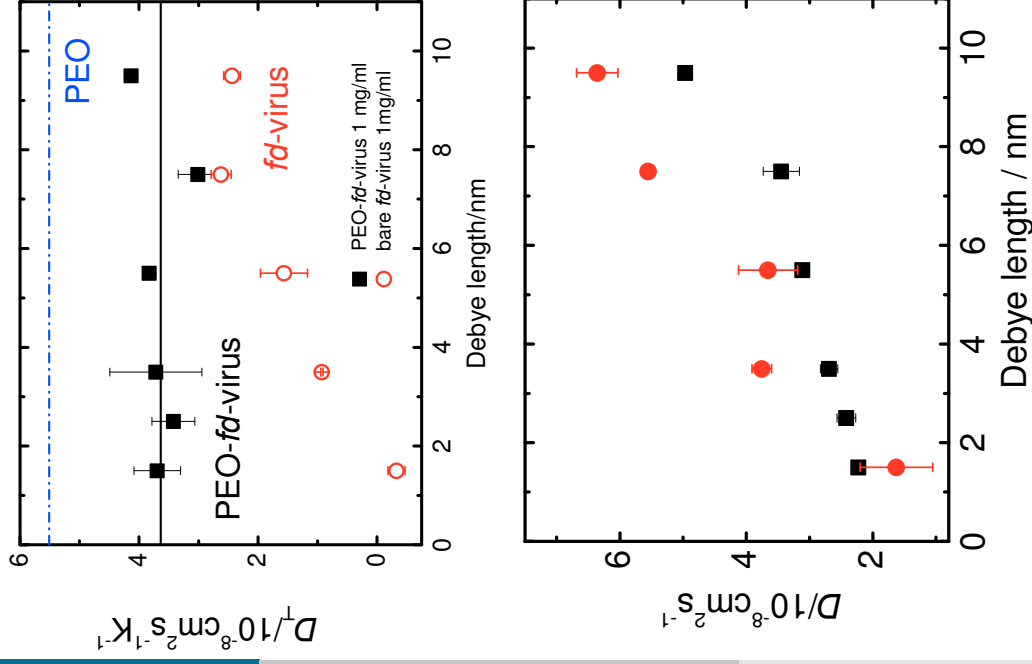


Bernhard Wolfrum –
Magma Move chip



Deutsche Forschungsgemeinschaft

Charged colloidal rod with hairs



Without hydrodynamic interactions:

$$D = \beta D_0 \frac{\partial \Pi}{\partial \rho}$$

$$\rho D_T = D_T^{\text{theo}} = \beta D_0 \frac{\partial \Pi}{\partial T}$$

.. Osmotic pressure

$$\Pi = \rho k_B T - \frac{2\pi}{3} \rho^2 \int_0^\infty dR R^3 \frac{dV^{\text{DLVO}}(R|T)}{dR} g(R|T)$$

$$D = D_0 [1 + 2B_2 \phi]$$

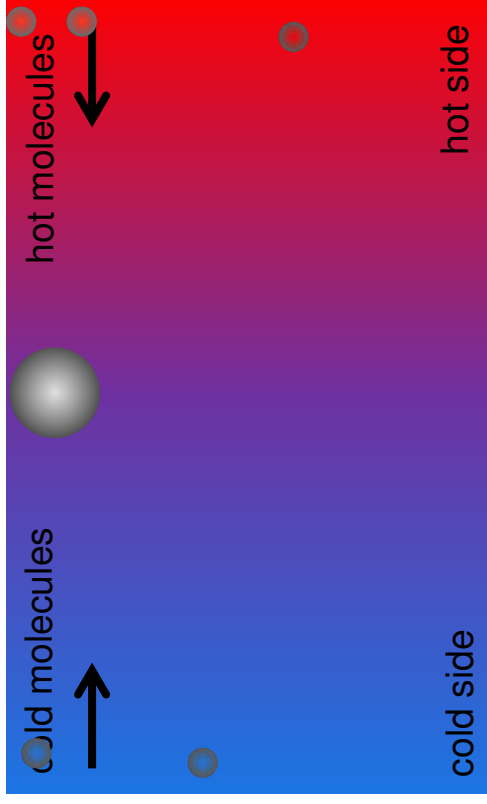
$$D_T = \frac{D_T^{\text{theo}}}{\rho} = \frac{D_0}{T} \left[1 + \frac{d(TB_2)}{dT} \phi \right]$$

- Both **coefficients** show an increasing trend
- Magnitude is comparable

More theoretical work is required



Mass effect: animation



higher momentum transfer
from the warm side

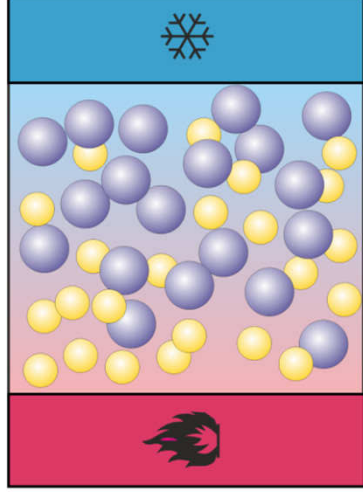
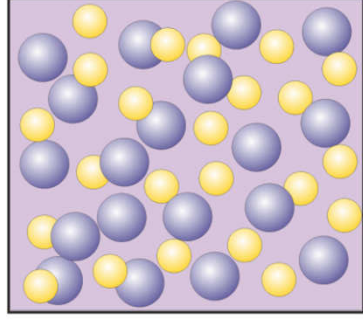


Enrichment of the heavy particles on the cold side

Phenomenological equation

(..., thermodiffusion, Soret effect) –

Movement of particles driven by a temperature gradient



$$\vec{j} = -D\vec{\nabla}c - c(1-c)D_T\vec{\nabla}T$$

Steady state $\vec{j}=0$

$$S_T = \frac{D_T}{D} \propto \frac{\Delta c}{\Delta T}$$

D - diffusion coefficient,

c - concentration,

D_T - thermodiffusion coefficient,

$\vec{j}$ - flux, T – temperature

S_T – Soret coefficient

