

## Multiferroicity in oxide thin films and heterostructures

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# Zusammenfassung

In dieser Arbeit wurden verschiedene Systeme von Übergangsmetalloxiden  $ABO_3$  (Perovskite wo B für ein Übergangsmetall und A für eine seltene Erde steht) in dünnen Schichten und Mehrschichtsystemen hergestellt und auf ihre strukturellen, magnetischen und ferroelektrischen Eigenschaften untersucht. Zur epitaktischer Herstellung wurde größtenteils Laserdeposition (PLD) verwendet, für eine Reihe wurde zusätzlich Sputterdeposition angewandt.

Die Multiferroica  $TbMnO_3$  und  $DyMnO_3$ , welche als Einzelmaterialien aufgrund ihrer zyklischen Magnetstruktur eine ferroelektrische Polarisation entwickeln, wurden hier in Einzelschichten zwischen 2 und 200 nm auf  $YAlO_3$  Substraten mit PLD hergestellt ( $TbMnO_3$  zusätzlich mit Sputterdeposition). Die strukturelle Charakterisierung der Oberflächen mit Röntgenreflektometrie und der Kristallstruktur mit Röntgendiffraktion zeigte ein gutes epitaktisches Wachstum mit glatten Oberflächen. Das magnetische Verhalten wurde makroskopisch mit SQUID Magnetometrie und mikroskopisch mit polarisierter Neutronendiffraktion und resonant magnetischer Röntgenstreuung untersucht. Während alle untersuchten Proben eine antiferromagnetische Ordnung, ähnlich der Kollinearen Magnetstruktur der Einzelmaterialien oberhalb der zyklischen Ordnungstemperatur, zeigten, konnte die multiferroische Tieftemperaturphase nur bei den Proben, welche mit Sputterdeposition hergestellt wurden, gemessen werden. Die Untersuchung der Erzeugung von zweiten harmonischen Wellen (SHG) konnte das Vorhandensein einer ferroelektrischen Polarisation in der Tieftemperaturphase bestätigen. Die jeweiligen Ordnungstemperatur der Dünnschichten kamen den Werten aus den Einzelmaterialien sehr nahe. Abweichend hiervon wurden erhöhte Ordnungstemperaturen der Tb Ionen beobachtet, welche die Mn Ordnung leicht abschwächte, was in  $TbMnO_3$  Kristallen nicht beobachtet wird.

Die Kopplung der antiferromagnetischen Ordnung in  $TbMnO_3$  zu ferromagnetischen Schichten von  $LaCoO_3$  wurde anhand von Übergittern von 20 Doppellagen  $TbMnO_3$ - $LaCoO_3$ , welche mit PLD auf  $YAlO_3$  hergestellt wurden, untersucht. Die SQUID Magnetometrie ergab einen starken Einfluss der antiferromagnetischen Übergänge auf die Magnetisierung. Die elementspezifische Magnetisierungsmessung mittels XMCD zeigte, dass die ferromagnetischen Beiträge nur von den Co Ionen herrühren. Die Analyse einer polarisierten Neutronendiffraktionsmessung führte zu einem komplexen magnetischen Modell, welches eine starke Kopplung des Mn Systems an die Co Magnetisierung beinhaltet.

Die Untersuchung von  $EuTiO_3$ - $BaTiO_3$  Übergittern, hergestellt mit PLD auf  $GdScO_3$  Substraten, auf eine magnetische Ordnung des Eu mittels polarisierter Neutronenreflektometrie konnte die Ordnung bis auf  $0.01 \mu_B$  ausschließen. An diesem System konnten allerdings Simulationsmodelle, welche für die Reflektivität und Diffraktion an anderen Systemen entwickelt wurde, getestet werden und zeigten perfekte Übereinstimmung mit den Experimenten.

Im Zusammenhang mit der Dissertation wurde zusätzlich zu den erwähnten Simulationsmodellen die Auswertungssoftware Plot.py entwickelt, welche für den größten Teil der Datenanalyse verwendet wurde.



## Summary

In this work a variety of different systems of transition metal oxides  $ABO_3$  (perovskite materials, where B stands for a transition metal and A for a rare earth element) were produced as thin films and heterostructures and analyzed for the structural, magnetic and ferroelectric properties. For the epitaxial film preparation mostly pulsed laser deposition (PLD) was applied. For one series high pressure oxide sputter deposition was used as well.

The bulk multiferroics  $TbMnO_3$  and  $DyMnO_3$ , which develop their electric polarization due to a cycloidal magnetic order, have been prepared as single layers with thicknesses between 2 and 200 nm on  $YAlO_3$  substrates using PLD and sputter deposition. The structural characterization of the surfaces and crystal structure were performed using x-ray reflectometry and diffraction, respectively. These yielded low surface roughness and good epitaxial growth. The magnetic behavior was macroscopically measured with SQUID magnetometry and microscopically with polarized neutron diffraction and resonant magnetic x-ray scattering. While all investigated samples showed antiferromagnetic order, comparable with the collinear magnetic phase of their bulk materials, only the sputter deposited samples exhibited the multiferroic low temperature cycloidal order. The investigation of the optical second harmonic generation in a  $TbMnO_3$  sample could proof the presence of a ferroelectric order in the low temperature phase. The respective transition temperatures of the thin films have been very similar to those of the bulk materials. In contrast an increase in the rare earth ordering temperature has been observed, which reduces the Mn order slightly, an effect not known from bulk  $TbMnO_3$  crystals.

The coupling of the antiferromagnetic order in  $TbMnO_3$  to ferromagnetic layers of  $LaCoO_3$  was investigated in super-lattices containing 20 bilayers produced with PLD on the same substrates. The SQUID magnetometry yielded a strong influence of the antiferromagnetic transitions on the overall magnetization. Element specific magnetization measurement from XMCD showed that the ferromagnetism has only Co contributions. The analysis of a polarized neutron diffraction experiment resulted in a complex magnetic model, which requires a strong coupling of the magnetic moments of Mn and Co.

The investigation of a system build of  $EuTiO_3$ - $BaTiO_3$  super-lattices, produced with PLD on  $GdScO_3$  substrates, for a magnetic order of the Eu system with polarized neutron reflectometry could eliminate ferromagnetism down to  $0.01 \mu_B$ . Nevertheless, the system could be used to test simulation models, build for reflectivity and diffraction on the other systems. All simulations showed very good agreement with the experiments.

In the context of this thesis and in addition to the already mentioned simulations the evaluation software Plot.py was developed, which was used for most of the data analysis.



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# Chapter 1

## Introduction

Multiferroics, materials possessing at least two (anti)ferroic properties, are of high interest in today's research because of a variety of possible applications and the physical principles behind the effect [31, 123, 124]. Especially magnetic and ferroelectric order are of interest for sensing, data storage and data processing [89]. "The revival of the magneto-electric effect" [40, 113] was strongly triggered by the observation of multiferroic behavior in a variety of manganites containing small rare earth cations [58, 70, 72]. In these compounds a strong coupling between the ferroelectric polarization and the (anti)ferromagnetic order of their spin system exists [38]. From a theoretical point of view, these compounds contradict the usual explanation for ferroelectricity and magnetic order in transition metal systems. The former usually requires  $d^0$ -ness, i.e. empty  $d$  orbitals, while the latter can only appear when partly filled  $3d$  orbitals are present. From an application's point of view, the control of the electrical degree of freedom via magnetic fields and vice versa offers fascinating new perspectives, e.g. devices where a magnetic field changes the optical properties [24]. When it comes to devices, thin films of multiferroic compounds are required. Furthermore, the mechanisms leading to multiferroic behavior may be altered by epitaxial strain, the interface to the substrate or the increased importance of interfaces and finite size [98].

The improvements of thin film deposition methods made it possible to produce oxidic superstructures of layers with only a few unit cells and atomic flat interfaces. Heterostructures of different oxide materials possess even more perspectives for application than bulk materials [99], as the properties of the different layers can be combined as e.g. in artificial multiferroics [22, 44] and even new phenomena are found (2D electron gas [90] and superconductivity [101] at an interface between two insulators, ferromagnetic clusters and superconducting order [36] or charge transfer at the interfaces [49, 106]).

In this work the multiferroic compounds  $\text{TbMnO}_3$  and  $\text{DyMnO}_3$  are studied in thin films and heterostructures for their magnetic and ferroelectric properties. Additionally, a potential artificial multiferroic structure of  $\text{EuTiO}_3$  and  $\text{BaTiO}_3$  is investigated.  $\text{TbMnO}_3$  thin films have already been grown on e.g.  $\text{SrTiO}_3$  and  $\text{LaAlO}_3$  substrates [33]. These films exhibit  $90^\circ$  twinning and show emerging ferromagnetism [73, 80, 102], while the antiferromagnetic spiral structure, which leads to the multiferroicity, was not directly observed. For the present study, the films and multilayers were deposited on orthorhombic  $\text{YAlO}_3$  substrates, which leads to untwinned films [47]. The structural and multiferroic properties of single layers with different thicknesses between 2 and 200 nm have been investigated (see **chapter 5**) by x-ray and neutron scattering techniques as well as macroscopic magnetization measurements. Thus

all important multiferroic properties were analyzed before progressing with the multilayer investigations.

The coupling of the magnetic order of  $\text{TbMnO}_3$  to adjacent ferromagnetic  $\text{LaCoO}_3$  layers has been investigated with microscopic and macroscopic methods in the second part of this work (**chapter 6**). Although in bulk  $\text{TbMnO}_3$  the coupling between magnetism and ferroelectricity is already strong, large fields are needed to switch the polarization, which could be overcome by a coupling to a ferromagnetic material.

Another form of interface effect has been studied for multilayers of  $\text{EuTiO}_3$  and  $\text{BaTiO}_3$  in **chapter 7**. Strained single layers of  $\text{EuTiO}_3$  are found to be ferromagnetic, while the alloy  $\text{Eu}_{0.5}\text{Ba}_{0.5}\text{TiO}_3$ , on the other hand, does not show any magnetic order. Therefore ferromagnetism in different multilayers of  $\text{BaTiO}_3$  and  $\text{EuTiO}_3$  were studied with polarized neutron reflectivity.

# Chapter 2

## Theoretical Background

The following sections will give a review of the theory behind the investigated material systems and experimental methods. For a description of the physical and mathematical symbols used, refer to the list of symbols in the appendix **chapter G**.

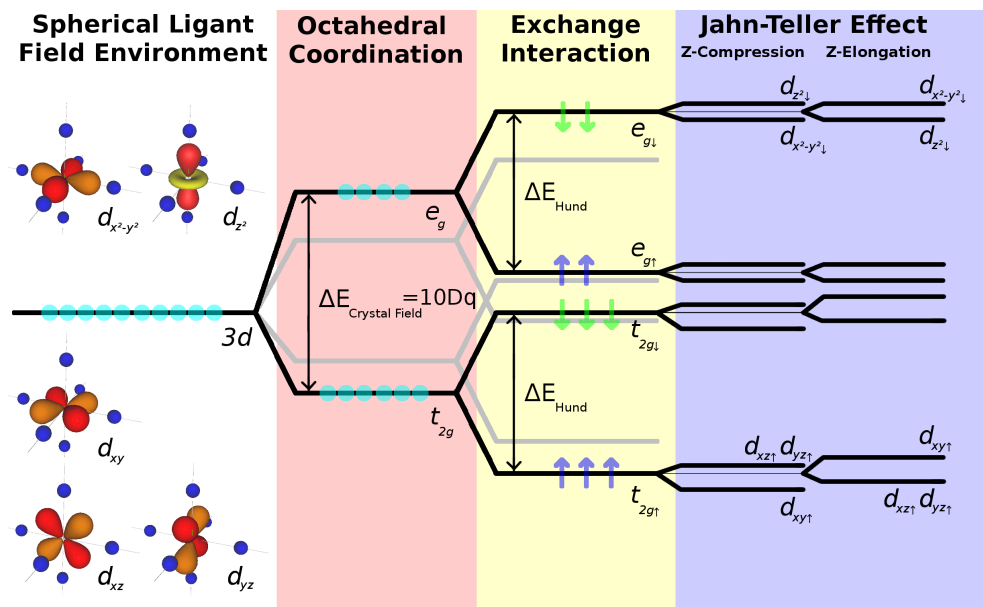
### 2.1 Transition metal oxides $\text{ABO}_3$ with Perovskite structure

The compounds under investigation in this thesis are transition metal oxides with the composition  $\text{ABO}_3$ . They possess a (distorted) Perovskite type crystal structure, where the B-site cation is positioned inside an octahedron of 6 oxygen anions. The octahedra are connected at the corners and the A-site cations occupy the spaces between the octahedra. Depending on the ion sizes the octahedra are buckled, which changes the symmetry from cubic to orthorhombic or rhombohedral. The crystal unit cell of orthorhombic Perovskites in the  $\text{Pbnm}$  space group setting (e.g.  $\text{YAlO}_3$  and  $\text{TbMnO}_3$ ) is illustrated in **figure 2.2**. The  $3d$  transition metals occupy the B-site while the A-site can be filled with a variety of elements from the second group, some of the  $4d$  transition metals, the lanthanoids and a mixture of these. Changes in the size of the A-site ion lead to tilting of the oxygen octahedra. Secondly the state of ionization at the A-site defines the population of the  $3d$  states of the B-site transition metal.

The described flexibility and the resulting tunability is one reason for the variety of effects found in this class of compounds (and slight variations) [122] as Mott-insulation, colossal magneto resistance (CMR), high temperature superconductivity and single phase multiferroicity (**section 2.2**). The magnetic order (dependent on the ground state) is an important driving force for these effects and thus will be covered in the next sections.

#### 2.1.1 Ground state and magnetic moment in Perovskites

Before addressing the coupling mechanisms leading to different magnetic order, this section will cover the derivation of the cation's ground state and the resulting magnetic moment. The  $3d$  transition metal on the B-site is octahedrally coordinated by 6 oxygen anions creating a crystal field, which – for the ideal undistorted octahedron – splits the 5 degenerate  $3d$  states



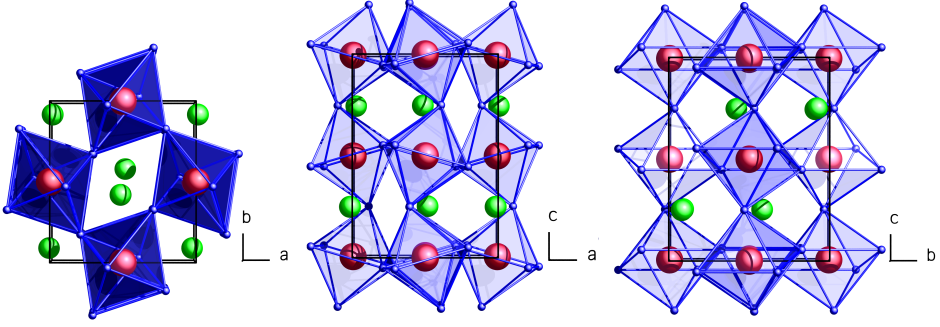
**Figure 2.1:** Crystal field splitting of the 3d-orbitals in an octahedral coordination. The crystal field effect is larger than the Hund's coupling, so the  $t_{2g\downarrow}$  states are filled before the  $e_{g\uparrow}$  states. The opposite case is also indicated (gray).

into 3 lower lying  $t_{2g}$  and 2 elevated  $e_g$  orbitals [5, 23], because of the different distances to the ligand charge. This splitting ( $\Delta E_{\text{CrystalField}}$ ) is found to be  $4Dq$  and  $6Dq$  for the  $t_{2g}$  and  $e_g$  levels (as the overall energy is conserved), respectively, and has been calculated with good agreement to experimental data (e.g. by Phillips [95]). In some systems the degeneracy of the  $t_{2g}$  and  $e_g$  orbitals is lifted by a distortion of the octahedra, which can lead to an overall energy gain<sup>1</sup>; the so called Jahn-Teller effect [62]. This can be a static cooperative distortion of the lattice or fluctuations without an average change of the crystal structure.

The magnetic moment depends on the electron configuration of the ion and the ratio between the crystal field splitting and the Hund's rule coupling energy ( $\Delta E_{\text{Hund}}$ ), which splits the  $\uparrow$  and  $\downarrow$  spin states (exchange splitting). This is illustrated in the energy diagram in **figure 2.1**. Ions with more than 3 and less than 8 d-electrons thus may have a high-spin or low-spin state in dependence of the ratio between  $\Delta E_{\text{CrystalField}}$  and  $\Delta E_{\text{Hund}}$ .

**Manganese** has the configuration  $[Ar] 3d^5 4s^2$ , for the two important oxidation states  $Mn^{3+}$  and  $Mn^{4+}$  this leads to 4 and 3 d-electrons, respectively. Because of an usually moderate crystal field splitting their ground states are  $t_{2g\uparrow}^3 e_{g\uparrow}^1$  for  $Mn^{3+}$  and  $t_{2g\uparrow}^3$  for  $Mn^{4+}$ .

<sup>1</sup>"The physical reason for this is that in first-order perturbation theory, the center of gravity of the levels remains the same after a perturbation that splits the levels, so that removal of the degeneracy, or splitting of the levels, results in a ground state that decreases linearly with the distortion." - p. 64 in [5]



**Figure 2.2:** Crystal structure of orthorhombic  $ABO_3$  transition metal oxides with the transition metal ions B (red) inside oxygen (blue) octahedra and the A site ions (green) in the spaces between the octahedra.

**Cobalt** with  $[Ar] 3d^7 4s^2$  has 6 d-electrons in trivalent-configuration, as present in the rare earth cobaltates. Exchange splitting and ligand field effect have the same order of magnitude, which results in a low- ( $\langle t_{2g}^6 \rangle$   $S=0$ ), intermediate- ( $\langle t_{2g}^4 \rangle t_{2g\uparrow} e_{g\uparrow}$   $S=1$ ) and high-spin state ( $\langle t_{2g}^2 \rangle t_{2g\uparrow}^2 e_{g\uparrow}^2$   $S=2$ ). For  $LaCoO_3$ , spin state transitions attracted a lot of attention in research over decades but are not completely settled yet [52, 81, 109, 117].

### 2.1.2 Magnetic exchange interactions

In a fully ionic bound crystal the magnetic ions would be isolated from neighboring magnetic moments<sup>2</sup>, which would lead to purely paramagnetic behavior. This holds for the rare earth ions, where interaction with other magnetic ions is quite small (ordering temperatures below 10 K) due to the adjacency of the  $4f$  electrons to the core. In the case of the transition metals the unoccupied d-bands lie relatively low above the Fermi-level, which allows virtual hopping from the ligand to the cation, partial covalent bonds or even metallic conductivity. The coupling across one or more anions, known as superexchange, can lead to ferro- or antiferromagnetic correlations with varying strength. Which type of coupling results from a superexchange path depends on the occupied and unoccupied cation orbitals and their spatial expansion with respect to the anion orbitals. The different possible cases and routes have been condensed [5, 17, 50, 67] to the so called Goodenough-Kanamori rules, which will be exemplified using the example of the A-type<sup>3</sup> antiferromagnet  $LaMnO_3$  (the parent compound of a CMR material [65]):

$LaMnO_3$  has a distorted Perovskite structure as illustrated in **figure 2.2**. Below  $\gtrsim 1150$  K cooperative Jahn-Teller distortion elongates the octahedra in the  $ab$ -plane in alternating directions for neighboring manganese ions. This lifts the degeneracy of the half filled manganese  $e_g$  orbitals, leading to orbital order below  $\approx 750$  K, where only the  $d_{z^2}$  states are occupied, while the  $d_{x^2-y^2}$  orbitals remain empty. Although the origin of these transitions is still under

<sup>2</sup>Leaving only the magnetic dipole-dipole interaction, which has an interaction energy of  $k_B \cdot T \approx \frac{\mu_0}{4\pi} \frac{g^2 \mu_B^2}{4a^2} \lesssim 100 \text{ mK}$  and thus can be neglected for temperatures above 1 K.

<sup>3</sup>Parallel ordered moments in planes with antiferromagnetic stacking.

debate [94], the complex interplay between superexchange, Jahn-Teller effect and magnetism is described generally with the Kugel'-Khomskii model [75].

The creation of covalent or semicovalent bonds is only possible, if there is an overlap of oxygen  $2p$  with empty  $d$ -orbitals of the transition metal ion (in this case the empty  $e_g$ , as it is the lowest in energy). The ordered unoccupied orbitals of  $\text{LaMnO}_3$  are illustrated in **figure 2.3a**. As can be seen there is a closed superexchange path in the  $c$ -direction for all Mn-ions, while in  $a$ - and  $b$ -direction only one Mn-ion can form a bond with the anion per site. Applying the Goodenough-Kanamori rules, this leads to weak ferromagnetic bonds in the  $ab$ -planes with an antiferromagnetic coupling between the layers, thus resulting in the found A-type antiferromagnetic order [45, 61, 83, 133]. It should be emphasized, that these considerations only hold for systems containing only trivalent Mn ions, while  $\text{Mn}^{4+}$  can form 6 semicovalent bonds and thus have antiferromagnetic interactions in all directions leading to G-type order as e.g. in  $\text{CaMnO}_3$ .

## 2.2 Multiferroics

The presence of at least two ferroic properties<sup>4</sup> – (anti)ferromagnetism, ferroelectricity<sup>5</sup> or ferroelasticity<sup>6</sup> – is called multiferroicity. While they are closely related, multiferroicity does not imply a coupling<sup>7</sup> between the different ferroic orders. Especially materials with combined ferromagnetic and ferroelectric order and magnetoelectric coupling possess a large potential for applications, as e.g. magnetic field sensors or magnetic random access memories (MRAM), without the need for high current densities for switching, as one could simply apply an electric field. There are very few single phase<sup>8</sup> multiferroics in nature with often low ordering temperatures, antiferromagnetism or a low coupling between both degrees of freedom.

### 2.2.1 Routes to simultaneous magnetic and electric dipolar ordering

When first looking for multiferroic compounds, one would investigate the class of materials, which is known to include materials exhibiting strong ferroelectricity and, on the other hand, materials with magnetic order. From this point of view the binary transition metal oxides are good candidates, because they comprise model ferroelectric materials as  $\text{BaTiO}_3$  or  $\text{PbZr}_x\text{Ti}_{1-x}\text{O}_3$  (PZT) and a diversity of magnetic compounds. Unfortunately, the physical mechanisms leading to both types of order in these compounds are contradictory. Ferroelectricity as in  $\text{BaTiO}_3$  requires empty  $d$ -shells ( $d^0$ -ness), as this allows for a full covalent bond to one adjacent oxygen ion, which can lead to an off-centering of the transition metal ion,

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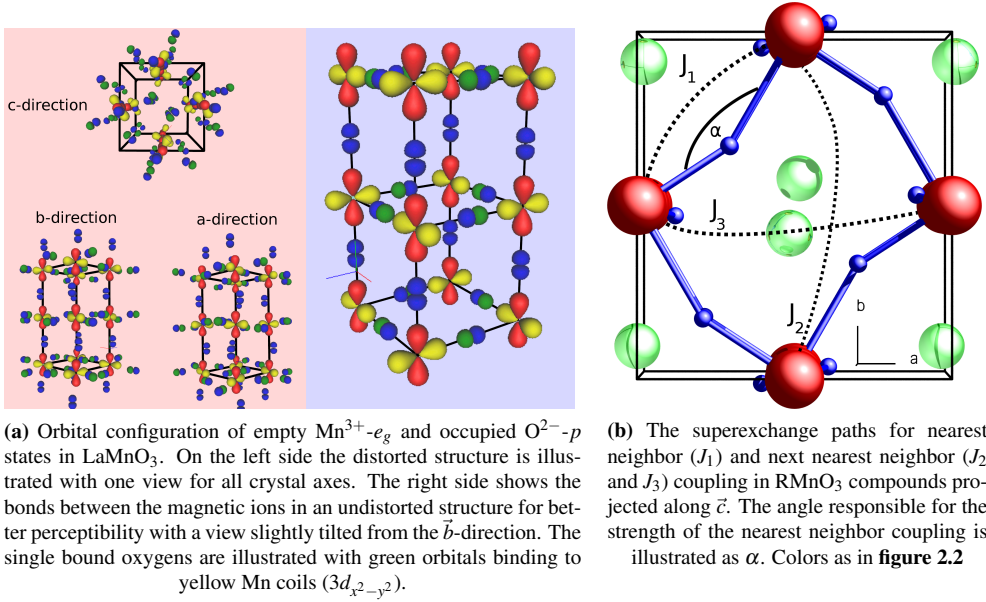
<sup>4</sup>We neglect the ferrotoroidicity here, because it isn't of large importance up to now.

<sup>5</sup>Forming of a long range ordered state of permanent electric dipoles, which can be switched with an electric field.

<sup>6</sup>Spontaneous strain in a crystal, which can be switched to another phase with different crystal structure or orientation.

<sup>7</sup>Magnetoelectric, piezoelectric or magnetostictive effects.

<sup>8</sup>In contrast to artificial heterostructures.



**Figure 2.3:** Superexchange in  $\text{RMnO}_3$

creating an electric dipole [32, 125]. Magnetism, on the other hand, obviously requires partly filled d-orbitals. Due to these facts the standard mechanism of ferroelectricity and magnetism in these compounds can't lead to multiferroicity. Hence other mechanisms are needed [40]:

- One possible route is to detach the magnetism from the B-site ion as in  $\text{BiFeO}_3$ , where Bi creates ferroelectric polarization with a lone-pair<sup>9</sup> mechanism [100, 118]. Due to the spatial separation of the magnetic and ferroelectric ion this mechanism generally leads to a weak coupling of both degrees of freedom.
- The ferroelectricity can be created due to charge order as proposed for  $\text{LuFe}_2\text{O}_4$  [18, 59, 134]. This would, in principal, lead to very strong magnetoelectric effects.
- Geometrical considerations have to be taken into account to explain the multiferroicity in hexagonal  $\text{YMnO}_3$  [126].
- The situation of most interest for this work is present in materials with competing interactions, which can lead to a spiral magnetic order. This magnetic structure itself can be the source for a electric polarization, which will be discussed in **section 2.2.2**.
- Artificial thin film heterostructures can be created [44], which couple a ferromagnetic to a ferroelectric material via e.g. a ferroelectric  $\rightarrow$  piezoelectric  $\rightarrow$  magnetostrictive  $\rightarrow$  ferromagnetic route. Besides their importance for application these structures are no "real" multiferroics in the sense of single phase materials.

<sup>9</sup>Two 5s or 6s electrons without a chemical bond.



**Symmetry considerations:** Another argument for the sparsity of multiferroic compounds is that they require breaking of two symmetries in one phase. For ordered magnetic moments, the time reversal symmetry is broken, as the time inversion changes the direction of a spin. Spatial inversion, on the other hand, only exchanges spins at different sites leaving the magnetic order unchanged in most cases. Electric polarization is produced by off-centered charges and therefore breaks the spatial inversion symmetry. Thus, for a multiferroic compound, both, time and spatial inversion symmetry, need to be broken.

## 2.2.2 Cycloidal magnetic order in multiferroic $\text{RMnO}_3$

For the explanation of the magnetic structure of  $\text{LaMnO}_3$  in **section 2.1.2** it was sufficient to consider nearest neighbor (NN) interactions ( $J_1$  in **figure 2.3b**). As the manganese valence state and the geometry is the same for all  $\text{RMnO}_3$  ( $\text{R}=[\text{La-Lu}]$ ) compounds, the NN coupling has the same sign. The main difference when exchanging the A-site ion is the ion size, which changes the tilting of the oxygen octahedra. Turning the Mn-O-Mn angle (illustrated as  $\alpha$  in **figure 2.3b**) further away from  $180^\circ$  weakens the ferromagnetic interactions in the ab-plane. This is evidenced by a decrease in magnetic ordering temperature starting from 140 K for  $\text{La}^{3+}$  with an ionic radius of  $1.032 \text{ \AA}$  ( $\alpha = 155^\circ$ ) down to below 50 K for  $\text{Gd}^{3+}$  with an ionic radius of  $0.938 \text{ \AA}$  ( $\alpha = 146^\circ$ )<sup>10</sup>. Despite the fact that the next nearest neighbor (NNN) superexchange (antiferromagnetic  $J_2$  and weak ferromagnetic  $J_3$  in **figure 2.3b**) can only occur via two oxygen ions, which generally weakens the coupling, it becomes important, when the NN interaction is further weakened going from Gd to Tb and Dy. Additionally the NNN exchange gets stronger as the O-O distance decreases ( $3.4 \text{ \AA}$  in  $\text{LaMnO}_3$  to  $3.0 \text{ \AA}$  in  $\text{HoMnO}_3$ ). The frustration arising from the ferromagnetic NN and antiferromagnetic NNN interaction leads to a cycloidal magnetic order<sup>11</sup> [69, 71] with a propagation vector in b-direction as ground state of those compounds.

Although this needs to be considered as the 2D frustrated Heisenberg model for  $S=2$ , the basic principal of this magnetic ground state can be understood using a classical one dimensional chain of NN ferromagnetic and NNN antiferromagnetic coupled moments. The Hamiltonian for this chain can be written as:

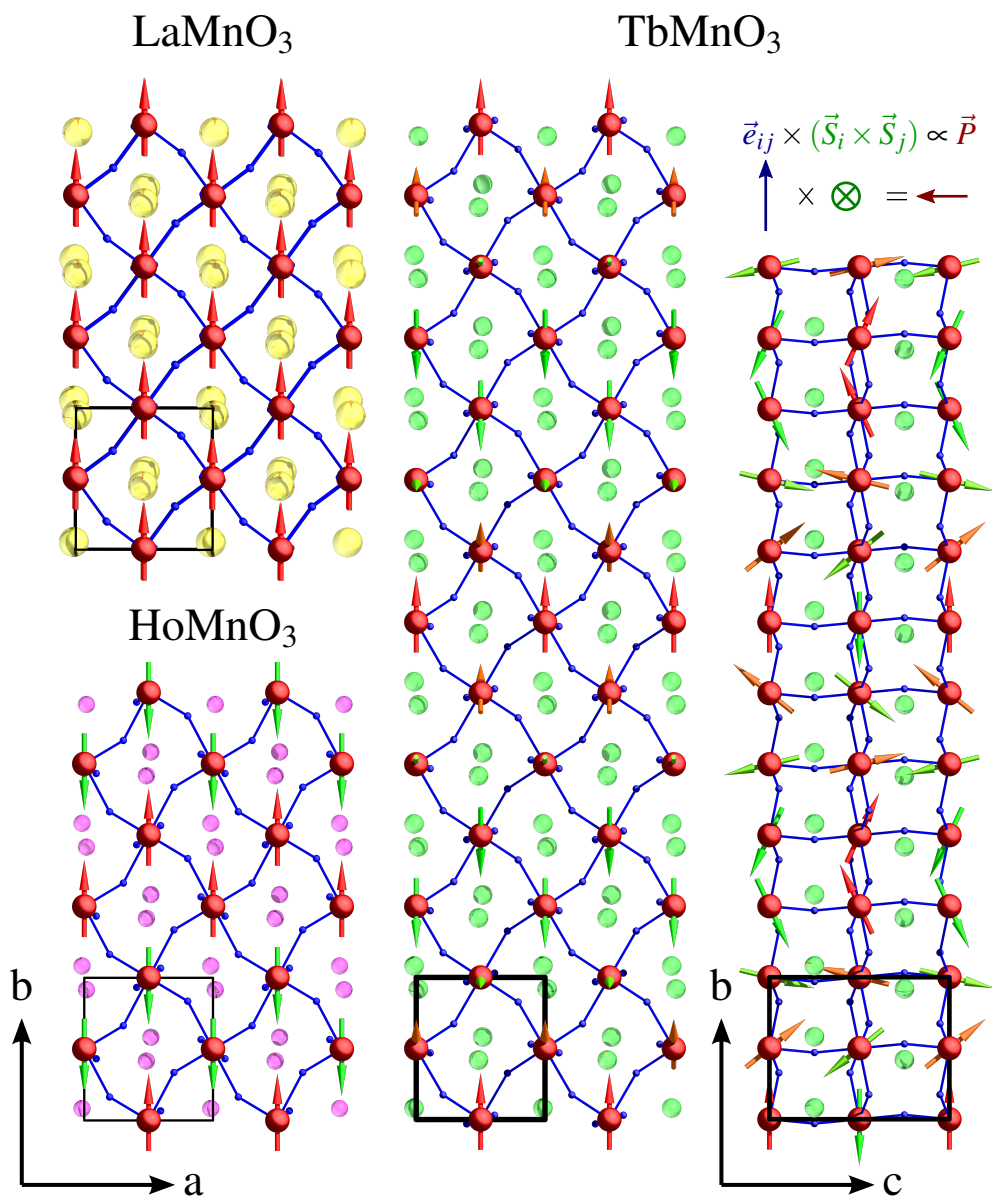
$$\mathcal{H} = \sum_j J_1 \vec{S}_j \cdot \vec{S}_{j+1} + \sum_j J_2 \vec{S}_j \cdot \vec{S}_{j+2} \quad (2.1)$$

with  $J_1 < 0$  and  $J_2 > 0$ . The energy of the system only depends on the relative angle between neighboring moments and as we assume a ordered ground state, we can rewrite the

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<sup>10</sup>Radii taken from [3] (page 14).

<sup>11</sup>The propagation vector lies in the plane of rotation of the magnetic moments in contrast to proper-screw type magnetic order.



**Figure 2.4:** Magnetic structure of LaMnO<sub>3</sub> (A-type), TbMnO<sub>3</sub> (cyclidal) and HoMnO<sub>3</sub> (E-type) in the low temperature ordered phase. In the case of the larger La ions, the Mn-O-Mn bond angle is  $\alpha = 155^\circ$ , which leads to a magnetic structure governed by the nearest neighbor interaction, which is ferromagnetic in the  $ab$ -plane. In HoMnO<sub>3</sub> the bond angle is about  $144^\circ$  and the ferromagnetic nearest neighbor interaction is weakened, giving rise to antiferromagnetic order in  $\vec{b}$ -direction through the next nearest neighbor coupling ( $J_2$  in **figure 2.3b**). In the intermediate case of TbMnO<sub>3</sub>, with a fitting ratio of NN and NNN coupling, the order is cyclidal with magnetic moments in the  $bc$ -plane and a periodicity close to  $7/2 \cdot b$ .

Hamiltonian per site to only contain the relative angle between neighbors:

$$\mathcal{H}_j = J_1 \cos(\phi_{j,j+1}) + J_2 \cos(2\phi_{j,j+1}) \quad (2.2)$$

$$\frac{\partial \mathcal{H}_j}{\partial \phi_{j,j+1}} \stackrel{!}{=} 0 \quad \text{for minimal energy} \quad (2.3)$$

$$\Rightarrow 0 = -J_1 \sin(\phi_{j,j+1}) \left( 1 + \frac{4J_2}{J_1} \cos(\phi_{j,j+1}) \right) \quad (2.4)$$

$$\frac{\partial^2 \mathcal{H}_j}{\partial \phi_{j,j+1}^2} = -J_1 \left( \cos(\phi_{j,j+1}) + \frac{4J_2}{J_1} \cos(2\phi_{j,j+1}) \right) \quad (2.5)$$

As one can see from the first and second derivative of the Hamiltonian, for  $J_2 \geq -\frac{1}{4}J_1$  an extremum at  $\cos(\phi_{j,j+1}) = -\frac{J_1}{4J_2}$  arises and the ferromagnetic solution  $\phi_{j,j+1} = 0$  is no longer a minimum (as the second derivative is  $-J_1(1 + \frac{4J_2}{J_1}) < 0$ ).

Further decreasing ion size on the A-site in  $\text{HoMnO}_3$  leads to ferromagnetic zik-zak chains in the ab-plane known as E-type antiferromagnetic order. The three types of order in the magnetic phase diagram are illustrated in **figure 2.4**. It should be noted that the mentioned frustration gives rise to a phase between the low temperature magnetic ordered and the paramagnetic phase, which exhibits a sinusoidally modulated spin wave<sup>12</sup> with moments in the  $\hat{b}$ -direction.

In contrast to the other routes to multiferroicity described in **section 2.2** the ferroelectricity in  $\text{TbMnO}_3$  and  $\text{DyMnO}_3$  directly arises from their uncommon magnetic structure. This gives rise to a strong coupling of both properties [51, 70] and a rich magnetoelectric phase diagram [72]. It was realized quite early [69] that the cycloidal magnetic structure breaks inversion symmetry as required for ferroelectricity. This leads to a phenomenological theory for the ferroelectricity and magnetoelectric effect [85]. The ferroelectric polarization derived with this model is equation 2.6, where  $\vec{P}$  is the electric polarization,  $\chi_e$  the dielectric susceptibility without magnetism,  $\gamma$  the magnetoelectric coupling coefficient,  $m_b$  and  $m_c$  the maximum component of the magnetic moments in  $\hat{b}$  and  $\hat{c}$ ,  $\vec{\tau}$  the propagation vector of the magnetic structure and  $\hat{a} = \hat{b} \times \hat{c}$  the direction of the magnetic moments rotation axis.

$$\vec{P} = \gamma \chi_e m_b m_c (\vec{\tau} \times \hat{a}) \parallel \hat{c} \quad (2.6)$$

The symmetry alone does not explain the effect itself. The microscopic origin of the ferroelectric polarization was identified to be the inverse Dzyaloshinsky-Moriya interaction [68, 88, 110, 111] (responsible for the coupling constant  $\gamma$  in equation 2.6). For the conventional Dzyaloshinsky-Moriya interaction an anisotropic superexchange leads to a non collinear magnetic structure, if there is no center of inversion. This effect was first predicted by Dzyaloshinsky based on symmetry arguments [37] and later theoretically deduced by introducing spin-orbit coupling in the energy terms describing the superexchange [84]. In the opposite case, where there is already a cycloidal magnetic structure, a small displacement (recently measured [131] to be in the range of femto meters) of the ions can lead to an energy gain via the Dzyaloshinsky-Moriya term  $E_{DM} = D \cdot (\hat{S}_i \times \hat{S}_j)$ , which is the source for the ferroelectric polarization.

<sup>12</sup>The magnetic phase diagram of the  $\text{RMnO}_3$  compounds is shown in [71].

|                | In-plane direction 1 |                   |        | In-plane direction 2 |                   |        |
|----------------|----------------------|-------------------|--------|----------------------|-------------------|--------|
|                | Miller Indices       |                   | Strain | Miller Indices       |                   | Strain |
|                | TbMnO <sub>3</sub>   | YAlO <sub>3</sub> |        | TbMnO <sub>3</sub>   | YAlO <sub>3</sub> |        |
| Orientation 1: | (1 0 0)              | (0 1 0)           | 0.6%   | (0 0 1)              | (0 0 1)           | 0.4%   |
| Orientation 2: | (6 1 0)              | (0 6 0)           | 1.1%   | (0 0 1)              | (0 0 1)           | 0.4%   |
| Orientation 3: | (7 1 0)              | (0 7 0)           | 0.7%   | (0 0 1)              | (0 0 1)           | 0.4%   |
| Orientation 4: | (5 3 0)              | (0 6 0)           | 0.6%   | (0 0 1)              | (0 0 1)           | 0.4%   |
| Orientation 5: | (2 7 0)              | (0 8 0)           | 0.6%   | (0 0 1)              | (0 0 1)           | 0.4%   |
| Orientation 6: | (3 2 1)              | (0 4 0)           | 2.1%   | (-7 3 7)             | (0 0 1)           | 0.9%   |
| Orientation 7: | (3 4 2)              | (0 6 0)           | 0.2%   | (1 -3 6)             | (0 0 1)           | 8.6%   |

**Table 2.1:** Theoretical possible growth orientations of TbMnO<sub>3</sub> on YAlO<sub>3</sub> substrates with the relative strain for both in-plane direction of the TbMnO<sub>3</sub> in-plane lattice.

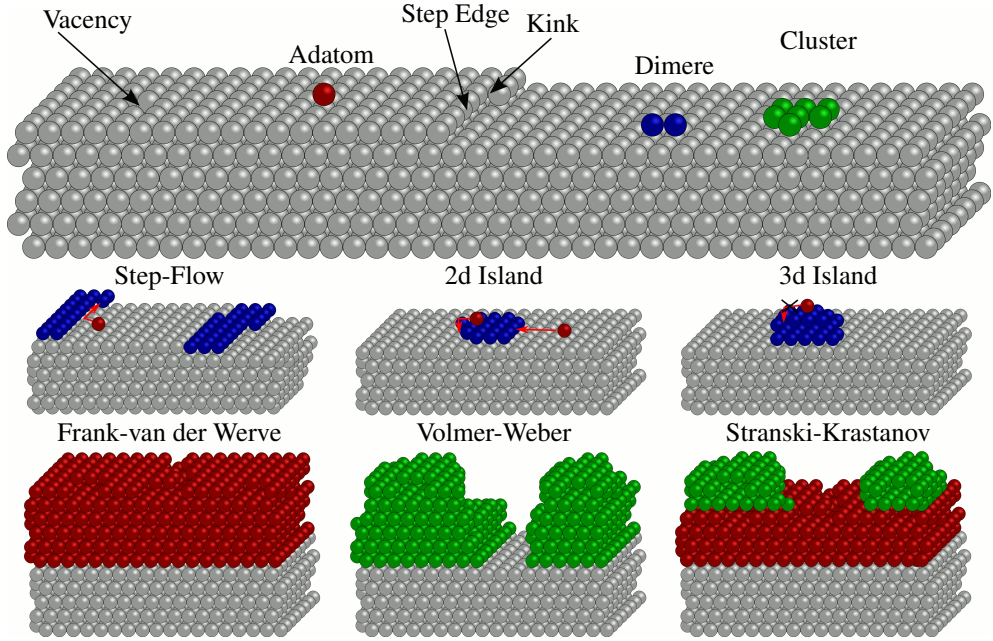
## 2.3 Epitaxial thin films

Thin film growth with a coherent crystalline structure is called epitaxy. In general, when depositing another material on a single crystalline substrate, there will always be some differences in crystal and electronic structure, which needs to be adopted at the interface [56]. The difference between the in-plane lattice parameters of the substrate and those of the deposited material will lead to strained films up to a critical thickness, where the strain relaxes due to dislocations [57] and other defects until the film has relaxed to its bulk crystal structure. Differences in the electronic structure at the interface<sup>13</sup> can lead to electron transfer and bond formation, which changes the band structure of the interface and the adjacent few unit cells [49, 90, 91, 101].

### 2.3.1 Orientation of deposited films

The coherent growth at the interface between two materials constrains the possible directions one material can grow on the other, because the unit cell geometry cannot be strained infinitely. To determine possible epitaxial growth directions, the in-plane lattice parameters of the substrate (or former deposited film) has to be compared with the unit cell metric of the deposited film. In most cases the growth direction, which can be accomplished by placing a small integer number of linear combinations of the film lattice vectors parallel to the substrate lattice with the lowest possible strain, will be preferred. E.g. growing Ag ( $a = b = c = 4.085 \text{ \AA}$ ) on GaAs with the in-plane lattice  $a_2 = b_2 = 5.6533 \text{ \AA}$  leads to a growth with  $(\vec{a} + \vec{b}) \parallel \vec{a}_2$  as  $|\vec{a} + \vec{b}| = 5.777 \text{ \AA} = 1.02 \cdot a_2$ . For new systems the possible growth directions can be estimated by simply comparing all possible linear combinations of the film lattice parameters for their compatibility with the substrate. **Table 2.1** shows all possibilities for TbMnO<sub>3</sub> films deposited on YAlO<sub>3</sub> (100) with a strain lower than 4% and up to 7 TbMnO<sub>3</sub> lattice vectors in each direction. Obviously, in-plane components with large vectors are very unlikely, as the substrate and film atoms can only have perfect bonding conditions at positions with this distance.

<sup>13</sup>Difference in e.g. valence, band gap, charge or electronic density of states.



**Figure 2.5:** Schematic of important terms for layer growth and the growth mode models. Ideas from [12, 13, 135].

### 2.3.2 Growth modes

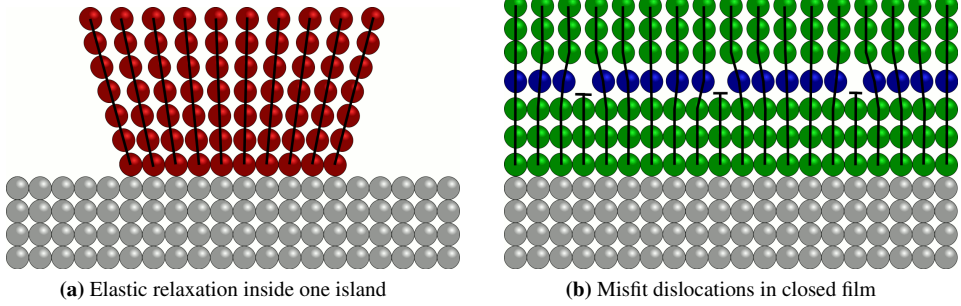
The microscopical development of the film during the growth can vary in dependence of the materials, deposition method, deposition rate and deposition temperature. An adatom impinging on the surface can diffuse on a terrace (with the diffusion constant  $D = k_s \cdot a^2$ )<sup>14</sup> until it hits a step or encounters another adatom or adatom cluster, loosing it's mobility due to the additional bond formation. Even the best substrates have step edges, as the polished surface normal never coincides with the crystal symmetry direction. The diffusion speed, the terrace width and the deposition rate determines, if the so called step flow or spontaneous nucleation dominates. The site-to-site hopping coefficient  $k_s$  is temperature dependent with  $k_s = e^{-V_s/k_B T}$  [128, 135]. As the coordination of atoms hopping down a step of an island is lowered, it forms an energy barrier which determines if clusters grow as 2d or 3d islands.

For deposited materials, which differ from the substrate material (heteroepitaxy), additional thermodynamic considerations<sup>15</sup> need to be taken into account, which can lead to three basic situations. These so called growth modes are commonly classified as introduced by Bauer [21]:

**Layer-by-layer** or *Frank-van der Merwe* growth: Each mono-atomic layer is closed one after the other. As this mode leads to defined film thickness and low roughnesses, it is the situation desired in most cases.

<sup>14</sup> $k_s$  is the site hopping rate of an atom and  $a$  the effective hopping distance.

<sup>15</sup>mainly concerning the different surface free energies as described below



**Figure 2.6:** Strain relaxation processes. Ideas from [12, 13].

**Island** or *Volmer-Weber* mode: Starting at the substrate the deposited material creates distinct islands, which grow separately.

**Stranski-Krastanov** (SK) mode: The growth starts in layer-by-layer mode and switches to island growth after a defined thickness is reached.

Which mode is favored depends on the substrate and film surface free energies  $\gamma_{\text{Substrate}}$ ,  $\gamma_{\text{Film}}$  and the interface energy  $\gamma_{\text{SF}}$ . If  $\gamma_{\text{Film}} + \gamma_{\text{SF}} < \gamma_{\text{Substrate}}$  layer-by-layer growth will be favored, while Volmer-Weber is favored otherwise. This fact leads to the consequence that a multilayer system of layers A and B will have different interface roughnesses for B grown on A than for A grown on B. For pseudomorphic growing films<sup>16</sup> the interface energy increases with each layer, which means that the layer-by-layer growth will switch to island mode after a critical thickness if the strain is not relaxed, which is called Stranski-Krastanov growth.

### 2.3.3 Strain relaxation

As long as the film thickness is limited and the islands are distinct, it is possible to partly relax the strain in pseudomorphic growth by elastic deformation as shown in **figure 2.6a**. When the islands grow together or the thickness of a closed layer gets too large, misfit dislocations can form [63, 66, 87] and the film crystal lattice can relax to its bulk values (**figure 2.6b**).

### 2.3.4 Influence of strain on the magnetic structure

As was described in **section 2.1.1** and **2.1.2**, the magnetic coupling in a compound can strongly depend on the unit-cell geometry. When a compound gets strained, the change in geometry can therefore lead to a change of the magnetic ordering temperature or even alter the type of order. As this effect is of importance for some compounds investigated in this work we will discuss some examples:

<sup>16</sup>The film lattice parameters are strained to fit the substrate.

**Magnetism in  $\text{EuTiO}_3$**  The growing accuracy of ab-initio calculations was used to predict a ferromagnetic ferroelectric state in the bulk paraelectric antiferromagnet  $\text{EuTiO}_3$  [76], if the material is extended in two directions (leading to a compression in the third direction). Strained films grown on  $\text{SrTiO}_3$  and  $\text{DyScO}_3$  could confirm these predictions [76]. This effect is of great interest for the field of multiferroicity as a large magnetoelectric coupling was found [112] in this compound, too. This material will be discussed further in the according sample section **section 4.2.4**.

**Ferromagnetic  $\text{LaCoO}_3$**  A similar effect can be found in  $\text{LaCoO}_3$  thin films which exhibit ferromagnetism [42]. The spin state transition found in the paramagnetic bulk material [81] is additionally suppressed partially. The origin for this effect is still under debate. It was suggested that a superexchange between high-spin and low-spin Co ions could be responsible for the ferromagnetic coupling [82], but this explanation would pose the additional question, why the intermediate spin state of the bulk material would not result in the same coupling. This effect is of specific importance for the systems introduced in **section 4.2.2** and **4.2.3**.

**Chemical strain in  $\text{RMnO}_3$**  Strain effects can also be produced by substituting elements with mixtures of other materials. This method was used to change the Mn-O-Mn bond angle in  $\text{EuMnO}_3$  by partially substituting Eu with Y. With this method it was possible to establish multiferroicity [55] as in  $\text{TbMnO}_3$ , which was an additional proof for the theoretical interpretation of the  $\text{RMnO}_3$  magnetic phase diagram.

## 2.4 Scattering theory

As several different types of scattering experiments were performed to investigate different physical properties of the samples, this section will give an overview on the basic scattering theory, needed to understand the different methods.

### 2.4.1 General scattering theory and Born approximation

A scattering experiment measures the angular dependent intensity (proportional to the differential scattering cross section  $\frac{d\sigma}{d\Omega}$ ) of radiation after interaction with the sample.

$$I = I_0 \frac{d\sigma(\Theta, \varphi)}{d\Omega} d\Omega = I_0 |f_k(\Theta, \varphi)|^2 \quad (2.7)$$

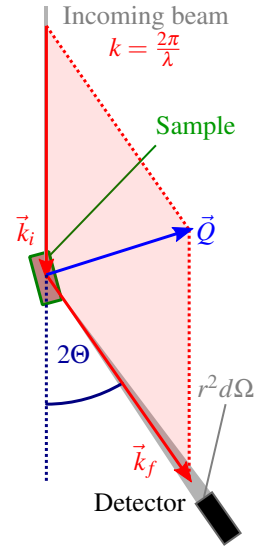
$$\Phi(r) \underset{r \rightarrow \infty}{\sim} e^{i\vec{k}_i \vec{r}} + f_k(\Theta, \varphi) \frac{e^{i\vec{k}_f \vec{r}}}{r} \quad (2.8)$$

$$V(\vec{r})\Phi(\vec{r}) = \frac{\hbar^2}{2m_{red}} (\nabla^2 + k^2) \Phi(\vec{r}) \quad (2.9)$$

The intensity  $I$  measured per given solid angle  $d\Omega$  and incident intensity  $I_0$  is given in equation 2.7. The derivation of the scattered intensity can be found in many textbooks as for example in [2], only the results will be described in the following paragraphs:

To describe an elastic scattering process<sup>17</sup> of non relativistic particles, one starts from the stationary Schrödinger, for scattering of photons with the Maxwell equations<sup>18</sup>, which both lead to the wave equation (equation 2.9 just with different prefactors) with wave function  $\Phi(\vec{r})$  and scattering potential  $V(\vec{r})$ . This equation needs to be solved for a plane incident wave (with wave vector  $\vec{k}_i$ ) with an additional scattered wave (with wave vector  $\vec{k}_f$  and  $k_i = k_f = \frac{2\pi}{\lambda}$ ) as given in equation 2.8. The wave equation can be transformed into an integral form, which can be solved in many cases by using the plane wave ( $\Phi_{(0)}(\vec{r}) = e^{i\vec{k}_i\vec{r}}$ ) as first approximation for the wave function, integrating the right side of equation 2.10 and iteratively putting the result as a next guess of  $\Phi$  into the equation.

$$\Phi_{(n+1)}(\vec{r}) = e^{i\vec{k}_i\vec{r}} + \frac{2m_{red}}{4\pi\hbar^2} \int \frac{e^{ik|\vec{r}-\vec{r}'|}}{|\vec{r}-\vec{r}'|} V(\vec{r}') \Phi_{(n)}(\vec{r}') d^3r' \quad (2.10)$$



**Figure 2.7:** Scattering geometry

If the interaction potential is weak, the first integration in this so called Born series is already a good approximation for the scattered wave (first Born approximation). The scattered amplitude in this framework is the Fourier transform of the scattering potential (introducing the scattering vector  $\vec{Q} = \vec{k}_f - \vec{k}_i$  and with  $e^{ik|\vec{r}-\vec{r}'|} = e^{i\vec{k}_f(\vec{r}-\vec{r}')} = e^{i\vec{Q}\vec{r}}$  and  $r \approx |\vec{r}-\vec{r}'|$  (far field)):

$$\xrightarrow{2.10+2.8} f_k^{(Born)}(\vec{Q}) = \frac{2m_{red}}{4\pi\hbar^2} \int V(\vec{r}) e^{-i\vec{Q}\vec{r}} d^3r \propto \mathfrak{F}(V) \quad (2.11)$$

As the phase of the wave can't be measured in most experiments (the phase is lost by taking the modulus squared), it is necessary to calculate the intensity from a model for the scattering potential  $V(\vec{r})$ . How this model is accomplished depends on the type of radiation used to probe the sample and on the sample composition itself. The different aspects which need to be taken into account for specific experiments are described in the following sections.

## 2.4.2 Single crystal diffraction

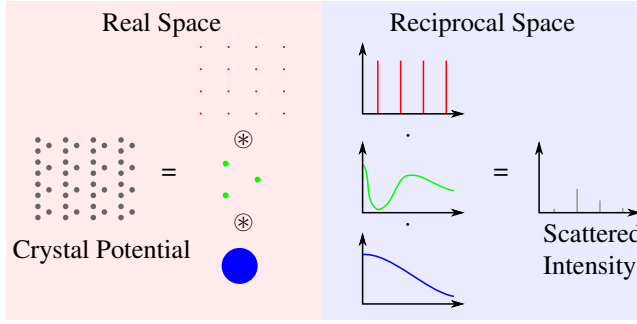
X-ray radiation and moderated neutrons have wavelengths in the Å range, making them a perfect probe for structures with atomic scale variations in the potential. Especially single crystals as long range periodic structures can be probed precisely in reciprocal space<sup>19</sup>. For a

<sup>17</sup>Scattering without energy transfer between radiation and sample.

<sup>18</sup>and for the interaction with the bound electrons perturbation theory as described in **section 2.4.5**

<sup>19</sup>Real space and reciprocal space are connected with the Fourier transform. In the Born approximation the diffraction experiment measures the modulus squared Fourier transform of the scattering potential and thus the scattering amplitude can be seen as reciprocal space representation of the real space structure.





**Figure 2.8:** Separation of the crystal structure into convolutions of components, which correspond to products in the reciprocal space. The parts shown the reciprocal lattice (top), structure factor (middle) and atomic form factor (bottom) along a certain direction in reciprocal space.

general understanding of the diffraction profile from single crystals the structure can mathematically be described as a convolution of the atomic scattering potential in a basis defining the atom positions and an (almost) infinite lattice.

$$\mathfrak{F}(A \circledast B) = \mathfrak{F}(A) \cdot \mathfrak{F}(B) \quad (2.12)$$

The convolution theorem equation 2.12 can be used to derive the Fourier transform, as each element can be separately transformed and the results only need to be multiplied afterwards [2]. The corresponding transformation terms in equation 2.13 are called Atomic Form Factor, Structure Factor and Reciprocal Lattice (from an infinite crystal) and are illustrated in **figure 2.8**.

$$A(\vec{Q}) \sim \underbrace{\sum_j}_{\text{Atomic Form Factor}} \underbrace{f_j(\vec{Q})}_{\text{Unit Cell Structure Factor}} \underbrace{e^{i\vec{Q}\vec{R}_j}}_{\text{Reciprocal Lattice}} \cdot \sum_{h,k,l} \delta(\vec{Q} - (h\vec{a}_1^* + k\vec{a}_2^* + l\vec{a}_3^*)) \quad (2.13)$$

$$\text{with} \quad \vec{a}_i^* = 2\pi \frac{\vec{a}_{(i+1) \bmod 3} \times \vec{a}_{(i+2) \bmod 3}}{\vec{a}_1 \cdot (\vec{a}_2 \times \vec{a}_3)} \quad (2.14)$$

Accordingly the diffraction profile consists of delta functions, which are scaled by the structure factor. For finite size crystals the sum of delta functions can be replaced by the Laue function, given in equation 2.15 of the subsequent section. The position of the peaks are defined by the lattice parameters and the intensities can be derived from the atom type and position in the unit cell.

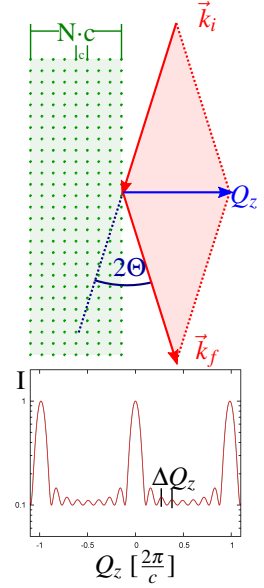
In real experiments there are several aspects which need to be taken into account to derive the real peak shape. Even for perfect crystals a minimal peak width is present due to the instrumental resolution. The finite coherence of the used radiation limits the maximal crystal size in the coherent scattering volume, which additionally broadens the reflections (This can be understood by considering the scattering potential spatially limited to the coherence volume, which is a product of the infinite crystal with a limiting function, leading to a scattering amplitude which is a convolution of equation 2.13 with the Fourier transform of the limiting function and thus each peak is no more a delta function.). For x-ray radiation the exponential

decay of the beam amplitude inside the sample due to absorption leads to Lorentz shaped peaks in  $\vec{Q}$  (Here the same argument as for the limited coherence volume applies, leading to a Lorentzian peak shape as absolute square of the Fourier transform of the heavy side exponential decay.). Real crystals always have imperfections leading to misaligned lattice planes (mosaic), which can be measured when scanning perpendicular to  $\vec{Q}$  (rocking scan). The mosaicity for very good single crystals lies in the order  $\lesssim 0.01^\circ$ .

## Diffraction from thin films and superlattices

There is no principal difference in the physics for crystalline layers with respect to the basic scattering theory. The scattering amplitude can be calculated as Fourier transform of the potential. The in-plane direction of deposited epitaxial films consists of a coherent structure on a very large length scale and can thus be treated as single crystal. For the out-of-plane scattering direction one needs to account for the finite thickness of the layers, as in most cases the coherence length is much larger than the film thickness<sup>20</sup>. In contrast to reflectometry (section 2.4.3), diffraction allows access to the crystal parameters and the size of the coherent lattice in thin films as well as the periodicity of multi-layer structures.

$$\begin{aligned}
 I(Q_z) &\sim \left| \mathfrak{F} \left( \sum_k \rho_{Atom}(z - k \cdot c) \right) \right|^2 = \left| \sum_{j,k} f_j(Q) e^{iQ_z R_{jz}} \cdot e^{iQ_z(k \cdot c)} \right|^2 \\
 &= N^2 \cdot \frac{\sin^2 \left( \frac{1}{2} N Q_z c \right)}{\sin^2 \left( \frac{1}{2} Q_z c \right)} \left| \sum_j f_j(Q) e^{iQ_z R_{jz}} \right|^2 \quad (2.15)
 \end{aligned}$$

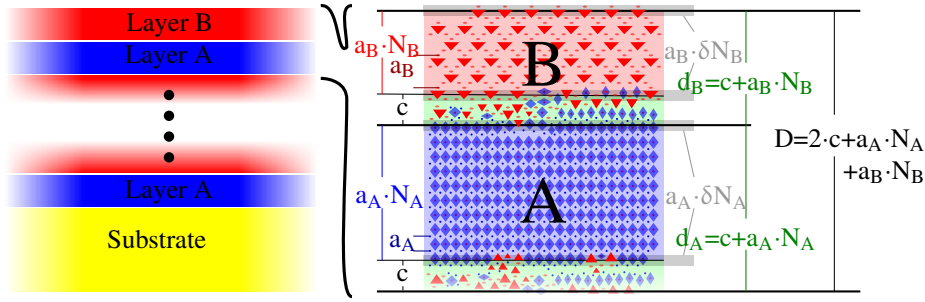


**Figure 2.9:** Scattering from a single layer

The main challenge when simulating the measured intensity, is to develop a suitable structural model for the sample. Perfect single layers can be described as finite size crystals, where the discrete Fourier transform can be analytically deduced from a geometric series (equation 2.15). As can be seen, there are large maxima at  $Q_z = n \cdot \frac{2\pi}{c}$  corresponding to the crystal lattice plane spacing with additional side maxima with the distance  $\Delta Q_z = \frac{2\pi}{N \cdot c}$  corresponding to the film thickness  $N \cdot c$  (see figure 2.9). As will be seen in section 5.1.4, this simple model gives a good qualitative agreement, but is not sufficient to produce a good fit to the intensity oscillations at the flanks. Deviations from the perfect crystal structure, such as strain relaxation, can be accounted for by numerically calculating the discrete Fourier transform for all diffraction planes.

Coherent multilayers lead to sharp features in the diffraction pattern corresponding to the multilayer periodicity. To calculate these diffraction patterns not only the crystal structure of each layer has to be taken into account, but e.g. layer thickness deviations and regions

<sup>20</sup>Films thicker than  $\approx 100$  nm can be treated as single crystals, as described in section 2.4.2, because the oscillations on the flanks of the peak can't be resolved any more.



**Figure 2.10:** Sketch of the layer model used to describe multilayer diffraction. The important parameters include the bilayer repetitions  $M$ , out-of-plane crystal unit cell parameters  $a_{A/B}$ , number of unit cells  $N_{A/B}$  and the thickness of the region without defined crystal structure  $c$ .

without defined crystal structure. Fullerton et al. have deduced a general formalism to simulate multilayers only from average parameters for each component [43]:

$$\begin{aligned}
 I(\vec{Q}) = & M \left( \langle F_A F_A^* \rangle + 2\Re \left( e^{\xi} \Phi_A \bar{F}_B \right) + \langle F_B F_B^* \rangle \right) \\
 & + 2\Re \left\{ \left( e^{-\xi} \Phi_B \bar{F}_A T_A^{-1} T_B^{-1} + \Phi_A \bar{F}_A T_A^{-1} + \Phi_B \bar{F}_B T_B^{-1} + e^{\xi} \Phi_A \bar{F}_B \right) \right. \\
 & \cdot \left. \left( \frac{M - (M+1)e^{2\xi} T_A T_B + (e^{2\xi} T_A T_B)^{M+1}}{(1 - e^{2\xi} T_A T_B)^2} - M \right) \right\} \quad (2.16)
 \end{aligned}$$

The general formalism was implemented for a  $M$  times repeated bilayer model as depicted in **figure 2.10** and can be found in **section B.1**. A model with thickness variations of integer numbers of unit cells was taken for the layers, which leads to the following parameters to be used in equation 2.16 (with  $X = A, B$  and  $Xj = Aj, Bj$  respectively, further parameter description in **chapter G**):

$$F_{Xj} = f_X \frac{1 - e^{iqN_{Xj}a_X}}{1 - e^{iqa_X}} \quad P(N_{Xj}) = e^{\frac{(N_{Xj} - N_X)^2}{-2\sigma_X^2}} \cdot (\sum P)^{-1} \quad (2.17)$$

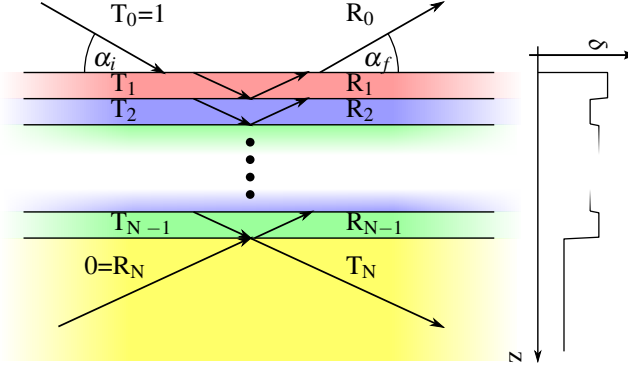
$$\bar{F}_X = \sum_j P(N_{Xj}) F_{Xj} \quad \Phi_X = \sum_j P(N_{Xj}) e^{(N_{Xj}-1)iq a_X} F_{Xj}^* \quad (2.18)$$

$$\langle F_X F_X^* \rangle = \sum_j P(N_{Xj}) F_{Xj} F_{Xj}^* \quad T_X = \sum_j P(N_{Xj}) F_{Xj} e^{(N_{Xj}-1)iq a_X} \quad (2.19)$$

### 2.4.3 Small incident angles - reflectometry

Reflectometry measures the scattered intensity under a small incident angle (in most cases with  $\theta \leq 2^\circ$ ) in the so called specular geometry, where both angles to the sample surface ( $\alpha_i$  as incident and  $\alpha_f$  as outgoing angle) are equal. In contrast to diffraction experiments described in **section 2.4.2**, the Born approximation does not hold for measurements with very small incident angles<sup>21</sup>. There is no sensitivity for the atomic structure in this  $\vec{Q}$  region anymore

<sup>21</sup>Or large wave length compared with the structural periodicity.



**Figure 2.11:** Sketch of the layer model used to describe the reflectivity. The right side illustrates the scattering power.

(as small structural features are measured at larger  $\vec{Q}$  in reciprocal space), which makes it possible to use a continuum description for the scattering potential. For the case of reflectivity of a layered system, the wave equation can be solved using an optical approach. As  $\vec{Q}$  is only measured in the out-of-plane direction when incident and scattered angle are equal, the wave equation 2.9 has to be solved for the one dimensional potential  $V(z)$ . As well known from quantum mechanics, a wave traveling across a step in the potential is partly reflected and transmitted according to the Fresnel coefficients (reflection  $r_{j,j+1}$  and transmission  $t_{j,j+1}$  coefficients for the interfaces between layer  $j$  and  $j+1$ ):

$$r_{j,j+1} = \frac{k_{z,j} - k_{z,j+1}}{k_{z,j} + k_{z,j+1}} \quad \text{with } k_{z,j} = k_0 \sqrt{n_j^2 - \cos^2(\alpha_i)} \quad (2.20)$$

$$t_{j,j+1} = \frac{2\sqrt{k_{z,j}k_{z,j+1}}}{k_{z,j} + k_{z,j+1}} \quad \text{and } n_j = 1 - \delta + i\beta \quad (2.21)$$

The values of the scattering power density  $\delta$  and absorption  $\beta$  governing the refractive index  $n$ , derived from the scattering potential, depend on the elements and their density in the material as well as the used radiation.

For more than one step in the potential (interfaces in a layered system) the interference between incoming and outgoing waves needs to be taken into account, leading to a system of coupled equations with boundary conditions at each interface. To solve this system of equations for any layered structure as shown in **figure 2.11**, Parratt introduced an iterative method [92], which uses the quotient of reflection and transmission inside each layer:

$$X_j = \frac{R_j}{T_j} = e^{-2ik_{z,j}z_j} \frac{r_{j,j+1} + X_{j+1}e^{2ik_{z,j+1}z_j}}{1 + r_{j,j+1}X_{j+1}e^{2ik_{z,j+1}z_j}} \quad (2.22)$$

Starting from the substrate where  $X_N = R_N = 0$ , the quotient can be calculated up to  $X_0 = R_0$  as  $T_0 = 1$ . The effect of rough interfaces and inter-diffusion can be accounted for by introducing a Gaussian refraction coefficient profile, which leads to Fresnel coefficients modified by a Debye-Waller type term [35]:

$$r_{j,j+1}(\sigma) = r_{j,j+1}(0)e^{-2\sigma_j^2 k_{z,j}k_{z,j+1}} \quad (2.23)$$

## 2.4.4 Neutron scattering

### Interaction of neutrons with matter

Neutrons can interact with the samples' nuclei via the strong interaction. It's range is much shorter than the wavelength of thermal neutrons ( $10^{-10}$  m compared to  $10^{-15}$  m). Therefore the scattering potential can be described by the Fermi pseudo potential, which only depends on the strength of the interaction (scattering length  $b$ ) determined by the inner structure of the nucleus:

$$V_{Fermi}(\vec{R}) = \frac{2\pi\hbar^2}{m} b \delta(\vec{r} - \vec{R}) \quad (2.24)$$

Because of the delta function in  $V_{Fermi}$ , the atomic form factor ( $\mathfrak{F}(V_{Fermi})$ ) for nuclear scattering is a constant (figuratively the scattering center is a point without "form"). Due to the neutron magnetic moment  $\vec{\mu}_n$  there is an additional magnetic dipole interaction of neutrons with the magnetic moment of electrons<sup>22</sup>. Using the Zeeman interaction potential  $V_{mag}$  of a dipole in an external magnetic field (equation 2.25), the magnetic scattering cross section in dependence of the magnetization component perpendicular to  $\vec{Q}$  can be derived (equation 2.26).

$$V_{Mag} = -\vec{\mu}_n \cdot \vec{B} \quad \vec{\mu}_n = -\gamma_n \mu_n \cdot \vec{\sigma} \quad (2.25)$$

$$\stackrel{[6, 10, 26, 53]}{\implies} \frac{d\sigma}{d\Omega} = (\gamma_n r_e)^2 \left| -\frac{1}{2\mu_B} \left\langle \sigma_z' \left| \vec{\sigma} \cdot \vec{M}_\perp(\vec{Q}) \right| \sigma_z \right\rangle \right|^2 \quad \vec{M}_\perp = \hat{Q} \times \vec{M} \times \hat{Q} \quad (2.26)$$

$$\stackrel{\text{spin-only scattering}}{\implies} \vec{M}(\vec{Q}) = -2\mu_B \cdot f_m(\vec{Q}) \cdot \sum_j e^{i\vec{Q}\vec{R}} \cdot \vec{S}_j \quad f_m = \int_{Atom} \rho_s(\vec{R}) e^{i\vec{Q}\vec{R}} d^3R \quad (2.27)$$

This includes the first important selection rule for magnetic neutron scattering, which states that only those components of the magnetic moment in the plane perpendicular to the scattering vector can be measured. The restriction to ions as only carrier of a magnetic moment allows one to determine the quantum mechanical state, averaged over the thermodynamic ensemble (equation 2.27) and to introduce the magnetic form factor  $f_m(\vec{Q})$  [2].

**Polarization and magnetic scattering** If not only the intensity of scattered neutrons is measured, but their polarization  $\vec{P}_n$  (average direction of the neutron spin) as well, the cross section needs to be calculated including the spin-state change of the neutron. The vector character of the neutron magnetic moment allows the determination of the magnetization direction and can be used to identify different types of magnetic order. The general treatment of polarized neutron scattering by magnetic materials was derived by Blume and Maleev [26, 79] and incorporates the second important selection rule that magnetic moments  $\vec{M}_\perp \perp \vec{P}_n$  change the polarization to the anti-parallel direction, so called spin-flip, while  $\vec{M}_\perp \parallel \vec{P}_n$  keep the polarization direction. For scattering from single crystal samples, where  $N = N(\vec{Q})$  denotes the nuclear scattering contribution,  $\vec{M} = \vec{M}(\vec{Q})$  the magnetization and  $\vec{P}_n$  the polarization vector,

<sup>22</sup>The magnetic moment of the nuclei is not considered, as the magnetic moment of a nucleus is extremely weak compared to the one of an electron due to it's larger mass.

one derives [26, 79, 108] (the spin- incoherent scattering intensity  $I_{spin-incoherent}$  is a constant background for some elements, which is the result of different scattering lengths for scattering of the neutrons with spin parallel and anti-parallel to the nuclear spin):

$$I = N^\dagger N + I_{spin-incoherent} + \vec{M}_\perp^\dagger \vec{M}_\perp + \vec{P}_n \cdot \vec{M}_\perp^\dagger N + \vec{P}_n \cdot \vec{M}_\perp N^\dagger + i\vec{P}_n(\vec{M}_\perp^\dagger \times \vec{M}_\perp) \quad (2.28)$$

$$\begin{aligned} \vec{P}_n' I = \vec{P}_n(N^\dagger N - \frac{1}{3}I_{spin-incoherent}) + (\vec{P}_n \cdot \vec{M}_\perp^\dagger) \vec{M}_\perp + (\vec{P}_n \cdot \vec{M}_\perp) \vec{M}_\perp^\dagger - \vec{P}_n(\vec{M}_\perp^\dagger \vec{M}_\perp) \\ + iN(\vec{P}_n \times \vec{M}_\perp^\dagger) - iN^\dagger(\vec{P}_n \times \vec{M}_\perp) + N\vec{M}_\perp^\dagger + N^\dagger \vec{M}_\perp - i(\vec{M}_\perp^\dagger \times \vec{M}_\perp) \end{aligned} \quad (2.29)$$

## 2.4.5 X-ray scattering

### Interaction of photons with matter

When an electromagnetic wave interacts with electrons due to the Coulomb force, the electron is accelerated in the electrical field of the radiation. The oscillating electron itself is a new source for radiation. The scattering cross-section for x-rays from a free electron is called Thomson scattering cross-section

$$\frac{d\sigma}{d\Omega_{Thomson}} = r_e^2 (\hat{e}_i \cdot \hat{e}_f)^2 \quad (2.30)$$

with the *classical electron radius*  $r_e = \frac{e^2}{m_e c^2}$  and the electric polarization vectors of the incoming and outgoing wave  $\hat{e}_{i/f}$ , which are always perpendicular to the wave vectors  $\vec{k}_{i/f}$ . For the two linear polarizations  $\sigma$  and  $\pi$  or circular polarizations right (+) and left (-) the vectors are defined as the following:

$$\begin{aligned} \hat{e}_{i/f} = \underline{SP}_{i/f} \cdot \hat{e}_{\sigma/\pi/+/-} \quad \underline{SP}_{i/f} = (\hat{e}_S, \hat{e}_{P,i/j})^T \quad \hat{e}_S = \widehat{k_i \times k_f} \quad \hat{e}_{P,i/j} = \hat{k}_{i/f} \times \hat{e}_S \\ \hat{e}_\sigma = \begin{pmatrix} 1 \\ 0 \end{pmatrix} \quad \hat{e}_\pi = \begin{pmatrix} 0 \\ 1 \end{pmatrix} \quad \hat{e}_+ = \frac{1}{\sqrt{2}} \begin{pmatrix} 1 \\ i \end{pmatrix} \quad \hat{e}_- = \frac{1}{\sqrt{2}} \begin{pmatrix} 1 \\ -i \end{pmatrix} \end{aligned}$$

For the electrons bound at an atom and high photon energies compared to the binding energy, the atomic form factor can be written as:

$$f_0(\vec{Q}) = \frac{r_e}{e} \int_V \rho_e(\vec{r}) e^{i\vec{Q} \cdot \vec{r}} d\vec{r} \quad (2.31)$$

The form factor thus is proportional to the Fourier transform of the charge density  $\rho_e$  of the atom. For small scattering vectors the integral in equation 2.31 is proportional to the charge number  $Z$ . As result, the contrast in x-ray reflectometry is only determined by the atom density and the elements in the system [9].

The electron density distribution is generally a quite complex function, as it consists of the spatial wave functions of all occupied orbitals. The form factors used to model intensities are tabulated values or empirical approximations of these values, as e.g. the expansion given in [4]:

$$f_0(\vec{Q}) \approx \sum_{j=1}^4 a_j e^{-b_j(2\pi\vec{Q})^2} + c \quad (2.32)$$

Obviously the form factor drops for larger  $\vec{Q}$ , which means that for diffraction experiments with x-rays the intensity of the observed reflections will drop with  $\vec{Q}$  in contrast to neutron experiments<sup>23</sup>. When used in kinematic models the absorption can be introduced as an imaginary part of  $f$ . For linear polarized photons the polarization term in equation 2.30 leads to an additional factor of  $\cos^2(2\Theta)$  for the intensity of the polarization in the scattering plane<sup>24</sup>.

Another major difference to neutrons is the large absorption  $\mu$  of x-rays penetrating a solid on the path  $\vec{x}$ , which defines the attenuation of the radiation  $I = I_0 e^{-\mu|\vec{x}|}$ . The absorption coefficient is related to the absorption cross-section  $\sigma_{abs}$  via

$$\mu = \rho_{atom} \sigma_{abs} = \rho_{atom} 2r_0 \lambda f_2(E) \quad (2.33)$$

and ranges from  $\lesssim 100$  nm for soft x-ray radiation to some  $\mu$ m for conventional copper x-ray tubes.

## Resonance effects

For photon energies close to the binding energy of the electrons the classical treatment used for the Thomson-scattering no longer yields good results and a quantum mechanical treatment is needed. The interaction Hamiltonian for the radiation field with the electron can be written as

$$\mathcal{H}_{int} = -\frac{i\hbar e}{m} \vec{A} \cdot \vec{\nabla} + \frac{e^2}{2m} \vec{A}^2 \quad (2.34)$$

if the spin is neglected. The probability of transition<sup>25</sup> from initial to final state<sup>26</sup> ( $|i\rangle \mapsto |f\rangle$ ) with a possible intermediate state  $n$  with the lifetime  $\tau_n$ ) can be calculated via Fermi's Golden Rule using 2<sup>nd</sup>-order time-dependent perturbation theory and the vector potential  $\vec{A}$  described with creation ( $a_{\vec{k},u}^\dagger$ ) and annihilation ( $a_{\vec{k},u}$ ) operators for the polarization state  $u$  and wave vector  $\vec{k}$  [1, 8, 11]:

$$W = \frac{2\pi}{\hbar} \left| \langle f | \mathcal{H}_{int} | i \rangle + \sum_n \frac{\langle f | \mathcal{H}_{int} | n \rangle \langle n | \mathcal{H}_{int} | i \rangle}{E_n - E_i \pm \hbar\omega + i\frac{\tau_n}{\hbar}} \right|^2 \rho_{DOS}(\epsilon_f) \quad (2.35)$$

$$\vec{A}(\vec{r}, t) = \sum_{\vec{k}, u} \hat{e}_u \sqrt{\frac{\hbar}{2\epsilon_0 V \omega_k}} \left( a_{\vec{k}, u} e^{i(\vec{k}\vec{r} - \omega t)} + a_{\vec{k}, u}^\dagger e^{-i(\vec{k}\vec{r} - \omega t)} \right) \quad (2.36)$$

$\rho_{DOS}$  denotes the density of states. Combining equation 2.35, 2.36 and 2.34 describes four major effects:

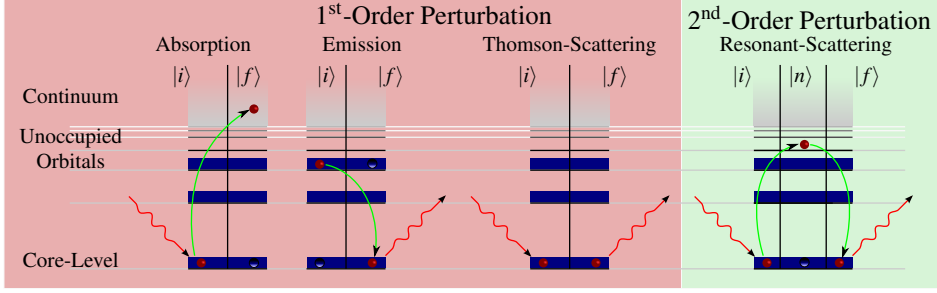
**Absorption/Stimulated Emission** results from the  $\vec{A} \cdot \vec{\nabla}$ -term in the first part of equation 2.35. As it is linear in the creation and annihilation operators, the transition from one state to a higher one can destroy a photon (absorption), while transitions from an excited state to a lower level (assumed there is an empty state) creates a photon (emission).

<sup>23</sup>Neglecting the Debye-Waller factor, which is no property of the radiation.

<sup>24</sup> $\pi$ -polarization in contrast to  $\sigma$ -polarization perpendicular to the scattering plane.

<sup>25</sup>Corresponding to the scattering and absorption cross section.

<sup>26</sup>The combined photon + electron states.



**Figure 2.12:** Interaction processes between photons and atoms in first and second order perturbation theory. The intermediate states  $j$  are only virtual excitations.

**Thomson-Scattering** the  $\vec{A}^2$  part can destroy and create a photon, as it is quadratic in  $\vec{A}$ , but cannot change the state of the electron and thus corresponds to the simple charge scattering described above.

**Resonant-Scattering** can occur when the photon energy  $\hbar\omega$  is close to the excitation energy of the intermediate state  $E_n - E_i$ , as the denominator in the second term of equation 2.35 approaches zero. Here also the  $\vec{A} \cdot \vec{\nabla}$  part can destroy and create a photon.

The form factor including these effects (anomalous atomic scattering factor ASF) can be written as

$$f(E, \vec{Q}) = f_0(\vec{Q}) + f_1(E) + if_2(E) \quad (2.37)$$

including the already introduced form factor  $|f_0|^2 = \frac{2\pi}{\hbar} \left| \langle f | \frac{e^2}{2m} \frac{\hbar}{2\varepsilon_0 V \omega} \hat{e}_i \hat{e}_f a a^\dagger | i \rangle \right|^2 \rho_{DOS}(\varepsilon_f) = 4r_e^2 |\hat{e}_i \hat{e}_f|^2 \rho_e$  and absorption coefficient  $f_2$  from equation 2.33. The resonant scattering part  $f_1$  is connected with the absorption through the Kramers-Kronig relations [74]:

$$f_1(E) = \frac{1}{\pi} \mathcal{P} \int_{-\infty}^{+\infty} \frac{E' f_2(E')}{E'^2 - E^2} dE' \quad (2.38)$$

$$f_2(E) = \frac{2E}{\pi} \mathcal{P} \int_0^\infty \frac{E' f_1(E')}{E'^2 - E^2} dE' \quad (2.39)$$

**Absorption and x-ray magnetic circular dichroism** We will now take a closer look at the absorption factor  $f_2$  and its relation to the electronic states of the atom. For this one needs to consider the first term in equation 2.35 with the annihilation part of the vector potential equation 2.36. As the electron wave function of the initial state (core electrons) is confined at the atom, the exponential part can be approximated by the linear terms of its Taylor series, which includes a dipole approximation<sup>27</sup>. One derives the transition rates:

$$W_{abs} = \frac{4\pi^2}{3c\hbar^2} \frac{e^2}{4\pi\varepsilon_0} I_0 |\langle f | \vec{r} | i \rangle|^2 \quad (2.40)$$

<sup>27</sup>The Tailor series  $e^{i(\vec{k}\vec{r})} = 1 + i\vec{k} \cdot \vec{r} + \dots$  for  $\vec{k} \cdot \vec{r} \ll 1$  can be truncated after the linear term. As for the relation  $\langle f | \vec{p} | i \rangle = i\frac{m}{\hbar} \omega_k \langle f | \vec{r} | i \rangle$  equation 2.35 and equation 2.36 can be written in terms of  $\langle f | -e\vec{r} | i \rangle$ , which constitutes the electric dipole approximation [8].



As can be shown [8], the matrix elements can be replaced by the 3j-symbols of the angular momentum quantum numbers of the initial and final state (with the Wigner-Eckard theorem)

$$\langle j_f m_f | \vec{r}_{e_h} | j_i m_i \rangle = (-1)^{j_f - m_f} \begin{pmatrix} j_f & 1 & j_i \\ -m_f & e_h & m_i \end{pmatrix} \langle j_f || \vec{r} || j_i \rangle \quad (2.41)$$

leading to selection rules for dipole transitions:

$$\begin{aligned} \Delta l &= \pm 1 & \Delta s &= 0 \\ \Delta j &= 0, \pm 1 & \Delta m &= e_h \end{aligned}$$

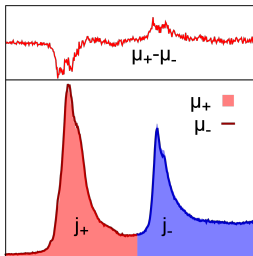
Here  $e_h$  denotes the helicity of the used light<sup>28</sup>. The spin does not change during the transition, as it doesn't appear in the Hamiltonian.

If circular polarized light is absorbed in a sample with an orbital magnetic moment  $\vec{M}_{orb}$  one derives for the projection of the total angular momentum:

$$m_f = \vec{j}_f \cdot \hat{M}_{orb} = m_i + \sigma(\hat{e}_h \cdot \hat{M}_{orb}) \quad (2.42)$$

The change is maximized for a magnetization axis pointing in the direction of the incident beam (which is the situation given in the selection rules above). As a result the absorption of left (+) and right (-) circular polarized light at an energy corresponding to the transition to a final state with finite angular magnetic moment is different. In the extreme case this so called x-ray magnetic circular dichroism (XMCD equation 2.43) for a transition, which has only empty  $\Delta m = +1$  orbitals can become unity.

$$XMCD = \frac{\mu_+ - \mu_-}{\mu_+ + \mu_-} \quad (2.43)$$



Although the electron spin is not involved in the transition, the spin polarization of corresponding excited states changes the absorption probability, if the excited electron gets spin-polarized through spin-orbit coupling, leading to a spin dependent XMCD signal. Thus experiments measuring the absorption signal for  $j_+$  and  $j_-$  ground states (like the one shown on the right measured at the Co  $L_{III}$  and  $L_{II}$  edges) can be used to determine the orbital and spin moment of a sample. The treatment of the theoretical foundation leads to the so called XMCD sum rules [29, 120, 121]:

<sup>28</sup>For linear polarization the helicity is 0.

$$C_L \langle L_z \rangle = \frac{\int_{j_+ + j_-} d\omega(\mu_+ - \mu_-)}{I_{ges}} \quad (2.44)$$

$$C_S \langle S_z \rangle + C_T \langle T_z \rangle = \frac{\int_{j_+} d\omega(\mu_+ - \mu_-) - C_j \int_{j_-} d\omega(\mu_+ - \mu_-)}{I_{ges}} \quad (2.45)$$

$$I_{ges} = \frac{1}{n_h} \int_{j_+ + j_-} d\omega(\mu_+ + \mu_-) \quad (2.46)$$

$$C_L = \frac{1}{2} \frac{l(l+1) + 2 - c(c+1)}{l(l+1)(4l+2-n)} \quad (2.47)$$

$$C_S = \frac{l(l+1) - 2 - c(c+1)}{3c(4l+2-n)} \quad (2.48)$$

$$C_T = \frac{l(l+1)[l(l+1) + 2c(c+1) + 4] - 3(c-1)^2(c+2)^2}{6lc(l+1)(4l+2-n)} \quad (2.49)$$

$$C_j = \frac{(c+1)}{c} \quad (2.50)$$

where the four constants  $C_x$  only depend on the orbital quantum numbers of the states involved [29]. The scaling factor  $I_{ges}$  depends on the number of holes in the valence state  $n_h = 4l + 2 - n$ . The expectation value of the orbital moment  $\langle L_z \rangle$  is, as expected, extracted from the XMCD signal of both transitions. On the other hand the weighted difference between the signals of both transitions can be used to derive the expectation values for the spin moment  $\langle S_z \rangle$  and the magnetic dipole operator  $\langle T_z \rangle$ .

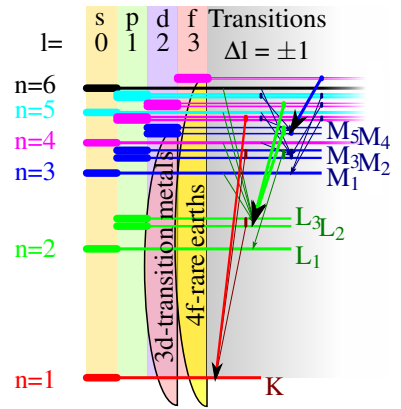
### M-edge and L-edge absorption of transition metals and rare earth ions

For the specific cases of 3d transition metals and 4f rare earths the sum rules can specifically be derived to make it possible to calculate orbital and spin moments from an experiment. For the first group the L-edge absorption is used as the transition  $2p \rightarrow 3d$  comprises the magnetic 3d levels. For most cases, where the environment is cubic (e.g. octahedral coordination), the  $\langle T_z \rangle$  term can be neglected, leading to simple sum rules [8, 29]:

$$\langle L_z \rangle = 2 \int_{L_{II} + L_{III}} d\omega(\mu_+ - \mu_-) / I_{ges} \quad (2.51)$$

$$\langle S_z \rangle = \frac{\frac{3}{2} \int_{L_{III}} d\omega(\mu_+ - \mu_-) - 3 \int_{L_{II}} d\omega(\mu_+ - \mu_-)}{I_{ges}} \quad (2.52)$$

Although the assumptions taken to derive these equations can lead to moderate deviations of the true expectation values (about 5-10% was found experimentally), they constitute a very



**Figure 2.13:** Atomic energy levels and possible dipole transitions. The important transitions for magnetic x-ray experiments are drawn bold.

powerful tool to derive both quantities from an experiment without further theoretical treatment and knowledge of the specific compound. If the scaling factor  $I_{ges}$  can't be estimated precisely, the sum rules can still be used to determine the ratio of orbital to spin moment.

For the rare earth ions the M-edge transition  $3d \rightarrow 4f$  directly probes the magnetic  $4f$  orbitals. Here the dipole operator is not zero, but as the configuration follows Hund's rules, one can analytically derive both terms for a specific element together with the sum rules [29, 127]:

$$\langle T_z \rangle = \langle M \rangle (l - n + 1/2) \frac{3(S-J)^2(S+J+1)^2 - L(L+1)[L(L+1) + 2S(S+1)2J(J+1)]}{2(2l+3)(2l-1)(2L-1)SJ(J+1)} \quad (2.53)$$

$$\langle S_z \rangle = \langle M \rangle \frac{J(J+1) + S(S+1) - L(L+1)}{2J(J+1)} \quad (2.54)$$

$$\langle L_z \rangle = 3 \int_{M_{IV}+M_V} d\omega(\mu_+ - \mu_-) \Big/ I_{ges} \quad (2.55)$$

$$\frac{2}{3} \langle S_z \rangle + \frac{309}{144} \langle T_z \rangle = \left( \int_{M_V} d\omega(\mu_+ - \mu_-) - \frac{3}{2} \int_{M_{IV}} d\omega(\mu_+ - \mu_-) \right) \Big/ I_{ges} \quad (2.56)$$

## Resonant (magnetic) scattering

As already touched in the beginning of the discussion the second part of equation 2.35 gives rise to an additional scattering contribution at the excitation energy of an element. The coupling of the real part  $f_1$  from the anomalous scattering cross section to the imaginary absorption part  $f_2$  via the Kramers-Kronig relations gives rise to the anomalous charge scattering and can be derived as shown for the absorption. This effect can be used to enhance element specific features (namely charge and orbital order) which could not be measured otherwise because of the very small contrast of the corresponding atoms.

The interaction of photons with the magnetic moment can be incorporated only with a relativistic treatment. To extract the contribution of magnetic scattering qualitatively it is possible to only use relativistic corrections within the already introduced quantum mechanical treatment. In this framework the form factor can be derived as [27]:

$$f_0(\vec{Q}) = \left| f_0^{charge} - i \frac{\hbar\omega}{mc^2} f_0^{magnetic} \right|^2 \quad (2.57)$$

$$\text{with } f_0^{magnetic} = 2r_e \left\langle f \left| e^{i\vec{Q}\vec{r}} \left( i \frac{(\vec{Q} \times \hat{p})}{\hbar k^2} \cdot \vec{e}_O + \frac{\hat{S} \cdot \vec{e}_S}{\hbar} \right) \right| i \right\rangle \rho_{DOS}(\epsilon_f) \quad (2.58)$$

$$\vec{e}_O = \hat{e}_i \times \hat{e}_f \quad \vec{e}_S = \hat{e}_i \times \hat{e}_f - (\hat{k}_f \times \hat{e}_i) \times (\hat{k}_i \times \hat{e}_f) - (\hat{k}_f \cdot \hat{e}_i) \cdot (\hat{k}_i \times \hat{e}_f) + (\hat{k}_f \times \hat{e}_i)(\hat{k}_i \cdot \hat{e}_f)$$

As for the XMCD there are separate contributions from the orbital and spin magnetic moments. The intensity ratio of the magnetic to charge scattering can be estimated as the contributions mainly differ by the factor  $\frac{\hbar\omega}{mc^2}$  and the density of the scatterers, which is the ratio

between unpaired electrons and the full charge of the atom. Overall, for a typical magnetic material probed with x-ray radiation, this gives a ratio of

$$\frac{\sigma_{\text{magnetic}}}{\sigma_{\text{charge}}} \approx 4 \cdot 10^{-6} \frac{M}{M_{\text{saturation}}}. \quad (2.59)$$

A much larger effect can be observed near a resonance, enhancing the magnetic scattering by several orders of magnitude using so called exchange scattering [54, 60]. Deriving the anomalous scattering contribution yields:

$$\begin{aligned} f_1^{\text{magnetic}} = & \frac{3}{4} r_e \{ (\hat{e}_i \cdot \hat{e}_f) [F_1^1 + F_{-1}^1] \\ & - i(\hat{e}_i \times \hat{e}_f) \cdot \hat{M} [F_1^1 - F_{-1}^1] \\ & + (\hat{e}_i \cdot \hat{M})(\hat{e}_f \cdot \hat{M}) [2F_0^1 - F_1^1 - F_{-1}^1] \} \end{aligned} \quad (2.60)$$

$$F_{\Delta m}^{\Delta l} = \sum_n \frac{|\langle 0 | D | n \rangle|^2}{E_n - E_0 - \hbar\omega - i\Gamma_n/2} \quad (2.61)$$

with the resonator strengths  $F_{\Delta m}^{\Delta l}$ , which describes the transition probability. The first term is independent of the magnetization and describes the anomalous charge scattering. The second term depends on the direction of the magnetization and contains the matrix elements responsible for the XMCD effect. The polarization dependence shows that it is possible for magnetic scattering to change the polarization direction of the photons. The last term, which is often neglected, depends on  $\hat{M}$  quadratically and provides an additional contribution to the magnetic scattering, which can be measured at a different position in reciprocal space (as squaring the magnetic moment for antiferromagnetic structures doubles the periodicity). The resonant exchange scattering (or x-ray resonant magnetic scattering XRMS) can be used to gather element specific information about (antiferro)magnetic order, as the resonant enhancement can lead to intensities comparable to off-resonant charge scattering ([46, 60, 132]) and is element specific (e.g. [77, 78, 115, 130]).



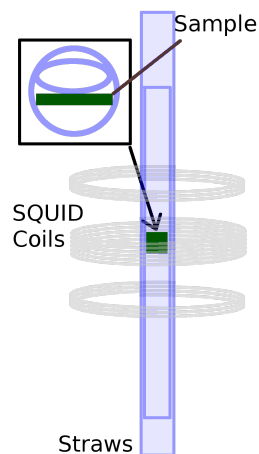
# Chapter 3

## Experimental Methods and Instruments

This chapter describes the methods and instruments used to investigate the samples as well as the basis of the numeric evaluation used for the experimental data. If not stated otherwise, all experimental data was treated, starting from the raw data, with the `plot.py` software [137], which was developed and expanded for this purpose. As the code is available under open source license and too extensive ( $\approx 40\,000$  lines), it won't be printed as part of this document.

### 3.1 SQUID magnetometry

For the magnetic characterization a Quantum Design MPMS SQUID magnetometer was used. It is equipped with a reciprocating sample orientation (RSO) option and has a resolution limited to  $>10^{-12} \text{ A}\cdot\text{m}^2$ . To produce as low background as possible, the samples were mounted inside a plastic straw and fixed with another straw, both much longer than the distance of the pickup coils (3 cm), leveling out their homogeneous magnetic moment (As shown in **figure 3.1**). For the zero field cooled measurements a flux gate sensor ultra low field option was used to decrease the remaining background field.



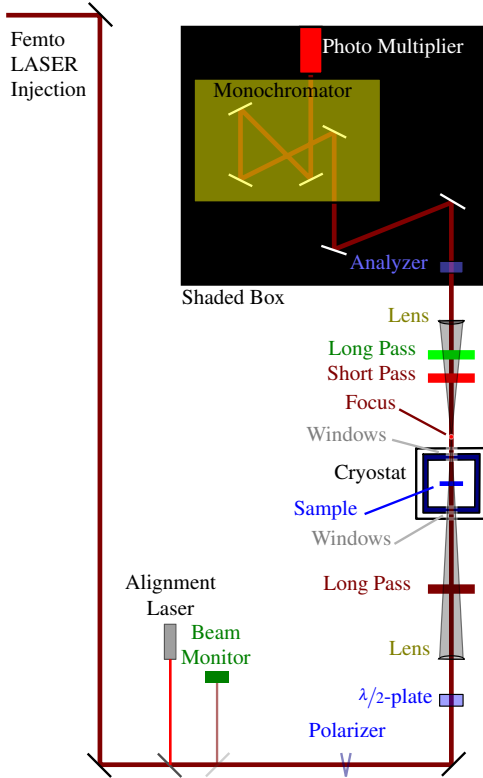
### 3.2 Atomic force microscopy (AFM)

Atomic force microscopy images were taken with an Agilent 5400 scanning probe instrument. The data were taken with a standard AC mode cantilever with  $\approx 4 \text{ nm}$  tip size at  $\approx 250 \text{ kHz}$ . The images were post-processed with the included *PicoView* software using standard corrections<sup>1</sup> to remove piezo non-linearity effects, electronic noise and sample tilt.

<sup>1</sup>Leveling, polynomial form removal, line correction.

### 3.3 Rutherford backscattering spectrometry (RBS)

High energy accelerated  $\text{He}^+$ -ions can be used to probe the depth resolved elemental density by measuring the energy of the backscattered ions. In the Rutherford backscattering spectrometry (RBS) instrument of the Peter Grünberg Institute a Tandetron tandem accelerator is used to produce a 1.4 MeV ion flow [136]. When the ions get backscattered by atoms in the sample, the energy after collision only depends on the mass of the scattering nuclei and can easily be calculated from energy and momentum conservation equation 3.1. Ions penetrating deeper into the sample lose energy gradually because of the Coulomb interaction, which is generally very complicated to calculate. Therefore one uses an empirical model with an energy loss depending on the atom density of the material (equation 3.2). The energy spectrum of the backscattered particles can thus be modeled from the depth resolved atom density. Iterative fit of the model can yield the film thicknesses and elemental content for film thicknesses of several tenths of nm. When a single crystalline sample is aligned with a high symmetry axis directly parallel to the incident beam, all nuclei lie inside of shadow cones of the first few atom layers and other trajectories can penetrate the sample much deeper before getting scattered. This so called "Channeling" leads to a much lower backscattering intensity and can be used together with an arbitrary oriented measurement to probe the crystalline quality of the sample.



**Figure 3.2:** Setup used for Second Harmonic Generation

$$E_1 = E_0 \cdot \frac{m_{\text{Atom}} - m_{\text{He}^+}}{m_{\text{Atom}} + m_{\text{He}^+}} \quad (3.1)$$

$$\frac{dE}{dx} = \rho_{\text{Material}} \cdot \sigma_{\text{stop}} \quad (3.2)$$

### 3.4 Second harmonic generation (SHG)

A second harmonic generation experiment has been performed at the group of Prof. M. Fiebig of the Helmholtz Institute for Radiation and Nuclear Physics, Bonn. For very large light fields the linear response model, used to derive the absorption and scattering in section 2.4.5, does no longer hold and additional susceptibility terms need to be considered. This can lead to the generation of higher harmonic waves ( $\omega = n \cdot \omega_0$ ) in the material. For the second harmonic these contributions can be written in terms of the susceptibility tensor  $\chi^{(2)}$  as:

$$E_i(2\omega) = \chi_{ijk}^{(2)} E_j(\omega) E_k(\omega) \quad (3.3)$$

Where  $i, j, k$  denote the direction of the linear polarization. This effect is a very sensitive probe of the symmetry properties in a crystal, as each tensor component can be forbidden, if a specific symmetry is present in the crystal. The selection rules for specific symmetries can be derived from all symmetry operation matrices  $\sigma^{(i)}$  applicable for the system. For a centrosymmetric system ( $\bar{1}$ ) all tensor components have to be zero as  $\chi_{ijk} = \sigma_{ip}^{(1)} \sigma_{jq}^{(1)} \sigma_{kr}^{(1)} \chi_{pqr} = -1 \chi_{ijk}$  [14]. Therefore this method can be used to probe ferroelectricity<sup>2</sup> and magnetism [105], which makes it a valuable probe for complex multiferroic materials (e.g. to investigate coupled domains [41]).

The SHG setup used for the experiment consists of a femto second laser ( $\approx 100$  fs) tunable between 1200 nm and 1450 nm with a 1 kHz repetition rate. The beam is polarized vertically and a  $\lambda/2$ -plate can be used to turn the polarization. After the  $\lambda/2$ -plate a lens focuses the light onto a spot some cm behind the sample (to prevent too much heating of the measured area) and the SHG light is collected with a confocal lens after the sample. The collected signal is analyzed with a turnable polarizer and monochromized to the half incident wavelength before the intensity is measured with a photo multiplier. The sample was mounted between two electric poles inside a cryostat with front and back windows. To get rid of any SHG contamination from the optical system, the beam is filtered with a long pass ( $>1000$  nm) directly before and with a long ( $>500$  nm to filter third harmonics) and short pass ( $<1000$  nm to filter the direct beam and protect the optics) filter directly behind the cryostat.

## 3.5 Scattering and resonant x-ray techniques

Several x-ray and neutron techniques were used to investigate the sample properties. The theoretical foundation to this experiments has been given in **section 2.4.5** and **section 2.4.4**. The following general definitions will be used in the subsequent sections:

**X-ray polarization** The photon polarization of linear polarized x-rays is denoted as  $\sigma$  or  $\pi$  for incident polarization perpendicular or parallel to the scattering plane, respectively. The scattered beam polarization is called  $\sigma'$  and  $\pi'$  accordingly. Circular polarization is marked as  $+$  for right-hand and  $-$  for left-hand polarization.

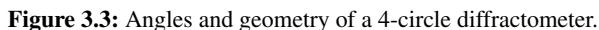
**Neutron polarization** The two neutron spin directions parallel and anti-parallel to the guide field are denoted as  $\uparrow$  and  $\downarrow$ , respectively. As the effect of imperfect polarization is always present, the corrected or theoretic spin-up and spin-down intensities are defined as  $I_+$ ,  $I_-$  in contrast to the measured  $I_\uparrow$  and  $I_\downarrow$ .

**Reciprocal space basis** For most experiments the absorption of the substrate blocks the beam, so that the only possible scattering geometry is in reflection (Bragg-geometry). For this it is convenient to define a common right handed coordinate frame of reciprocal space directions, where one base vector lies in the out-of-plane (surface normal) direction ( $\hat{Q}_z$ ), one base vector perpendicular to the scattering plane ( $\hat{Q}_y$ ) and the last one in beam direction perpendicular to both ( $\hat{Q}_x$ ).

**Real space propagations** are defined accordingly as x, y and z.

<sup>2</sup>As it requires a broken inversion symmetry.

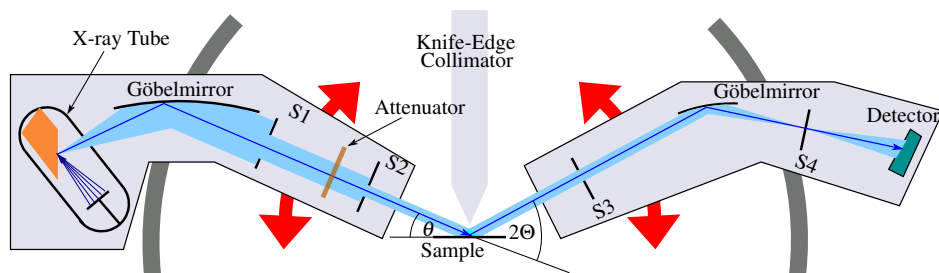




### 3.5.1 X-ray reflectometry (XRR)

### 3.5.2 X-ray diffraction (XRD)

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**Figure 3.4:** Sketch of the Bruker D8 x-ray reflectometer. The sample stage angle is fixed horizontally and the tube and detector can be moved.

using a Huber 4-circle diffractometer with a Copper tube equipped with double Göbel mirror monochromator and xyz-translation stage. The beam size is  $\approx 0.5 \times 0.5 \text{ mm}^2$  and the maximum scattering angle  $2\Theta = 155^\circ$ . The *SPEC* instrument software was used to calculate the lattice parameters from a set of collected reflections. As the high degree of freedom of the 4-circle allows to measure a couple of symmetry equivalent reflections<sup>3</sup> in Bragg geometry, more than 20 reflections were used to fit the lattice parameters. The general 4-circle diffraction geometry is shown in **figure 3.3**.

### 3.5.3 Resonant x-ray diffraction

Resonant x-ray experiments were performed at the beamline P09 of the PETRA-III source. The beamline uses a 2 m spectroscopy undulator as source and monochromizes the beam with a high heat load Si double monochromator and a high resolution Bartels monochromator. The incidence polarization can be turned from horizontal to vertical, using diamond quarter and half wave plates. The scattered beam can be analyzed with a  $90^\circ$  reflection from a suitable analyzer crystal, which can be turned around the detector axis to measure any polarization direction. The beam focusing mirrors generate a  $145 \times 50 \text{ }\mu\text{m}^2$  spot at the sample position and the available energy range is 2.4 - 24 keV. The sample can be mounted inside a closed cycle cryostat on a 6-circle diffractometer including xyz-translation.

Soft x-ray resonant magnetic scattering was done at the XUV-diffractometer end station of the UE46-PGM-1 beamline of BESSY II. The pole pieces of the 3.2 m permanent magnet undulator can be shifted with respect to each other to achieve linear polarization in any direction as well as circular polarization. With a plane grating monochromator the energy range from 121 up to 2000 eV is covered. Two samples are mounted with a copper cylinder which is fixed on the copper cool finger of the cryostat inside the UHV experimental chamber. To reach temperatures below 10 K an additional cooling shield can be pulled down around the sample area during operation. The absorption in the sample can be measured as total electron yield (TEY) by recording the current into the sample. The intensity is measured by a photo diode with  $10 \times 10 \text{ mm}^2$  sensitive area behind a ( $1 \times 10 \text{ mm}^2$  in our case) slit, which is read out using a *Keithley* amplifier with variable range depending on the signal strengths. As the noise of the measured signal (typical  $\approx 0.5\%$ ) depends on the amplifier range set during

<sup>3</sup> As  $(h \ k \ l), (h \ -k \ l), (h \ k \ -l)$  and  $(h \ -k \ -l)$  (for orthorhombic systems).

signal acquisition, it would only be possible to know the errors on the intensity, if the range for each point was known, too. This range is not written to the datafile (or fixed at a specific value), so the error can only be estimated from the scatter of the signal. Besides the  $\theta$  and  $2\theta$  motors the sample can be moved in x-, y- and z-direction and turned inside the holder by hand around the  $\phi$  axis.

### 3.5.4 X-ray magnetic circular dichroism (XMCD)

Element specific magnetization has been measured at the 6.5 T end-station 4-ID-C of the Advanced Photon Source (APS), Argonne. The beamline has an electromagnetic undulator, which makes it possible to switch between left and right circular polarized light with 0.5 Hz. The available energy range for circular polarized light is 500-2800 eV, the beam size at the sample position is  $0.3 \times 0.1 \text{ mm}^2$  and the magnetic field can be applied in the beam direction. The absorption can be measured with TEY and a silicon based SII-Vortex fluorescence detector, which can be set to a defined energy window below the incident energy, to measure total fluorescence yield (TFY) at  $2\theta = 90^\circ$ . Several samples can be mounted simultaneous on the cool finger of the cryostat.

### 3.5.5 Polarized neutron diffraction (PND)

Polarized neutron diffraction was used to measure antiferromagnetic order in the samples. For these experiments the two multi detector instruments DNS-JCMS@FRM II and D7@ILL were used, which consist of the same basic components. The incident neutrons coming from a single crystal monochromator are purged of  $\lambda/2$  contaminations with a Be-filter, polarized with a super mirror bender and pass a flipper. The sample is mounted inside the cryostat and can be turned the full range in  $\theta$ . The scattered neutrons are detected within a large  $2\theta$  region by a multi detector bank, where each detector is placed behind a bender polarization analyzer. For the DNS instrument the bank covers  $125^\circ$  with 25 detectors at  $\approx 80 \text{ cm}$  distance to the sample, at D7 132 detectors in a larger distance cover  $140^\circ$ . The incident beam has a divergence of  $\Delta\theta \approx 2.5^\circ$  and a wavelength spread of  $\frac{\Delta\lambda}{\lambda} \approx 1.5\%$ . The background is subtracted by an empty sample holder measurement and the detector sensitivity is corrected using a measurement from an incoherent scatterer<sup>4</sup> to scale the intensities of each detector. A correction of the imperfect polarization of the instrument, generally used for such measurement, was not applied as it did not improve the results. The mosaicity of the substrate and film reflections is much smaller than the beam divergence, which leads to the fact, that only a part (generally not well defined) of the incident beam is scattered. As the polarization measured with a spin incoherent scattering sample, normally used for the polarization correction, only gives an average polarization value over the whole beam, the correction is not possible.

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<sup>4</sup>Vanadium in this case.

### 3.5.6 Polarized neutron reflectometry (PNR)

Polarized neutron reflectometry has been performed at the TREFF-JCNS instrument of FRM II and D17 of ILL. Both instruments have two variable resolution slits before the sample and a 2d-detector with analyzer super-mirrors on the  $2\Theta$  scattering arm. At TREFF a pyrolytic graphite monochromator and a supermirror polarizer define the incoming neutron beam, while at D17 a magnetic multilayer monochromator defines polarization and wavelength. A flipper before and after the sample allows one to measure all four spin channels  $I_{\uparrow\uparrow}, I_{\uparrow\downarrow}, I_{\downarrow\uparrow}, I_{\downarrow\downarrow}$ . The samples are mounted in a cryomagnet with the field in the scattering plane. The asymmetric wave length contributions of the multilayer monochromator of D17 has been characterized polarization dependent using the time-of-flight option of the instrument. For TREFF  $\frac{\Delta\lambda}{\lambda} \approx 1.5\%$  does not limit the  $\vec{Q}$ -resolution and thus has no impact on the measurement.

The modeling of data is similar to x-ray reflectivity done with a Parratt formalism, including the magnetic scattering length density [103]. Thus each scattering channel can be simulated separately comprising the imperfect polarization of both flippers, polarizer and analyzer.

### 3.5.7 Modeling of reflectivity and diffraction data

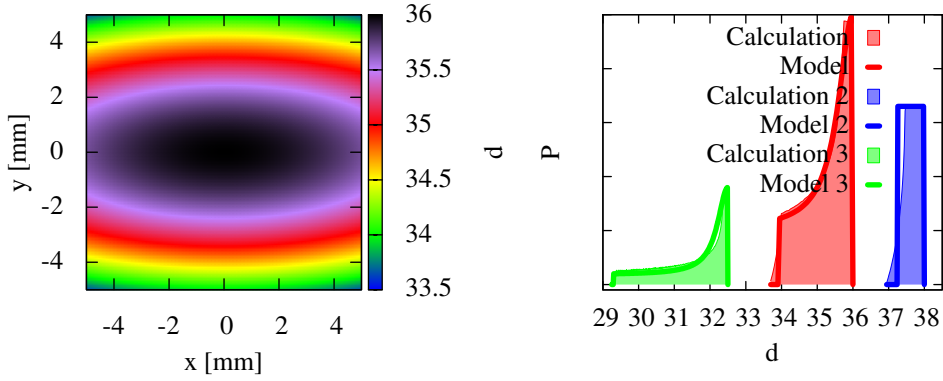
#### Implementation of kinematic multilayer diffraction simulation

For the diffraction measurements a mathematical model described by Fullerton et al. [43] (see **section 2.4.2**) was implemented in an object oriented python module as plug-in to the plot.py program. The model describes a system of  $M$  repetitions of two crystal layers A and B (depicted in **figure 2.10**). Each layer can be described by averaged quantities and, in this case, is a Laue function multiplied by the structure factor calculated from the unit cell. Each layer has an average thickness of  $N$  unit cells and a thickness variation  $\delta N$ , which is applied by averaging over integer variations of the layer thickness. The layers are separated by a region without defined crystal structure  $c$ . After calculating the intensity for the crystal multilayer it is corrected for the beam footprint, which defines the scattering volume of the layers. Substrate peaks are added as Lorentzian functions and the polarization factor is corrected afterwards. An optional resolution can be applied by convolution with a Gaussian. The written code can be found in **section B.2**. For the form factors used for this model and the simulation of the single layers the expansion given in **section 2.4.5** was used.

#### Reflectivity model for oxide samples

To refine the neutron and x-ray reflectivity data an expansion to a standard model was used. In addition to the default layer system, which includes the scattering power and a Gaussian roughness on the surface of each layer, some additional properties of the oxide systems needed to be taken into account.

With the following modifications the data could be modeled very well (see e.g. **section 5.1.2**).



(a) Simulation of the thickness of a film deposited with PLD with line focus on a  $10 \times 10 \text{ mm}^2$  substrate. For the plasma coil deposition function  $d(x,y) = k_x^2 k_y^2 (1 + k_x^2 \cdot \tan^2(\theta_x))(1 + k_y^2 \cdot \tan^2(\theta_y))$ ,  $k_x = 1.5$  and  $k_y = 4$  was chosen.

(b) Thickness distribution  $P(d)$  calculated from the model in (a) with different values of the inhomogeneity parameters  $k_x$  and  $k_y$ . For the corresponding model functions (see text) the parameters  $\gamma$ ,  $w$  and *fraction* were fit to the numeric calculation.

**Figure 3.5:** Visualization of the model used for the thickness inhomogeneity in the reflectivity model. As the real deposition height distribution function is not known a combination of a step function and a heavy side Lorentzian was used to weight the simulated thicknesses of the layers.

**Surface** Very smooth surfaces can't be refined by only using a Gaussian roughness, as oxide layers tend to grow in steps or islands. PLD films have additional droplets on the surface, which also lead to non Gaussian roughnesses. To model non Gaussian roughnesses one or more surface layers with the same atomic scattering powers as the uppermost layer and less density were used.

**Thickness inhomogeneity** Large samples ( $1 \text{ cm}^2$ ) showed a thickness variation from the center to the edge regions, especially for the PLD samples. As this variation is not on the scale of the coherence lengths of the radiation, it cannot be modeled by increasing the roughness parameter, but intensities have to be averaged. The distribution of the thicknesses is not an easy analytic function and depends on many unknown parameters. For PLD the distribution can be analytically calculated for deposition on substrates at a large distance to the target in vacuum [19] (which is only a rough estimate of the situation present for the samples investigated here) with a product of two  $k_{x/y}^2 \cdot (1 + k_{x/y}^2 \cdot \tan^2(\theta_{x/y}))$  functions, which has been done in **figure 3.5a**. As the parameters governing this height profile are system dependent and generally unknown the distribution was modeled with the sum of a heavy side Lorentzian function and a plateau. As can be seen in the example **figure 3.5b**, this gives a relatively good agreement with different possible distributions calculated for three sets of  $k_{x/y}$  parameters. Thus the height variation can be described with only three parameters: The width of the Lorentzian  $\gamma$ , the width of the plateau region  $w$  and the fraction of both contributions.

**Multilayer roughness gradient** The general multilayer model, which only repeats the same layers, was changed to allow a linear increase in roughness from the bottom to the top layers, as has to be expected for a real system.

**D17 Resolution** For the polarized neutron measurements from the D17 instrument a asymmetric shaped resolution function was implemented to reflect the wavelength distribution from the multilayer monochromator, measured with the time-of-flight option.

The code implementation of this model was used with the software *GenX* and can be found in **section B.3**.



# Chapter 4

## Sample Preparation and Description

All samples under investigation consist of epitaxial  $\text{ABO}_3$  layers deposited on single crystalline  $\text{YAlO}_3$  (1 0 0) and  $\text{GdScO}_3$  (1 1 0) substrates. Except for the  $\text{TbMnO}_3$  single layers created with sputter deposition, all samples were grown with pulsed laser deposition (PLD) by Jürgen Schubert of the PGI-9 of the Jülich research center.

### 4.1 Thin-film deposition methods used

#### 4.1.1 Pulsed laser deposition

The material deposition in PLD is achieved by focusing a pulsed laser beam on target material of the composition desired for the film. The deposited energy leads to expeditious evaporation of material and plasma formation. For the deposition of oxide films the process is performed under an oxygen atmosphere of  $10^{-3}$ -1 mbar. The used apparatus works with cylindrical targets, which are turned during deposition to yield a homogeneous ablation. The excimer laser has a line focus along the target axis of 1.5 cm, an energy density of  $5 \text{ J/cm}^2$  at 10 Hz and the distance from the target to the sample heater is about 5 cm. A detailed description of the setup can be found in [136].

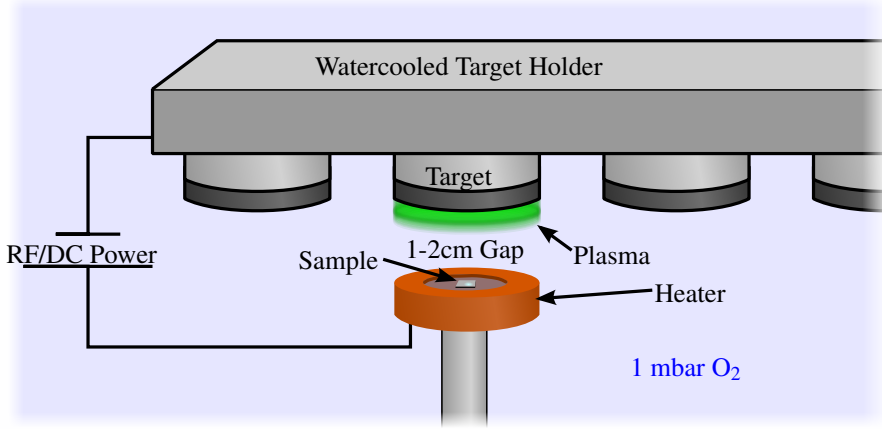
The targets used for the deposited films were created with a solid state reaction from the corresponding unitary oxides. The primary materials (e.g.  $\text{Tb}_4\text{O}_7$  and  $\text{MnO}_2$  powder) were calcined for 6 h at  $1100^\circ\text{C}$ , then compressed for 10 min at 0.13 GPa and subsequently sintered for additional 6 h at  $1300^\circ\text{C}$ .

The main benefits of this method are high deposition rates, applicability to almost any chemical composition where stoichiometric powder (and thus target material) is available and the possibility to work in high oxygen pressure to assure fully oxidized films. These benefits render the method especially suitable to create multilayer structures of complex oxides.

#### 4.1.2 Oxide sputter deposition

Additionally to PLD, thin films of  $\text{TbMnO}_3$  have been created with sputter deposition (**figure 4.1**). For this method the target is a flat disk of 5 cm diameter, connected to a radio frequency generator, which excites a plasma below the target surface. The plasma ions are accelerated





**Figure 4.1:** Schematics of the sputter deposition technique

onto the target by the electric field and sputter off the material. The sample is placed in  $\approx 2$  cm distance below the target. In contrast to conventional sputtering, which is done in e.g. Argon atmosphere of about  $10^{-4}$  mbar, the oxide sputtering is done with a oxygen pressure of up to several mbar. This leads to a much lower deposition rate and has the benefit of a very low mean free path, which inhibits high energy oxygen ions from damaging the sample surface [96]. The large target area makes it possible to create very homogeneous film thicknesses for samples up to  $1 \text{ cm}^2$ .

The target used for the deposition was bought from *Lesker*. To fix the targets to the holder and obtain a good electronic contact, the targets need to be "bonded". In this process the backside of the target is roughened and soldered to a metallic target holder.

## 4.2 Samples under investigation

The following sections will summarize the samples under investigation, their deposition parameters, relevant bulk properties and possible influences when depositing the materials in thin films and multilayers.

### 4.2.1 TbMnO<sub>3</sub>/DyMnO<sub>3</sub>-single layers on YAlO<sub>3</sub>

As described in **section 2.2.2** TbMnO<sub>3</sub> and DyMnO<sub>3</sub> bulk crystals exhibit ferroelectricity as result of a complex magnetic order, which leads to a strong coupling between magnetism and ferroelectricity. Especially TbMnO<sub>3</sub> is a prototype compound for spiral multiferroics and therefore well studied. At room temperature the compounds are paraelectric and paramagnetic. At temperatures below  $T_{NDW} = 41 \text{ K (TbMnO}_3\text{)}/39 \text{ K (DyMnO}_3\text{)}$  the

Mn moments order in the  $\vec{b}$ -direction as sinusoidal spin density wave (SDW) with propagation vector  $(0 \tau_{Mn} 1)$ . Below  $T_{NSDW}$   $\tau_{Mn}$  changes until it almost locks-in at  $T_{NC} = T_{CFE} = 28 \text{ K (TbMnO}_3\text{)}/18 \text{ K (DyMnO}_3\text{)}$  where the magnetic structure changes to a cycloidal with magnetic moments in the bc-plane. At the same temperature a ferroelectric polarization in  $\vec{c}$ -direction emerges. The paramagnetic Tb/Dy moments show a strong coupling to the Mn order evidenced by resonant magnetic scattering [97, 107, 130] on the Tb/Dy-edge. Below  $T_{Nb/Dy} = 7 \text{ K (TbMnO}_3\text{)}/10 \text{ K (DyMnO}_3\text{)}$  the rare earth moments order with a different wave vector of  $(0 \tau_{Tb/Dy} 1)$  collinearly in the anisotropy direction, which lies in the ab-plane. The complete magnetoelectric phase diagram of TbMnO<sub>3</sub> and DyMnO<sub>3</sub> has been published by Kimura [72] with later refinements from other authors [20, 114].

Thin films of orthorhombic TbMnO<sub>3</sub> have already been studied on SrTiO<sub>3</sub> substrates [33, 34, 80, 102, 129] for their macroscopic properties and strain relaxation. Anomalous ferromagnetism has been found in these films [73], which contradicts the cycloidal order, that leads to the ferroelectricity. Unfortunately these films exhibited 90° domains, as the SrTiO<sub>3</sub> surface has a square crystal lattice and thus this is no well defined system especially for studies of direction dependent properties.

The TbMnO<sub>3</sub> and DyMnO<sub>3</sub> films investigated in this work were deposited on orthorhombic YAlO<sub>3</sub> (1 0 0) substrates, which has a rectangular surface lattice structure, which corresponds to the TbMnO<sub>3</sub>/DyMnO<sub>3</sub> ac-plane. This leads to  $\vec{b}$  as the only preferable growth direction [47] with a low strain of  $\approx 0.5\%$ . Therefore it is possible to investigate single crystalline films for the influence of finite size or interface effects in a well defined system without a strong influence of the substrate. Various film thicknesses of TbMnO<sub>3</sub> and DyMnO<sub>3</sub> have been produced between 2 nm and 400 nm using PLD and for TbMnO<sub>3</sub> additional sputter films were produced for comparison. The films were deposited at  $\approx 700^\circ \text{C}$  with an oxygen pressure of  $5 \cdot 10^{-3}$  mbar for PLD and 3 mbar for sputtering.

The films will be referred to as  $\mathbb{T}_x^{\text{PLD}}$ ,  $\mathbb{T}_x^{\text{SD}}$  and  $\mathbb{D}_x$  for PLD TbMnO<sub>3</sub>, sputtered TbMnO<sub>3</sub> and PLD DyMnO<sub>3</sub> films of x nm thickness, respectively.

## 4.2.2 LaCoO<sub>3</sub>-single layers on YAlO<sub>3</sub>

To investigate the coupling between adjacent magnetic materials to the spiral magnetism in TbMnO<sub>3</sub>, LaCoO<sub>3</sub> was chosen in the multilayers described in **section 4.2.3**. LaCoO<sub>3</sub> has a perovskite structure and as described in **section 2.3.4** gets ferromagnetic under strain with a transition temperature close to  $T_{NSDW}$  of TbMnO<sub>3</sub>. To make sure, that the effect is present in the used LaCoO<sub>3</sub> layers on YAlO<sub>3</sub> substrates, a single layer (with the emblem  $\mathbb{L}_{35}$ ) has been investigated deposited by PLD, too. The deposition parameters have been chosen equal to those of the TbMnO<sub>3</sub> layers. The layer thickness of 35 nm yields a reasonable magnetic moment for SQUID investigations.

## 4.2.3 [TbMnO<sub>3</sub>-LaCoO<sub>3</sub>]-multilayers on YAlO<sub>3</sub>

The effect of exchange coupling of the antiferromagnetic TbMnO<sub>3</sub> order to adjacent ferromagnetic LaCoO<sub>3</sub> films has been studied with multilayers, consisting of  $\approx 10$  nm TbMnO<sub>3</sub>

and 2 nm  $\text{LaCoO}_3$  bilayers. The  $\text{TbMnO}_3$  thickness was chosen to comprise approximately 3 propagations of the magnetic spiral, separated only by a few unit cells of the ferromagnetic interlayer. The deposition parameters for PLD were the same as for the single layers and most investigations were performed on multilayers with 20 periods. As the sample consists of 18 UC  $\text{TbMnO}_3$  and 3 UC  $\text{LaCoO}_3$  it will be referred to as  $\text{TbL}_{\times 20}^{18/3}$ .

#### 4.2.4 $[\text{EuTiO}_3\text{-BaTiO}_3]$ -multilayers on $\text{GdScO}_3$

Similar to the  $[\text{TbMnO}_3\text{-LaCoO}_3]$ -multilayers, the magnetic exchange interaction at the interface  $\text{EuTiO}_3$  to  $\text{BaTiO}_3$  has been investigated with different multilayers. While strained  $\text{EuTiO}_3$  layers can become ferromagnetic (section 2.3.4), the alloy  $\text{Eu}_{0.5}\text{Ba}_{0.5}\text{TiO}_3$  tends to show no magnetic order at all, up to very low temperatures [104]. The absence of magnetic order together with a large magnetic moment on Eu and a strong magnetoelectric effect allows the material to be used as a very sensitive probe in the search for an electric dipole moment of the electron [104, 116], an important quantity in the field of particle physics. In a multilayer structure the effect of strain and magnetic exchange interaction could lead to either ferromagnetic  $\text{EuTiO}_3$  layers in an artificial multiferroic structure or a similar behavior as in the alloy compound.

For a systematic investigation, multilayers with the composition  $\text{EuTiO}_3/\text{BaTiO}_3$  1 nm/1 nm, 1.5 nm/2.5 nm, 2 nm/4 nm and 5 nm/4 nm (labeled  $\text{EB}_{\times 20}^{x/y}$  for 20 repetitions with x UC  $\text{EuTiO}_3$  and y UC  $\text{BaTiO}_3$ ) have been produced with PLD, using parameters (similar to the  $\text{TbMnO}_3$  system but with 650 °C substrate temperature) and targets already used for earlier studies of Jürgen Schubert.  $\text{GdScO}_3$  (1 1 0) was selected as substrate, as the lattice constant (3.97 Å) is in between of bulk  $\text{EuTiO}_3$  (3.9 Å) and  $\text{BaTiO}_3$  (4.0 Å) which results in a strain of  $\approx 1.2\%$ <sup>1</sup>.

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<sup>1</sup>An epitaxial system of thin layers with different lattice constants the average strain between the substrate and the multilayer can be calculated from the substrate lattice parameters and the thickness weighted mean of the component materials.

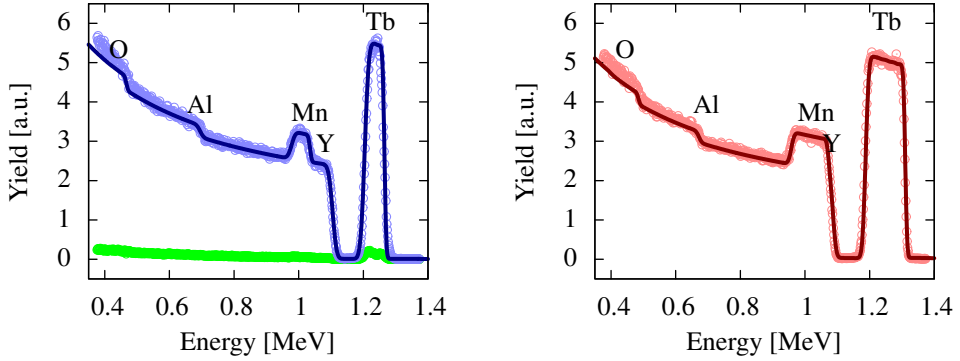
# Chapter 5

## Experiments I: TbMnO<sub>3</sub> and DyMnO<sub>3</sub> Single Layers

To investigate the influence of finite size on the multiferroicity originating from spiral magnetic structures, RMnO<sub>3</sub> thin films have been examined. In the almost unstrained system with YAlO<sub>3</sub> substrates this study allows the comparison to other work on TbMnO<sub>3</sub> thin films, where ferromagnetic order has been observed as discussed in **section 4.2.1**. The multiferroic behavior of TbMnO<sub>3</sub> and DyMnO<sub>3</sub> has been studied with a variety of methods for different film thicknesses deposited by PLD and sputtering. The main parameters of the investigated films are summed up below. (All parameters determined for the samples are collected in the appendix as **table A.1** and **table A.2**.) The samples used to improve the deposition parameters and produced with incorrect stoichiometry were omitted.

| ID                              | A[mm <sup>2</sup> ] | d[nm]    | δd[%]   | σ[nm]   | δθ <sub>200</sub> [°] | T <sub>N<sub>SDW</sub></sub> | T <sub>N<sub>C</sub></sub> | T <sub>N<sub>Tb</sub></sub> | Method  |
|---------------------------------|---------------------|----------|---------|---------|-----------------------|------------------------------|----------------------------|-----------------------------|---------|
| T <sub>2</sub> <sup>PLD</sup>   | 10 × 10             | 2.24(5)  | 20.(15) | 0.37(1) | 0.010(3)              | 21 K                         |                            |                             | PLD     |
| T <sub>5</sub> <sup>PLD</sup>   | 10 × 10             | 4.99(3)  | 7.8(5)  | 0.41(1) | 0.015(1)              |                              |                            |                             | PLD     |
| T <sub>9</sub> <sup>PLD</sup>   | 10 × 10             | 9.2(1)   | 1.3(5)  | 0.50(1) | 0.011(1)              | 36 K                         | -                          | 15 K                        | PLD     |
| T <sub>18</sub> <sup>PLD</sup>  | 10 × 10             | 17.6(1)  | 2.3(5)  | 0.55(1) | 0.012(1)              | 36 K                         | -                          | 15 K                        | PLD     |
| T <sub>54</sub> <sup>PLD*</sup> | 10 × 10             | 54.4(2)  | 4.2(5)  | 1.09(3) | 0.013(1)              |                              |                            |                             | PLD     |
| T <sub>200</sub> <sup>PLD</sup> | 10 × 10             | 200.(50) |         |         | 0.017(1)              | 35*/41 K                     | -                          | 15 K *                      | PLD     |
| T <sub>2</sub> <sup>SD</sup>    | 5 × 5               | 2.01(4)  |         | 0.63(5) | 0.020(1)              |                              |                            |                             | Sputter |
| T <sub>6</sub> <sup>SD</sup>    | 5 × 5               | 5.88(3)  | 1.0(2)  | 0.85(1) | 0.015(1)              | 39 K                         | 23 K                       |                             | Sputter |
| T <sub>11</sub> <sup>SD</sup>   | 5 × 5               | 10.6(15) | 1.2(4)  | 0.56(2) | 0.008(1)              | 41 K                         | 27.5 K                     | 10.5 K                      | Sputter |
| T <sub>16</sub> <sup>SD</sup>   | 10 × 10             | 15.9(1)  | 0.7(4)  | 0.37(1) | 0.011(1)              | 41.5 K                       |                            | 10 K                        | Sputter |
| T <sub>20</sub> <sup>SD</sup>   | 5 × 5               | 19.62(3) | 0.2(2)  | 0.84(9) | 0.013(1)              | 43 K                         | 29 K                       |                             | Sputter |
| T <sub>31</sub> <sup>SD</sup>   | 10 × 10             | 30.9(2)  | 0.6(4)  | 0.48(1) | 0.010(1)              | 39 K                         |                            | 10 K                        | Sputter |
| T <sub>46</sub> <sup>SD</sup>   | 5 × 5               | 46.2(3)  | 2.4(5)  | 0.88(9) | 0.018(1)              |                              |                            |                             | Sputter |
| T <sub>100</sub> <sup>SD</sup>  | 5 × 5               | 100.7(2) | 0.4(1)  | 1.45(2) |                       | 42 K                         | 27 K                       | 10 K                        | Sputter |
| T <sub>400</sub> <sup>SD</sup>  | 5 × 5               | 400.(50) |         |         |                       | 43 K                         | 28 K                       | 9 K                         | Sputter |
| D <sub>2</sub>                  | 10 × 10             | 2.07(3)  | 11.(5)  | 0.60(3) | 0.013(1)              |                              |                            |                             | PLD     |
| D <sub>5</sub>                  | 10 × 10             | 5.30(4)  | 5.(2)   | 0.64(4) | 0.017(1)              |                              |                            |                             | PLD     |
| D <sub>10</sub>                 | 10 × 10             | 9.6(1)   | 13.(5)  | 0.47(2) | 0.013(1)              | 35 K                         | -                          | 15 K                        | PLD     |
| D <sub>20</sub>                 | 10 × 10             | 20.(2)   | 10.(3)  | 0.64(4) | 0.010(1)              | 35 K                         | -                          | 15 K                        | PLD     |
| D <sub>50</sub>                 | 10 × 10             | 50.(5)   |         |         |                       |                              |                            |                             | PLD     |
| D <sub>100</sub>                | 10 × 10             | 100.(10) |         | 2.0(5)  |                       |                              |                            |                             | PLD     |

**Table 5.1:** TbMnO<sub>3</sub> and DyMnO<sub>3</sub> single layers used for the experiments with some important parameters. Parameters obtained by reflectometry, diffraction, SQUID, SHG and resonant scattering are colored accordingly. "\*" denotes off-stoichiometric samples, empty fields are not measured, "-" represents a property not present in this sample.



(a) Sample  $T_{50}^{PLD*}$ , fit: 50 nm Tb<sub>1.05(2)</sub>Mn<sub>0.86(2)</sub>O<sub>3.5(5)</sub>

(b) Sample  $T_{100}^{SD}$ , fit: 101 nm Tb<sub>1.00(2)</sub>Mn<sub>1.00(2)</sub>O<sub>3.1(5)</sub>

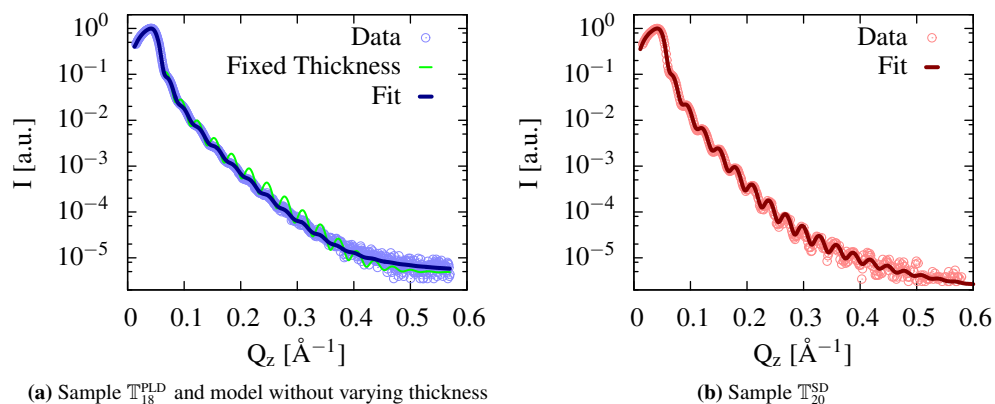
**Figure 5.1:** RBS measurements and fit including channeling. Channeling (green) aligned to a high symmetry axis of the crystal yields a drop to 5% with respect to random orientation of the crystal axis (data (points) and simulation (line)).

## 5.1 Structural characterization

A very important feature related to the quality of epitaxial layers is the crystalline and surface structure as well as the chemical composition. Layer by layer growth will yield low surface roughnesses and a high crystalline quality. Together with the stoichiometry this is a prerequisite to study a well defined system for e.g. magnetism. The following sections sum up the data measured with x-ray reflectivity, x-ray diffraction, RBS and AFM.

### 5.1.1 Stoichiometry of the films

Layers with at least 50 nm thickness have been characterized by Rutherford backscattering spectrometry<sup>1</sup>. The method gives a rough estimate of the layer thickness of  $\approx 10\%$  and can be used to measure the elemental content of a layer. A typical RBS spectrum recorded for  $T_{50}^{PLD*}$  is shown in **figure 5.1a** together with its simulation. The large drop in the channeling direction is a sign for a good crystal quality. The method was used to determine the thickness of films with more than 100 nm. From measurements on films deposited on silicon substrates, the first target created for TbMnO<sub>3</sub> was found to produce layers with 10-15% Mn deficiency. Therefore a second target with additional Mn content was created, yielding stoichiometric samples (with an accuracy of  $\approx 2\%$ ). Samples produced with the old target are marked with a "\*" .



**Figure 5.2:** X-ray reflectivity data from Huber D8 together with simulation (enlarged in **section A.2**)

### 5.1.2 Film thickness and roughness

The layer thicknesses for films of up to  $\approx 100$  nm could be measured with x-ray reflectivity (XRR). The data was simulated according to the model of **section 3.5.7**, using scattering powers calculated from the crystal structure and tabulated elemental scattering, to obtain thickness  $d$ , roughness  $\sigma$  and overall thickness inhomogeneity  $\delta d$ . The interface roughness between substrate and film was found to be quite low (1-2.5 Å), justifying to abdicate any pretreatment of the substrate surface before growth. For most samples it was not possible to simulate the data with a simple single layer model. Although the Kiesing fringes fitted quite well, the intensity drop of the simulation did not follow the measured curve. Together with the surface structure measured with AFM (**section 5.1.3**) this can be explained by a non Gaussian height distribution of the roughness. As the mathematic description of the asymmetric roughness is not fully developed yet, the derived roughness values in the model are overestimated.

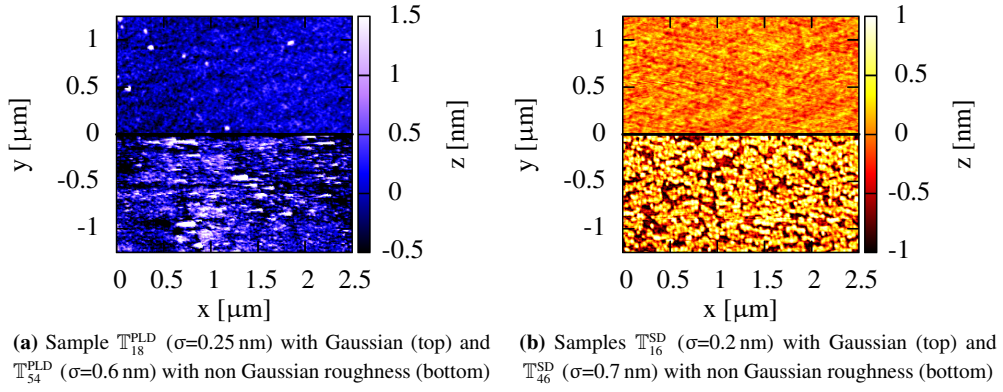
**Figure 5.2** compares the measurements of  $T_{18}^{\text{PLD}}$  and  $T_{20}^{\text{SD}}$ . The best fit of a model without thickness inhomogeneity shows a strong deviation from the measured data in **figure 5.2a**. The other fits used to extract the film parameters are presented in **section A.2**. As can be seen, the oscillations in the data of the PLD sample have a lower contrast and die out more quickly than in the case of the sputter sample, which is a sign for a larger thickness inhomogeneity. This has been found to be the case for most of the PLD samples, but sputter films created later showed increased inhomogeneity due to problems during the bonding process<sup>2</sup>, too.

### 5.1.3 Surface structure

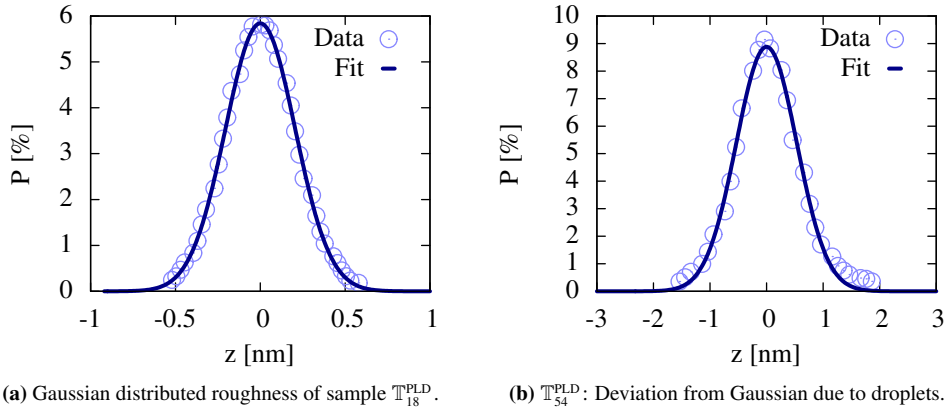
Selected PLD and sputter  $\text{TbMnO}_3$  samples, which needed extraordinary high and low asymmetric shaped roughnesses for the reflectivity simulations, have been investigated for their

<sup>1</sup>The experiments were performed by Willi Zander and analyzed by Jürgen Schubert.

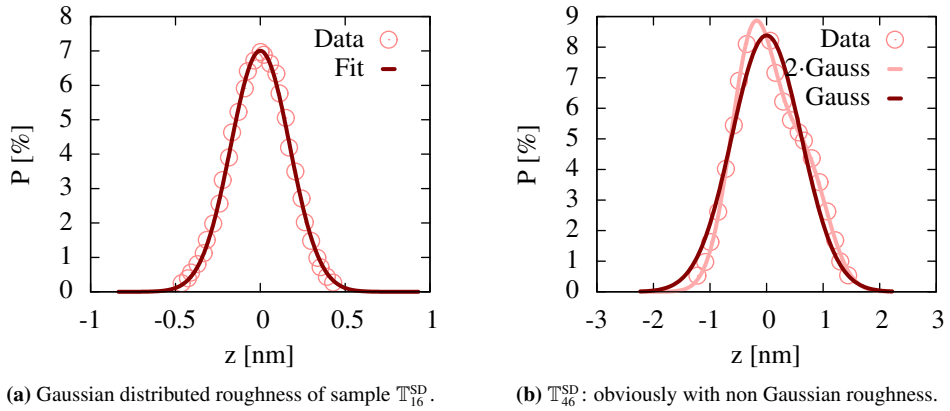
<sup>2</sup>Cutting the target to the appropriate shape and fixing it to the target holder.



**Figure 5.3:** AFM images of  $5 \times 5 \mu\text{m}^2$  section of the  $\text{TbMnO}_3$  film surface



**Figure 5.4:** Height distribution extracted from figure 5.3a with best Gaussian fit



**Figure 5.5:** Height distribution extracted from figure 5.3b with best Gaussian fit

surface structure with AFM. The resulting images are shown in **figure 5.3**. The root mean square (rms) roughness calculated from these measurements is comparable to the reflectivity results of these samples. The obvious difference between the PLD and sputter samples is the droplets resulting from the PLD method. For the PLD samples the asymmetric height distribution seems to originate from a large droplet density. The rough sputter sample, on the other hand, shows a surface build from clusters with similar size and shape in contrast to the arbitrary, noise like surface of the smooth sample. The height distributions depicted in **figure 5.5** show a clear difference for both sputter samples. The roughness of the smooth sample, where XRR could be fitted without any additional surface layer, shows a clear Gaussian shape, in contrast to the rougher sample. These results justify the addition of surface layers to the XRR simulations to describe the non Gaussian height distribution. A model is in development, which makes it possible to fit the full rms roughness of such non Gaussian height distribution by mapping the scattering length density distribution of a two or more surface layer model to a height distribution of one rough layer.

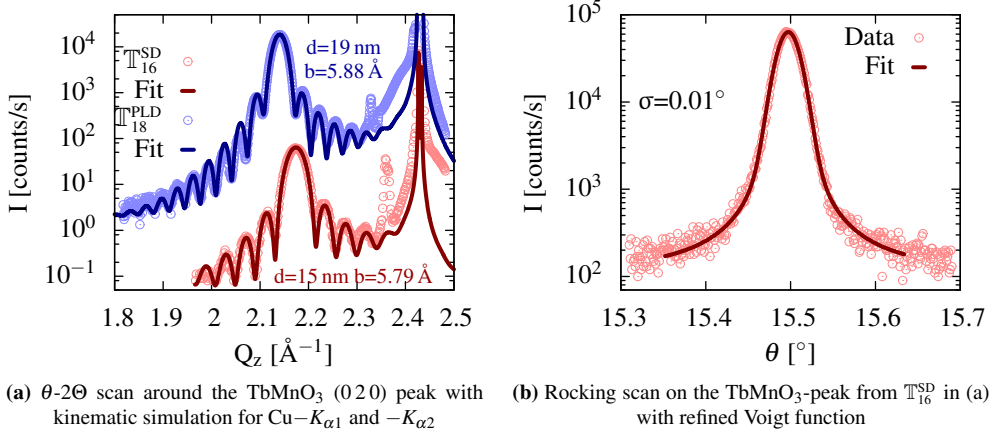
### 5.1.4 Crystalline structure

The crystalline quality of the epitaxial layers was investigated using x-ray diffraction. Both instruments used (D8 and 4-circle) have a Cu anode with a monochromator, which transmits  $K_{\alpha 1}$  and  $K_{\alpha 2}$  together with some Bremsstrahlung. The mosaicity of the crystal structure was measured on the  $\text{TbMnO}_3/\text{DyMnO}_3$  (0 2 0)-peak, which is exemplified in **figure 5.6b** and **5.8a**. A Voigt function was used to fit the mosaicity and calculate the standard deviations given in the tables. The corresponding out-of-plane reciprocal lattice scan is shown in **figure 5.6a** including a kinematic simulation<sup>3</sup> of a crystalline  $\text{TbMnO}_3$  layer with discrete roughness on a  $\text{YAlO}_3$  substrate. The Laue oscillations corresponding to the film thicknesses were found for all layers with less than 40 nm thickness and could be simulated. For the models the thicknesses were found to have  $\approx 1\text{-}2$  nm less extent than in the corresponding XRR model. This can be explained with an interface region of undefined crystal structure of corresponding size. The sharp peak between the substrate and film reflections could be identified as the  $\text{YAlO}_3$  (0 2 0) peak and was found for most samples deposited on a second batch of substrates. The presence of these peaks could only be explained by wrong oriented crystallites in the substrates, which is confirmed by additional measurements on unused substrates showing the same peak. (A comparison of a first and second batch substrate can be found in **section A.3**.)

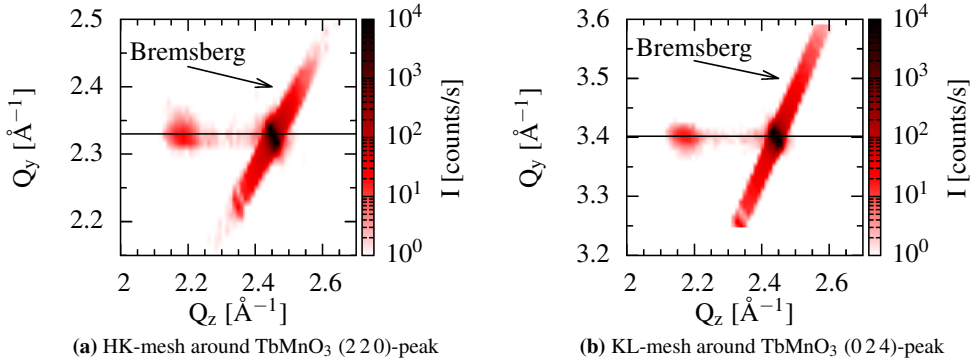
Reciprocal space maps around partly in-plane reflections were recorded with the 4-circle diffractometer. The film peaks lie on the same in-plane reciprocal space position  $Q_y$  as the substrate peaks, which confirms the fact that the film lattice is matched to the substrate. **figure 5.7** and **figure 5.8b** show example meshes for a  $\text{TbMnO}_3$  and  $\text{DyMnO}_3$  sample. For the stronger reflections one can see the Bremsberg and tungsten peaks, which are not suppressed by the Göbelmirror, on a line between the peak position and the origin.

<sup>3</sup>No resolution has been taken into account.

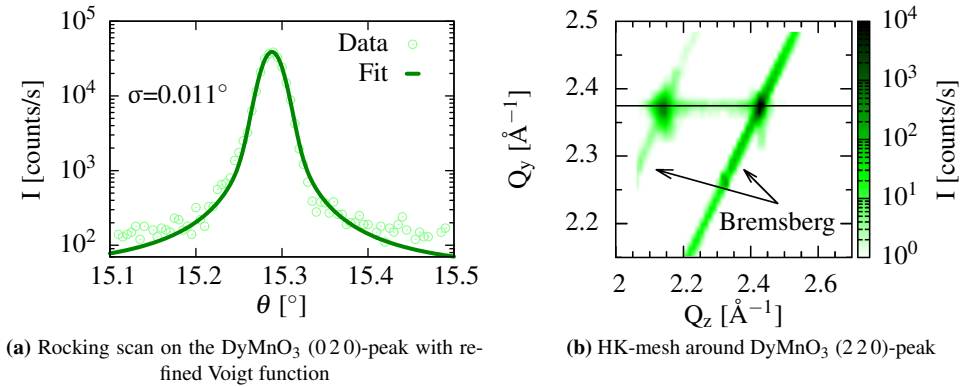




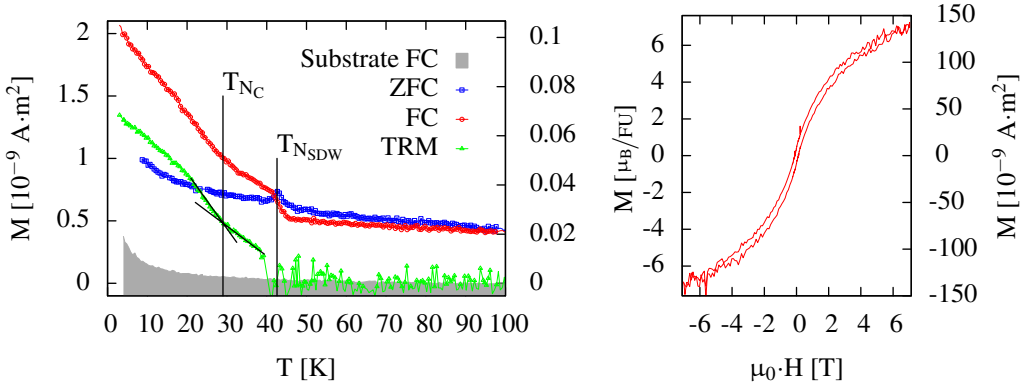
**Figure 5.6:** Out-of-plane XRD measurements performed with the D8 instrument on  $\mathbb{T}_{16}^{\text{SD}}$  and  $\mathbb{T}_{18}^{\text{PLD}}$



**Figure 5.7:** Reciprocal space meshes measured on  $\mathbb{T}_{11}^{\text{SD}}$  with the 4-circle diffractometer. The in-plane lattice parameters are obviously fit to the substrate, within the instrumental resolution.



**Figure 5.8:** Reciprocal space meshes measured on  $\mathbb{D}_{100}$  with the 4-circle diffractometer. The in-plane lattice parameters are obviously fit to the substrate, within the instrumental resolution.



(a) Temperature dependence measured zero field cooled (ZFC) and field cooled (FC) in 10 mT and the resulting thermal remanent magnetization (TRM), corrected for the diamagnetism of the substrate. Black lines are guides to the eye.

(b) Field dependence at 3 K, corrected for the diamagnetism of the substrate

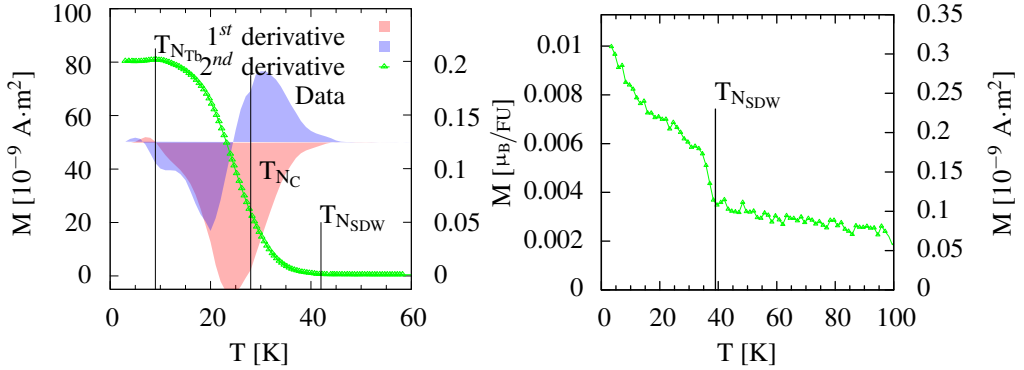
**Figure 5.9:** Magnetization measurements on  $T_{20}^{SD}$  in  $\vec{c}$ -direction

## 5.2 Macroscopic magnetization

The magnetization measurements were performed with the SQUID magnetometer, using the reciprocating sample option (RSO). As there is no ferromagnetic order in the films, the magnetic moment of the layers is relatively small and in the same order of magnitude as the diamagnetism of the substrate. This makes it challenging to measure the film signal even with a precise magnetometer. To keep additional influences as low as possible, the samples were mounted without any glue, tape or capsule inside a plastic straw as described in [section 3.1](#). To reduce the remanent magnetization of the instrument, a degauss sequence<sup>4</sup> was used before each temperature dependent measurement and the remaining field was minimized using the ultra low field option. After this procedure the samples were cooled to 3 K and measured at 10 mT during heating up to 300 K (ZFC). After this the samples were measured cooling inside the same field again down to 3 K (FC), where the field was reset to 0 and the thermal remanent magnetization (TRM) was measured during heating.

For the  $\text{TbMnO}_3$  and  $\text{DyMnO}_3$  samples the magnetization measured in  $\vec{a}$ - and  $\vec{b}$ -directions show only background magnetization from the substrate and paramagnetism from the layer, as the Tb/Dy anisotropy axes lie in the  $ab$ -plane. Hence the magnetic moment of the rare earths dominate the measurement. Therefore later measurements were only performed with the  $\vec{c}$  axes in the direction of the magnetic field. The magnetic moment per formula unit ( $\mu_B/\text{FU}$ ) was calculated from the measured film thickness and the surface area and thus has a low precision of some %. **figure 5.9a** shows a typical measurement series from a  $\text{TbMnO}_3$  thin film together with an empty substrate measurement for comparison. As can be seen there is only a very weak magnetic signal from the film, dominated by weak ferromagnetism (proofed with the hysteresis in **figure 5.9b**) that sets in at the Mn spin density wave transition

<sup>4</sup>Field oscillations with decreasing amplitude between 1 T and 0.



(a)  $T_{400}^{\text{SD}}$ : The derivatives have been given in arbitrary scale to illustrate the position of  $T_{\text{NC}}$  and  $T_{\text{NDy}}$ .  $T_{\text{NSDW}}$  is present at the point where the magnetization drops to zero,  $T_{\text{NC}}$  can only be estimated due to small kinks in the derivatives and  $T_{\text{NDy}}$  is present at the maximum of the magnetization slightly below 10 K.

(b)  $T_{31}^{\text{SD}}$ : Ferromagnetic impurities in the substrate lead to remanent magnetization even above  $T_{\text{NSDW}}$ . Due to this background and the low magnetization, no other transitions could be observed for smaller films.

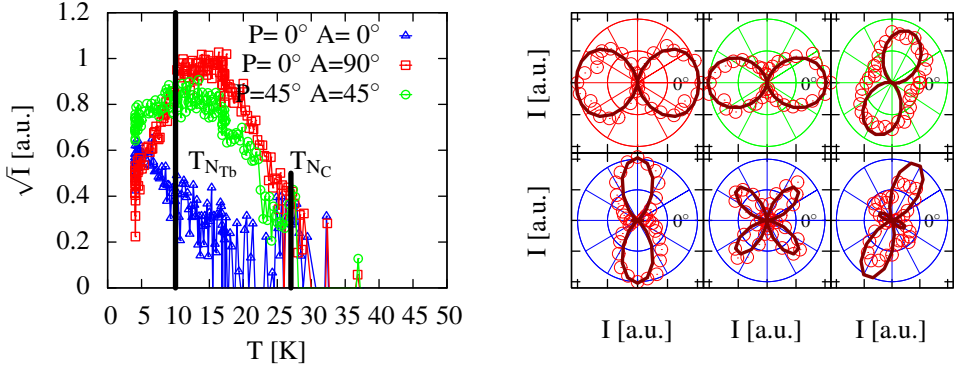
**Figure 5.10:** Thermal remanent magnetization measured in  $\vec{c}$ -direction after field cooling in 10 mT

temperature  $T_{\text{NSDW}}$ . This is the only transition, that is prominent for all samples and is best identified in the TRM measurement, as the paramagnetic background is not present (see also **figure 5.10**). The two other transition ( $T_{\text{NC}}$  and  $T_{\text{NDy}}/T_{\text{NDy}}$ ) can only be roughly estimated from small kinks in the magnetization curves or their derivative for samples with limited impurities.

## 5.3 Symmetry and ferroelectricity

For  $T_{100}^{\text{SD}}$  the ferroelectricity was investigated with second harmonic generation (SHG). The sample was mounted with  $\vec{b}$  in the beam direction (z-direction) and measured in transmission. In this geometry the only independent susceptibility terms measurable are (see **section 3.4**)  $\chi_{xxx}$ ,  $\chi_{xyx} = \chi_{xyx}$ ,  $\chi_{xyy}$ ,  $\chi_{yyy}$ ,  $\chi_{yyx} = \chi_{yyx}$  and  $\chi_{yxx}$ . TbMnO<sub>3</sub> has a Pbnm space group, which has the point symmetry  $mmm$ . That means it is centro-symmetric and thus SHG from the crystal structure is forbidden. The broken symmetry at the interface and surface does not affect the measurable terms, as it only breaks the mirror symmetry in the z-direction. Ferroelectric order in  $\vec{c}$  (x-direction) reduces the symmetry to  $mm2$ , which has no inversion symmetry and, as can be looked up in [15], only forbids  $\chi_{xxx}$ ,  $\chi_{xyy}$  and  $\chi_{yxy}$ . If the ferroelectricity would occur in  $\vec{a}$  (y-direction), the other three terms would be forbidden, thus both directions of the ferroelectric polarization can be distinguished.

For the investigated sample a small but clear SHG signal was detected below 27 K and is shown in **figure 5.11**. To make sure, that the signal does not originate from fluorescence or any other source, the monochromator energy was scanned and only a signal with half the radiation wavelength was found. As a second test filters were used to identify the position



(a) Temperature dependence of the square root SHG intensity for three polarizer (P) and analyzer (A) positions. The SHG signal vanishes above  $\approx 27$  K. At  $T_{N_{Tb}}$  the electric polarization is lowered and an additional term gains intensity.

(b) Complete set of anisotropy scans performed at 11 K together with simulation including  $\chi_{yyy}$ ,  $\chi_{yxx}$  and  $\chi_{xyx}$ . From left to right, line 1: polarizer = analyzer scan, analyzer scans with polarizer at  $90^\circ$  and  $135^\circ$ , line 2: polarizer scans with analyzer at  $0^\circ$ ,  $90^\circ$  and  $135^\circ$

**Figure 5.11:** Second harmonic generation on  $T_{100}^{SD}$ , the electric polarization lies in the  $\vec{c}$ -direction. Polarizer/analyzer  $0^\circ$  corresponds to an electric field in the  $\vec{a}$ -direction,  $90^\circ$  to the  $\vec{c}$ -direction.

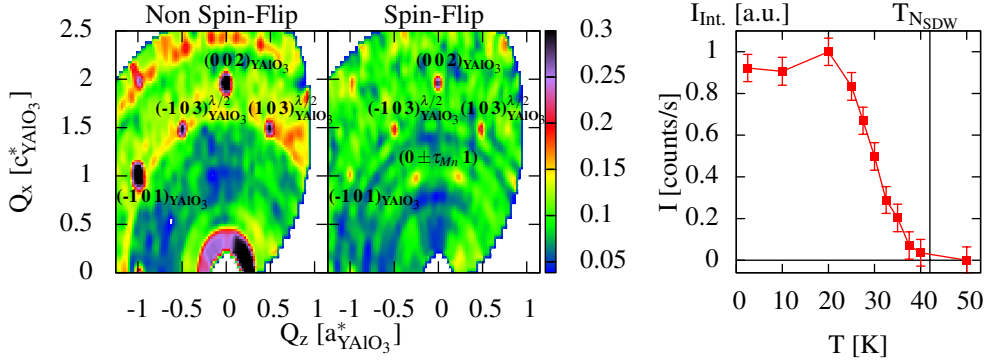
where the SHG signal was created and any source outside the cryostat could be eliminated. An even clearer proof was the completely vanishing signal, when heating up the sample above 27 K. The polarization analysis of the SHG intensity at 11 K (**figure 5.11b**) can nicely be explained with the  $\chi_{yyy}$ ,  $\chi_{yxx}$  and  $\chi_{xyx}$  tensor components allowed for an electric polarization in  $\vec{c}$ -direction. This is in accordance to bulk behavior.

As the SHG signal scales with the order parameter squared, **figure 5.11a** shows the square root of the measured intensity. There is a clear drop of the larger tensor components (and thus the electric polarization) below 10 K, which we explain with the onset of the Tb order at  $T_{N_{Tb}}$ . This points towards a contribution of Tb to the ferroelectricity, which is not present in bulk  $TbMnO_3$ , but can be found in  $DyMnO_3$ . The main difference between both compounds is the size of the rare earth ions and thus even small strain from the substrate could be the reason for this behavior. Additional components arising below  $T_{N_{Tb}}$  have not yet been explained but could originate from the Tb magnetic order, which needs to be treated differently from ferroelectricity as the time reversal has to be considered, too.

## 5.4 Microscopic magnetization

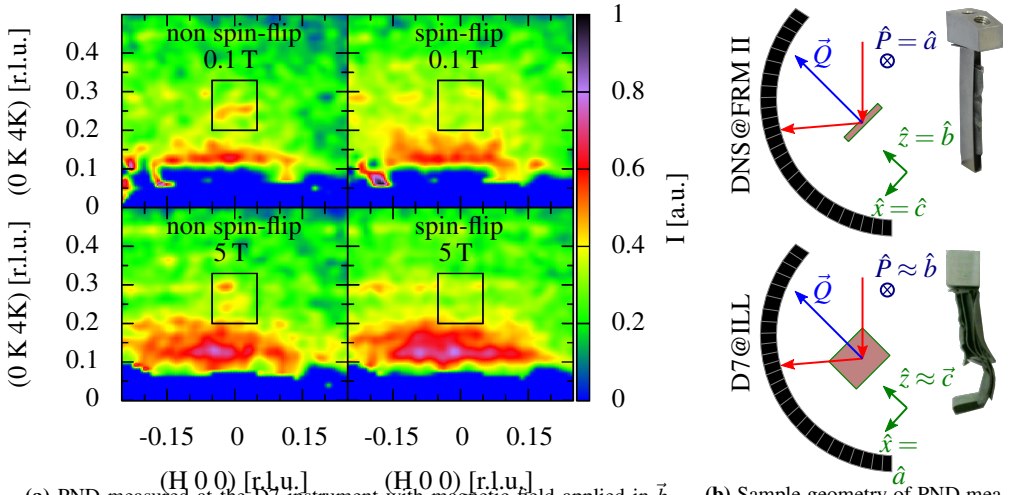
### 5.4.1 Polarized neutron diffraction

The antiferromagnetic order in a stack of  $T_{200}^{PLD}$  samples has been measured using polarized neutron diffraction at the DNS instrument. This allows the investigation of antiferromagnetic order within a large  $\vec{Q}$ -range together with selectivity for the direction of the magnetic



(a) Reciprocal space map measured at 2.5 K. The Bragg peaks in the spin-flip channel verify the long range magnetic order with magnetic moments in the  $\text{TbMnO}_3$  bc-plane. (b) Integrated intensities of the magnetic  $(0 \pm \tau_{Mn} 1)$  reflection measured in the spin-flip channel.

**Figure 5.12:** Polarized neutron diffraction on  $\text{TbMnO}_3^{\text{PLD}}$  with polarization in  $\text{TbMnO}_3$   $\vec{a}$ -direction measured with DNS. In this geometry magnetic moments lying in  $\vec{a}$ -direction lead to non spin-flip, moments in the bc-plane to spin-flip scattering. The strong, sharp peaks originate from the substrate crystal structure and are visible due to the finite flipping ratio of the instrument.



(a) PND measured at the D7 instrument with magnetic field applied in  $\vec{b}$ -direction at 10.5 K. No switching of magnetic moments to the ac-plane is observed in the spin-flip channel. The large background in the smaller  $Q$  region can be explained by magnetic scattering from the large Tb moments, as it is lower for  $\vec{Q}$  in  $\vec{a}$ - than in  $\vec{c}$ -direction due to the strong anisotropy axis of Tb, which lies in the ab-plane. Additionally the background rises with increasing magnetic field. (b) Sample geometry of PND measurements performed at ILL and FRM II. Although the scattering plane in the two measurements is quite different, both allow to access the magnetic reflection at  $\approx (0.25 1)$

**Figure 5.13:** Polarized neutron diffraction on  $\text{TbMnO}_3^{\text{PLD}}$

moments. The samples were mounted in the cryostat with the  $\text{TbMnO}_3$   $\vec{a}$ -direction perpendicular to the scattering plane, parallel to the neutron polarization vector. In this geometry (the same as shown in **figure 6.9** on page 70) the whole  $bc$ -plane can be investigated and magnetic moments in the scattering plane lead to spin-flip scattering, while magnetic moments in  $\vec{a}$ -direction contribute to the intensity in the non spin-flip channel.

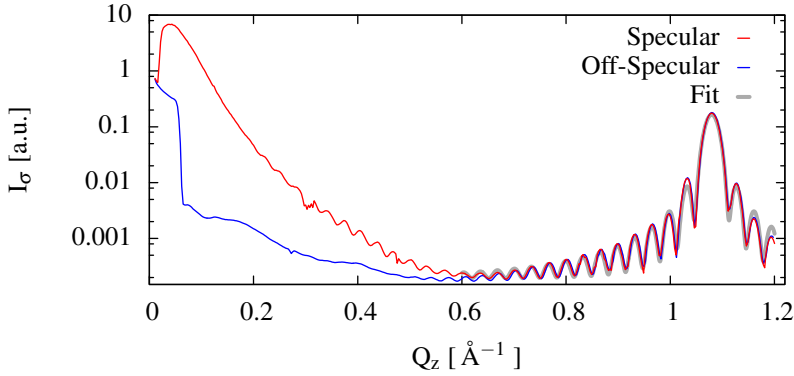
A part of an overview  $\theta$ -scan at base temperature is shown in **figure 5.12a**. Despite the Be-filter some small contamination ( $\approx 2\%$ ) of  $\lambda/2$  is still left in the incident beam and is depolarized by the spin flipper, which leads to a noticeable contribution of structural substrate reflections in the spin-flip channel. Additional strong peaks from the substrate can be seen in the non spin-flip channel and as result of the finite polarization in the spin-flip channel with reduced intensity. The only magnetic reflections found in this scattering plane were the  $\text{TbMnO}_3$  ( $0 \pm \tau_{Mn} 1$ ) peaks with  $\tau_{Mn} = 0.27$  similar to the bulk value. A small omega scan around this peak was measured temperature dependent with an integrated intensity shown in **figure 5.12b**. The transition temperature  $T_{\text{NSDW}} \approx 40 \text{ K}$  is close to the bulk values, too. As the peak intensity of these thick layers is only 50% of the instrumental background and had to be measured with 10 min per  $\theta$  position, no thinner layers have been investigated.

A similar experiment at the D7 instrument with a second batch of samples could reproduce this result. For the measurements shown in **figure 5.13a** the samples were mounted with the  $\vec{b}$ -axis slightly tilted to the magnetic field, to make it possible to measure the magnetic reflection at  $\approx (0 0.25 1)$ , while applying the field in  $\vec{b}$  direction (see **figure 5.13b** for a sketch of the geometry). Unfortunately, in this geometry the alignment of the sample is hardly possible, as no substrate reflection in the  $(0 1 4)$ -direction can be reached at  $\lambda_n \approx 4.8 \text{ \AA}$ . In this geometry a magnetic moment in the  $\vec{b}$ -direction leads to non spin-flip scattering, which can be observed at  $K \approx 0.26$  for 0.1 and 5 T. In this experiment, in contrast to bulk  $\text{TbMnO}_3$ , the magnetic structure could not be switched from the  $bc$ -plane to the  $ac$ -plane by applying a magnetic field up to 5 T, which would result in a magnetic reflection in the spin-flip channel.

## 5.4.2 Soft x-ray resonant magnetic scattering

The strong resonance enhancement at the  $\text{MnL}_{-}$ ,  $\text{DyM}_{-}$  and  $\text{TbM}_{-}$  edges was used to perform resonant magnetic scattering experiments at the UE46-PGM-1 beamline of BESSY-II. The long wavelengths of  $\lambda_{\text{MnL}_{\text{III}}} \approx 19 \text{ \AA}$ ,  $\lambda_{\text{DyM}_{\text{V}}} \approx 7.4 \text{ \AA}$  and  $\lambda_{\text{TbM}_{\text{V}}} \approx 10 \text{ \AA}$  limits the available  $Q$ -range, so that no allowed crystal reflections can be reached to align the sample. The Tb and Dy 4f orbitals have a non spherical charge distribution, which breaks the mirror symmetry of the unit cell and cancels out some selection rules so that the  $(0 1 0)$  reflection gets allowed at the resonance (anomalous tensor or Templeton-Templeton scattering [119]). This fact allows the precise orientation of the crystal direction needed due to the low mosaicity of the films. **Figure 5.14** shows an example ( $\delta k 0$ ) scan with  $\sigma$  polarization, energy corresponding to  $\text{TbM}_{\text{V}}$  and  $\vec{Q}$  in the direction of the sample surface ( $\delta=0$ ) and with a small tilt between  $\vec{Q}$  and  $\vec{n}$  ( $0 < \delta < 10^{-3}$ ) to reduce the reflectivity part (**figure 5.15**).

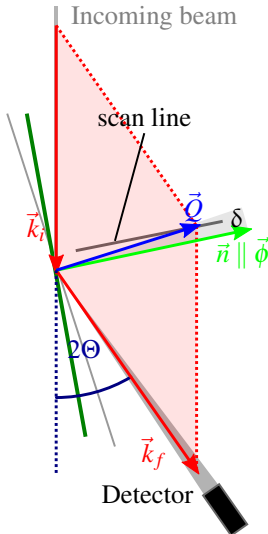
At elevated temperatures the absorption spectra around the  $\text{O K}_{-}$ ,  $\text{MnL}_{-}$ ,  $\text{DyM}_{-}$  and  $\text{TbM}_{-}$  edges were measured for both linear polarizations using TEY in  $\theta=90^\circ$  geometry. The measurements at the  $\text{O K}_{-}$  edge could be used to check the  $\phi$  alignment of the samples, as  $\text{TbMnO}_3$  and  $\text{DyMnO}_3$  show a large difference in the absorption spectrum for the light field oscillating



**Figure 5.14:** Reciprocal lattice scan in out-of-plane ( $Q_z$ ) direction on  $\mathbb{D}_{20}$  performed with  $\vec{Q}$  in the direction of the surface normal (Specular) and with a slight offset (Off-Specular). The (0 1 0) reflection and its Laue oscillations were simulated with the same model used for the laboratory XRD experiments (see [section 3.5.7](#) and [2.4.2](#)) including surface roughness and x-ray absorption. ( $d=18.4(5)$  nm,  $\sigma=0.3(9)$  nm,  $b=5.82(1)$  Å)

in the  $\vec{a}$ - and  $\vec{c}$ -directions. This effect has been measured for bulk TbMnO<sub>3</sub> single crystals [30] and was explained with anisotropic bonds between oxygen and manganese. As can be seen in [figure 5.16a](#) especially the sharp feature around 530 eV and the split peak at 535 eV can be used to distinguish both crystal directions. From theoretical calculations [30] the features can be attributed to hybridizations to the following orbitals:

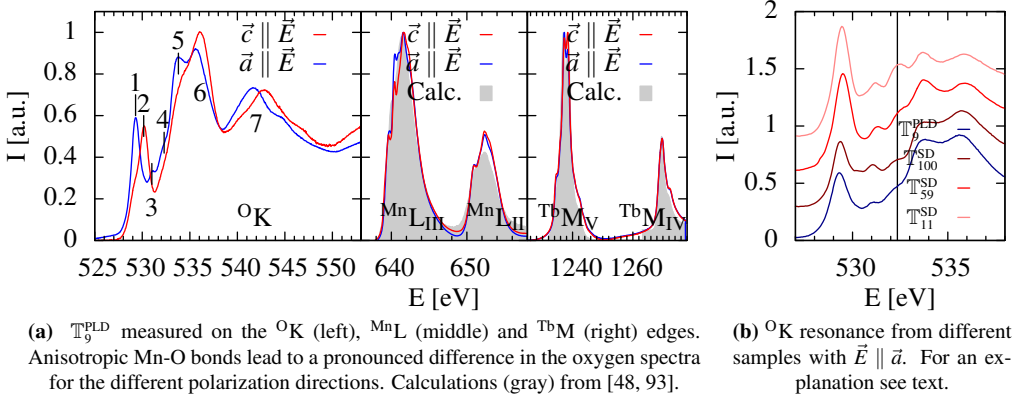
| 1                  | 2,3                                     | 4                    | 5,6     | 7                    |
|--------------------|---|----------------------|---------|----------------------|
| Mn $e_{g\uparrow}$ | Mn $t_{2g\downarrow} + e_{g\downarrow}$ | Mn $e_{g\downarrow}$ | Tb $5d$ | Mn $4sp$ and Tb $6s$ |



**Figure 5.15:** Scan geometry

The spectrum of the  $\text{TbM}$ -edges fits the calculations in [48] and the  $\text{MnL}$  absorption reproduces the  $\text{Mn}^{3+}$  spectrum published by Paterson et al. [93] quite well. (The experimental data on bulk TbMnO<sub>3</sub> [30] comes even closer to the measured Mn spectrum.) For the later produced samples, which had disoriented crystallites in the substrate ([section 5.1/section A.3](#)), the oxygen spectra show an increase of the intensity of some features [figure 5.16b](#) because of parts of the layer with  $\vec{b}$  oriented in-plane. The measured absorption spectra were used to determine the resonance energies for the scattering experiments.

The long wavelength of the Mn resonance limits the search for magnetic order as the available  $Q$ -range is  $\lesssim 0.75 \text{ Å}^{-1}$ . Thus the propagation vector of the manganese order found by neutron diffraction ( $0 \tau_{Mn} 1$ ) (A-type) with  $0.9 \text{ Å}^{-1}$  cannot be reached. The magnetic order can be described as a propagating SDW/cycloid in the  $\vec{b}$ -direction with periodicity  $\tau_{Mn}$  and an antiferromagnetic stacking in  $\vec{c}$ -direction. For a perfect collinear SDW and proper cycloid the  $(0 \tau_{Mn} 0)$  (F-type) peak, corresponding to the periodicity of the magnetic order in  $\vec{b}$ -direction, is forbidden



**Figure 5.16:** X-ray absorption near edge structure (XANES) from  $\text{TbMnO}_3$

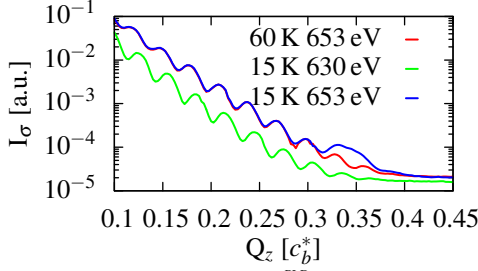
as the magnetic moment averaged in  $\vec{c}$ -direction is zero. It has been found experimentally, that there is a small F-type component in the magnetic structure, which was recently explained by a Dzyaloshinsky-Moriya interaction induced spin canting leading to a SDW component with magnetization in  $\vec{c}$ -direction and a so called off-phase synchronized bc-cycloidal for the low temperature phase [64]. Because of this, the soft x-rax magnetic scattering at  $(0 \tau_{Mn} 0)$  can be used to measure the c-component of the SDW and the off-phase bc-component of the cycloid.

To distinguish the SDW from the cycloidal magnetic order, the samples were mounted with  $\vec{c}$  perpendicular to the scattering plane. In this geometry the selection rules for x-ray magnetic scattering for the magnetic moments in  $\vec{c}$  leads to intensity in the  $\pi\pi'$  and for moments in the ab-plane in the  $\sigma\pi'$  and  $\pi\sigma'$  channels [28]. Although the instrument does not analyze the polarization, magnetic signals measured with  $\sigma$  polarization can only be present for magnetic moments in the ab-plane, while the  $\pi$  polarized beam can be used to search for any magnetic order (see equation 5.2)<sup>5</sup>. As the sample surfaces are cut in the ab-plane, the reflectivity of the surface lies in the  $(0 k 0)$ -direction. To be able to measure low intensity signals, a small offset  $\delta$  was used to reduce the reflectivity signal by two orders of magnitude, as the crystal mosaicity is much wider than the reflectivity (figure 5.14).

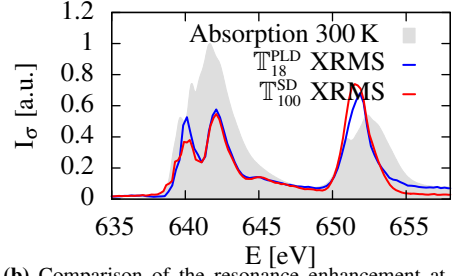
For all investigated samples except  $\text{T}_2^{\text{PLD}}$  a magnetic peak has been found. figure 5.17 shows an example of magnetic scattering measured at 15 K. The reciprocal space scan figure 5.17a compares the  $\pi$  incident measurements above the ordering temperature, at 15 K below the resonance and the resonant scattering. It is obvious, that the peak at  $(0 0.34 0)$  is only present below the ordering temperature and at the  $\text{Mn L}$ -edge. The comparison of both resonant measurements show, that the background from reflectivity is independent of temperature and is subtracted to extract the pure magnetic signal for all later plots. The resonant nature of the magnetic signal was further investigated by a constant  $\vec{Q}$  energy scan at the peak position shown in figure 5.17b. The peaks for  $\text{T}_{18}^{\text{PLD}}$  and  $\text{T}_{100}^{\text{SD}}$  are clearly of resonant nature. There is

<sup>5</sup>This only holds for measuring magnetization at a dipole transition. As no contributions of quadrupole transitions were reported in earlier measurements on bulk  $\text{TbMnO}_3$  and  $\text{DyMnO}_3$  [64, 107] this was assumed for the data evaluation on the thin films, too.



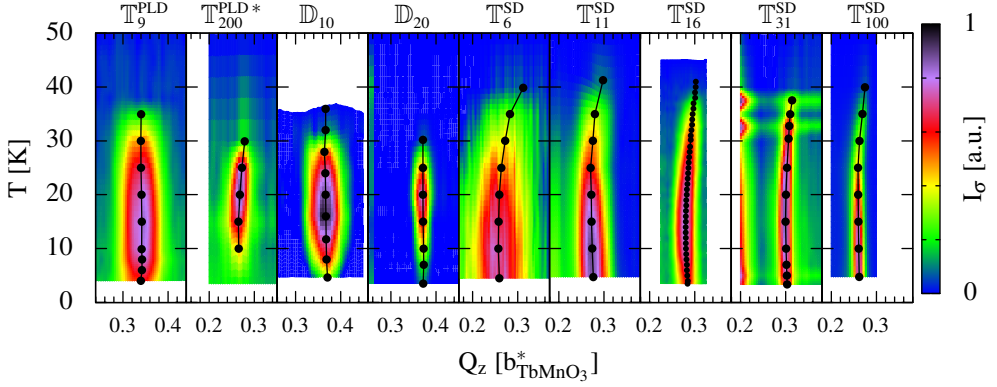


(a) Reciprocal lattice scans on  $T_{18}^{\text{PLD}}$  above the magnetic ordering temperature on the resonance, below the ordering temperature below the resonance and with magnetic peak in resonance.

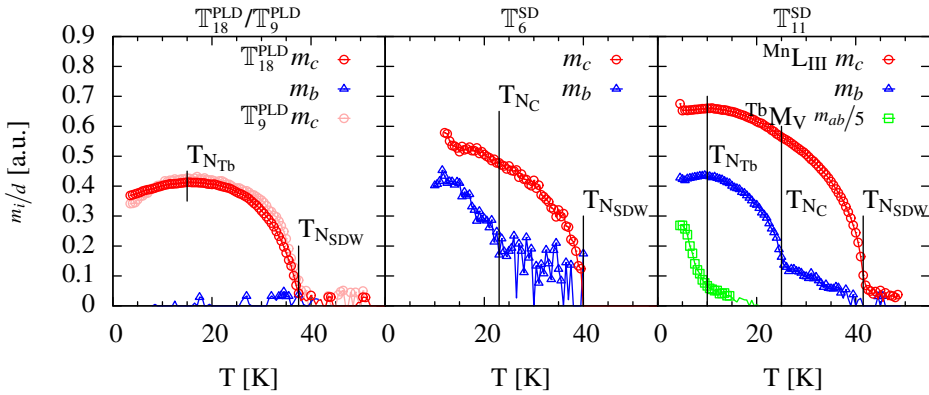


(b) Comparison of the resonance enhancement at the magnetic ( $\delta \tau_{Mn} 0$ )-peak for PLD and sputter samples with the absorption measured at room temperature.

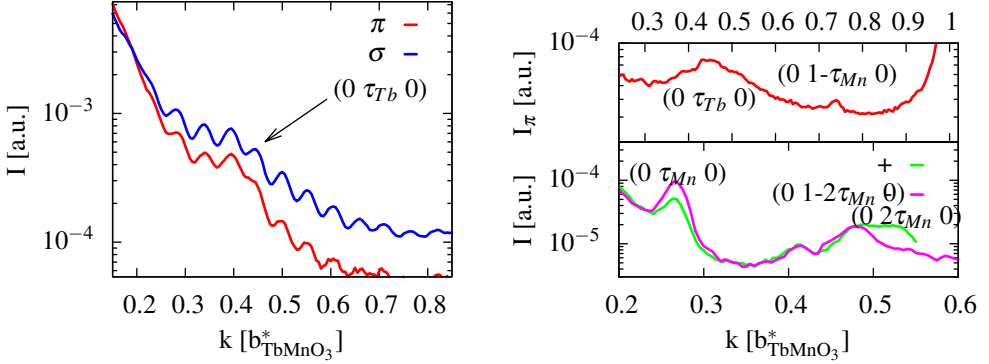
**Figure 5.17:** Resonant magnetic scattering at the  $\text{MnL}_{\text{III}}$ -edge with  $\sigma$ -polarization



**Figure 5.18:** Temperature dependence of the ( $\delta \tau_{Mn} 0$ ) reflection of several films, measured at the  $\text{MnL}_{\text{III}}$  resonance with  $\sigma$ -polarization. The fitted peak positions from each measured temperature are indicated with the black dots. For the PLD samples (except  $T_{200}^{\text{PLD}*}$  with wrong stoichiometry) there is no noticeable shift in the peak positions in contrast to the sputter samples on the right side.



**Figure 5.19:** Magnetic order parameter per film thickness extracted from ( $\delta \tau_{Mn} 0$ ) on  $\text{MnL}_{\text{III}}$  and ( $\delta \tau_{Tb} 0$ ) on  $\text{TbM}_{\text{IV}}$  peak intensities versus temperature. The PLD samples do not show the transition to a cycloidal magnetic structure  $T_{Nc}$  in contrast to the films deposited with sputtering.



(a) Measurements on  $\mathbb{T}_{11}^{\text{SD}}$  at the  $\text{TbMnO}_3$ -edge for both polarizations at 4 K, the broad reflection at  $(\delta \tau_{Tb} 0)$  is superimposed with the reflectivity background

(b) Reciprocal lattice scans on  $\mathbb{T}_{100}^{\text{SD}}$  at the  $\text{TbMnO}_3$ - (top) and  $\text{MnL}_{\text{III}}$ -edges showing additional peaks from the manganese order.

**Figure 5.20:** Resonant magnetic scattering showing the ordering of the Tb-subsystem at  $(0 \tau_{Tb} 0)$ , coupling from the Tb- to the Mn-order and second harmonic reflections at  $(0 2 \tau_{Mn} 0)$  and  $(0 1-2 \tau_{Tb} 0)$

a prominent difference between the structure of the XRMS signal and the absorption, which reflects the specific selection rules for the transitions involved in the magnetic state in contrast to the full spectrum of the absorption edge.

The temperature dependence of  $I_\pi$  for the investigated samples is shown in **figure 5.18**. The maps show the background subtracted measured intensity against the reciprocal space position and temperature. Each  $\vec{Q}$ -scan has been fit with a Gaussian and the positions are shown in the plot as black points. The peak widths stay constant below the transition temperature and correspond to a magnetic order with a correlation length  $>2/3$  of the film thickness<sup>6</sup>. The behavior of the sputter deposited samples is very similar with  $T_{\text{NSDW}}$  slightly above 40 K and a clear temperature dependent peak position. This is well known from bulk  $\text{TbMnO}_3$  and the propagation  $\tau_{Mn} \approx 0.28$  (except for  $\mathbb{T}_{31}^{\text{SD}}$ ) corresponds to the bulk values, too. For the PLD samples the transition temperatures are lowered. The peaks appear at positions different from bulk and there is no significant change in peak positions. At lower temperatures the intensity of all peaks decreases again, which was attributed to the  $T_{\text{NTb}}$  and  $T_{\text{NDy}}$  order, below which the rare earth moments do no longer support the Mn order.

The polarization dependence was used to extract the magnetic order parameter, as the maximum site specific local magnetic moment  $m_i$  is related to the measured intensity (assuming purely dipolar transitions and a T-independent transition matrix element):

$$I_\sigma \propto |S_{\sigma\sigma'}|^2 + |S_{\sigma\pi'}|^2 \quad I_\sigma \propto |S_{\pi\pi'}|^2 + |S_{\pi\sigma'}|^2 \quad (5.1)$$

$$[7] \quad I_\sigma \propto m_a^2 \cos^2(\theta) + m_b^2 \sin^2(\theta) \quad I_\pi \propto m_a^2 \cos^2(\theta) + m_b^2 \sin^2(\theta) + m_c^2 \sin^2(2\theta) \quad (5.2)$$

$$\xrightarrow{m_a=0} \quad m_b \propto \frac{\sqrt{I_\sigma}}{\sin(\theta)} \quad m_c \propto \frac{\sqrt{I_\pi - I_\sigma}}{\sin(2\theta)} \quad \left| \quad \xrightarrow{m_a=?} \quad m_{ab} \propto \sqrt{I_\sigma} \quad (5.3) \right.$$

<sup>6</sup>The correlation length is limited due to the large absorption ( $\lesssim 100$  nm), especially for large film thicknesses.

These magnetization components were extracted from the measured intensities on the <sup>Mn</sup>L<sub>II</sub>-edge at ( $\delta \tau_{Mn} 0$ ) and are shown in **figure 5.19**. For comparison the results are scaled with the inverse film thicknesses. For some samples it was even possible to measure the Tb order on <sup>Tb</sup>M<sub>V</sub> with moments in the ab-plane at ( $\delta \tau_{Tb} 0$ ) ( $\tau_{Tb} \approx 0.42$ , see **figure 5.20** for  $\mathbb{T}_{11}^{SD}$  and  $\mathbb{T}_{100}^{SD}$ ). All samples exhibit a magnetic order in  $\vec{c}$  at  $T_{NSDW}$ , which corresponds to the F-type spin canting of the SDW with primary spin orientation in  $\vec{b}$ . Only the sputter samples show an additional transition  $T_{NC}$ , where a  $\vec{b}$  component develops. This behavior perfectly agrees with the F-type component of the off-phase cycloid, as measured on bulk TbMnO<sub>3</sub> [64]. The Tb transition measured for  $\mathbb{T}_{11}^{SD}$  proves the association of the decrease in Mn order with the Tb antiferromagnetic order below  $T_{NTb}$ . For the sample with the strongest magnetic scattering  $\mathbb{T}_{100}^{SD}$  additional ( $0.2\tau_{Mn} 0$ ) and ( $0.1-2\tau_{Mn} 0$ ) peaks have been observed, which originate from the third term in equation 2.60 and thus have a different polarization dependence. In the cycloidal phase a weak reflection at ( $0.1-\tau_{Mn} 0$ ) appears at the <sup>Tb</sup>M<sub>V</sub> resonance as evidence for the coupling of the Tb spins to the Mn ordering (**figure 5.20b**).

The pure existence of  $m_b$  and  $m_c$  magnetization components is no direct proof for the cycloidal magnetic structure. For this the helicity of the magnetic components can be probed with circular polarized x-rays due to the magnetic structure factor [39, 86]. The intensity of the resonant magnetic scattering with circular polarization can be written as:

$$I_{\pm} = 1/2 (|S_{\sigma\sigma'}|^2 + |S_{\pi\pi'}|^2 + |S_{\sigma\pi'}|^2 + |S_{\pi\sigma'}|^2) \pm \Im(S_{\sigma\sigma'}S_{\pi\sigma'}^* + S_{\sigma\pi'}S_{\pi\pi'}^*) \quad (5.4)$$

In most cases the second term vanishes and both circular polarizations have equal intensity as the average of  $I_{\sigma}$  and  $I_{\pi}$ . The interference structure factors for the different chirality ( $\odot$  and  $\ominus$ ) cycloids can be derived from the resonant magnetic scattering form factor [86] of the corresponding magnetic moments  $\vec{m}_j$  presented in **section 2.4.5**:

$$\xrightarrow{\text{equation 2.60}} f_j^{XRMS} = -i\frac{3}{4}r_e(\hat{e}_i \times \hat{e}_f) \cdot \hat{m}_j[F_{11} - F_{1-1}] \quad (5.5)$$

$$\vec{m}_j = m \begin{cases} \hat{b} \cdot \cos(\vec{\tau}\vec{r}_j) + \hat{c} \cdot \sin(\vec{\tau}\vec{r}_j) = \frac{1}{2} \left( \hat{e}_{\mp} e^{i\vec{\tau}\vec{r}_j} + \hat{e}_{\pm} e^{-i\vec{\tau}\vec{r}_j} \right) & \text{for } \odot \\ \hat{b} \cdot \cos(\vec{\tau}\vec{r}_j) - \hat{c} \cdot \sin(\vec{\tau}\vec{r}_j) = \frac{1}{2} \left( \hat{e}_{\mp} e^{i\vec{\tau}\vec{r}_j} - \hat{e}_{\pm} e^{-i\vec{\tau}\vec{r}_j} \right) & \text{for } \ominus \end{cases} \quad (5.6)$$

$$\text{with} \quad \hat{e}_{\pm} = \hat{b} + i\hat{c} \quad \text{and} \quad \hat{e}_{\mp} = \hat{b} - i\hat{c} \quad (5.7)$$

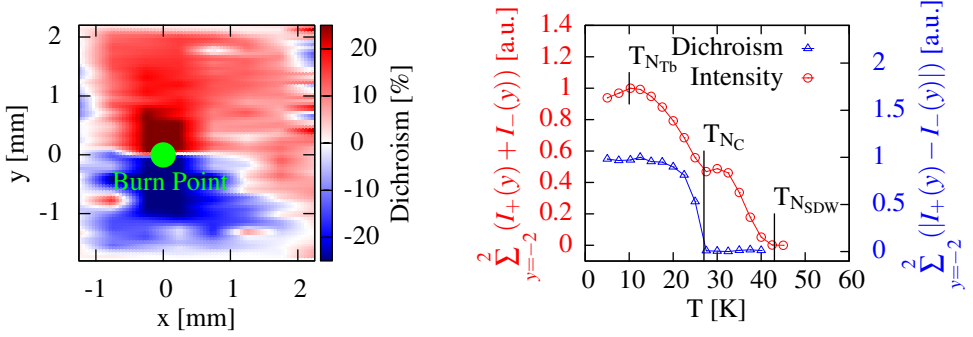
The polarization terms in equation 5.5 are  $\hat{\sigma}' \times \hat{\sigma} = 0$ ,  $\hat{\pi}' \times \hat{\pi} = \hat{c}$ ,  $\hat{\sigma}' \times \hat{\pi} = \hat{k}_i$  and  $\hat{\pi}' \times \hat{\sigma} = -\hat{k}_f$ . From this one derives the magnetic structure factors and the intensity for the cycloidal domains by summing over all magnetic moments:

$$S_{e;e_j}^{XRMS} = \sum_j -i\frac{3}{4}r_e(\hat{e}_i \times \hat{e}_j) \cdot \hat{m}_j[F_{11} - F_{1-1}] \quad (5.8)$$

$$\xrightarrow{[86]} \text{equation 5.2 and } I_{\pm} \propto \begin{cases} \sin^2(\theta) + \frac{1}{2}\sin^2(2\theta) \mp \sin(\theta)\sin(2\theta) & \text{for } \odot \\ \sin^2(\theta) + \frac{1}{2}\sin^2(2\theta) \pm \sin(\theta)\sin(2\theta) & \text{for } \ominus \end{cases} \quad (5.9)$$

Depending on the chirality of the magnetic structure, the sign of the circular dichroism is changed. Collinear magnetic structures, on the other hand, do not produce any dichroism through the structure factor<sup>7</sup>.

<sup>7</sup>Magnetic dichroism through XMCD is still possible for collinear structures.



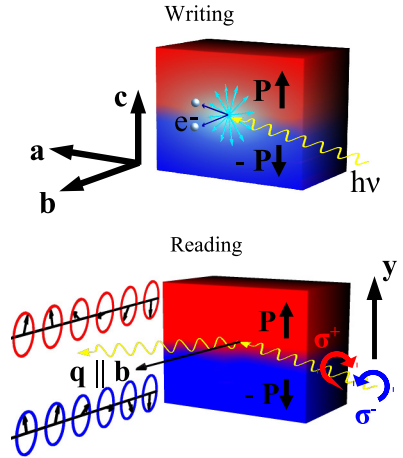
(a) Dichroism measured over the whole sample area at 5 K. There are two large domains separated by a sharp domain wall at  $y=0$ . The strength of the dichroism decreases with the distance to the burn point at 0.

(b) Temperature dependence of the dichroism. The sum and absolute differences of intensities  $I_+$  and  $I_-$  for  $y$ -scans at each temperature are shown, normalized to the maximum.

**Figure 5.21:** X-ray circular dichroism of  $\mathbb{T}_{100}^{\text{SD}}$  at  $(\delta \tau_{\text{Mn}} 0)$  at  $\text{MnL}_{\text{II}}$

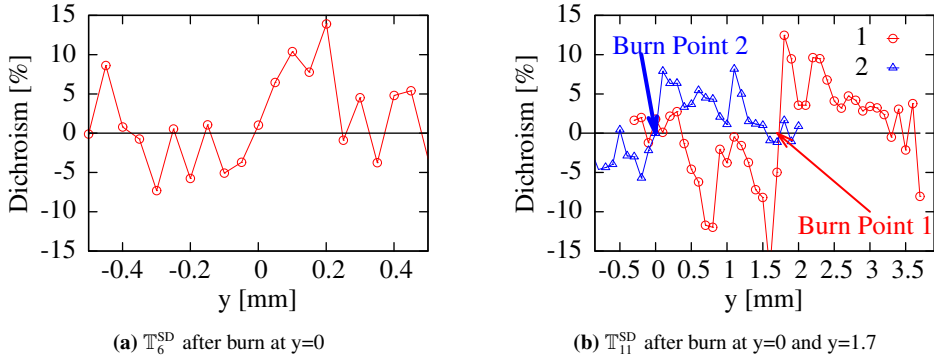
To proof the cycloidal magnetic order, the circular dichroism on a single domain needs to be measured. For samples with low electric conductivity the photoelectric ionization at an absorption edge can be used to generate a charged area at the beam footprint while cooling the sample. At this position the ferroelectric domains will have a domain wall with the adjacent polarization pointing away from the positive charge. Below the transition temperature a lower intensity circular beam can be used to measure the domains above and below the "burn point" (**figure 5.22**), as has been done for  $\text{DyMnO}_3$  bulk crystals [107].

Circular dichroism was measured for  $\mathbb{T}_6^{\text{SD}}$ ,  $\mathbb{T}_{11}^{\text{SD}}$  and  $\mathbb{T}_{100}^{\text{SD}}$ . The written domains are more stable than for the bulk  $\text{DyMnO}_3$  samples, making it possible to measure without attenuation of the beam. **figure 5.21a** shows the spatial resolved dichroism  $\frac{I_+ - I_-}{I_+ + I_-}$  of  $\mathbb{T}_{100}^{\text{SD}}$ , calculated from two  $xy$ -meshes with circular polarization. There are only two large domains on the whole sample area of  $5 \times 5 \text{ mm}^2$  and the intensity of the dichroic signal decreases with the distance to the burn point. The magnetic intensity varies over the sample area as result of the imperfect substrate and low intensity positions could be correlated to areas with higher amount of wrong crystallites by 4-circle measurements (see **section A.3**). The temperature dependence of the dichroism and the magnetic intensity was measured by  $y$ -scans over the phase boundary. For the measured points at each temperature the absolute value of the dichroism and the full magnetic signal were summed up and are plotted in **figure 5.21b**.



**Figure 5.22:** Schematics of domain writing with the photoelectric effect and reading via circular dichroism taken from [107]

The measurements on  $\mathbb{T}_6^{\text{SD}}$  and  $\mathbb{T}_{11}^{\text{SD}}$  are shown in **figure 5.23**. For the thinner films the lower



**Figure 5.23:** y-scans of x-ray circular dichroism at  $(\delta \tau_{Mn} 0)$  at  $MnL_{III}$ . The error bars cannot be extracted from the measured data, as they are range dependent (described in [section 3.5.3](#)).

magnetic signal complicates the measurement and the substrates of these samples turned out to have even more imperfections. Nevertheless both samples show a clear switch of the dichroism sign at the domain boundary. Cooling the sample with the beam at different positions clearly changes the position of the domain wall (**figure 5.23b**). Writing domains in the ordered state as possible in bulk [107] was not found due to very stable domains, only depolarization of domains far away (4 mm) from the burn point (close to one edge of the sample) was observed by two subsequent measurements.

These investigations do not only proof the cycloidal magnetic order in the films, but can only be explained, if the magnetic structure is coupled to a ferroelectric polarization, as there would not be any influence of the x-ray beam on the domain structure without ferroelectric polarization.

## 5.5 Summary

Samples of TbMnO<sub>3</sub> and DyMnO<sub>3</sub> have been produced by PLD and sputter deposition. All samples show untwinned epitaxial growth with very good crystal quality (mosaicity  $< 0.02^\circ$ ). The surface roughnesses were reasonably low in the order of 0.5 nm. For all samples the x-ray reflectivity could be simulated with an adapted model including surface layers with reduced density ([section 5.1.2](#)), which is explained by non-Gaussian roughness ([section 5.1.3](#)). The overall thickness inhomogeneity is much higher (some %) for the PLD samples than for sputter deposition, but is not important for the local quality of the films (crystal structure and roughnesses). The crystal structure of the films is strained to the substrate even for large layer thicknesses of 100 nm ([section 5.1.4](#)). The Laue oscillations of the layer (0 2 0) reflection could be modeled and yield a comparable thickness as the reflectivity reduced by a small layer of undefined crystal structure ( $\approx 1.5$  nm).

The magnetic and ferroelectric behavior of the samples was studied in detail with macroscopic and microscopic methods. The SQUID magnetometry ([section 5.2](#)) could show a

weak ferromagnetism developing below  $T_{\text{NSDW}}$ . For a few samples even  $T_{\text{NC}}$  and  $T_{\text{NTb}}$  could be estimated from small kinks in the magnetization curves. Due to impurities in the substrate, leading to large paramagnetic and ferromagnetic background, not all samples could be measured. The microscopic magnetism measured with neutron diffraction and resonant magnetic scattering show a antiferromagnetic order below  $T_{\text{NSDW}}$  comparable to the bulk behavior. The transition temperatures and propagation vectors for the PLD samples don't always fit to the bulk values and don't show a temperature dependence, which can be interpreted as sign for commensurability. For these samples the transition to the cycloidal magnetic order seems not to be present, as the second magnetic component was not measured. Thus these samples cannot be ferroelectric. For three sputter samples the transition to the cycloidal state has been observed directly with circular dichroic XRMS (**section 5.4.2**), proving the ferroelectricity for these samples. For the 100 nm  $\text{TbMnO}_3$  film the macroscopic ferroelectricity could be confirmed using SHG (**section 5.3**).

The quality of the sputter samples is reduced due to imperfections in the substrates, which could be directly correlated by position dependent XRMS and 4-circle diffraction measurements **section A.3**. Although the structural quality of the PLD and sputter samples are almost equal, there is a substantial difference in their properties. The origin of this is yet unclear, but could be the chemical purity of the films<sup>8</sup>, which is very challenging to detect. The higher stability of the multiferroic domains in the thin films compared to bulk can be explained by the lower lying domains in bulk samples, which will not be poled by the photon beam making the poled domains easier switchable. To finalize the study of multiferroic manganite thin films, additional resonant x-ray measurements on sputtered  $\text{DyMnO}_3$  and  $\text{HoMnO}_3$  samples should be performed, especially to investigate the influence of the rare earth moments.

$\text{TbMnO}_3$  deposited on  $\text{YAlO}_3$  substrates has thus been proven to be multiferroic with a behavior almost exactly following the bulk properties. The cycloidal magnetic order is present up to film thicknesses below three periods of the spin spiral with only slightly reduced transition temperatures. The only prominent difference to the bulk behavior is the higher ordering temperature of the Tb moments ( $T_{\text{NTb}} \approx 10 \text{ K}$ ) and the reduction of the ferroelectricity and Mn magnetic order below this temperature. For the not multiferroic PLD samples this temperature is even higher and could be one reason for the inhibited cycloidal state. Due to these properties the system is very well suited to study interface effects of  $\text{TbMnO}_3$  to any other material, as the substrate does not have a significant influence on the film properties.

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<sup>8</sup>E.g. the oxygen used for the pulsed laser deposition could be less pure with regard to contaminations.



# Chapter 6

## Experiments II: $\text{LaCoO}_3$ Thin Films and $[\text{TbMnO}_3\text{-LaCoO}_3]\text{-Multilayers}$

For applications of multiferroic materials an antiferromagnetic structure will not be suitable, because it is not very sensitive to a magnetic field (for e.g. sensors) and does not have a spontaneous macroscopic magnetization. Because of this a strong coupling of such materials will be needed, which we investigated by introducing interfaces to a ferromagnetic compound with similar (Perovskite) crystal structure. The data shown in this chapter was taken for a  $\text{LaCoO}_3$  single layer sample  $\mathbb{L}_{35}$  with 35 nm thickness and 4 nominally identical multilayers of 20 repetitions with 2 nm  $\text{LaCoO}_3$  and 10 nm  $\text{TbMnO}_3$  layers ( $\mathbb{T}\mathbb{L}_{\times 20}^{18/3}$ ) created with PLD.

### 6.1 Structural characterization

The structure of the  $\text{LaCoO}_3$  layer was investigated with x-ray reflectivity and diffraction. Bulk  $\text{LaCoO}_3$  has a rhombohedral structure with  $a=b=c=5.38 \text{ \AA}$  and  $\alpha=\beta=\gamma=60^\circ$  unit cell. Although the bulk crystal structure of  $\text{LaCoO}_3$  differs from the orthorhombic substrate, the same deposition parameters as for the  $\text{TbMnO}_3$  layers lead to epitaxial growth with good quality. The reflectivity measurement **figure 6.3a** reveals 0.5 nm surface roughness and  $\approx 2\%$  thickness inhomogeneity for a 35 nm film. The crystal structure quality itself is proofed with the diffraction measurement **figure 6.3c** and could be simulated with the same roughness and (as for the  $\text{TbMnO}_3$  and  $\text{DyMnO}_3$  single layers) with 2 nm less thickness. The out-of-plane lattice constant was found to be  $5.38 \text{ \AA}$ , as in the bulk crystal. Diffraction from the (2 2 0) reflection (**figure 6.3c**) confirmed, that even 35 nm films are already relaxed.

Because of the fast relaxation of the  $\text{LaCoO}_3$  layers a small thickness of 3 unit cells was chosen for the multilayers with  $\text{TbMnO}_3$ . Reflectivity from the multilayers did not show any multilayer peaks due to the low contrast between  $\text{LaCoO}_3$  and  $\text{TbMnO}_3$  in addition to the thickness inhomogeneity. Therefore diffraction measured on the P09 beamline was used to get precise information on the multilayer structure (**figure 6.1a**). From the simulation the  $\text{LaCoO}_3$  layers have been found to be highly strained, as the out-of-plane lattice parameters of  $\text{LaCoO}_3$  and  $\text{TbMnO}_3$  were deduced as  $5.7 \text{ \AA}$  and  $5.75 \text{ \AA}$ . This can be explained by looking at the crystal structure of distorted Perovskites shown in **figure 6.1b**. The rhombohedral and orthorhombic unit cells can be traced back to the unit cell of the undistorted cubic structure. For the rhombohedral the lattice parameter is  $a_3 \approx \sqrt{2} \cdot a$  and for the orthorhombic cell the three



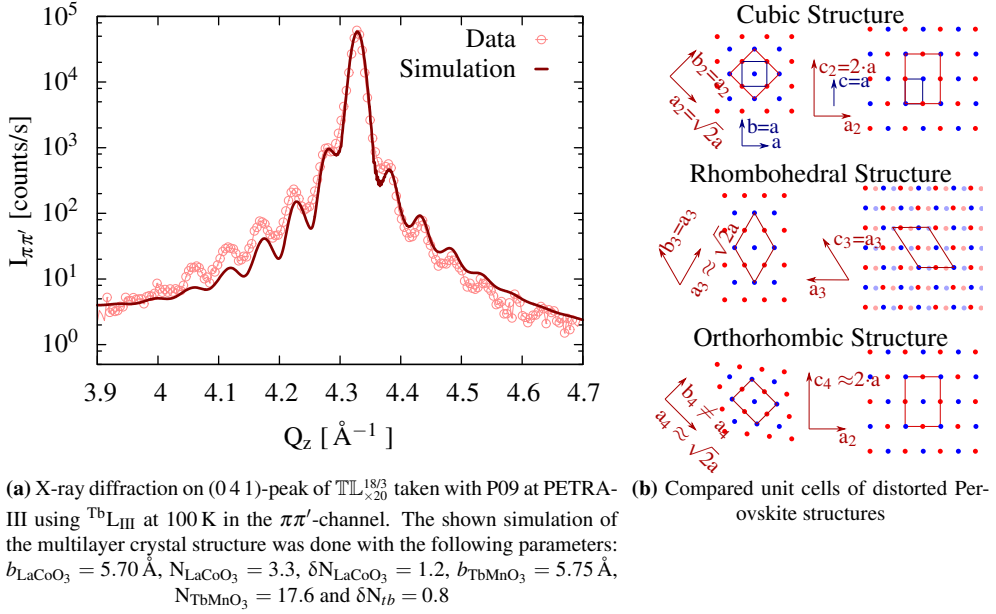


Figure 6.1

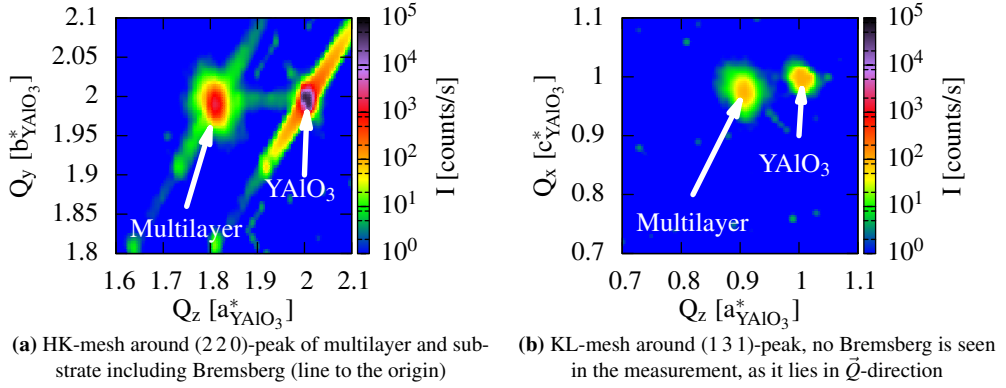
lattice parameters are  $a_4 \approx \sqrt{2} \cdot a \approx b_4$  and  $c_4 \approx 2 \cdot a$ . Constructing a notional orthorhombic unit cell from the LaCoO<sub>3</sub> bulk structure leads to lattice parameters  $a_4 = b_4 = 5.38 \text{ \AA}$  and  $c_4 = 7.61 \text{ \AA}$ . To match these parameters to the YAlO<sub>3</sub> surface, the  $a_4$  and mainly the  $c_4$  parameters need to be compressed, which leads to an elongation of  $b_4$ . Keeping the unit cell volume of the bulk LaCoO<sub>3</sub> structure of  $112 \text{ \AA}^3$  constant and setting the in-plane lattice parameters fixed to the YAlO<sub>3</sub> values  $a = 5.33 \text{ \AA}$  and  $c = 7.37 \text{ \AA}$ , one calculates an out-of-plane propagation vector of  $b = 5.70 \text{ \AA}$ .

Thus the LaCoO<sub>3</sub> structure is strongly distorted (strained to the substrate **figure 6.2a**) in the multilayer. The roughnesses are in the order of 0.6 nm and the average layer thicknesses are 3.3 unit cells for LaCoO<sub>3</sub> and 17.6 unit cells for TbMnO<sub>3</sub>. These parameters could be reproduced with diffraction data from the D8 instrument with limited quality. The roughnesses and the TbMnO<sub>3</sub> lattice parameter are similar to the single layer samples investigated previously.

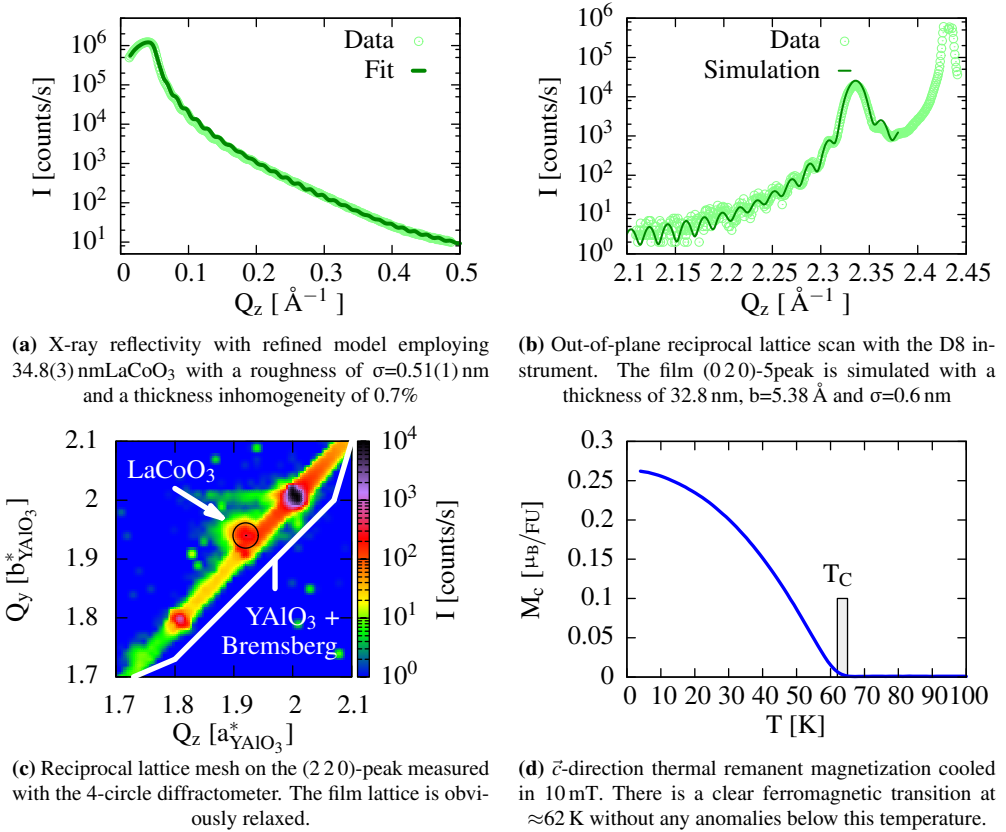
## 6.2 Macroscopic magnetization

### 6.2.1 SQUID magnetometry

The LaCoO<sub>3</sub> layer was investigated with SQUID magnetometry showing ferromagnetism below  $T_C \approx 62 \text{ K}$ . The magnetic moment per Co ion was calculated using the sample surface



**Figure 6.2:** X-ray diffraction reciprocal lattice maps on  $\text{TL}_{18/3}^{18/3}$  measured with the 4-circle diffractometer. The measurements in both in-plane directions show that the multilayer crystal structure is strained to the substrate.



**Figure 6.3:** XRD and SQUID measurements performed on  $\text{L}_{35}$

and measured thickness, which results in a systematic error of  $\approx 2\%$ . The thermal remanent magnetization in-plane is shown in **figure 6.3d** and has no sign for additional transitions below  $T_C$ . Although this behavior is not present in bulk LaCoO<sub>3</sub>, it is known for strained films on different substrates [42]. Although the films are fully relaxed in out-of-plane direction, the remanent magnetization is comparable to those samples investigated on other substrates. The small remanent magnetization can be explained by Co having the intermediate spin-state. The relaxation could reduce the effective magnetic layer thickness, leading to a further decrease of the magnetization.

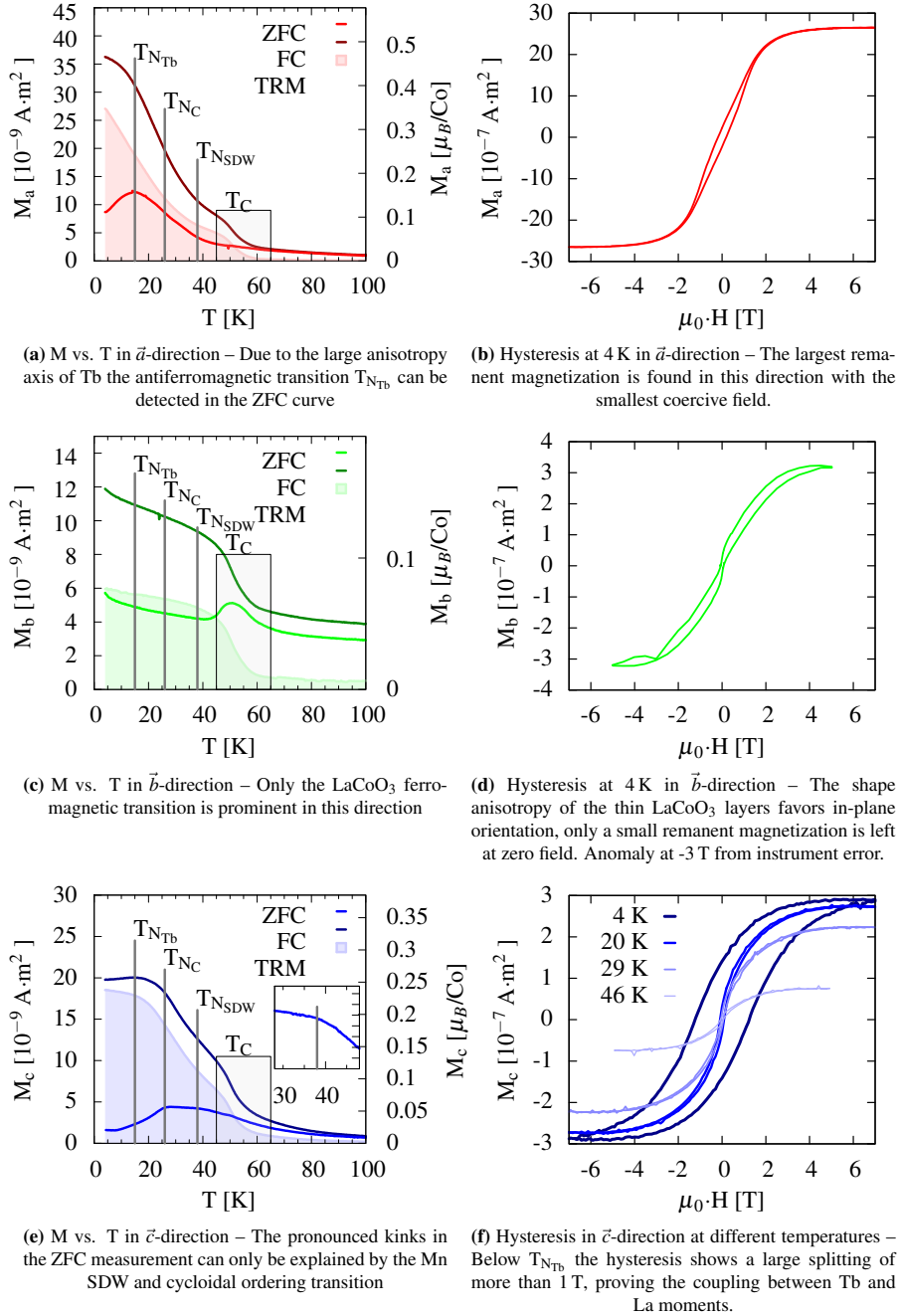
In contrast to the TbMnO<sub>3</sub> single layers the multilayer showed a reasonable magnetic signal due to the ferromagnetism of the LaCoO<sub>3</sub> layers. Temperature and field dependent magnetization measurements have been performed in all crystal directions and are depicted in **figure 6.4**. The systematic error on the moment per Co ion for these measurements is 5 – 10% due to the less precise thickness determination compared to the single layer. Field cooled measurements were performed in 10 mT before the corresponding thermal remanent magnetization. The sample shows a complex temperature dependence, different for each crystal direction. A broad ferromagnetic transition around 55-60 K is found in all crystal directions and attributed to the LaCoO<sub>3</sub> layers. Additional transitions due to the Mn order are most prominent in  $\vec{c}$ -direction as for the single layers. In contrast to the PLD single layers there is a trace of the cycloidal transition  $T_{N_C}$  in the zero field cooled measurement in  $\vec{c}$ . A transition attributed to Tb was found in  $\vec{a}$ -direction at 15 K.

The hysteresis measurements in all directions show a small ferromagnetic component with low coercive field below  $T_C$  in all directions. The remanent magnetization in  $\vec{c}$  increases to lower temperatures presumably due to the Tb paramagnetic moment. Below  $T_{N_{Tb}}$  the hysteresis shows a huge increase in coercive field as sign of a coupling between the ferromagnetic LaCoO<sub>3</sub> layers to the magnetic order, that sets in at  $T_{N_{Tb}}$ .

The interpretation of the different transitions below  $T_C$  need to be verified by microscopic magnetization measurements beyond the experiments in **section 6.3**.

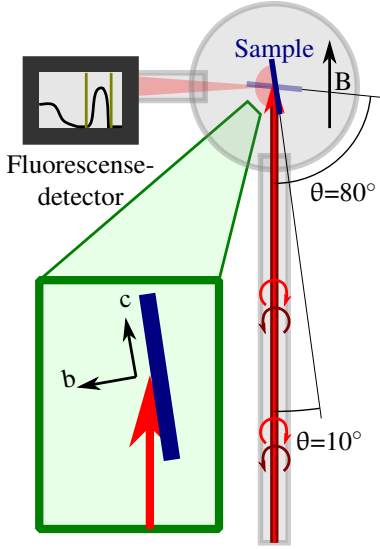
## 6.2.2 X-ray magnetic circular dichroism

To clarify the origin of the ferromagnetic order in the multilayer, XMCD at the <sup>Mn</sup>L-, <sup>Tb</sup>M- and <sup>Co</sup>L-edges has been measured at the beamline 4-ID of the APS. In addition to the multilayer sample a TbMnO<sub>3</sub> and LaCoO<sub>3</sub> single layer was measured as reference, too. In the used setup (**figure 6.5**) the magnetic field is applied in beam direction and the sample surface is illuminated with 10° and 80° incident angle to measure the in-plane and out-of-plane magnetization components, respectively. The resistance of the substrate and the multilayer below 50 K is much too high to measure the absorption with electron yield, therefore a fluorescence detector was mounted at  $2\Theta=90^\circ$ . For the total fluorescence yield a window of  $\approx 200$  eV width reaching up to the excitation energy was used to get rid of background from e.g. oxygen fluorescence. For strong fluorescence signals, as for Tb, the beam needed to be attenuated to 10%, still leaving a detector dead time of 5-15% near the peak. As the incident beams with right and left circular polarizations did not have the same intensity, the non linearity of the detector due to dead time effects lead to a XMCD "ghost" signal even without magnetization. To get rid of this effect, measurements with positive and negative field have been performed



**Figure 6.4:** SQUID magnetometry on  $Tl_{18/3} \times 20$ , all temperature dependent measurements were measured/cooled in 10 mT external field – Combining the temperature dependence of all crystal directions four transitions can be identified: The ferromagnetic order of LaCoO<sub>3</sub> at  $T_C$ , the spin-density wave transition of Mn at  $T_{N_{SDW}}$ , the cycloidal order transition at  $T_{N_C}$  and the Tb ordering temperature at  $T_{N_{Tb}}$ .

at 5 T and 0.1 T to extract this measurement artifact, which than could be used to correct the data taken at other fields. The extracted background signal for Tb is shown in **figure 6.6a** and has obviously no field dependence. No further corrections were applied to the TFY signal.



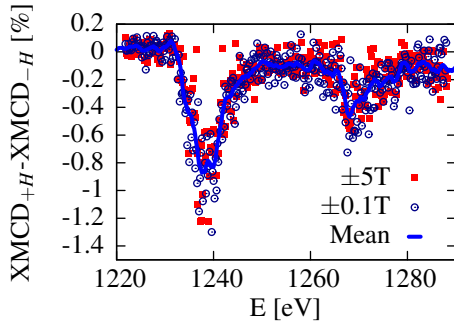
**Figure 6.5:** Setup used for XMCD

For the  $\text{LaCoO}_3$  reference sample the magnetic field was applied in-plane. The 10 K measurement is shown in **figure 6.6b**. There is only a small XMCD with comparable weight on the  $^{\text{Co}}\text{L}_{\text{III}}$  and  $^{\text{Co}}\text{L}_{\text{II}}$  edges, which has a remanent component of approximately 40%. Using the L-edge sum rules described in **section 2.4.5** one obtains the orbital and spin components of the magnetic moment by integrating over the two edges of the XMCD signal, shown in the graph **figure 6.6b** as blue and red regions, and dividing by the complete TFY signal over the number of holes (4 for Co, 3 for Mn and 6 for Tb). This formalism yields the magnetization components per ion directly from the measured absorption intensities and thus does not rely on any additional information about the samples (as e.g. elemental content). From this analysis no significant orbital moment was found while the spin components were  $S_z(0.1\text{ T}) = 0.074(2)$  and  $S_z(5\text{ T}) = 0.18(1)$ , corresponding to a remanent magnetization of  $\approx 0.15\mu_B$ .

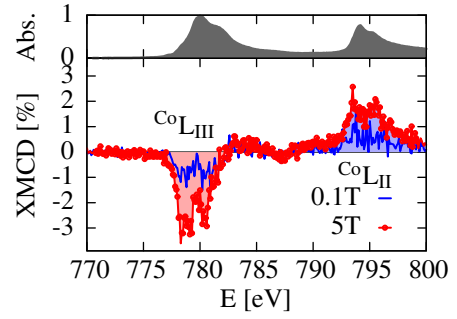
The multilayer sample was mounted with  $\vec{a}$  parallel to the incident beam and the magnetic field. The XMCD measurements were performed in different magnetic fields as shown in **figure 6.7**. The remanent and saturation moments were extracted as for the single layer sample and were found to be  $S_z(0.1\text{ T}) = 0.096(4)$  and  $S_z(5\text{ T}) = 0.543(2)$  with a orbital contribution of  $L_z(5\text{ T}) = 0.344(8)$ . About 50% of the cobalt ions are in the intermediate spin state, the remaining ions in the low spin configuration. The calculated remanent moment of  $\approx 0.21\mu_B$  is close to the values measured with SQUID thermal remanent magnetization of  $\approx 0.3\mu_B$ . The saturation and remanent moment measured on the multilayer is larger than for the single layer. A reasonable explanation for this effect is given by the crystal structure relaxation in the single layer, which lowers the magnetic moment especially close to the surface, where the XMCD signal is measured. The larger ratio between remanence and saturation for the multilayer can be interpreted as influence from the (rough) interfaces on the ferromagnetic coupling.

On the  $^{\text{Tb}}\text{M}$ -edge only a small magnetization was found at 6 K in 5 T with  $L_z = 0.063(4)$  and  $(S_z + 3 \cdot T_z) = 0.087(5)$  pointing to antiferromagnetic correlations. There is no measurable remanent magnetization on Tb.

For the manganese absorption edge it is not possible to directly extract the absorption from the TFY measurement, as there is a large self absorption of the fluorescence photons in the material, leading to non linear response and in addition the proximity to the oxygen edge makes it difficult to fit the right energy window for the Mn fluorescence. Therefore a method proposed by Achkar et al. was applied [16]. The fluorescence detector window was set on the

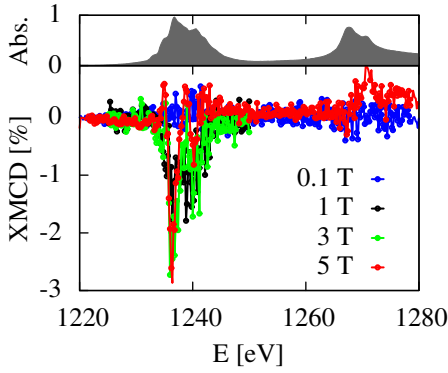


(a) XMCD background at 10 K at  $\text{TbM}$ -edge due to saturation effects in the fluorescence detector

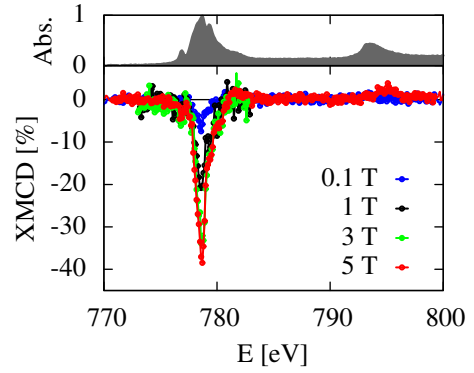


(b)  $\text{CoL}$  XMCD of  $\text{Tl}_{35}$  at 10 K in 0.1 T and 5 T with the associated TFY absorption.

**Figure 6.6**

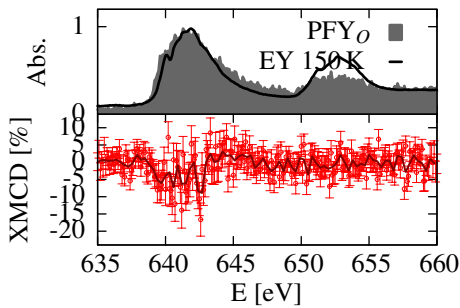


(a)  $\text{TbM}$ -edge

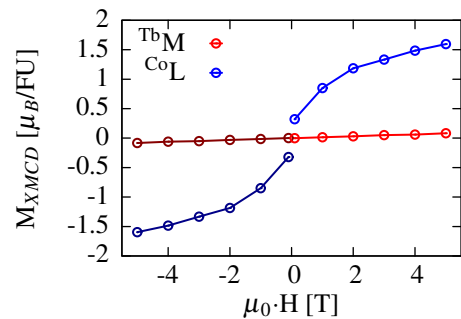


(b)  $\text{CoL}$ -edge

**Figure 6.7:** Field dependent XMCD measurements on  $\text{Tl}_{18/3}^{18/20}$  with corresponding absorption measured at 10 K. The 0.1 T and 5 T data was averaged from positive and negative field measurements.



(a)  $\text{MnL}$ -edge XMCD extracted from  $\text{O}_2$ -fluorescence data at 6 K,  $\pm 5$  T



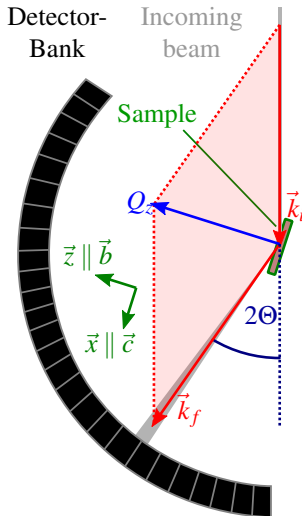
(b) Field dependent magnetization of  $\text{Tl}_{18/3}^{18/20}$  at 10 K approximated from data of **figure 6.7**

**Figure 6.8**

oxygen emission energy to measure the non resonant photo absorption inside the material. As the absorption coefficient far from the oxygen edge does not change very much over this small energy range, the oxygen ions can be used to measure the intensity of the direct beam inside the sample without strong self absorption effects. The reduced transmission at the <sup>Mn</sup>L-edge reduces the penetration depth of the incident beam and thus leads to lower intensity. It was shown, that the measured intensity is inverse proportional to the absorption of another element. **figure 6.8a** shows the absorption and XMCD signal around the Mn edge at 10 K, 5 T extracted with this method. Although the statistics are much lower than for the other edges, a clean absorption spectrum could be extracted. There is no measurable remanent magnetization on manganese and the orbital and spin contributions are low even at 5 T ( $L_z = 0.12(3)$  and  $S_z = 0.04(1)$ ).

The cobalt saturation and remanent magnetization was also measured with the incident beam in  $\vec{b}$ -direction. Although the penetration depth with normal incidence is higher, no significant remanent moment was found. The easy magnetic axis thus is lying in-plane, as is expected for thin magnetic layers. The 5 T measurements yielded  $L_z = 0.16(4)$  and  $S_z = 0.192(8)$ . The orbital moment is quenched less than measured in  $\vec{a}$ -direction, which could be a result of the adjacent TbMnO<sub>3</sub> layers, which reduce the in-plane orbital moment contribution.

A field dependence of the approximated magnetization<sup>1</sup> of Tb and Co is plotted in **figure 6.8b**, showing ferromagnetic behavior for Co and paramagnetism for Tb. Thus the macroscopic magnetization is governed by the LaCoO<sub>3</sub> ferromagnetism, which couples to the Tb and Mn moments. Although the Tb magnetization per ion is lower than for Co, the difference in layer thickness can lead to a reasonable enhancement of the magnetization by the Tb moments especially above  $T_{N_{Tb}}$ .



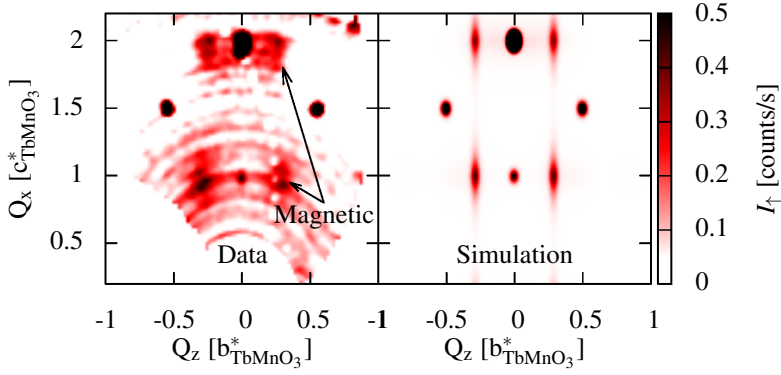
**Figure 6.9:** Setup of PND

## 6.3 Microscopic magnetization

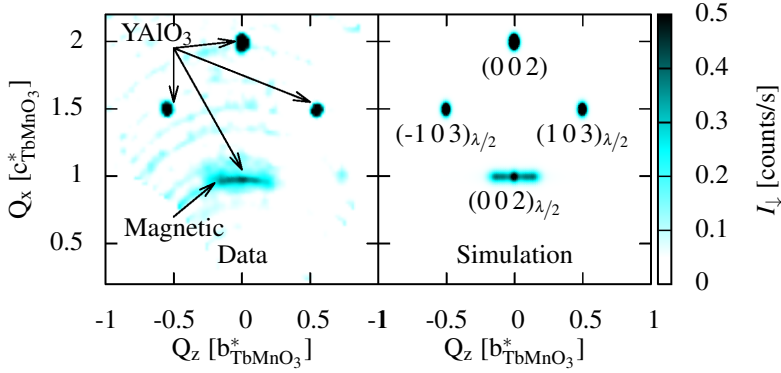
### 6.3.1 Polarized neutron diffraction

The magnetic order of a stack of four samples was measured with polarized neutron diffraction at the DNS instrument. The samples were mounted with the  $\vec{a}$  axis parallel to the neutron polarization and perpendicular to the scattering plane (see **figure 6.9**), cooled down to 4 K and the spin-flip and non spin-flip intensities have been measured (**figure 6.10**). The measurement shows a strong deviation from the measurements on TbMnO<sub>3</sub> single layers shown in **section 5.4.1**. The magnetization in the bc-plane measured in spin-flip shows only a short range order in out-of-plane direction (broad peak in  $Q_z$ ) with a long range antiferromagnetic stacking in the  $\vec{z}$ -direction. As

<sup>1</sup>Calculated from the orbital and spin momentum deduced by the sum rules, which needs to be considered with care (**section 2.4.5**).



(a) Non spin-flip channel, magnetic peaks from magnetic moment in  $\vec{a}$ -direction at  $(0 \pm \tau_{Mn}/2)$  and  $(0 \pm \tau_{Mn})$

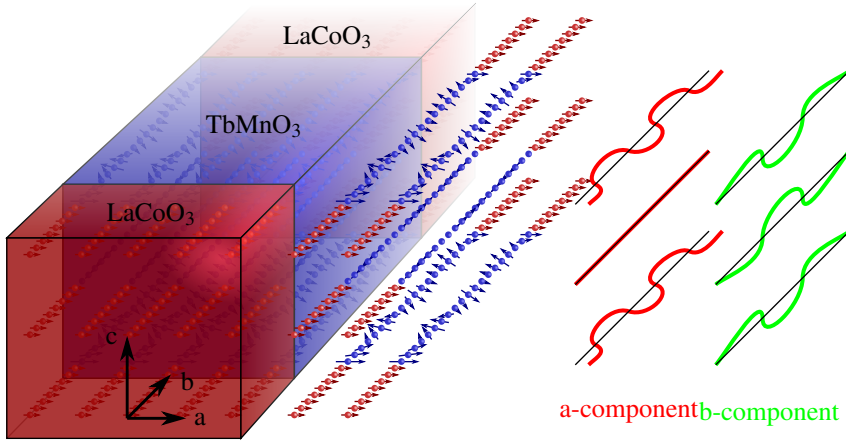


(b) Spin-flip channel, magnetic peaks with magnetic moment in the bc-plane at  $(00.12\ 1)$

**Figure 6.10:** Polarized neutron diffraction data (left) of  $\text{Tb}_{18/20}\text{Ti}_{2/20}\text{O}_{60}$  measured with DNS at 4 K with simulation from proposed magnetic structure (right). Although the background from an empty sample holder measurement is subtracted, there is still some background visible due to the very low scattering intensity (originating from e.g. limited statistics of the background signal, paramagnetic scattering from the substrate and from the Tb-moments as found for the single layers in [section 5.4.1](#)).

$\vec{Q}$  has mainly a  $Q_x$  component, which is parallel to  $\vec{c}$ , the magnetization measured,  $\vec{M}_\perp$ , in this region lies in  $\vec{b}$ -direction. An additional ordered component is found in the non spin-flip channel with magnetic moments in  $\vec{a}$ -direction, which is also long range correlated in out-of-plane direction and has a lower in-plane correlation length than found for the b-component. The magnetic peaks are found at  $(0 \pm 0.28\ L)$  positions with approximately equal structure factor. From this it is clear, that the order in  $\vec{c}$ -direction can be neither ferromagnetic nor antiferromagnetic, as these would forbid odd or even L reflections, respectively. All reflections are still found at 30 K, which is a clear sign, that order of the Tb moments cannot be the main source of the scattering, as their coupling is much weaker. The multilayer reflections in spin-flip and non spin-flip channel are clearly of magnetic nature, as they are much broader than the structural peaks, vanish above 40 K and appear at  $K < 0.5$  (where no structural peaks were found with x-ray diffraction at this temperature).

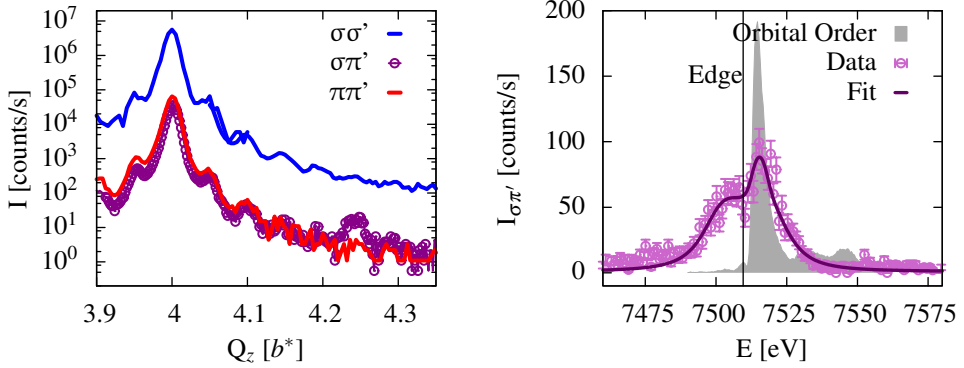




**Figure 6.11:** Magnetic structure model used for the simulation in **figure 6.10**. From left to right: Crystal directions and layer structure of the sample, ordered spin orientations in LaCoO<sub>3</sub> (red) and TbMnO<sub>3</sub> (blue), a-component and b-component of the magnetization in the TbMnO<sub>3</sub> layer.

Although different magnetic structures could lead to the observed scattering, a model has been developed, which explains the results consistently with the structure model and magnetization measurements: A sketch of the model is shown in **figure 6.11**. The samples are cooled with the guide field in  $\vec{a}$ -direction, leading to ferromagnetic alignment of all Co spins in the LaCoO<sub>3</sub> layers in  $\vec{a}$ , too. The Mn moments in the adjacent TbMnO<sub>3</sub> monolayers are assumed to couple ferromagnetically to these ions, which leads to an  $\vec{a}$ -component of the magnetization, which forms a SDW with a propagation vector close to  $\tau_{Mn}$ , fitting inside the layer. The antiferromagnetic superexchange in  $\vec{c}$ -direction contradicts this magnetic structure for every TbMnO<sub>3</sub> ab-plane, so that only every other Mn spin shows this magnetic order with parallel moments (A small anti-parallel component on the Mn ions in between could still be present. The quality of the data does not allow a final conclusion on the intensity ratio between the  $(0\ \tau\ 1)$  and  $(0\ \tau\ 2)$  reflections to compare it with the magnetic form factor and rule out antiferromagnetic correlations.). Through this mechanism the structure can form coherently through the whole multilayer, but has only a limited coherence length in  $\vec{c}$ -direction. For the  $\vec{b}$ -component the only constraints are nodal points at the interfaces (as the magnetization there is parallel to the adjacent Co). This allows SDW order with different periodicities governed by impurities and thickness fluctuations. This leads to magnetic structures without any inter layer coherence. The superexchange in  $\vec{c}$  can be fulfilled and thus leads to large coherence length in-plane.

This model explains the strong coupling of the ferromagnetic moment to the antiferromagnetic order parameter found in the SQUID measurements as well as the increased remanent magnetization found for the in-plane field direction below  $T_{N_{SDW}}$ . The intensities calculated from this model are shown in **figure 6.10** and were derived by calculating the structure factor (**section B.3**) as FFT of the spin structure, building the absolute square of the structure factor, adding substrate delta peaks and convolving with a Gaussian resolution function.



(a) Resonant signal at the  $\text{Tb}_{\text{LIII}}$ -edge ( $\approx 7520$  eV) for the different polarization channels at 4 K. The strong structural signal cannot be fully suppressed due to a finite polarization of  $\approx 99\%$ .

(b) Resonance enhancement of the magnetic  $(04+\tau 1)$  reflection with two energy level fit from equation (4) in [115], compared to the scaled intensity of a reflection at  $(03 1)$  from the non spherical charge distribution of Tb.

**Figure 6.12:** Resonant magnetic x-ray scattering from  $\text{Tb}_{\text{LIII}}$  at  $\text{Tb}_{\text{LIII}}$ -edge

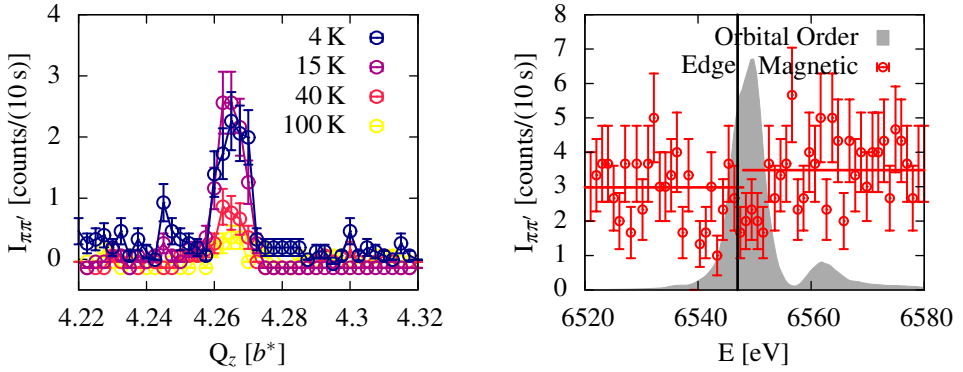
### 6.3.2 X-ray resonant magnetic scattering

A multilayer sample was investigated with resonant magnetic scattering at the  $\text{Tb}_{\text{L}}$ - and  $\text{Mn}_{\text{K}}$ -edges at the P09 beamline of PETRA-III. Although the resonant enhancement at these edges is much lower than in the soft x-ray regime (especially for Mn) due to no direct involvement of the orbitals containing magnetic electrons in the scattering process, the larger  $\vec{Q}$  range accessible makes it possible to study higher order peaks. The experiments were performed with linear polarization and polarization analysis, the absorption edges were determined using metal foils. The sample was mounted in a cryostat with the  $b$ -direction parallel to  $\phi$  ( $z$ ) and the  $a$ -direction perpendicular to the scattering plane ( $y$ ). Unfortunately the closed cycle cryostat, which was designated for the experiment, had a broken Joule-Thomson cooler and needed to be replaced with a backup system with higher base temperature. Only two days were left for the measurements after the replacement.

In resonance orbital order or Templeton scattering ([119]) of Mn and Tb have been found, as expected, on the forbidden  $(0\text{ K L})$ -peaks with K odd. As can be seen in the measurement used to determine the structure of the multilayer **figure 6.1a** the background from Thomson scattering of the multilayer crystal reflections is quite high, even far away from the Bragg-peaks. This made it impossible to measure the short range order found with neutron diffraction. To be able to measure magnetic scattering from the long range order, reflections with large  $|\vec{Q}|$  were used<sup>2</sup> to search for  $(0\text{ K} \pm \tau_{\text{Mn}} 1)$  reflections with K even.

At the  $\text{Tb}_{\text{LIII}}$ -resonance a magnetic reflection was found at  $(04+\tau_{\text{Mn}} 1)$  in the  $\sigma\pi'$  channel (**figure 6.12a**). The energy dependence of this peak shown in **figure 6.12b** has a large shoulder 5 eV below the absorption edge and a peak directly at the resonance energy. A similar resonance shape is reported for bulk Tb metal and Er/Tb superlattices [115]. A fit to the

<sup>2</sup>In contrast to magnetic neutron and Thomson scattering no form factor applies to resonant scattering as the spatial distribution of the initial state, the core level, determines the interaction region.



(a) Non resonant (6520 eV) magnetic scattering in the  $\pi\pi'$  channel. The background is extremely low because of prohibited Thomson scattering at  $2\Theta \approx 90^\circ$ .

(b) Energy dependence of the magnetic peak at 4 K compared to a orbital order reflection at (0 1 0). There is hardly any resonance enhancement on the  $^{\text{Mn}}\text{K}$ -edge visible.

**Figure 6.13:** Magnetic x-ray scattering from  $\text{Tl}_{18/3}\text{L}_{20}$  close to the  $^{\text{Mn}}\text{K}$  resonance

resonant scattering interference of two excitation energies, as has been done in the former case (equation (4) of [115]), gives good agreement with the experimental data. As there is no peak in the  $\pi\pi'$  channel, but only in  $\sigma\pi'$ , the major part of the magnetic moment lies in the bc-plane (cf. equation 2.60 with  $\hat{e}_\pi \times \hat{e}_{\pi'} = \hat{a}$  and  $\hat{e}_\sigma \times \hat{e}_{\pi'} \perp \hat{a}$ ), while there seems to be no large  $\vec{a}$ -component (which would lead to  $\pi\pi'$  scattering). Thus the long range order of Tb in the low temperature phase reveals an additional complexity of the magnetic structure.

At the  $^{\text{Mn}}\text{K}$ -edge the situation at the (0 4.25 1) position is providential, as the scattering angle  $2\Theta$  is almost exactly  $90^\circ$ . This has the consequence, that Thomson scattering with  $\pi$  polarization is completely forbidden, reducing the background several orders of magnitude. On the other hand, the resonance enhancement at this edge is very weak. At an energy slightly below the resonance a non resonant magnetic signal was detected (**figure 6.13a**) in  $\pi\pi'$  with less than 1 cps but with a background level of only about one count per ten minutes. The peak shows a clear temperature dependence and is very narrow, evidencing the long range order through the multilayer stack. The magnetic moments have a component in the  $\vec{a}$ -direction, as the peak appears in the  $\pi\pi'$  channel. There is hardly any resonance enhancement visible (**figure 6.13b**), which could be a sign that Tb and/or Co moments contribute to this magnetic order. These results do perfectly match the findings in **section 6.3.1**.

## 6.4 Summary

Thin films of strained LaCoO<sub>3</sub> and multilayers combining LaCoO<sub>3</sub> and TbMnO<sub>3</sub> have been created using PLD and investigated by different methods for their structural and magnetic properties. While single LaCoO<sub>3</sub> layers of 35 nm are already relaxed to the rhombohedral bulk structure, the multilayer with 20 bilayers is still strained to the YAlO<sub>3</sub> substrate **section**

**6.1.** The layer and crystal structure of the samples could be deduced from diffraction data obtained with synchrotron radiation at a multilayer Bragg-reflection.

SQUID magnetometry revealed that the strained  $\text{LaCoO}_3$  layers develop ferromagnetic order below  $\approx 62\text{ K}$  and comparing the moment deduced with XMCD with the multilayer reveals that relaxation reduces the magnetism, an effect that leads to a larger magnetization at the substrate-film interface than at the sample surface. The orthorhombic distortion in the strained layers could thus be the major key to explain the ferromagnetism in  $\text{LaCoO}_3$  thin films. Magnetization measurements on the multilayer show a complex anisotropic behavior with several transitions **section 6.2.1**. From element specific magnetization measurements with soft x-ray magnetic circular dichroism (in-plane and out-of-plane) the only ferromagnetism found belongs to Co moments with easy axis in-plane **section 6.2.2**.

The antiferromagnetic order in the multilayer was probed with polarized neutron and resonant x-ray diffraction **section 6.3**. A long range order through the whole multilayer with the magnetic moments in  $\vec{a}$ -direction was observed with both methods and explained with a spin model, which was also used to model the neutron data. An additional magnetic moment component in  $\vec{b}$ -direction with long range in-plane, but only short range out-of-plane order, was observed with polarized neutrons. Even more complexity of the magnetic structure is evidenced by resonant diffraction on the Tb edge with magnetic moments in the bc-plane and long range correlations through the multilayer with a magnetic propagation vector  $(0\ \tau\ 1)$ .

Although additional investigations of the magnetic order (especially in dependence of external fields and temperature) are needed to understand the full complexity of the magnetic structure, a strong coupling of the Mn and Tb moments in the  $\text{TbMnO}_3$  layers to the ferromagnetic Co moments has been observed. To measure the layered ferromagnetism in the system with neutron reflectivity, large samples with homogeneous thicknesses and well defined periodicity are needed, which could be produced with sputter deposition as described in **chapter 5**.

The spin model introduced for the  $[\text{TbMnO}_3\text{-LaCoO}_3]$ -multilayers should be tested with further scattering measurements including xyz-polarization analysis and a more detailed temperature dependence. As the kinematic multilayer simulation proved very useful to deduce the layer parameters of films with small contrast in reflectivity, a user interface in the evaluation program and an option to calculate arbitrary scattering directions will be implemented to allow fast evaluation of measured diffraction patterns.



# Chapter 7

## Experiments III: [EuTiO<sub>3</sub>-BaTiO<sub>3</sub>]-Multilayers

The emergent ferromagnetism observed in EuTiO<sub>3</sub> single layers (see **section 2.3.4**) was investigated for systems containing interfaces to BaTiO<sub>3</sub>. Although the EuTiO<sub>3</sub> lattice in these heterostructures is highly strained, the interface to BaTiO<sub>3</sub> could inhibit long range magnetic order. Multilayers of different thickness ratios between EuTiO<sub>3</sub> and BaTiO<sub>3</sub> have been created on GdScO<sub>3</sub> substrates using PLD and are listed in **table 7.1**. The magnetization of the layers could not be measured with SQUID magnetometry because of the large paramagnetism of the GdScO<sub>3</sub> substrates and was thus investigated layer resolved with polarized neutron reflectivity at D17 of ILL. All samples have been additionally characterized with x-ray reflectivity and diffraction.

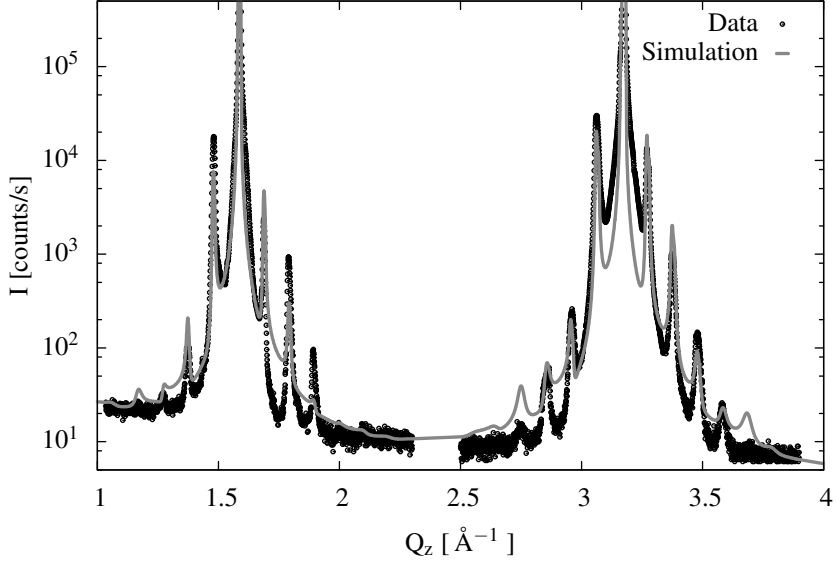
Polarized neutron and x-ray reflectivity measurements were refined together with the same model (**section 3.5.7**), only exchanging the elemental scattering powers for each radiation. The x-ray diffraction was simulated with a multilayer model (**section 3.5.7**), too. The refinements are challenging as the x-ray reflectivity contrast is limited and the thickness inhomogeneity modeling adds further parameters to the already large number of parameters in the model. Nevertheless, very good agreement of the reflectivity data with the refinement could be achieved as can be seen in **figure 7.3** and **7.4**.

### 7.1 Crystal structure

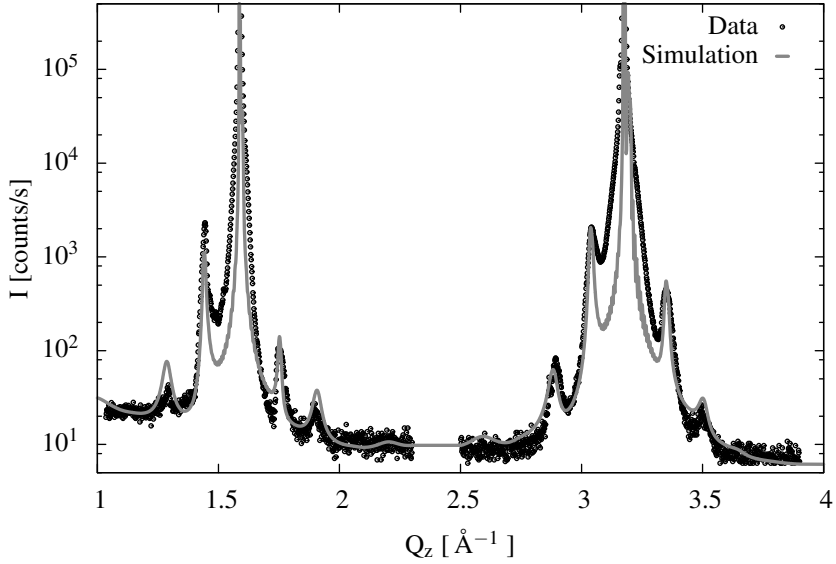
The simulation over a large  $\vec{Q}$  range requires the correct model parameters for each layer as well as the crystal unit cell (structure factor). Even if it can be assumed that the model itself

| ID                                 | d <sub>EuTiO<sub>3</sub></sub> | d <sub>BaTiO<sub>3</sub></sub> | $\sigma_{avg.}$ |
|------------------------------------|--------------------------------|--------------------------------|-----------------|
| EB <sup>3/3</sup> <sub>×20</sub>   | 1.0(1) nm                      | 1.1(1) nm                      | 0.7(1)          |
| EB <sup>4/6</sup> <sub>×20</sub>   | 1.44(6) nm                     | 2.48(5) nm                     | 0.38(4)         |
| EB <sup>4/10</sup> <sub>×20</sub>  | 1.8(1) nm                      | 3.8(1) nm                      | 0.18(5)         |
| EB <sup>12/10</sup> <sub>×20</sub> | 4.9(7) nm                      | 3.9(5) nm                      | 0.7(1)          |

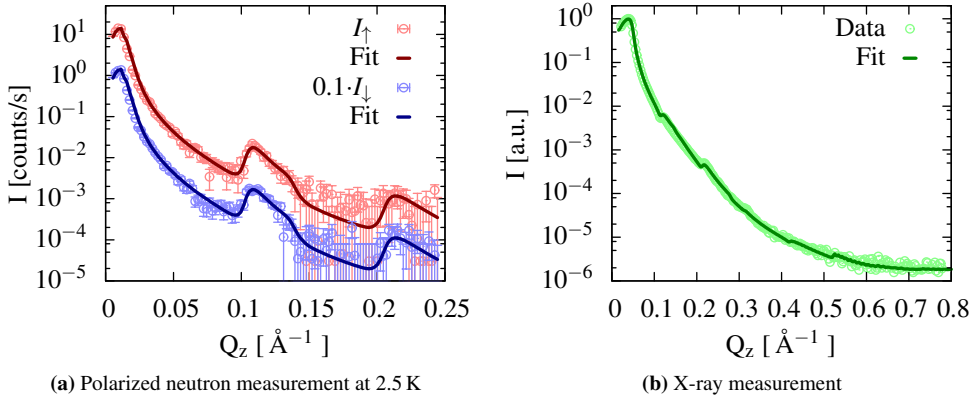
**Table 7.1:** Parameters overview of [EuTiO<sub>3</sub>-BaTiO<sub>3</sub>]-multilayer samples created for the study. A complete list of all extracted parameters can be found in **table A.3**.



**Figure 7.1:** X-ray diffraction from  $\mathbb{E}\mathbb{B}_{\times 20}^{4/10}$  with kinematic simulation: Bilayer periodicity  $D=6.01$  nm, ratio  $d_{\text{BaTiO}_3}/D=0.64$ ,  $a_{\text{BaTiO}_3}=4.01$  Å,  $a_{\text{EuTiO}_3}=3.90$  Å,  $\delta N_A=0.3$ ,  $\delta N_B=0.3$



**Figure 7.2:** X-ray diffraction from  $\mathbb{E}\mathbb{B}_{\times 20}^{4/6}$  with kinematic simulation: Bilayer periodicity  $D=4.02$  nm, ratio  $d_{\text{BaTiO}_3}/D=0.67$ ,  $a_{\text{BaTiO}_3}=3.97$  Å,  $a_{\text{EuTiO}_3}=3.86$  Å,  $\delta N_A=0.7$ ,  $\delta N_B=0.1$



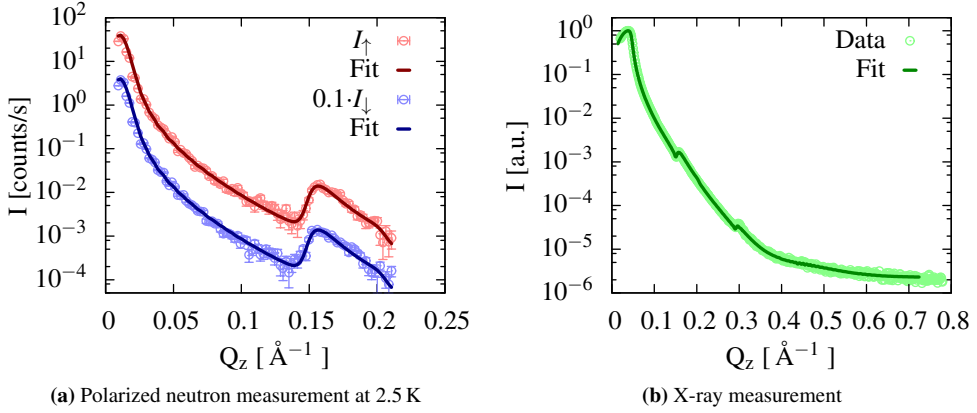
**Figure 7.3:** X-ray and neutron reflectivity from  $\text{EB}_{\times 20}^{4/10}$  refined with the same model: Bilayer periodicity  $D = 5.56(5) \pm 0.37$  nm,  $d_{\text{BaTiO}_3}/D = 0.68$ ,  $\sigma_{\text{BaTiO}_3} = 0.13(10)$  nm and  $\sigma_{\text{EuTiO}_3} = 0.30(2)$  nm

describes the samples very well, these parameters need to be found with a good first guess, as they do not always influence the intensity profile predictably. Refinement of the simulation parameters was not possible as the background of the Bremsberg from the substrate peaks dominates the spaces between the multilayer peaks. The high quality of the epitaxial growth is obvious in the sharp peaks on both sides of the substrate peaks in **figure 7.1** and **7.2**. Although the agreement with the simulation is qualitatively correct they could not be numerically refined to deduce the parameters with errors. It is found by varying the simulation parameters that for more than 1 UC thickness variance ( $\delta N$ ), the peaks are much broader than measured and vanish completely above 2-3 UCs. This fact is verified with the measurements done on  $\text{EB}_{\times 20}^{3/3}$  and  $\text{EB}_{\times 20}^{12/10}$ , which have increased roughness values and do hardly show any peaks in the diffraction measurement. From the peak positions, the bilayer periodicity can be extracted precisely and, due to the inhomogeneity, is larger than the average as it is measured in the center of the sample. The lattice parameters extracted from the simulation can only be seen as estimates, as they are determined from the peak intensities together with the structure factor (determined by position and occupancy of elements in the unit cell).

## 7.2 Layer structure and magnetization

**Figure 7.3a** and **7.4a** show the spin-up and spin-down neutron reflectivity measured on  $\text{EB}_{\times 20}^{4/10}$  and  $\text{EB}_{\times 20}^{4/6}$  together with the refinements. The spin-down intensities are scaled by a factor of 10 for better visibility. As for the x-ray data **figure 7.3b** and **7.4b** the main features are sharp drops at the total reflection angle and a broad multilayer peak with a sharp inclination at the low  $|\vec{Q}|$  side. The position of the total reflection plateau is determined by the average scattering length density of the multilayer and the SLD of the substrate. On the other hand the peak height is determined by the difference in SLD and thickness ratio of the  $\text{BaTiO}_3$  and  $\text{EuTiO}_3$  layers. From both features, together with the different contrast between neutrons and





**Figure 7.4:** X-ray and neutron reflectivity from  $\text{EuTiO}_3/\text{BaTiO}_3$  refined with the same model: Bilayer periodicity  $D = 3.92(2) \pm 0.17 \text{ nm}$ ,  $d_{\text{BaTiO}_3}/D = 0.63$ ,  $\sigma_{\text{BaTiO}_3} = 0.42(3) \text{ nm}$  and  $\sigma_{\text{EuTiO}_3} = 0.35(2) \text{ nm}$

x-rays, the ratio between both layers and their density can be extracted precisely. For multilayers with homogeneous thickness the multilayer reflection would be a symmetric peak, but the asymmetric thickness distribution explained in **section 3.5.7** leads to a sharp increase and slow drop.

The combined neutron and x-ray refinement yielded large thickness inhomogeneities between 4% and 8%. The model also used in former chapters for reflectivity simulation has been verified, as the form of the multilayer Bragg-peak in the combined neutron and x-ray reflectivity data could only be fitted using the implemented thickness variations. Although this imperfection in the samples reduce the Bragg intensity and broadens the peaks, the data can be simulated to gain precise information on roughness and magnetization. The roughnesses of the layers vary from sample to sample between 0.2 nm and 0.7 nm and are larger on top of the  $\text{EuTiO}_3$  layers. For the neutron data taken at 2.5 K the multilayer Bragg-peaks in  $I_{\uparrow}$  and  $I_{\downarrow}$  are identical and the fit shows that there is no ferromagnetism in the multilayers with an upper limit of  $0.01 \mu_B/\text{Eu}$ . Although the wavelength spread of the D17 monochromator supermirror was measured in time-of-flight mode and included in the model, no significant change in the intensity profile is observed due to the broad multilayer peaks.

## 7.3 Summary

It has been shown with x-ray diffraction, that epitaxial strained  $[\text{EuTiO}_3\text{-BaTiO}_3]$ -multilayers were created with pulsed laser deposition. Although the  $\text{EuTiO}_3$  layers are highly strained in the multilayer structures, ferromagnetism could be excluded with high precision using polarized neutron reflectivity down to 2.5 K. This contradicts the expectations, as single films have been found to exhibit ferromagnetism below 4 K in similar systems [76]. This effect can be explained by an electronic exchange mechanism between  $\text{EuTiO}_3$  and  $\text{BaTiO}_3$  layers, as the alloy  $\text{Eu}_{0.5}\text{Ba}_{0.5}\text{TiO}_3$  does not order at all, although an influence of the sample quality

can never be excluded. The refinements of the data proof the applicability of the introduced models to similar oxide systems, as has been done in the previous chapters. The different contrast in the neutron and x-ray reflectometry could be used to improve the reliability of the extracted physical parameters.



# Chapter 8

## Conclusion

In the framework of this dissertation several transition metal oxide compounds have been created in thin films and heterostructures by pulsed laser and oxide sputter deposition. The samples have been investigated for their structural, magnetic and ferroelectric properties using a variety of experimental methods. For the data treatment a general evaluation program with graphical user interface *Plot.py* ( $\approx 40\,000$  lines - [137]) was written and several modules have been implemented, which allow the treatment of magnetometry, reflectivity, diffraction and small angle scattering in a modular, platform independent framework.

The layer dimensions, interface and surface roughnesses were explored with x-ray reflectivity and out-of-plane diffraction. For the reflectivity data standard Parratt modeling schemes were expanded by describing non-Gaussian roughness on the surfaces with additional layers and introducing lateral layer thickness variations by averaging intensities of multiple simulations with a custom weighting function. The diffraction patterns were modeled with kinematic simulations for single and multiple crystal layers incorporating meandering from the average layer thicknesses. Macroscopic magnetization measurements have been performed with SQUID magnetometry and element specific x-ray magnetic circular dichroism. Although the magnetization of the samples is low compared to background due to inclusions in the substrates, different transitions could be observed. The orbital and spin contributions of the magnetic moment could be extracted by analyzing the XMCD spectra. Polarized neutron and resonant x-ray diffraction have been used to probe the microscopic magnetic structure inside the films. Different antiferromagnetic states could be observed including their temperature dependence. For the thin films the cycloidal magnetic structure and ferroelectricity has been probed with resonant x-ray diffraction and second harmonic generation.

On  $\text{YAlO}_3$  substrates, epitaxial thin films of  $\text{TbMnO}_3$  and  $\text{DyMnO}_3$  with thicknesses between 2 nm and 400 nm were created by PLD and sputtering to analyze their multiferroic behavior in dependence of the film thickness. In contrast to earlier studies of  $\text{TbMnO}_3$  thin films deposited on different substrates [73, 80, 102], ferromagnetism was not observed in these investigations. The spin density wave antiferromagnetic order of the Mn moments, found in bulk material, was observed in all samples with polarized neutron diffraction, soft x-ray resonant magnetic scattering and via a weak ferromagnetic component from canted moments in SQUID magnetometry. A trace of the Tb and Dy order has been noticed in a reduction of the Mn order parameter below this temperature. In a few samples this order was directly observed with resonant scattering. While the ordering temperature ( $T_{\text{N}_{\text{Tb}}}$ ) varies from sample to sample, it is generally elevated as compared to bulk values. The cycloidal magnetic structure, responsible for the ferroelectricity, was found in the  $\text{TbMnO}_3$  sputter samples

with circular dichroic soft x-ray resonant magnetic scattering. The dependence of the magnetic domain walls on the position of the photoelectric charge while cooling (as observed for bulk  $\text{DyMnO}_3$  [107]) and the second harmonic generation is the first direct observation of ferroelectricity in  $\text{TbMnO}_3$  thin films. A significant structural or stoichiometric difference between samples produced with sputtering and PLD was not observed, thus the difference in magnetic behavior can be explained by the morphology of the layers (droplets, inclusions) and small deviations in the stoichiometry in the PLD samples. The ferroelectric ordering parameter also decreases below  $T_{\text{NTb}}$  which is known from  $\text{DyMnO}_3$ , but can't be observed in bulk  $\text{TbMnO}_3$ . Down to 6 nm film thickness no significant change in the magnetic behavior was found, a slight decrease of the ordering temperature of a few Kelvin could be observed. In summary, the films behave similar to their bulk crystals concerning multiferroic properties, measured for the first time on orthorhombic  $\text{TbMnO}_3$  films, as they are almost unstrained by the used substrates. The increased ordering temperature of the rare earth ions and the influence on the Mn order in  $\text{TbMnO}_3$ , that both have been found in all films are different, though. These characteristics proofed the combination of  $\text{YAlO}_3$  substrates with  $\text{TbMnO}_3$  perfectly suited to look for interlayer exchange processes in heterostructures with other transition metal oxides.

Due to the ferromagnetism reported for strained  $\text{LaCoO}_3$  films [42], single layers of the material deposited with PLD were investigated as candidates to interface with  $\text{TbMnO}_3$  in a multilayer system. Epitaxial growth on  $\text{YAlO}_3$  could be verified with x-ray diffraction, although 35 nm films are already relaxed to their rhombohedral bulk crystal structure. A ferromagnetic transition at 62 K could be observed with SQUID magnetometry. Combining these results with XMCD analysis leads to the hypothesis that only the strained regions close to the substrate get ferromagnetic due to orthorhombic distortion, as the measured magnetic moment per Co ion is lower than for the unrelaxed films in multilayers.

20 repetitions of 2 nm  $\text{LaCoO}_3$  and 10 nm  $\text{TbMnO}_3$  have been produced on  $\text{YAlO}_3$  substrates with PLD, intended to probe interlayer exchange coupling between the ferromagnetism in the  $\text{LaCoO}_3$  layers and the antiferromagnetic Mn order in  $\text{TbMnO}_3$ . The  $\text{LaCoO}_3$  lattice parameters determined with x-ray diffraction are compatible with a fully strained orthorhombic crystal structure. The ferromagnetic components in the multilayer investigated with XMCD show Co contributions and are much stronger in average than for the single film due to the higher strain. The SQUID magnetometry measurements reveal a strong influence of the  $\text{TbMnO}_3$  ordering transitions on the  $\text{LaCoO}_3$  ferromagnetism. A complex magnetic order has been observed by polarized neutron diffraction. Correlations through the multilayer with magnetic moment in the  $\text{TbMnO}_3$   $\vec{a}$ -direction and short range correlations with moments in  $\vec{b}$ -direction have been found. The scattering intensities could be simulated from a spin structure with moments ordering in  $\vec{b}$ -direction only inside a single  $\text{TbMnO}_3$  layer and the  $\vec{a}$ -component coupled ferromagnetically to the adjacent Co moments. The propagation vector and the high correlation length of this order could be confirmed with non resonant magnetic x-ray diffraction.

As a candidate for a artificial multiferroic compound, multilayers of the ferroelectric  $\text{BaTiO}_3$  and  $\text{EuTiO}_3$ , which develops ferromagnetism in strained films [76] with a large magnetoelectric coupling [112], were produced by PLD with different thickness ratios. The good structural quality was confirmed by x-ray and neutron reflectivity and x-ray diffraction. From

the refinement of the polarized neutron reflectivity with a well matched model, a ferromagnetic order could be excluded with high precision ( $<0.01\mu_B/\text{Eu}$ ) down to a temperature of 2.5 K.

Finally, the combined results of the different systems testify, that x-ray diffraction on film Bragg-reflections together with x-ray (and neutron) reflectometry constitute the perfect tools to gain precise structural information from oxide thin films. The pure reflectivity measurements are often limited due to low contrasts, while the diffraction (which gains contrast from different lattice constants) is complicated to model without further information and less precise in determining roughnesses. The implemented models show a perfect agreement with the measurements on all samples and are consistent between the different methods, using the same parameters. Non-Gaussian roughness, used to explain additional surface layers introduced for the reflectivity modeling, could be confirmed with atomic force microscopy on  $\text{TbMnO}_3$  layers. In the future, an improvement of the model will be added, with a mathematic foundation to calculate the rms roughness from these additional layers. The lateral thickness variations, often found in large PLD samples, could be described with a simplified distribution function, leading to good agreement with the experimental data, most prominently evident in the combined x-ray and neutron refinement of the  $[\text{EuTiO}_3\text{-BaTiO}_3]$ -multilayers.



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I want to thank the following people, who contributed a lot to the outcome of this work:

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# Appendix A

## Additional Figures and Tables

In this chapter additional figures are listed. The according descriptions can be found in the earlier chapters.

### A.1 Sample parameters

The tables on the following pages list the quantitative results measured for the different samples described in **chapter 5**, **chapter 6** and **chapter 7**. The  $\Delta$  values after each parameter denote the errors extracted from fits to the experimental data. Many parameter have asymmetric errorbars, in those cases the average of the upper and lower bounds were taken for simplicity. If the experiments could only be simulated without refinement the errors could not be calculated.

|                    | Sample                                | T <sub>PbD</sub><br>2 | T <sub>PbD</sub><br>5 | T <sub>PbD</sub><br>9 | T <sub>PbD</sub><br>18 | T <sub>PbD</sub><br>54 | T <sub>PbD</sub><br>200 | T <sub>SrD</sub><br>2 | T <sub>SrD</sub><br>6 | T <sub>SrD</sub><br>11 | T <sub>SrD</sub><br>16 | T <sub>SrD</sub><br>20 | T <sub>SrD</sub><br>31 | T <sub>SrD</sub><br>36 | T <sub>SrD</sub><br>100 | T <sub>SrD</sub><br>400 |
|--------------------|---------------------------------------|-----------------------|-----------------------|-----------------------|------------------------|------------------------|-------------------------|-----------------------|-----------------------|------------------------|------------------------|------------------------|------------------------|------------------------|-------------------------|-------------------------|
| X-ray Reflectivity | thickness d [Å]                       | 22.4                  | 49.9                  | 92.4                  | 175.5                  | 544.6                  |                         | 20.1                  | 58.75                 | 106                    | 159.2                  | 196.2                  | 309                    | 461                    | 1007                    |                         |
|                    | Δ                                     | 0.5                   | 0.3                   | 1                     | 1.5                    | 2                      |                         | 0.4                   | 0.3                   | 1.6                    | 1.3                    | 0.3                    | 1.5                    | 3                      | 2                       |                         |
|                    | layer roughness σ [Å]                 | 3.7                   | 4.16                  | 5                     | 5.48                   | 5.67                   |                         | 3.9                   | 5.08                  | 4.7                    | 3.6                    | 5.3                    | 4.8                    | 6.4                    | 7.6                     |                         |
|                    | Δ                                     | 0.1                   | 0.04                  | 0.1                   | 0.005                  | 0.2                    |                         | 0.07                  | 0.3                   | 0.15                   | 0.02                   | 0.5                    | 0.1                    | 0.2                    | 0.05                    |                         |
|                    | cap layer σ [Å]                       |                       |                       |                       |                        |                        |                         | 5                     | 6.79                  | 3.1                    | 0.6                    | 6.5                    |                        | 6.2                    | 12.4                    |                         |
|                    | Δ                                     |                       |                       |                       |                        | 0.3                    |                         | 0.5                   | 0.13                  | 0.2                    | 1                      | 0.8                    |                        | 0.6                    | 0.2                     |                         |
|                    | combined σ [Å]                        | 3.7                   | 4.16                  | 5                     | 5.48                   | 10.9                   |                         | 6.3                   | 8.5                   | 5.6                    | 3.7                    | 8.4                    | 4.8                    | 8.8                    | 14.5                    |                         |
|                    | Δ                                     | 0.1                   | 0.04                  | 0.1                   | 0.005                  | 0.4                    |                         | 0.5                   | 0.3                   | 0.25                   | 1.                     | 0.9                    | 0.1                    | 0.8                    | 0.2                     |                         |
|                    | substrate roughness σ [Å]             | 1.5                   | 1.56                  | 2                     | 1.57                   | 1.9                    |                         | 1.1                   | 1                     | 1                      | 2                      |                        | 1.1                    | 1                      | 1.4                     |                         |
|                    | Δ                                     | 0.1                   | 0.2                   | 0.3                   | 0.005                  | 0.1                    |                         | 0.1                   | 0.2                   | 0.1                    | 0.1                    | 0.2                    | 0.1                    | 0.25                   | 0.1                     |                         |
|                    | inhom. Lorentz γ [%]                  | 20                    | 17.7                  | 17.3                  | 19                     | 2                      |                         | 18.75                 | 2.12                  | 1.5                    | 1.1                    | 3.9                    | 1                      | 0.8                    | 1.56                    |                         |
|                    | Δ                                     | 5                     | 0.25                  | 1.3                   | 1                      | 0.3                    |                         | 1.6                   | 0.3                   | 4                      | 0.6                    | 3                      | 0.5                    | 0.1                    | 0.1                     |                         |
|                    | inhom. plateau width [%]              | 18                    | 7.14                  | 17                    | 5.6                    | 4.5                    |                         | 24.8                  | 30                    | 17.5                   | 13.6                   | 18.5                   | 5                      | 7.14                   | 1.8                     |                         |
|                    | Δ                                     | 13                    | 0.8                   | 1.5                   | 0.5                    | 2                      |                         | 5                     | 0.1                   | 6                      | 2.5                    | 3                      | 5                      | 4                      | 0.2                     |                         |
|                    | inhom. fraction of Lorentz            | 0.25                  | 0.7                   | 0.96                  | 0.9                    | 0.73                   |                         | 0.5                   | 0.936                 | 0.92                   | 0.95                   | 0.97                   | 0.991                  | 0.85                   | 0.83                    |                         |
|                    | Δ                                     | 0.5                   | 0.15                  | 0.3                   | 0.15                   | 0.1                    |                         | 0.25                  | 0.02                  | 0.1                    | 0.03                   | 0.1                    | 0.1                    | 0.05                   | 0.2                     |                         |
|                    | inhom. std. deviation [%]             | 20                    | 7.8                   | 1.26                  | 2.33                   | 4.2                    |                         | 16                    | 1.01                  | 1.2                    | 0.95                   | 0.7                    | 0.15                   | 0.6                    | 2.4                     |                         |
| XRD                | Vogt σ <sub>(200)</sub> [°]           | 0.01                  | 0.015                 | 0.011                 | 0.012                  | 0.013                  | 0.                      | 0.02                  | 0.015                 | 0.0081                 | 0.011                  | 0.0128                 | 0.01                   | 0.018                  | 0.43                    |                         |
|                    | Δ                                     | 0.003                 | 0.001                 | 0.0009                | 0.0004                 | 0.005                  | 0.026                   | 0.001                 | 0.003                 | 0.0003                 | 510 <sup>-6</sup>      | 0.0003                 | 0.0002                 | 610 <sup>-6</sup>      |                         |                         |
|                    | Vogt γ <sub>(200)</sub> [°]           | 0                     | 0                     | 0.001                 | 0.0006                 | 0.005                  | 0.02                    | 0                     | 0.001                 | 0.005                  | 0.0021                 | 0.0015                 | 0.0026                 |                        |                         |                         |
|                    | Δ                                     | 0.002                 | 0.002                 | 0.0009                | 0.0004                 | 0.0008                 | 1·10 <sup>-6</sup>      | 0.001                 | 0.0003                | 0.0003                 | 510 <sup>-3</sup>      | 0.0003                 | 0.0003                 |                        |                         |                         |
|                    | TbMnO <sub>3</sub> a [Å]              |                       |                       |                       | 5.67                   |                        |                         |                       |                       | 5.39                   |                        |                        |                        |                        | 5.32                    | 5.32                    |
| SQUID              | TbMnO <sub>3</sub> b [Å]              |                       |                       |                       |                        |                        |                         |                       |                       | 5.66                   | 5.72                   |                        |                        |                        | 5.83                    | 5.76                    |
|                    | TbMnO <sub>3</sub> c [Å]              |                       |                       |                       |                        |                        |                         |                       |                       | 7.39                   |                        |                        |                        |                        | 7.32                    | 7.37                    |
|                    | TbMnO <sub>3</sub> b (D8) [Å]         | 21                    |                       | 36                    | 5.85                   |                        |                         | 5.57                  | 5.75                  | 5.82                   | 5.78                   | 5.83                   | 5.82                   | 5.83                   | 5.83                    |                         |
|                    | T <sub>Nsrw</sub> [K]                 |                       |                       |                       | 36                     |                        |                         |                       |                       | 40                     |                        |                        |                        |                        |                         | 42                      |
|                    | T <sub>Nc</sub> [K]                   |                       |                       |                       |                        |                        | 7                       |                       |                       |                        |                        | 29                     |                        |                        |                         | 9                       |
| Soft X-ray RMS     | T <sub>Nb</sub> [K]                   |                       |                       |                       |                        |                        |                         |                       |                       |                        |                        |                        |                        |                        | 42                      |                         |
|                    | T <sub>Nsw</sub> [K]                  |                       |                       | 38                    | 37                     |                        | 30                      |                       | 40                    | 41.5                   |                        |                        |                        |                        | 27                      |                         |
|                    | T <sub>Nc</sub> [K]                   |                       |                       | -                     | -                      |                        | -                       |                       | 23                    | 25                     |                        |                        |                        |                        |                         |                         |
|                    | T <sub>Nb</sub> [K]                   |                       |                       | 11                    | 15                     |                        | 15                      |                       |                       | 10                     |                        |                        |                        |                        |                         |                         |
|                    | layer thickness d(200) [Å]            |                       |                       |                       |                        |                        |                         |                       |                       |                        | 145                    |                        | 285                    |                        | 1,000                   |                         |
| SHG                | Δ                                     |                       |                       |                       | 2.3                    |                        |                         |                       | 34                    |                        | -                      |                        | -                      |                        | 195                     |                         |
|                    | mgc. corr. length d <sub>mg</sub> [Å] |                       |                       | 56                    | 3.2                    |                        |                         |                       |                       | 80                     | 115                    |                        | 191                    |                        |                         |                         |
|                    | Δ                                     |                       |                       |                       | 3                      |                        |                         |                       |                       | -                      | 3                      |                        | 4                      |                        |                         |                         |
|                    | TbMnO <sub>3</sub> b [Å]              |                       |                       |                       | 5.84                   |                        |                         |                       |                       | 5.74                   | -                      |                        | 5.82                   |                        | 5.81                    |                         |
|                    | Δ                                     |                       |                       |                       | 0.01                   |                        |                         |                       |                       |                        | -                      |                        | -                      |                        | 5.81                    |                         |
|                    | T <sub>Nc</sub> [K]                   |                       |                       |                       |                        |                        |                         |                       |                       |                        |                        |                        |                        |                        | 27                      |                         |
|                    | T <sub>Nb</sub>                       |                       |                       |                       |                        |                        |                         |                       |                       |                        |                        |                        |                        |                        | 12                      |                         |

**Table A.1:** Sample parameters measured with different methods on TbMnO<sub>3</sub> single film samples

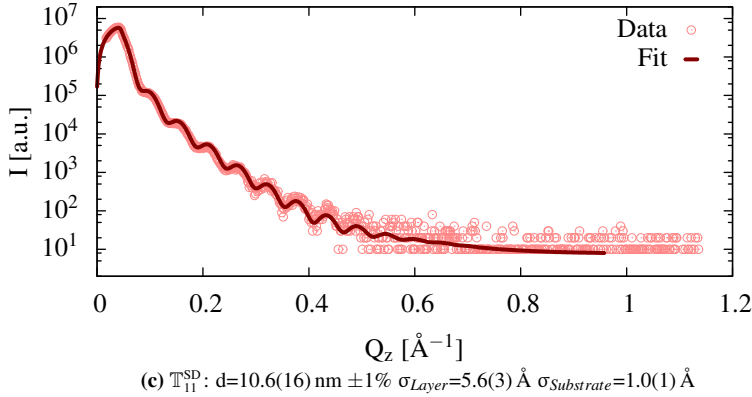
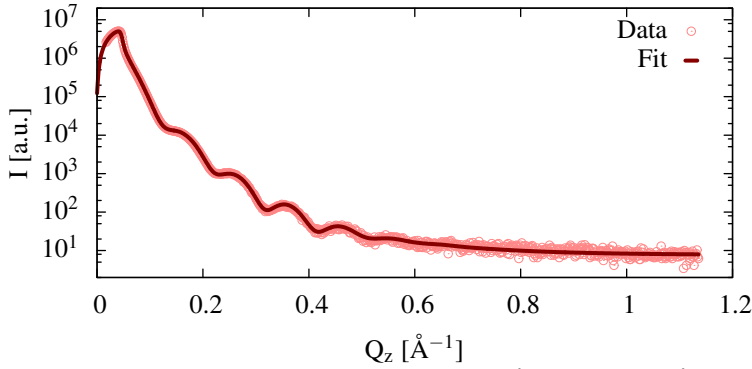
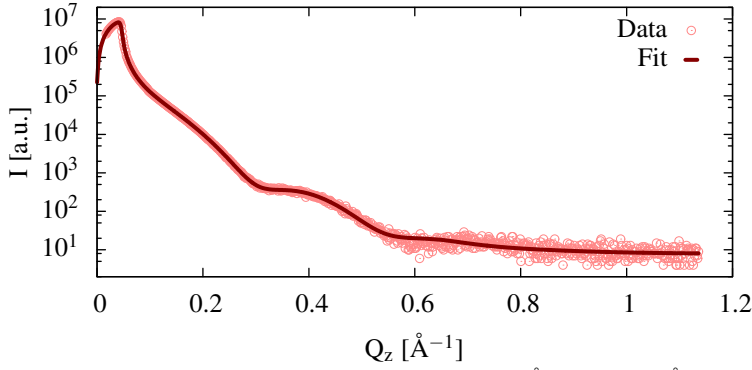
|                    | Sample  | $\mathbb{D}_2$ | $\mathbb{D}_5$ | $\mathbb{D}_{10}$ | $\mathbb{D}_{20}$ | $\mathbb{D}_{100}$ |
|--------------------|---|----------------|----------------|-------------------|-------------------|--------------------|
| X-ray Reflectivity | thickness $d$ [ $\text{\AA}$ ]                      | 20.7           | 52.96          | 95.7              | 195.7             | 1,000              |
|                    | $\Delta$  | 0.3            | 0.4            | 1                 | 1.8               |                    |
|                    | layer roughness $\sigma$ [ $\text{\AA}$ ]           | 5.06           | 7              | 4                 | 5.3               | 3.3                |
|                    | $\Delta$  | 0.3            | 1              | 0.25              | 0.4               | 0.05               |
|                    | cap layer $\sigma$ [ $\text{\AA}$ ]                 | 3.2            | 2.738          | 2.4               | 3.55              | 20                 |
|                    | $\Delta$  | 0.15           | 0.1            | 0.001             | 0.06              | 5                  |
|                    | combined $\sigma$ [ $\text{\AA}$ ]                  | 5.987          | 7.516          | 4.665             | 6.379             | 20.27              |
|                    | $\Delta$  | 0.335          | 1.005          | 0.25              | 0.404             | 5                  |
|                    | substrate roughness $\sigma$ [ $\text{\AA}$ ]       | 1.2            | 1.5            | 1.36              | 2.2               |                    |
|                    | $\Delta$  | 0.3            | -              | 0.1               | 1                 |                    |
|                    | inhom. Lorentz $\gamma$ [%]                         | 35.8           | 18             | 22.9              | 17.6              |                    |
|                    | $\Delta$  | 5              | 1              | 2                 | 2.5               |                    |
|                    | inhom. plateau width [%]                            | 37             | 18             | 49.95             | 40                |                    |
|                    | $\Delta$  | 4              | 7              | 3                 | 2                 |                    |
|                    | inhom. fraction of Lorentz                          | 0.3            | 0.54           | 0.997             | 0.899             |                    |
|                    | $\Delta$  | 0.2            | 0.2            | 0.1               | 0.2               |                    |
|                    | inhom. std. deviation [%]                           | 11             | 5.3            | 13                | 10.8              |                    |
| XRD                | Voigt $\sigma_{(200)}$ [ $^\circ$ ]                 | 0.013          | 0.017          | 0.0127            | 0.01              |                    |
|                    | $\Delta$  | 0.0004         | 0.0006         | 0.00006           | 0.0001            |                    |
|                    | Voigt $\gamma_{(200)}$ [ $^\circ$ ]                 | 0.00076        | 0.0015         | 0.0015            | 0.003             |                    |
|                    | $\Delta$  | 0.0004         | 0.00056        | 0.00007           | 0.0001            |                    |
|                    | DyMnO <sub>3</sub> a [ $\text{\AA}$ ]               |                |                |                   |                   | 5.30               |
|                    | DyMnO <sub>3</sub> b [ $\text{\AA}$ ]               |                |                |                   |                   | 5.84               |
|                    | DyMnO <sub>3</sub> c [ $\text{\AA}$ ]               |                |                |                   |                   | 7.47               |
| Soft X-ray RMS     | DyMnO <sub>3</sub> b (D8) [ $\text{\AA}$ ]          | 5.6            | 5.84           | 5.86              | 5.85              |                    |
|                    | $T_{\text{N}_{\text{SPW}}}$ [ K ]                   |                | 35(5)          |                   | 33                | 30                 |
|                    | $T_{\text{N}_{\text{C}}}$ [ K ]                     |                |                |                   |                   |                    |
|                    | $T_{\text{N}_{\text{Dy}}}$ [ K ]                    |                |                |                   | 16                | 20                 |
|                    | layer thickness $d_{(200)}$ [ $\text{\AA}$ ]        |                |                |                   | 185               |                    |
|                    | $\Delta$  |                |                |                   | 4                 |                    |
|                    | mag. corr. length $d_{\text{mag}}$ [ $\text{\AA}$ ] |                |                |                   |                   |                    |
|                    | layer roughness $\sigma$ [ $\text{\AA}$ ]           |                |                |                   | 3.4               |                    |
|                    | $\Delta$  |                |                |                   |                   |                    |
|                    | DyMnO <sub>3</sub> b [ $\text{\AA}$ ]               |                |                |                   | 5.82              |                    |
|                    | $\Delta$  |                |                |                   | 0.01              |                    |

Table A.2: Sample parameters measured with different methods on DyMnO<sub>3</sub> single film samples

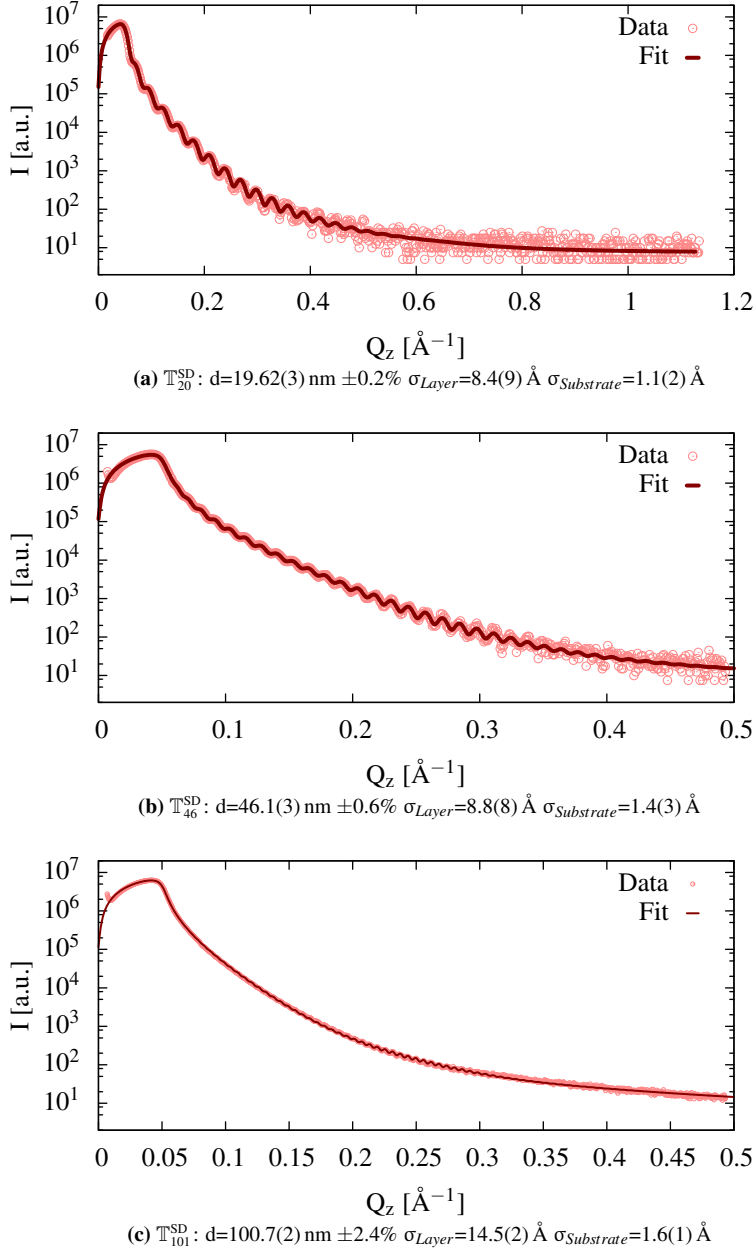
| Sample                                  | [EuB <sub>3</sub> ]<br>x <sub>20</sub> |  |  |  | [EuB <sub>4</sub> ]<br>x <sub>20</sub>   |  |  |  | [EuB <sub>4</sub> /10]<br>x <sub>20</sub> |  |  |  | [EuB <sub>12</sub> /10]<br>x <sub>20</sub> |                    |                                   |  | [La <sub>45</sub> ] |  | [Tb <sub>183</sub> ]<br>x <sub>20</sub> |  |
|---|--|--|--|--|--|--|--|--|---|--|--|--|--|--------------------|-----------------------------------|--|---------------------|--|---|--|
|   | Layer 1<br>Layer 2                     | EuTiO <sub>3</sub><br>BaTiO <sub>3</sub> | EuTiO <sub>3</sub><br>BaTiO <sub>3</sub> | EuTiO <sub>3</sub><br>BaTiO <sub>3</sub> | EuTiO <sub>3</sub><br>BaTiO <sub>3</sub> | EuTiO <sub>3</sub><br>BaTiO <sub>3</sub> | EuTiO <sub>3</sub><br>BaTiO <sub>3</sub> | EuTiO <sub>3</sub><br>BaTiO <sub>3</sub> | EuTiO <sub>3</sub><br>BaTiO <sub>3</sub>  | EuTiO <sub>3</sub><br>BaTiO <sub>3</sub> | EuTiO <sub>3</sub><br>BaTiO <sub>3</sub> | EuTiO <sub>3</sub><br>BaTiO <sub>3</sub> | EuTiO <sub>3</sub><br>BaTiO <sub>3</sub>   | LaCoO <sub>3</sub> | -                                 | TbMnO <sub>3</sub><br>LaCoO <sub>3</sub> |                     |  |   |  |
| substrate roughness σ [Å]               |  | 9.6                                      | 10.1                                     | 9.6                                      |  |  |  |  |   |  |  |  |  |                    | 3.4                               |  |                     |  |   |  |
| Δ                                       |  | 6  | 0.5                                      |  |  |  |  |  |   |  |  |  |  |                    | 0.1                               |  |                     |  |   |  |
| inhom. Lorentz γ [%]                    |  | 12                                       | 13.7                                     |  |  |  |  |  |   |  |  |  |  |                    | 6.6                               |  |                     |  |   |  |
| Δ                                       |  | 2  | 3  |  |  |  |  |  |   |  |  |  |  |                    | 1                                 |  |                     |  |   |  |
| inhom. plateau width [%]                |  | 13.9                                     | 14.9                                     |  |  |  |  |  |   |  |  |  |  |                    | 2.1                               |  |                     |  |   |  |
| Δ                                       |  | 3  | 1  |  |  |  |  |  |   |  |  |  |  |                    | 10                                |  |                     |  |   |  |
| inhom. fraction of Lorentz              |  | 0.99                                     | 0.96                                     |  |  |  |  |  |   |  |  |  |  |                    | 0.71                              |  |                     |  |   |  |
| Δ                                       |  | 0.2                                      | 0.01                                     |  |  |  |  |  |   |  |  |  |  |                    | 0.1                               |  |                     |  |   |  |
| inhom. standard deviation [%]           |  | 3.9                                      | 4.3                                      |  |  |  |  |  |   |  |  |  |  |                    | 0.68                              |  |                     |  |   |  |
| thickness d <sub>1</sub> [Å]            |  | 10                                       | 14.4                                     |  |  |  |  |  |   |  |  |  |  |                    | 348                               |  |                     |  |   |  |
| Δ                                       |  | 1  | 0.6                                      |  |  |  |  |  |   |  |  |  |  |                    | 3                                 |  |                     |  |   |  |
| layer roughness σ <sub>1</sub> [Å]      |  | 7.2                                      | 3.3                                      |  |  |  |  |  |   |  |  |  |  |                    | 5.1                               |  |                     |  |   |  |
| Δ                                       |  | 0.7                                      | 0.3                                      |  |  |  |  |  |   |  |  |  |  |                    | 0.1                               |  |                     |  |   |  |
| thickness d <sub>2</sub> [Å]            |  | 11.1                                     | 24.8                                     |  |  |  |  |  |   |  |  |  |  |                    | -                                 |  | 38                  |  |   |  |
| Δ                                       |  | 1  | 0.5                                      |  |  |  |  |  |   |  |  |  |  |                    | T <sub>N</sub> <sup>sow</sup> [K] | -  | 26                  |  |   |  |
| layer roughness σ <sub>2</sub> [Å]      |  | 7  | 4.1                                      |  |  |  |  |  |   |  |  |  |  |                    | T <sub>Nc</sub> [K]               | -  | 15                  |  |   |  |
| Δ                                       |  | 2  | 0.4                                      |  |  |  |  |  |   |  |  |  |  |                    | T <sub>Ntb</sub> [K]              | -  | 58                  |  |   |  |
| SQUID                                   |  |  |  |  |  |  |  |  |   |  |  |  |  |                    |                                   |  |                     |  |   |  |
| layer thickness d <sub>1</sub> [Å]      |  |  | 13.3                                     |  |  |  |  |  |   |  |  |  |  |                    | 328                               |  | 101                 |  |   |  |
| thickness distributions δN <sub>1</sub> |  |  | 0.1                                      |  |  |  |  |  |   |  |  |  |  |                    |                                   |  | 0.8                 |  |   |  |
| lattice parameter b <sub>1</sub> [Å]    |  |  | 3.86                                     |  |  |  |  |  |   |  |  |  |  |                    | 5.38                              |  | 5.75                |  |   |  |
| layer thickness d <sub>2</sub> [Å]      |  |  | 26.9                                     |  |  |  |  |  |   |  |  |  |  |                    |                                   |  | 18.8                |  |   |  |
| thickness distributions δN <sub>2</sub> |  |  | 0.7                                      |  |  |  |  |  |   |  |  |  |  |                    |                                   |  | 1.2                 |  |   |  |
| lattice parameter b <sub>2</sub> [Å]    |  |  | 3.97                                     |  |  |  |  |  |   |  |  |  |  |                    |                                   |  | 5.7                 |  |   |  |
| XRD                                     |  |  |  |  |  |  |  |  |   |  |  |  |  |                    |                                   |  |                     |  |   |  |
| layer thickness d <sub>1</sub> [Å]      |  |  | 13.3                                     |  |  |  |  |  |   |  |  |  |  |                    | 328                               |  | 101                 |  |   |  |
| thickness distributions δN <sub>1</sub> |  |  | 0.1                                      |  |  |  |  |  |   |  |  |  |  |                    |                                   |  | 0.8                 |  |   |  |
| lattice parameter b <sub>1</sub> [Å]    |  |  | 3.86                                     |  |  |  |  |  |   |  |  |  |  |                    | 5.38                              |  | 5.75                |  |   |  |
| layer thickness d <sub>2</sub> [Å]      |  |  | 26.9                                     |  |  |  |  |  |   |  |  |  |  |                    |                                   |  | 18.8                |  |   |  |
| thickness distributions δN <sub>2</sub> |  |  | 0.7                                      |  |  |  |  |  |   |  |  |  |  |                    |                                   |  | 1.2                 |  |   |  |
| lattice parameter b <sub>2</sub> [Å]    |  |  | 3.97                                     |  |  |  |  |  |   |  |  |  |  |                    |                                   |  | 5.7                 |  |   |  |

**Table A.3:** Sample parameters measured with different methods on LaCoO<sub>3</sub> single layer, [EuTiO<sub>3</sub>-BaTiO<sub>3</sub>]-multilayer and [TbMnO<sub>3</sub>-LaCoO<sub>3</sub>]-multilayer 5 samples

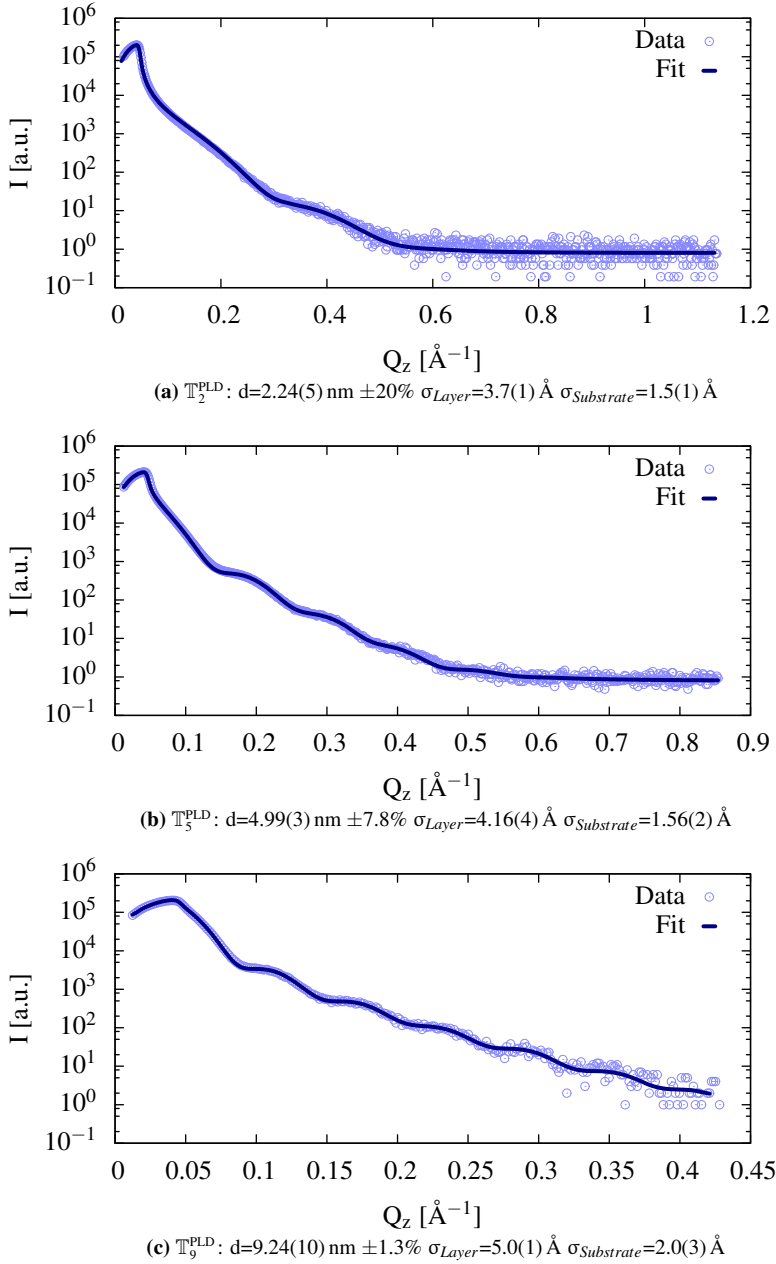
## A.2 X-ray reflectivity simulations



**Figure A.1:** X-ray reflectivity on  $\text{TbMnO}_3$  single layers created by sputter deposition

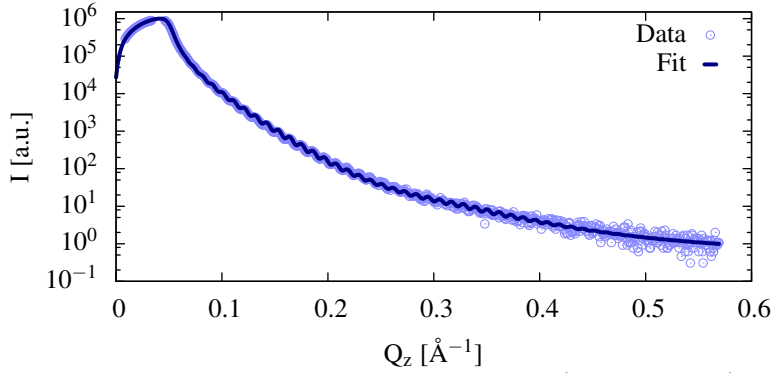
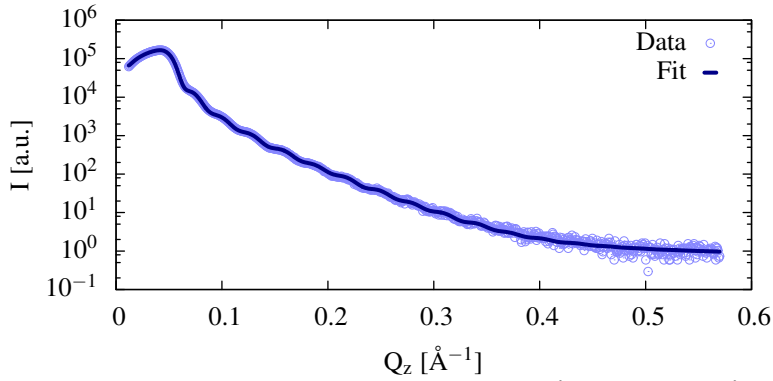


**Figure A.2:** X-ray reflectivity on TbMnO<sub>3</sub> single layers created by sputter deposition

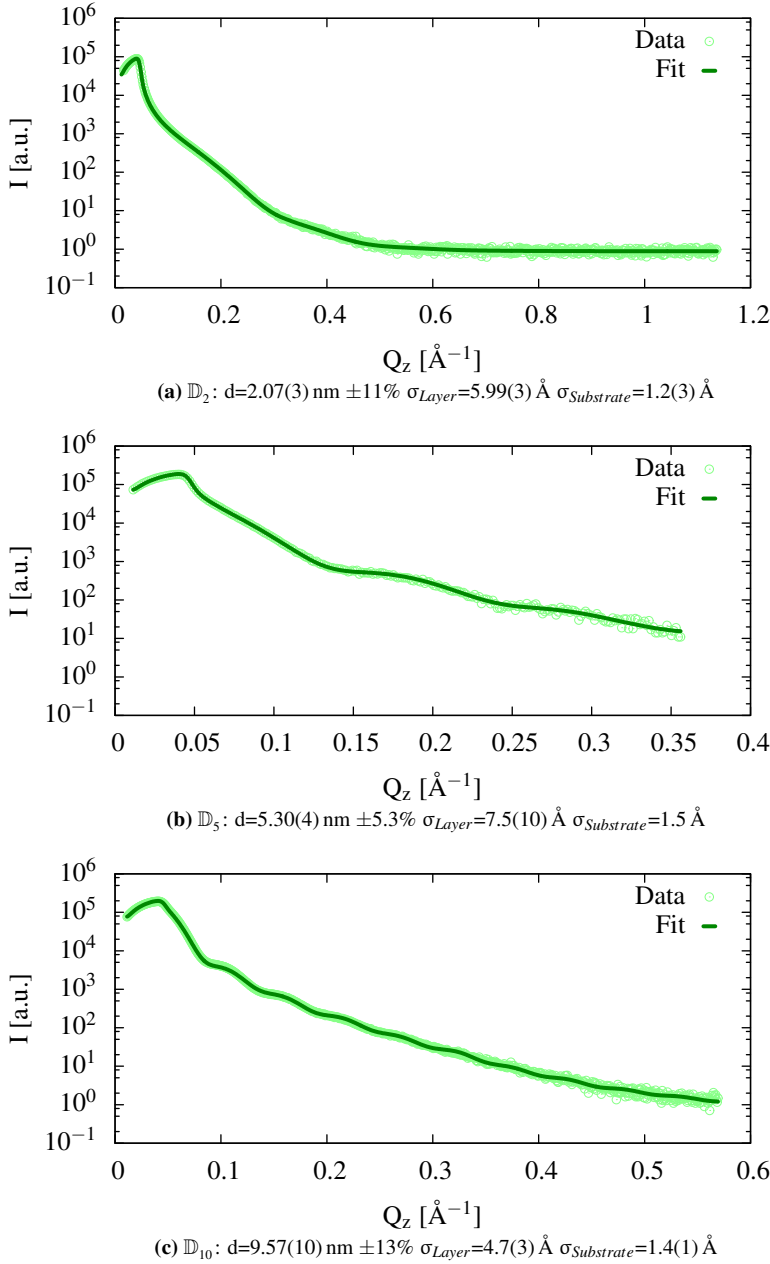


**Figure A.3:** X-ray reflectivity on TbMnO<sub>3</sub> single layers created by PLD

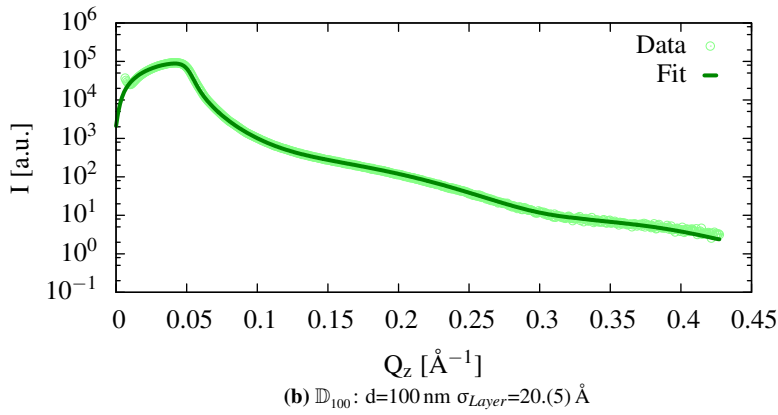
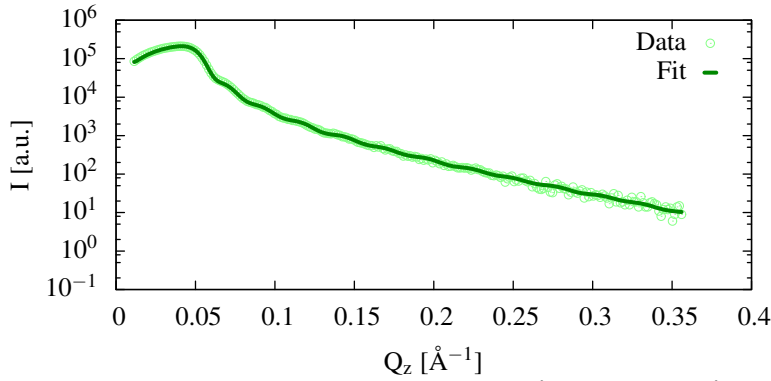




**Figure A.4:** X-ray reflectivity on  $\text{TbMnO}_3$  single layers created by PLD

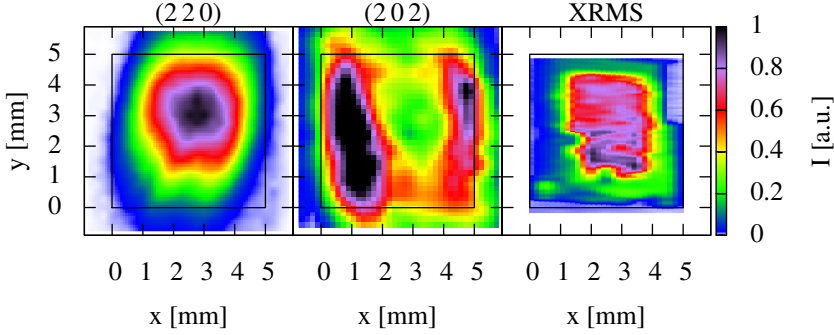


**Figure A.5:** X-ray reflectivity on  $\text{DyMnO}_3$  single layers created by PLD

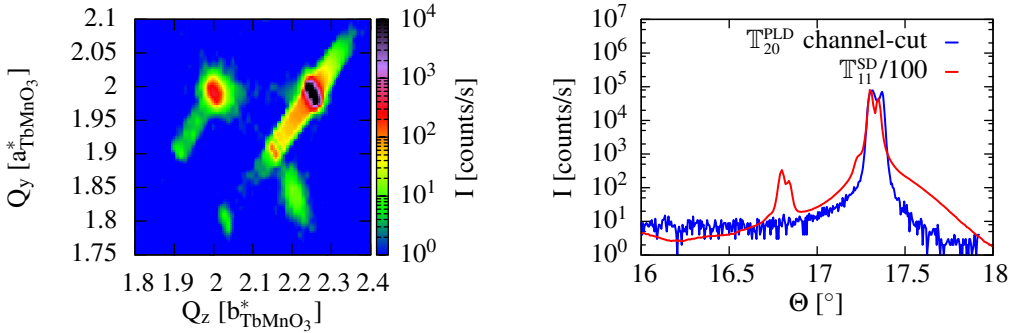


**Figure A.6:** X-ray reflectivity on DyMnO<sub>3</sub> single layers created by PLD

### A.3 Substrate imperfections



**Figure A.7:** Comparison of the xy-meshes measured on  $T_{100}^{SD}$  with the 4-circle diffractometer. Measurement on the  $TbMnO_3$  (220) reflection with right crystal orientation (left), the (202) peak corresponding to the wrong orientation (center) and the resonant magnetic scattering signal measured on  $(\delta \tau_{Mn} 0)$ . Besides the lower resolution of the 4-circle measurements, the regions with lower magnetic signal coincide with an increased intensity of the wrong oriented crystallites.



**(a)** Reciprocal space map around (220) on  $T_{100}^{SD}$  showing a second film peak as result of imperfections in the substrate

**(b)** Out-of-plane reciprocal lattice scan from the substrate (220) peaks of a sample with bad crystal quality and a good quality substrate measured with a channel cut monochromator for increased resolution.

**Figure A.8:** X-ray diffraction measurements investigating imperfections of wrong oriented crystallites in the substrate. The miss aligned crystal direction of the substrate directly lead to miss aligned film crystallites.



# Appendix B

## Used Models

### B.1 Implementation of multilayer diffraction simulation

```
1 import os
2 import numpy
3 import scipy
4 import gtk
5 from copy import deepcopy
6
7 import fit_data
8 import collect_cif_info
9 from diffpy.Structure.SpaceGroups import mmLibSpaceGroupList,
   sgtbxSpaceGroupList
10 SpaceGroupList=mmLibSpaceGroupList+sgtbxSpaceGroupList
11 from diffpy.Structure import Lattice, Atom, Structure
12
13 FitFunction=fit_data.FitFunction
14
15 class CrystalMultilayer(FitFunction):
16     """
17         Simulate diffraction from a stack of crystalline bilayers with finite size
18         and roughness.
19         The class tries to implement the high scattering angle diffraction
20         formalism for crystalline
21         multilayers deduced in
22         E. E. Fullerton et al.:
23         Structural refinement of superlattices from x-ray diffraction
24         Physical Review B, American Physical Society 45 (1992) 9292–
25         Naming conventions are also taken from that paper.
26
27         The code is focused on readability, not on speed!
28     """
29
30     # define class variables.
31     name="CrystalMultilayer"
32     max_iter=50. # maximum number of iterations
33     parameters=[0.181584, 5.,
34                 20, 1., 3.8843, 1., 4.07864, 0.,
35                 67.5205, 0.5, 0.2,
36                 0.2, 3.963, 0.000125,
37                 0.5, 0.99752006,
38                 ]
39     parameter_names=['I', 'BG', # Multilayer intensity and background
40                     'M', 'f1', 'a1', 'f2', 'a2', 'δA',
41                     'D', 'd1/D', 'c',
42                     'I_substrate', 'a_substrate', 'mu',
43                     'I-αK2', 'λ-αK2', # Relative intensity and wavelength of Cu
44                     -αK2
```

```

42         ]
43     parameter_description={
44         'I': 'Multilayer Intensity',
45         'BG': 'Background',
46         'M': 'Multilayer Periods',
47         'f1': 'Scatterin Power of layer 1',
48         'a1': 'd-spacing of layer 1',
49         'f2': 'Scatterin Power of layer 2',
50         'a2': 'd-spacing of layer 2',
51         'δA': 'Distribution of scattering plane repetitions',
52         'D': 'Bilayer thickness',
53         'd1/D': 'Thickness ration of layer 1 compared to
                    bilayer thickness',
54         'c': 'Width of interlayer spacing distribution',
55         'I_substrate': 'Substrate peak intensity',
56         'a_substrate': 'd-spacing of Substrate',
57         'mu': 'Absorption lengths',
58         'I-αK2': 'Intensity ratio of αK2',
59         'λ-αK2': 'Wavelength ratio of αK2',
60     }
61     fit_function_text='Multilayer'
62
63     def __init__(self, initial_parameters=[]):
64         '''
65         Constructor.
66         '''
67         FitFunction.__init__(self, initial_parameters)
68         # By default only fit intensity
69         self.refine_parameters=[0]
70
71     def create_model(self, p, q):
72         '''
73         Create the model object from given parameters.
74         '''
75         M=p[2]
76         f1=p[3]
77         a1=p[4]
78         f2=p[5]
79         a2=p[6]
80         delta=p[7]
81         D=p[8]
82         d1=D*p[9]
83         d2=D-d1
84         amin=(p[9]*a1+(1.-p[9])*a2)
85         N1=(d1-amin)/a1+1
86         N2=(d2-amin)/a2+1
87         a=amin
88         if delta==0.:
89             N1=int(N1)
90             N2=int(N2)
91             a=(D-((N1-1)*a1+(N2-1)*a2))/2.
92         c=p[10]
93         # Single crystalline layers
94         A=CrystallayerStructureModel(q, a1, f1, N1, delta)
95         B=CrystallayerStructureModel(q, a2, f2, N2, delta)
96         # Stack of bilayers
97         Model=MultilayerModel(q, A, B, M, a, c)
98         return Model
99
100     def fit_function(self, p, x):
101         '''
102         Implements the complete model. Parameters are initialized and the model
103             object is created, afterwards
104             the basic function (7) is calculated. Substrate peaks are simulated as
105             Lorentzian and Cu-Kalpha radiation
106             is simulated as two discrete q-arrays, which are summed up in Intensity
107             afterwards.
108         '''
109         I_0=p[0]

```

```

107 BG=p[1]
108 I_alpha2=p[14]
109 lambda_alpha2=p[15]
110 exp=numpy.exp
111 q=numpy.array(x, copy=False, dtype=numpy.complex)
112 # Create an additional q-array for K_alpha2 and join them as one array for
    the calculation
113 if I_alpha2!=0:
114     q=numpy.append(q, q*lambda_alpha2)
115 Model=self.create_model(p, q)
116 # Calculate Intensity from the multilayer stack
117 I=Model.I
118 # Substrate peaks
119 I_substrate=p[11]
120 a=p[12]
121 mu=p[13]
122 # Correct intensity for the scattering volume of the film dependent on  $\Theta$ 
123 Theta=numpy.arcsin(1.54/(4.*numpy.pi)*numpy.abs(q))
124 I*=I_0/numpy.sin(Theta)
125 #
126 I+=I_substrate*self.F_substrate(q, a, mu)
127 # Combine the intensities of K_alphal and K_alpha2
128 if I_alpha2!=0:
129     items=len(q)/2
130     I=(I[:items]+I_alpha2*I[items:])/ (1.+I_alpha2)
131     return I+BG
132
133 def F_substrate(self, q, a, mu):
134     '''
135     Substrate intensity as Lorentzian.
136     '''
137     a_star=2.*numpy.pi/a
138     q=numpy.abs(q)
139     F_substrate=numpy.zeros_like(q)
140     for i in range(1, 20):
141         q_i=a_star*i
142         if q_i<=q.max() and q_i >= q.min():
143             F_substrate+=1./ (mu**2+(q-q_i)**2)
144         # print q_i
145     return F_substrate
146
147 class CrystalMultilayerSF(CrystalMultilayer):
148     # define class variables.
149     name="CrystalMultilayerSF"
150     polarization=0.5
151     max_iter=50. # maximum number of iterations
152     parameters=[0.001, 1.0,
153                 20.0, 1., 1., 0.4, 0.4,
154                 67.5112, 0.6667, 0.,
155                 0.00005, 1., 0.000125,
156                 0.5, 0.99752,
157                 0., 15, 1.54]
158
159     parameter_names=['I', 'BG', # Multilayer intensity and background
160                     'M', 'arel_A', 'arel_B', 'delta_A', 'delta_B',
161                     'D', 'd_A/D', 'c',
162                     'I_substrate', 'a_substrate', 'mu',
163                     'I-alphaK2', 'lambda-alphaK2', # Relative intensity and wavelength of Cu
164                     'q-res', 'steps-res', 'lambda', # q resolution of the instrument
165                     , steps for resolution, measured wavelength
166                     ]
167     parameter_description={
168         'I': 'Multilayer Intensity',
169         'BG': 'Background',
170         'M': 'Multilayer Periods',
171         'arel_A': 'stretching factor of the out-of-plane
172                 lattice parameter of layer A',

```



```

171         'arel_B': 'stretching factor of the out-of-plane
172                 lattice parameter of layer B',
173         'δA': 'Distribution of scattering plane repetitions',
174         'δB': 'Distribution of scattering plane repetitions',
175         'D': 'Bilayer thickness',
176         'd1/D': 'Thickness ration of layer 1 compared to
177                bilayer thickness',
178         'c': 'Width of interlayer spacing distribution',
179         'I_substrate': 'Substrate peak intensity',
180         'a_substrate': 'd-spacing of Substrate',
181         'mu': 'Absorption lengths',
182         'I-αK2': 'Intensity ratio of αK2',
183         'λ-αK2': 'Wavelength ratio of αK2',
184         'q-res': 'q-resolution of the instrument (Gauss)',
185         'λ': 'Wavelength used',
186     }
187
188     fit_function_text='Multilayer'
189     fittable_elements={
190
191     }
192
193     def __init__(self, initial_parameters=[]):
194         '''
195         Constructor.
196         FitFunction.__init__(self, initial_parameters)
197         # By default only fit intensity
198         self.refine_parameters=[0]
199         # use global parameter to initialize the crystal structure model
200         self.bases=dict(model_basis)
201
202     def create_model(self, p, q):
203         '''
204         Create the model object from given parameters.
205
206         M=p[2]
207         # calculate lattice steps from crystal structure, scaling and growth
208         direction
209         direction=self.bases['A'][1]
210         lattice=self.bases['A'][0][0].lattice
211         a1=p[3]/numpy.sqrt((numpy.dot(lattice.rebase, direction)**2).sum())
212         direction=self.bases['B'][1]
213         lattice=self.bases['B'][0][0].lattice
214         a2=p[4]/numpy.sqrt((numpy.dot(lattice.rebase, direction)**2).sum())
215         deltaA=p[5]
216         deltaB=p[6]
217         D=p[7]
218         d1=D*p[8]
219         d2=D-d1
220         amin=(p[8]*a1+(1.-p[8])*a2)
221         N1=(d1-amin)/a1+1
222         N2=(d2-amin)/a2+1
223         a=amin
224         if deltaA==0. or deltaB==0:
225             N1=int(N1)
226             N2=int(N2)
227             a=(D-((N1-1)*a1+(N2-1)*a2))/2.
228         c=p[9]
229         f1=CrystalStructureFactor(p[3], self.bases['A'], q)
230         f2=CrystalStructureFactor(p[4], self.bases['B'], q)
231         # Single crystalline layers
232         A=CrystalLayerStructureModel(q, a1, f1, N1, deltaA)
233         B=CrystalLayerStructureModel(q, a2, f2, N2, deltaB)
234         # Stack of bilayers
235         Model=MultilayerModel(q, A, B, M, a, c)
236         return Model
237
238     def calc_I(self, p, q):
239         '''

```

```

237     Implements the complete model. Parameters are initialized and the model
238     object is created, afterwards
239     the basic function (7) is calculated. Substrate peaks are simulated as
240     Lorentzian.
241     ...
242     Model=self.create_model(p, q)
243     # Calculate Intensity from the multilayer stack
244     I=Model.I
245     # Substrate peaks
246     direction=self.bases['substrate'][1]
247     lattice=self.bases['substrate'][0][0].lattice
248     a=p[11]/numpy.sqrt((numpy.dot(lattice.recbase, direction)**2).sum())
249     mu=p[12]
250     fs=CrystalStructureFactor(p[11], self.bases['substrate'], q)
251     Is=numpy.abs(fs)**2*self.F_substrate(q, a, mu)
252     # Combine the intensities of K_alphal and K_alpha2
253     return I, Is
254
255 def fit_function(self, p, x):
256     ...
257     Implements the complete model. Parameters are initialized and the model
258     object is created, afterwards
259     the basic function (7) is calculated. Substrate peaks are simulated as
260     Lorentzian and Cu-Kalpha radiation
261     is simulated as two discrete q-arrays, which are summed up in Intensity
262     afterwards.
263     ...
264     numpy.seterr(all='raise')
265     I_0=p[0]
266     BG=p[1]
267     I_substrate=p[10]
268     I_alpha2=p[13]
269     lambda_alpha2=p[14]
270     sigma=p[15]
271     sigma_steps=p[16]
272     lambda_xray=p[17]
273     if len(p)>18:
274         self.use_additional_parametters(p)
275     q=numpy.array(x, copy=True, dtype=numpy.complex)
276     if sigma==0:
277         qs=[q]
278         Ps=[1.]
279     else:
280         qi=numpy.linspace(-3.*sigma, 3.*sigma, int(sigma_steps))
281         Ps=numpy.exp(-0.5*qi**2/sigma**2)
282         Ps=(Ps/Ps.sum()).tolist()
283         qs=[q+qii for qii in qi]
284     # Create an additional q-array for K_alpha2 and join them as one array for
285     the calculation
286     if I_alpha2!=0:
287         if sigma==0:
288             qs.append(q*lambda_alpha2)
289             Ps.append(I_alpha2)
290         else:
291             qs+=[qi*lambda_alpha2 for qi in qs]
292             Ps+=[Pi*I_alpha2 for Pi in Ps]
293     # calculate Intensities for each q and P
294     I=numpy.zeros_like(x)
295     Is=numpy.zeros_like(x)
296     for qi, Pi in zip(qs, Ps):
297         Ii, Isi=self.calc_I(p, qi)
298         if any(Ii==numpy.nan):
299             print "I is NaN"
300         if any(Isi==numpy.nan):
301             print "Is is NaN"
302         I+=Pi*Ii
303         Is+=Pi*Isi
304     # Correct intensity for the scattering volume of the film dependent on  $\Theta$ 
305     theta=numpy.arcsin(q.real/4./numpy.pi*lambda_xray)

```

```

300     I/=numpy.sin(theta)
301     I_sum=I*I_0+Is*I_substrate
302     # Correct intensity for the polarization factor
303     polfac=self.polarization**2+(1.-self.polarization)*numpy.cos(2.*theta)**2.
304     return I_sum*polfac+BG
305
306 def use_additional_paramerters(self, p):
307     """
308     User function to connect additional fit parameters to variables.
309     """
310     b=self.bases
311     for i, item in self.fittable_elements.items():
312         elem=p[18+i]
313         old=b[item[0]][item[1]]
314         b[item[0]][item[1]]=(old[0], old[1], elem)
315
316 class CrystalMultilayerSF2(CrystalMultilayerSF):
317     # define class variables.
318     name="CrystalMultilayerSF2"
319     max_iter=50. # maximum number of iterations
320     parameters=[0.000223394, 0.0,
321                 20.0, 5.34, 5.8, 0.4, 0.4,
322                 10, 2, 0.1,
323                 0.00005, 5.18, 0.000125,
324                 0.5, 0.99752,
325                 0., 15, 1.54]
326
327     parameter_names=['I', 'BG', # Multilayer intensity and background
328                     'M', 'a1', 'a2', 'δA', 'δB',
329                     'NA', 'NB', 'c',
330                     'I_substrate', 'a_substrate', 'mu',
331                     'I-αK2', 'λ-αK2', # Relative intensity and wavelength of Cu
332                     'q-res', 'steps-res', 'λ', # q resolution of the instrument
333                     , steps for resolution, measured wavelength
334                     ]
334     parameter_description={
335         'I': 'Multilayer Intensity',
336         'BG': 'Background',
337         'M': 'Multilayer Periods',
338         'a1': 'd-spacing of layer 1',
339         'a2': 'd-spacing of layer 2',
340         'δA': 'Distribution of scattering plane repetitions',
341         'δB': 'Distribution of scattering plane repetitions',
342         'NA': 'Number of Monolayers',
343         'NB': 'Number of Monolayers',
344         'c': 'Width of interlayer spacing distribution',
345         'I_substrate': 'Substrate peak intensity',
346         'a_substrate': 'd-spacing of Substrate',
347         'mu': 'Absorption lengths',
348         'I-αK2': 'Intensity ratio of αK2',
349         'λ-αK2': 'Wavelength ratio of αK2',
350         'q-res': 'q-resolution of the instrument (Gauss)',
351         'λ': 'Wavelength used',
352     }
353     fit_function_text='Multilayer'
354
355     def create_model(self, p, q):
356         """
357         Create the model object from given parameters.
358         """
359         M=p[2]
360         a1=p[3]
361         a2=p[4]
362         deltaA=p[5]
363         deltaB=p[6]
364         N1=p[7]
365         N2=p[8]
366         amin=((N1/(N1+N2))*a1+(N2/(N1+N2))*a2)

```

```

367     a=amin
368     if deltaA==0. or deltaB==0:
369         N1=int(N1)
370         N2=int(N2)
371         a=(D-((N1-1)*a1+(N2-1)*a2))/2.
372     c=p[9]
373     f1=CrystalStructureFactor(a1, self.bases['A'], q)
374     f2=CrystalStructureFactor(a2, self.bases['B'], q)
375     # Single crystalline layers
376     A=CrystalLayerStructureModel(q, a1, f1, N1, deltaA)
377     B=CrystalLayerStructureModel(q, a2, f2, N2, deltaB)
378     # Stack of bilayers
379     Model=MultilayerModel(q, A, B, M, a, c)
380     return Model
381
382 class AtommicFormFactor(object):
383     """
384     Form factor of an atom represented as bessel functions.
385     """
386
387     def __init__(self, parameters):
388         self.parameters=parameters
389         a=[parameters[0]]
390         b=[parameters[1]]
391         a.append(parameters[2])
392         b.append(parameters[3])
393         a.append(parameters[4])
394         b.append(parameters[5])
395         a.append(parameters[6])
396         b.append(parameters[7])
397         c=parameters[8]
398         self.a=a
399         self.b=b
400         self.c=c
401
402     def __call__(self, q):
403         """
404         Calculate the formfactor of q when an instance gets called.
405         """
406         f=numpy.zeros_like(q)
407         q_over_4pi_2=(q/(4.*numpy.pi))**2
408         exp=numpy.exp
409         a=self.a
410         b=self.b
411         c=self.c
412         for i in range(4):
413             f+=a[i]*exp(-b[i]*q_over_4pi_2)
414         f+=c
415         return f
416
417 from ml_includes.form_factors import FORM_FACTOR_PARAMETERS
418
419 class CrystalStructureFactor(numpy.ndarray):
420     """
421     A ndarray object which calculates the structure factor of a crystal basis
422     each time the q vector is changed.
423     """
424
425     # Form factors for common atoms/ions
426     f=dict([(key, AtommicFormFactor(value)) for key, value in
427             FORM_FACTOR_PARAMETERS.items()])
427
428     # crystal elongation in out-of-plane direction
429     scale=1.0
430
431     # Direction of the layer growths
432     n_qz=numpy.array([1., 0., 0.])
433
434     # zero out-of-plane q position
435     q_0=numpy.array([0., 0., 0.])
436
437     # one over volume of the unit cell divided by the out-of-plane lattice
438     parameter

```

```

434 volume_scale=1.
435
436 def __new__(subtype, a, basis, q, dtype=numpy.complex, buffer=None, offset
    =0,
    strides=None, order=None):
437     shape=len(q)
438     instance=numpy.ndarray.__new__(subtype, shape, dtype, buffer, offset,
    strides, order)
439     lattice=basis[0][0].lattice
440     instance.a=lattice.stdbase
441     instance.scale=a
442     instance.basis=collect_cif_info.get_all_atoms(*basis[0]) # expand the
    lattice and symmetry to all atom positions
443     instance.n_qz=numpy.array(basis[1])/numpy.sqrt((basis[1]**2).sum())
444     dqz=a/numpy.sqrt((numpy.dot(lattice.recbase, basis[1])**2).sum())
445     instance.q_0=2.*numpy.pi*numpy.dot(lattice.recbase, basis[2]) # origin of
    the scan in q
446     volume=numpy.dot(lattice.stdbase[:, 0], numpy.cross(lattice.stdbase[:, 1],
    lattice.stdbase[:, 2]))
447     instance.volume_scale=dqz/volume
448     instance.q=q
449     return instance
450
451
452 def _get_q(self):
453     return self._q
454
455 def _set_q(self, qz):
456     """
457     Calculate the structure factor as function of the new q and set the
458     array values accordingly.
459     """
460     qz=self.scale*qz
461     self._q=qz
462     a=self.a
463     f=self.f
464     q_0=self.q_0
465     n_qz=self.n_qz
466     exp=numpy.exp
467     if len(qz)!=len(self):
468         self.resize(len(qz), refcheck=False)
469     numpy.ndarray.__setslice__(self, 0, len(self), 0.)
470     # calculate q-vector
471     q=(n_qz*(qz.transpose())[:, numpy.newaxis])+q_0
472     absq=numpy.sqrt((q**2).sum(axis=1))
473     for atom in self.basis:
474         #f(lq!)*occupancy*exp(i·q·r)
475         self+=f[atom.element.lower()](absq)*atom.occupancy*exp(1j*numpy.dot(q,
    numpy.dot(atom.xyz, a)))
476
477     q=property(_get_q, _set_q)
478
479 class CrystalLayerStructureModel(object):
480     """
481     Structural model of single crystalline layer.
482     For better readability of code using this object, all functions are
    wrapped as properties.
483     (e.g. object.F returns object._get_F())
484     """
485
486     def __init__(self, q, d, f, N, deltaN=0.):
487         """
488         Create the structure model for a given q.
489         """
490         self.q=numpy.array(q, copy=False, dtype=numpy.complex) # q-vector
491         self.d=d # lattice plane distance
492         self.f=f # scattering power, can be a function of q
493         self.N=N # Averadge number of lattice planes (Integer)
494         self.deltaN=deltaN # Spread of number of lattice planes
495

```

```

496 def _get_F(self):
497     """
498     Return the average scattering amplitude factor <F> of the layer. (F-bar
      in equation (6))
499     """
500     exp=numpy.exp
501     matrix=numpy.asmatrix
502     q=self.q
503     N=self.N
504     d=self.d
505     f=self.f
506     deltaN=self.deltaN
507     if deltaN==0.:
508         # no spread in thickness (8)
509         F=f*(1.-exp(1j*q*N*d))/(1.-exp(1j*q*d))
510     else:
511         # discrete fluctuation of layer thicknesses (10)
512         Nj=self.Nj
513         P=self.P
514         #  $\sum P(N_j) \cdot F_j$  implemented as matrix multiplications ((column-line)·
      column→matrix·column→ sum_column)
515         F=f*(numpy.array(((1.-exp(1j*matrix(q).transpose()*matrix(Nj)*d))*matrix
      (P).transpose()))).flatten()/\
      (1.-exp(1j*q*d))
516
517     return F
518
519 def _get_FFstar(self):
520     """
521     Return the average structure factor <FF*> of the layer.
522     """
523     exp=numpy.exp
524     matrix=numpy.asmatrix
525     q=self.q
526     N=self.N
527     d=self.d
528     f=self.f
529     deltaN=self.deltaN
530     if deltaN==0.:
531         # no spread in thickness
532         F=f*(1.-exp(1j*q*N*d))/(1.-exp(1j*q*d))
533         FFstar=F*F.conj()
534     else:
535         # discrete fluctuation of layer thicknesses (10)
536         Nj=self.Nj
537         P=self.P
538         #  $\sum P(N_j) \cdot F_j \cdot F_j^*$  implemented as matrix multiplications ((column-line)·
      column→matrix·column→ sum_column)
539         Fpart=numpy.asarray(1.-exp(1j*matrix(q).transpose()*matrix(Nj)*d))
540         Fpart*=Fpart.conj()
541         FFstar=f**2*(numpy.asarray(matrix(Fpart)*matrix(P).transpose()).flatten
      ())/(1.-exp(1j*q*d))*(1.-exp(1j*q*d)).conj())
542     return numpy.abs(FFstar)
543
544 def _get_T(self):
545     """
546     Average phase factor <exp(iqt)> of the layer. (T in equation (6))
547     """
548     exp=numpy.exp
549     matrix=numpy.asmatrix
550     N=self.N
551     d=self.d
552     q=self.q
553     deltaN=self.deltaN
554     if deltaN==0.:
555         # no spread in thickness
556         t=(N-1)*d
557         T=exp(1j*q*t)
558     else:
559         # discrete fluctuation of layer thicknesses (10)

```

```

560     Nj=self.Nj
561     P=self.P
562     #  $\sum P(N_j) \cdot \exp((N_j-1)iqd)$  implemented as matrix multiplications ((
563         column·line)·column→matrix·column→ sum_column)
564     T=numpy.asarray((exp(1j*matrix(q).transpose()*matrix(Nj-1.)*d))*matrix(P
565         ).transpose()).flatten()
566     return T
567
568 def _get_Phi(self):
569     """
570     Averadge phase and complex conjugated amplitude <exp(iqt)F*> of the
571     layer. (Phi in equation (6))
572     """
573     exp=numpy.exp
574     matrix=numpy.asmatrix
575     q=self.q
576     N=self.N
577     d=self.d
578     f=self.f
579     deltaN=self.deltaN
580     if deltaN==0.:
581         # no spread in thickness
582         t=(N-1.)*d
583         F=f*(1.-exp(1j*q*N*d))/(1.-exp(1j*q*d))
584         Fstar=F.conj()
585         Phi=exp(1j*q*t)*Fstar
586     else:
587         # discrete fluctuation of layer thicknesses (10)
588         Nj=self.Nj
589         P=self.P
590         #  $\sum P(N_j) \cdot \exp((N_j-1)iqd) \cdot F_j$  implemented as matrix multiplications
591         ((column·line)·column→matrix·column→ sum_column)
592         exp_part=numpy.asarray(exp(1j*matrix(q).transpose()*matrix(Nj-1.)*d))
593         q_iqNj=exp(matrix(1j*q).transpose()*matrix(Nj)*d)
594         factor=f/(1.-exp(1j*q*d))
595         Fpart=numpy.asarray(((1.-q_iqNj).transpose()).transpose())
596         Phi=numpy.asarray(numpy.matrix(exp_part*Fpart.conj()*matrix(P).
597             transpose()).flatten()*factor.conj())
598     return Phi
599
600 def _get_Nj(self):
601     """
602     Get an array of integers between 0 and 2·N.
603     """
604     N=self.N
605     deltaN=self.deltaN
606     return numpy.arange(int(N-3.*deltaN)-1, N+3.*deltaN+2, 1)
607
608 def _get_P(self):
609     """
610     Get an array of the gaussian probabilities for a specific number of
611     lattice plane repetitions Nj.
612     """
613     N=self.N
614     Nj=self.Nj
615     deltaN=self.deltaN
616     if deltaN<1. and int(N)!=N:
617         # the discrete gaussian does not produce the right averadge
618         # for small sigma values so we integrate the probabilities
619         # with smaller steps
620         N_down=int(N)
621         N_up=int(N)+1.
622         P_up=numpy.exp(-0.5*(Nj-N_up)**2/deltaN**2)
623         P_up/=P_up.sum()
624         P_down=numpy.exp(-0.5*(Nj-N_down)**2/deltaN**2)
625         P_down/=P_down.sum()
626         a=(N-N_down)/(N_up-N_down)
627         P=a*P_up+(1.-a)*P_down
628     else:

```

```

624     P=numpy.exp(-0.5*(Nj-N)**2/deltaN**2)
625     P=P.sum()
626     return P
627
628     F=property(_get_F)
629     FFstar=property(_get_FFstar)
630     Phi=property(_get_Phi)
631     T=property(_get_T)
632     # Only for distribution of thicknesses
633     Nj=property(_get_Nj)
634     P=property(_get_P)
635
636 class MultilayerModel(object):
637     """
638     Structural model of a multilayer consisting of bilayers. It is general in
639     the sense,
640     that the Layers can be calculated separately.
641     For better readability of code using this object, all functions are
642     wrapped as properties.
643     (e.g. object.F returns object._get_F())
644
645     """
646     def __init__(self, q, A, B, M, a, c):
647         """
648         Create the structure model for a given q.
649
650         self.q=numpy.array(q, copy=False, dtype=numpy.complex) # q-vector
651         self.A=A # Structure model of layer 1
652         self.B=B # Structure model of layer 2
653         self.M=M # Repetitions
654         self.a=a # distance between adjacent layers (region without defined
655         crystal lattice)
656         self.c=c # fluctuations of a  $\sigma()$ 
657
658     """
659     def _get_psi(self):
660         """
661         Phase between layer (defined between equation (5) and (6)).
662
663         """
664         q=self.q
665         a=self.a
666         exp=numpy.exp
667         c=self.c
668         psi=1j*q*a-q**2*c**2/2.
669         return psi
670
671     def _get_I(self):
672         """
673         Calculate the scattering intensity of the multilayer using equation (7).
674         Subscripted items in the equation are written as attributes of the
675         associated layer.
676         (E.g. T_A <==> A.T or <F_A F_A*> <==> A.FFstar)
677
678         """
679         exp=numpy.exp
680         A=self.A
681         B=self.B
682         M=self.M
683         psi=self.psi
684         I=numpy.zeros_like(numpy.abs(self.q)).astype(numpy.float64) # the result
685         # should be of type float
686         I+=M*(A.FFstar+2.*(exp(psi)*A.Phi*B.F).real+B.FFstar) # first term in (7)
687         s1=(exp(-psi)*B.Phi*A.F/(A.T*B.T)+A.Phi*A.F/A.T+B.Phi*B.F/B.T+exp(psi)*A.
688         Phi*B.F) # second term in (7)
689         s2=((M-(M+1)*exp(2.*psi)*A.T*B.T+(exp(2.*psi)*A.T*B.T)**(M+1))/(1.-exp(2.*
690         psi)*A.T*B.T)**2-M) # third term in (7)
691         I+=2.* (s1*s2).real
692         return I
693
694     psi=property(_get_psi)
695     I=property(_get_I)

```



```

686
687 model_basis={
688     'B': [(Structure(atoms=[Atom('O2-', [0., 0., 0.])],
689                     lattice=Lattice(3., 3., 3., 90., 90., 90)),
690           SpaceGroupList[0]),
691           numpy.array([1., 0., 0.]), numpy.array([0., 0.,
692           0.])], # out-of-plane direction and scan
693           origin
694     'A': [(Structure(atoms=[Atom('O2-', [0., 0., 0.])],
695                     lattice=Lattice(3., 3., 3., 90., 90., 90)),
696           SpaceGroupList[0]),
697           numpy.array([1., 0., 0.]), numpy.array([0., 0.,
698           0.])], # out-of-plane direction and scan
699           origin
700     'substrate': [(Structure(atoms=[Atom('O2-', [0., 0., 0.])],
701                             lattice=Lattice(3., 3., 3., 90., 90.,
702                             90)), SpaceGroupList[0]),
703                   numpy.array([1., 0., 0.]), numpy.array([0., 0.,
704                   0.])], # out-of-plane direction and scan
705                   origin
706     }
707
708 #+++++ Plugin settings ++++++
709 SESSIONS=['CircleSession', 'ReflectometerSession']
710
711 def activate(window, session):
712     # Add simulation to fit functions in the GUI
713     fit_data.register_class(CrystalMultilayer)
714
715 #+++++ GUI functions ++++++
716 def menu(window, session):
717     """
718     Menu Entruies.
719     """
720     global active_session, active_window
721     active_session=session
722     active_window=window
723     string=""
724     <menu action='MLSimu'>
725         <menuitem action='MLNew Model' />
726         <menuitem action='MLEdit Model' />
727     </menu>
728     """
729     # Create actions for the menu
730     actions=(
731         ("MLSimu", None, # name, stock id
732          "Multilayer simulation", None, # label, accelerator
733          None, # tooltip
734          None),
735         ("MLNew Model", None, # name, stock id
736          "Create new multilayer model...", None, # label, accelerator
737          None, # tooltip
738          create_new_model),
739         ("MLEdit Model", None, # name, stock id
740          "Edit multilayer model...", None, # label, accelerator
741          None, # tooltip
742          edit_model),
743     )
744     return string, actions
745
746 def create_new_model(action, widget):
747     """
748     Open a dialog to input special model parameters and
749     create the model for the active dataset.
750     """
751     global model_basis
752     dialog=ModelDialog(model_basis)
753     result=dialog.run()
754     if result==1:

```

```

746     model_basis=dialog.model_basis
747     dataset=active_session.active_file_data[active_window.index_mess]
748     if dataset.fit_object is None:
749         dataset.fit_object=fit_data.FitSession(dataset)
750     dataset.fit_object.functions.append([CrystalMultilayerSF([],
751                                     False, True, True, True])
752     if 'Q_z' in dataset.dimensions():
753         dataset.xdata=dataset.dimensions().index('Q_z')
754     dialog.destroy()
755
756 def edit_model(action, widget):
757     """
758     Open a dialog to input special model parameters and
759     create the model for the active dataset.
760     """
761     dataset=active_session.active_file_data[active_window.index_mess]
762     fit=None
763     for fititem in dataset.fit_object.functions:
764         if hasattr(fititem[0], 'bases'):
765             fit=fititem[0]
766     if fit is None:
767         return
768     dialog=ModelDialog(fit.bases, copy=False, buttons=('Apply', 1, 'Close', 0))
769     dialog.show()
770     dialog.connect('response', responde_edited, dataset)
771
772 def responde_edited(dialog, id, dataset):
773     if id==1:
774         dataset.fit_object.simulate()
775         active_window.replot()
776     else:
777         dialog.destroy()
778
779 class ModelDialog(gtk.Dialog):
780     """
781     Dialog that holds three entries for the structure of substrat,
782     layer A and layer B plus additional options for the model creation.
783     """
784     current_folder=os.path.curdir
785
786     def __init__(self, model_basis, copy=True, buttons=('Create Model', 1, '
787         Cancel', 0), **args):
788         """
789         Create the Dialog and entries.
790         """
791         if copy:
792             self.model_basis=deepcopy(model_basis)
793         else:
794             self.model_basis=model_basis
795         keys=self.model_basis.keys()
796         keys.sort()
797         gtk.Dialog.__init__(self, title='Model Parameters...', buttons=buttons, **
798             args)
799         # structure the dialog with options left and structure right
800         hbox=gtk.HBox()
801         hbox.show()
802         self.vbox.add(hbox)
803         vbox=gtk.VBox()
804         vbox.show()
805         self.structure_entries={}
806         for key in keys:
807             entries, table=self._create_structure_entries('Structure of %s:'%key,
808                 self.model_basis[key][0])
809             self.structure_entries[key]=entries
810             vbox.add(table)
811             entries['load button'].connect('clicked', self._load_cif, key)
812             entries['symmetry selection'].connect('changed', self._change_symmetry,
813                 key)
814             entries['new button'].connect('clicked', self._add_atom, key)

```

```

811     entries=self._create_option_entries()
812     frame=gtk.Frame()
813     frame.add(entries)
814     frame.show()
815     align=gtk.Alignment()
816     align.add(frame)
817     align.show()
818     hbox.pack_start(align, expand=False)
819     sw=gtk.ScrolledWindow()
820     sw.set_policy(gtk.POLICY_NEVER, gtk.POLICY_AUTOMATIC)
821     sw.add_with_viewport(vbox)
822     sw.show()
823     hbox.pack_end(sw)
824
825 def _create_structure_entries(self, title, basis):
826     '''
827     Create entries for crystal structure information.
828     '''
829     unit_cell=basis[0]
830     abcABG=unit_cell.lattice.abcABG()
831     symmetry=basis[1]
832     entries={'lattice parameters':{}, 'atoms':{}}
833     # Create table with entries and labels
834     table=gtk.Table(12, 6)
835     label=gtk.Label(title)
836     table.attach(label, 0, 9, 0, 1, 0, 0, 0, 0)
837     label.show()
838     button=gtk.Button('Load CIF')
839     table.attach(button, 9, 12, 0, 1, 0, 0, 0, 0)
840     button.show()
841     entries['load button']=button
842     #####
843     label=gtk.Label('Space Group:')
844     table.attach(label, 0, 6, 1, 2, 0, 0, 0, 0)
845     label.show()
846     selection=gtk.combo_box_new_text()
847     for i, sg in enumerate(SpaceGroupList):
848         selection.append_text("%i: %s"%(sg.number, sg.short_name))
849         if symmetry.number==sg.number:
850             selection.set_active(i)
851     table.attach(selection, 6, 12, 1, 2, gtk.EXPAND|gtk.FILL, 0, 0, 0)
852     selection.show()
853     entries['symmetry selection']=selection
854     label.show()
855     #####
856     label=gtk.Label('Lattice Parameters')
857     table.attach(label, 0, 6, 2, 3, 0, 0, 0, 0)
858     label.show()
859     label=gtk.Label('Basis Angles')
860     table.attach(label, 6, 12, 2, 3, 0, 0, 0, 0)
861     label.show()
862     for i, item in enumerate(['a', 'b', 'c', ' $\alpha$ ', ' $\beta$ ', ' $\gamma$ ']):
863         label=gtk.Label(item)
864         entry=gtk.Entry()
865         entry.set_text("%.4g"%abcABG[i])
866         entry.set_width_chars(5)
867         table.attach(label,
868             # X direction #           # Y direction
869             2*i, 2*i+1, 3, 4,
870             0, 0,
871             0, 0)
872         table.attach(entry,
873             # X direction #           # Y direction
874             2*i+1, 2*i+2, 3, 4,
875             gtk.EXPAND|gtk.FILL, 0,
876             0, 0)
877         label.show()
878         entry.show()

```

```

879         entry.connect('changed', self._change_lattice_parameter, unit_cell.
880                        lattice, i)
881         entries['lattice parameters'][item]=entry
882         #####
883         atom_table=self._create_atom_table(unit_cell)
884         align=gtk.Alignment(xalign=0.5, xscale=1.0)
885         align.add(atom_table)
886         align.show()
887         table.attach(align,
888                     # X direction #           # Y direction
889                     0, 12, 4, 5,
890                     gtk.EXPAND|gtk.FILL, 0,
891                     0, 0)
892         entries['atoms']=align
893         #####
894         button=gtk.Button('New Atom')
895         table.attach(button, 0, 6, 5, 6, 0, 0, 0, 0)
896         button.show()
897         entries['new button']=button
898         #####
899         table.show()
900         return entries, table
901
902     def _create_atom_table(self, unit_cell):
903         """
904         Create an entry table for atoms.
905         """
906         table=gtk.Table(12, 1+len(unit_cell), False)
907         label=gtk.Label('Atom')
908         table.attach(label, 0, 2, 0, 1, 0, 0, 0, 0)
909         label.show()
910         label=gtk.Label('Position')
911         table.attach(label, 2, 4, 0, 1, 0, 0, 0, 0)
912         label.show()
913         label=gtk.Label('x')
914         table.attach(label, 4, 6, 0, 1, 0, 0, 0, 0)
915         label.show()
916         label=gtk.Label('y')
917         table.attach(label, 6, 8, 0, 1, 0, 0, 0, 0)
918         label.show()
919         label=gtk.Label('z')
920         table.attach(label, 8, 10, 0, 1, 0, 0, 0, 0)
921         label.show()
922         label=gtk.Label('Occ.')
923         table.attach(label, 10, 12, 0, 1, 0, 0, 0, 0)
924         label.show()
925         entries=[]
926         for i, atom in enumerate(unit_cell):
927             button=gtk.Button('del')
928             table.attach(button, 2, 4, 1+i, 2+i, 0, 0, 0, 0)
929             button.show()
930             widgets=[]
931             button.connect('clicked', self._delete_atom, unit_cell, atom, table,
932                             widgets)
933             elements=sorted(FORM_FACTOR_PARAMETERS.keys())
934             atom_selection=gtk.combo_box_new_text()
935             for element in elements:
936                 atom_selection.append_text(element)
937                 atom_selection.set_active(elements.index(atom.element.lower()))
938                 atom_selection.connect('changed', self._change_atom_type, atom)
939                 table.attach(atom_selection, 0, 2, 1+i, 2+i, 0, 0, 0, 0)
940                 atom_selection.show()
941                 widgets.append(atom_selection)
942             entry=gtk.Entry()
943             entry.set_text("%.4g"%atom.xyz_cartn[0])
944             entry.set_width_chars(5)
945             table.attach(entry, 4, 6, 1+i, 2+i, gtk.EXPAND|gtk.FILL, 0, 0, 0)
946             entry.show()
947             widgets.append(entry)

```

```

946     entry.connect("changed", self._change_atom_position, atom, 0)
947     entry=gtk.Entry()
948     entry.set_text("%.4g"%atom.xyz_cartn[1])
949     entry.set_width_chars(5)
950     table.attach(entry, 6, 8, 1+i, 2+i, gtk.EXPAND|gtk.FILL, 0, 0, 0)
951     entry.show()
952     widgets.append(entry)
953     entry.connect("changed", self._change_atom_position, atom, 1)
954     entry=gtk.Entry()
955     entry.set_text("%.4g"%atom.xyz_cartn[2])
956     entry.set_width_chars(5)
957     table.attach(entry, 8, 10, 1+i, 2+i, gtk.EXPAND|gtk.FILL, 0, 0, 0)
958     entry.show()
959     widgets.append(entry)
960     entry.connect("changed", self._change_atom_position, atom, 2)
961     entry=gtk.Entry()
962     entry.set_text("%.4g"%atom.occupancy)
963     entry.set_width_chars(5)
964     entry.connect("changed", self._change_atom_occupancy, atom)
965     table.attach(entry, 10, 12, 1+i, 2+i, 0, 0, 0, 0)
966     entry.show()
967     widgets.append(entry)
968     table.show()
969     return table
970
971 def _change_lattice_parameter(self, entry, lattice, index):
972     try:
973         entry_float=float(entry.get_text())
974     except ValueError:
975         return
976     else:
977         items=['a', 'b', 'c', 'alpha', 'beta', 'gamma']
978         lattice.setLatPar(**{items[index]:entry_float})
979
980 def _change_atom_position(self, entry, atom, index):
981     try:
982         entry_float=float(entry.get_text())
983     except ValueError:
984         return
985     else:
986         atom.xyz_cartn[index]=entry_float
987
988 def _change_atom_occupancy(self, entry, atom):
989     try:
990         entry_float=float(entry.get_text())
991     except ValueError:
992         return
993     else:
994         atom.occupancy=entry_float
995
996 def _change_atom_type(self, selection, atom):
997     elements=sorted(FORM_FACTOR_PARAMETERS.keys())
998     atom.element=elements[selection.get_active()]
999
1000 def _delete_atom(self, button, unit_cell, atom, table, widgets):
1001     unit_cell.remove(atom)
1002     for widget in widgets:
1003         table.remove(widget)
1004     table.remove(button)
1005
1006 def _load_cif(self, button, key):
1007     """
1008     Load parameters from a CIF file the user selects with another dialog.
1009     """
1010     file_selection=gtk.FileChooserDialog(title='Select CIF file ...',
1011                                         parent=self,
1012                                         action=gtk.FILE_CHOOSER_ACTION_OPEN,
1013                                         buttons=('OK', 1, 'Cancel', 0))
1014     file_selection.set_select_multiple(False)

```

```

1015     file_selection.set_current_folder(self.current_folder)
1016     filter=gtk.FileFilter()
1017     filter.set_name('Crystallographic Information (CIF)')
1018     filter.add_pattern('*.cif')
1019     filter.add_pattern('*.CIF')
1020     file_selection.add_filter(filter)
1021     filter=gtk.FileFilter()
1022     filter.set_name('All')
1023     filter.add_pattern('*')
1024     file_selection.add_filter(filter)
1025     result=file_selection.run()
1026     if result==1:
1027         self.current_folder=file_selection.get_current_folder()
1028         file_name=unicode(file_selection.get_filename())
1029         if file_name is not None and os.path.exists(file_name):
1030             file_handler=open(file_name, 'r')
1031             self.model_basis[key][0]=collect_cif_info.eval_cif_file(file_handler)
1032             self.update_entries(key)
1033             file_selection.destroy()
1034
1035     def _add_atom(self, button, key):
1036         """
1037         Add a new button to the unit cell.
1038         """
1039         unit_cell=self.model_basis[key][0][0]
1040         unit_cell.addNewAtom('o2-')
1041         self.update_entries(key)
1042
1043     def _change_symmetry(self, selection, key):
1044         """
1045         Change the symmetry of the crystal from the dialog selection.
1046         """
1047         self.model_basis[key][0]=(self.model_basis[key][0][0], SpaceGroupList[
            selection.get_active()])
1048
1049     def update_entries(self, key):
1050         """
1051         Update the entry settings after parameter change.
1052         """
1053         entries=self.structure_entries[key]
1054         unit_cell, symmetry=self.model_basis[key][0]
1055         abcABG=unit_cell.lattice.abcABG()
1056         entries['symmetry selection'].set_active([item.number for item in
            SpaceGroupList].index(symmetry.number))
1057         for i, item in enumerate(['a', 'b', 'c', 'α', 'β', 'γ']):
1058             entries['lattice parameters'][item].set_text("%.4g"%abcABG[i])
1059         align=entries['atoms']
1060         align.remove(align.get_children()[0])
1061         atom_table=self._create_atom_table(unit_cell)
1062         align.add(atom_table)
1063
1064     def _create_option_entries(self):
1065         """
1066         Create entries for the model not directly including the crystal unit
1067         cell.
1068         """
1069         keys=self.model_basis.keys()
1070         keys.sort()
1071         table=gtk.Table(8, 9)
1072         label=gtk.Label('General Model Parameters:')
1073         label.show()
1074         table.attach(label, 0, 8, 0, 1, gtk.EXPAND|gtk.FILL, 0, 0, 0)
1075         # direction and origin of the scan
1076         for i, key in enumerate(keys):
1077             direction_vector=self.model_basis[key][1]
1078             label=gtk.Label('Growths direction %s:'%key)
1079             label.show()
1080             table.attach(label, 0, 5, 1+i*2, 2+i*2, 0, 0, 0, 0)
            # Add entries for the HKL direction of the epitaxial growth

```

```

1081     for j in range(3):
1082         spinner=gtk.SpinButton(adjustment=None, climb_rate=1., digits=0)
1083         spinner.set_range(0, 10)
1084         spinner.set_increments(1, 10)
1085         spinner.set_width_chars(2)
1086         spinner.show()
1087         spinner.set_value(direction_vector[j])
1088         spinner.connect('changed', self._change_direction, key, j)
1089         table.attach(spinner, 5+j, 6+j, 1+i*2, 2+i*2, 0, 0, 0, 0)
1090     origin_vector=self.model_basis[key][2]
1091     label=gtk.Label('Scan origin %s:'%key)
1092     label.show()
1093     table.attach(label, 0, 5, 2+i*2, 3+i*2, 0, 0, 0, 0)
1094     # Add entries for the HKL direction of the epitaxial growth
1095     for j in range(3):
1096         spinner=gtk.SpinButton(adjustment=None, climb_rate=1., digits=0)
1097         spinner.set_range(0, 10)
1098         spinner.set_increments(1, 10)
1099         spinner.set_width_chars(2)
1100         spinner.show()
1101         spinner.set_value(origin_vector[j])
1102         spinner.connect('changed', self._change_origin, key, j)
1103         table.attach(spinner, 5+j, 6+j, 2+i*2, 3+i*2, 0, 0, 0, 0)
1104     table.show()
1105     return table
1106
1107 def _change_direction(self, spinner, key, index):
1108     '''
1109     Change the direction vector when the
1110     '''
1111     item=self.model_basis[key][1]
1112     new_value=spinner.get_value()
1113     item[index]=new_value
1114
1115 def _change_origin(self, spinner, key, index):
1116     '''
1117     Change the origin vector when the
1118     '''
1119     item=self.model_basis[key][2]
1120     new_value=spinner.get_value()
1121     item[index]=new_value

```

## B.2 Reflectivity model for oxide samples

```

1  '''
2      Changed reflectivity model from spec_nx.py introducing typical imperfections
3      for oxide layers. General help information in spec_nx.py.
4  '''
5  from numpy import *
6  from scipy.special import wofz
7
8  import lib.paratt as Paratt
9  import lib.neutron_refl as MatrixNeutron
10 from lib.instrument import *
11
12 # Preamble to define the parameters needed for the models outlined below:
13 ModelID='SpecNXInhom'
14 __pars__=['Layer', 'Stack', 'Sample', 'Instrument']
15 instrument_string_choices={'probe': ['x-ray', 'neutron', 'neutron pol', \
16     'neutron pol spin flip', 'neutron tof', 'neutron pol tof'], 'coords': ['q',
17     'tth'], \
18     'restype': ['no conv', 'fast conv', \
19     'full conv and varying res.', 'fast conv + varying res.', 'varying delta
20     theta and asymmetric delta lambda'], \
21     'footype': ['no corr', 'gauss beam', 'square beam'], \
22     'pol': ['uu', 'dd', 'ud']}

```

```

21 InstrumentParameters={'probe':'neutron', 'wavelength':5.616, 'coords':'q', \
22   'IO':1.0, 'res':0.001, \
23   'restype':'no conv', 'respoints':5, 'resinrange':2, 'beamw':0.01, \
24   'lambdars': 0.03, 'asymmetry': 0.,
25   'footype': 'no corr', 'samplelen':10.0, 'incangle':0.0, 'pol': 'uu', \
26   'Ibkg': 0.0}
27 InstrumentGroups=[('General', ['wavelength', 'coords', 'IO', 'Ibkg']),
28   ('Resolution', ['restype', 'res', 'respoints', '
29   resinrange']),
30   ('Neutron', ['probe', 'pol', 'incangle']),
31   ('Footprint', ['footype', 'beamw', 'samplelen', ]),
32   ]
33 LayerParameters={'sigma':0.0, 'dens':1.0, 'd':0.0, 'f':0.0+1.0j*1e-20, \
34   'b':0.0+1.0j*1e-20, 'xs_ai': 0.0, 'magn':0.0, 'magn_ang':0.0}
35 LayerGroups=[('Standard', ['f', 'dens', 'd', 'sigma']),
36   ('Neutron', ['b', 'xs_ai', 'magn', 'magn_ang'])]
37 StackParameters={'Layers':[], 'Repetitions':1, 'sigma_gradient': 0., '
38   d_gradient': 0.}
39 SampleParameters={'Stacks':[], 'Ambient':None, 'Substrate':None,
40   'sigma_inhom': 1., 'lscale_inhom': 0.9, 'flatwidth_inhom': 0.3,
41   'steps_inhom': 20, 'type_inhom': 2,
42   'cap_steps': 0, 'cap_sigma': 3, 'cap_step_height
43   ': 5, 'cap_gauss_center': 0.}
44
45 # A buffer to save previous calculations for spin-flip calculations
46 class Buffer:
47     Ruu=0
48     Rdd=0
49     Rdu=0
50     Rud=0
51     parameters=None
52
53 def Specular(TwoThetaQz, sample, instrument):
54     """
55     The model function. Averadging the intensities for different
56     layer thicknesses as found for e.g. large PLD samples.
57     """
58     # average thicknesses before inhomogeneity average
59     d0=[array([Layer.getD() for Layer in Stack.Layers]) for Stack in sample.
60         Stacks]
61     sigma_d=sample.getSigma_inhom()*0.01 # Inhomogeneity in % (gamma for type
62         2)
63     lorentz_scale=sample.getLscale_inhom()
64     flat_width=sample.getFlatwidth_inhom()*0.01
65     # Define the thicknesses to calculate and their propability
66     if sigma_d==0 or flat_width==0: # no inhomogeneity
67         d_fact=[1.]
68         P=[1.]
69     elif sample.getType_inhom()==1: # half gaussian chape inhomogeneity
70         d_fact=1.+linspace(-2.*sigma_d, 0, sample.getSteps_inhom())
71         P=exp(-0.5*(d_fact-sigma_d-1.)**2/sigma_d**2)
72         P/=P.sum()
73         mean_d=(P*d_fact).sum()
74         d_fact+=1.-mean_d
75     elif sample.getType_inhom()==2: # inhomogeneity of a PLD line focus,
76         better approximation
77         d_fact=1.+linspace(-1.*max(2.*sigma_d, flat_width), 0, sample.
78             getSteps_inhom())
79         Pg=where(d_fact>flat_width, lorentz_scale*1./((1.+((d_fact-1.)/sigma_d)
80             **2), 0.)
81         Pf=(1.-lorentz_scale)*where(d_fact>flat_width, 1., 0.)
82         P=Pg+Pf
83         P/=P.sum()
84         mean_d=(P*d_fact).sum()
85         d_fact+=1.-mean_d
86     else: # gaussian inhomegeniety
87         d_fact=1.+linspace(-sigma_d, sigma_d, sample.getSteps_inhom())
88         P=exp(-0.5*(d_fact-1.)**2/sigma_d**2)
89         P/=P.sum()

```



```

81 # Empty reflectivity
82 R=zeros_like(spec_raw(TwoThetaQz, sample, instrument))
83 for d_facti, Pi in zip(d_fact, P): # Reflectivity for each thickness
84     di=[d_facti*d0i for d0i in d0]
85     for i, Stack in enumerate(sample.Stacks):
86         for j, Layer in enumerate(Stack.Layers):
87             Layer.setD(di[i][j])
88     R+=Pi*spec_raw(TwoThetaQz, sample, instrument)
89 # Reset layer options
90 for i, Stack in enumerate(sample.Stacks):
91     for j, Layer in enumerate(Stack.Layers):
92         Layer.setD(d0[i][j])
93 # add instrumental resolution before returning the intensities
94 return spec_res(TwoThetaQz, sample, instrument, R)
95
96 def spec_raw(TwoThetaQz, sample, instrument):
97     '''
98     Calculate raw reflectivity without resolution.
99     '''
100     # preamble to get it working with my class interface
101     restype=instrument.getRestype()
102
103     if restype==2 or restype==instrument_string_choices['restype'][2]:
104         (TwoThetaQz, weight)=ResolutionVector(TwoThetaQz[:], \
105             instrument.getRes(), instrument.getRespoints(), \
106             range=instrument.getResinrange())
107     elif restype==4 or restype==instrument_string_choices['restype'][4]:
108         (TwoThetaQz, weight)=ResolutionVectorAsymmetric(TwoThetaQz[:], \
109             instrument.getRes(), instrument.getRespoints(), \
110             instrument.getLambdars(), instrument.getAsymmetry(), \
111             range=instrument.getResinrange())
112     # TTH values given as x
113     if instrument.getCoords()==instrument_string_choices['coords'][1]\
114         or instrument.getCoords()==1:
115         Q=4*pi/instrument.getWavelength()*sin(TwoThetaQz*pi/360.0)
116     # Q vector given ....
117     elif instrument.getCoords()==instrument_string_choices['coords'][0]\
118         or instrument.getCoords()==0:
119         Q=TwoThetaQz
120     else:
121         raise ValueError('The value for coordinates, coords, is WRONG!'
122             'should be q(0) or tth(1).')
123
124     type=instrument.getProbe()
125     pol=instrument.getPol()
126
127     lamda=instrument.getWavelength()
128     parameters=sample.resolveLayerParameters()
129     if type==instrument_string_choices['probe'][0] or type==0:
130         fb=array(parameters['f'], dtype=complex64)
131     else:
132         fb=array(parameters['b'], dtype=complex64)*1e-5
133
134     dens=array(parameters['dens'], dtype=complex64)
135     d=array(parameters['d'], dtype=float64)
136     magn=array(parameters['magn'], dtype=float64)
137     #Transform to radians
138     magn_ang=array(parameters['magn_ang'], dtype=float64)*pi/180.0
139
140     sigma=array(parameters['sigma'], dtype=float64)
141     sld=dens*fb*instrument.getWavelength()*2/2/pi
142
143     # Ordinary Paratt X-rays
144     if type==instrument_string_choices['probe'][0] or type==0:
145         R=Paratt.ReflQ(Q, instrument.getWavelength(), 1.0-2.82e-5*sld, d,
146             sigma)
147     #Ordinary Paratt Neutrons
148     elif type==instrument_string_choices['probe'][1] or type==1:
149         R=Paratt.ReflQ(Q, instrument.getWavelength(), 1.0-sld, d, sigma)

```

```

149 #Ordinary Paratt but with magnetization
150 elif type==instrument_string_choices['probe'][2] or type==2:
151     msld=2.645e-5*magn*dens*instrument.getWavelength()**2/2/pi
152     # Polarization uu or ++
153     if pol==instrument_string_choices['pol'][0] or pol==0:
154         R=Paratt.ReflQ(Q, instrument.getWavelength(), \
155             1.0-sld-msld, d, sigma)
156     # Polarization dd or --
157     elif pol==instrument_string_choices['pol'][1] or pol==1:
158         R=Paratt.ReflQ(Q, instrument.getWavelength(), \
159             1.0-sld+msld, d, sigma)
160     else:
161         raise ValueError('The value of the polarization is WRONG.'
162             ' It should be uu(0) or dd(1)')
163 # Spin flip
164 elif type==instrument_string_choices['probe'][3] or type==3:
165     # Check if we have calculated the same sample previous:
166     if Buffer.parameters!=parameters:
167         msld=2.645e-5*magn*dens*instrument.getWavelength()**2/2/pi
168         np=1.0-sld-msld
169         nm=1.0-sld+msld
170         wl=instrument.getWavelength()
171         (Ruu, Rdd, Rud, Rdu)=MatrixNeutron.Refl(Q, wl, np, nm, d, magn_ang
172             )
173         Buffer.Ruu=Ruu; Buffer.Rdd=Rdd; Buffer.Rud=Rud
174         Buffer.parameters=parameters.copy()
175     else:
176         pass
177     # Polarization uu or ++
178     if pol==instrument_string_choices['pol'][0] or pol==0:
179         R=Buffer.Ruu
180     # Polarization dd or --
181     elif pol==instrument_string_choices['pol'][1] or pol==1:
182         R=Buffer.Rdd
183     # Polarization ud or +-
184     elif pol==instrument_string_choices['pol'][2] or pol==2:
185         R=Buffer.Rud
186     else:
187         raise ValueError('The value of the polarization is WRONG.'
188             ' It should be uu(0), dd(1) or ud(2)')
189 # tof
190 elif type==instrument_string_choices['probe'][4] or type==4:
191     sld=dens[:, newaxis]*fb[:, newaxis]*\
192         (4*pi*sin(instrument.getIncangle()*pi/180)/Q)**2/2/pi
193     R=Paratt.Refl_nvary2(instrument.getIncangle()*ones(Q.shape), \
194         (4*pi*sin(instrument.getIncangle()*pi/180)/Q), \
195         1.0-sld, d, sigma)
196 # tof spin polarized
197 elif type==instrument_string_choices['probe'][5] or type==5:
198     sld=dens[:, newaxis]*fb[:, newaxis]*\
199         (4*pi*sin(instrument.getIncangle()*pi/180)/Q)**2/2/pi
200     msld=2.645e-5*magn[:, newaxis]*dens[:, newaxis]\
201         *(4*pi*sin(instrument.getIncangle()*pi/180)/Q)**2/2/pi
202     # polarization uu or ++
203     if pol==instrument_string_choices['pol'][0] or pol==0:
204         R=Paratt.Refl_nvary2(instrument.getIncangle()*ones(Q.shape), \
205             (4*pi*sin(instrument.getIncangle()*pi/180)/Q), \
206             1.0-sld-msld, d, sigma)
207     # polarization dd or --
208     elif pol==instrument_string_choices['pol'][1] or pol==1:
209         R=Paratt.Refl_nvary2(instrument.getIncangle()*ones(Q.shape), \
210             (4*pi*sin(instrument.getIncangle()*pi/180)/Q), \
211             1.0-sld+msld, d, sigma)
212     else:
213         raise ValueError('The value of the polarization is WRONG.'
214             ' It should be uu(0) or dd(1)')
215 else:
216     raise ValueError('The choice of probe is WRONG')

```

```

217     return R
218
219 def spec_res(TwoThetaQz, sample, instrument, R):
220     '''
221         Calculate resolution. Resolution type 4 introduces asymmetric wavelength
222         distribution.
223     '''
224     # preamble to get it working with my class interface
225     restype=instrument.getRestype()
226
227     if restype==2 or restype==instrument_string_choices['restype'][2]:
228         (TwoThetaQz, weight)=ResolutionVector(TwoThetaQz[:, \
229             instrument.getRes(), instrument.getRespoints(), \
230             range=instrument.getResinrange())
231     elif restype==4 or restype==instrument_string_choices['restype'][4]:
232         (TwoThetaQz, weight)=ResolutionVectorAsymmetric(TwoThetaQz[:, \
233             instrument.getRes(), instrument.getRespoints(), \
234             instrument.getLambdare(), instrument.getAsymmetry(),
235             range=instrument.getResinrange())
236
237     # TTH values given as x
238     if instrument.getCoords()==instrument_string_choices['coords'][1]\
239         or instrument.getCoords()==1:
240         Q=4*pi/instrument.getWavelength()*sin(TwoThetaQz*pi/360.0)
241     # Q vector given ....
242     elif instrument.getCoords()==instrument_string_choices['coords'][0]\
243         or instrument.getCoords()==0:
244         Q=TwoThetaQz
245     else:
246         raise ValueError('The value for coordinates, coords, is WRONG!'
247             'should be q(0) or tth(1).')
248
249     type=instrument.getProbe()
250     pol=instrument.getPol()
251
252     lamda=instrument.getWavelength()
253     parameters=sample.resolveLayerParameters()
254     if type==instrument_string_choices['probe'][0] or type==0:
255         fb=array(parameters['f'], dtype=complex64)
256     else:
257         fb=array(parameters['b'], dtype=complex64)*1e-5
258
259     dens=array(parameters['dens'], dtype=complex64)
260     d=array(parameters['d'], dtype=float64)
261     magn=array(parameters['magn'], dtype=float64)
262     #Transform to radians
263     magn_ang=array(parameters['magn_ang'], dtype=float64)*pi/180.0
264
265     sigma=array(parameters['sigma'], dtype=float64)
266     sld=dens*fb*instrument.getWavelength()*2/2/pi
267
268     #FootprintCorrections
269
270     foocor=1.0
271     footype=instrument.getFootype()
272     beamw=instrument.getBeamw()
273     samlen=instrument.getSamplelen()
274     theta=arcsin(Q*instrument.getWavelength()/4.0/pi)*180/pi
275     if footype==1 or footype==instrument_string_choices['footype'][1]:
276         foocor=GaussIntensity(theta, samlen/2.0, samlen/2.0, beamw)
277     elif footype==2 or footype==instrument_string_choices['footype'][2]:
278         foocor=SquareIntensity(theta, samlen, beamw)
279     elif footype==0 or footype==instrument_string_choices['footype'][0]:
280         pass
281     else:
282         raise ValueError('The choice of footprint correction, footype,'
283             'is WRONG')
284
285     #Resolution corrections
286     if restype==instrument_string_choices['restype'][1] or restype==1:

```

```

285     R=ConvoluteFast(TwoThetaQz, R[:] * foocor, instrument.getRes(), \
286                     range=instrument.getResinrange())
287     elif restype==instrument_string_choices['restype'][2] or restype==2:
288         R=ConvoluteResolutionVector(TwoThetaQz, R[:] * foocor, weight)
289     elif restype==instrument_string_choices['restype'][3] or restype==3:
290         R=ConvoluteFastVar(TwoThetaQz, R[:] * foocor, instrument.getRes(), \
291                             range=instrument.getResinrange())
292     elif restype==instrument_string_choices['restype'][4] or restype==4:
293         R=ConvoluteResolutionVector(TwoThetaQz, R[:] * foocor, weight)
294     elif restype==instrument_string_choices['restype'][0] or restype==0:
295         R=R[:] * foocor
296     else:
297         raise ValueError('The choice of resolution type, restype,'
298                           'is WRONG')
299
300     return R * instrument.getIO() + instrument.getIbkg()
301
302 def ResolutionVectorAsymmetric(Q, dQ, points, dLambda, asymmetry, range=3):
303     """
304     Resolution vector for a asymmetric wavelength distribution found in
305     neutron experiments with multilayer monochromator.
306     """
307     Qrange=max(range*dQ, range*dLambda*Q.max())
308     Qstep=2*Qrange/points
309     Qres=Q+(arange(points)-(points-1)/2)[: , newaxis]*Qstep
310     Quse=transpose(Q[: , newaxis])
311
312     gamma_asym=2.*dLambda*Quse/(1+exp(asymmetry*(Quse-Qres)))
313     z=(Quse-Qres+(abs(gamma_asym)*1j))/abs(dQ)/sqrt(2.)
314     z0=(0.+(abs(gamma_asym)*1j))/abs(dQ)/sqrt(2)
315     weight=wofz(z).real/wofz(z0).real
316     Qret=Qres.flatten()
317     return (Qret, weight)
318
319 def OffSpecularMingInterdiff(TwoThetaQz, ThetaQx, sample, instrument):
320     raise NotImplementedError('Not implemented use model interdiff insteads')
321     return TwoThetaQz, ThetaQx
322
323 def SLD_calculations(z, sample, inst):
324     """
325     Calculates the scatteringlength density as at the positions z
326     """
327     parameters=sample.resolveLayerParameters()
328     dens=array(parameters['dens'], dtype=complex64)
329     f=array(parameters['f'], dtype=complex64)
330     b=array(parameters['b'], dtype=complex64)
331     type=inst.getProbe()
332     magnetic=False
333     mag_sld=0
334     if type==instrument_string_choices['probe'][0] or type==0:
335         sld=dens*f
336     elif type==instrument_string_choices['probe'][1] or type==1 or \
337          type==instrument_string_choices['probe'][4] or type==4:
338         sld=dens*b
339     else:
340         magnetic=True
341         sld=dens*b
342         magn=array(parameters['magn'], dtype=float64)
343         #Transform to radians
344         magn_ang=array(parameters['magn_ang'], dtype=float64)*pi/180.0
345         mag_sld=2.645*magn*dens
346
347     d=array(parameters['d'], dtype=float64)
348     d=d[1:-1]
349     # Include one extra element - the zero pos (substrate/film interface)
350     int_pos=cumsum(r_[0, d])
351     sigma=array(parameters['sigma'], dtype=float64)[: -1] + 1e-7
352     if z==None:
353         z=arange(-sigma[0]*5, int_pos.max()+sigma[-1]*5, 0.5)

```

```

354     if not magnetic:
355         rho=sum((sld[:,-1]-sld[1:])* (0.5-\
356             0.5*erf((z[:, newaxis]-int_pos)/sqrt(2.)/sigma)), 1)+sld[-1]
357         dic={'real sld': real(rho), 'imag sld': imag(rho), 'z':z}
358     else:
359         sld_p=sld+mag_sld
360         sld_m=sld-mag_sld
361         rho_p=sum((sld_p[:,-1]-sld_p[1:])* (0.5-\
362             0.5*erf((z[:, newaxis]-int_pos)/sqrt(2.)/sigma)), 1)+sld_p[-1]
363         rho_m=sum((sld_m[:,-1]-sld_m[1:])* (0.5-\
364             0.5*erf((z[:, newaxis]-int_pos)/sqrt(2.)/sigma)), 1)+sld_m[-1]
365         dic={'real sld +': real(rho_p), 'imag sld +': imag(rho_p), \
366             'real sld -': real(rho_m), 'imag sld -': imag(rho_m), 'z':z}
367     return dic
368
369 SimulationFunctions={'Specular':Specular, \
370                     'OffSpecular':OffSpecularMingInterdiff, \
371                     'SLD': SLD_calculations\
372                     }
373
374 import lib.refl as Refl
375 (Instrument, Layer, Stack, Sample)=Refl.MakeClasses(InstrumentParameters, \
376 LayerParameters, StackParameters, SampleParameters, SimulationFunctions, \
377 ModelID)
378
379 # Add gradient for sigma and thickness to multilayers
380 def resolveLayerParameter(self, parameter):
381     if parameter=='sigma':
382         sigma_gradient=self.sigma_gradient
383         #parameters for layers with roughness gradient
384         par=[lay._getattribute__(parameter)+0.0 for lay in self.Layers]
385         for i in range(self.Repetitions-1):
386             par+=[lay._getattribute__(parameter)*((1.+sigma_gradient*i/self.
387                 Repetitions)) for lay in self.Layers]
388     elif parameter=='d':
389         d_gradient=self.d_gradient
390         #parameters for layers with roughness gradient
391         par=[]
392         for i in range(self.Repetitions):
393             par+=[lay._getattribute__(parameter)*((1.-d_gradient/2.+d_gradient*i/
394                 self.Repetitions)) for lay in self.Layers]
395     else:
396         par=[lay._getattribute__(parameter)+0.0 for lay in self.Layers]*self.
397             Repetitions
398     return par
399
400 Stack.resolveLayerParameter=resolveLayerParameter
401
402 # Add cap with step-like drop in sld on top of the sample
403 def sample_resolveLayerParameters(self):
404     par=self.Substrate._dict_.copy()
405     for k in par.keys():
406         par[k]=[self.Substrate._getattribute__(k)+0.0]
407     cap_steps=int(self.getCap_steps())
408     if cap_steps>0:
409         cap_sigma=self.getCap_sigma()
410         cap_center=self.getCap_gauss_center()
411         cap_step_height=(4.*cap_sigma)/cap_steps
412     for k in Layer()._dict_.keys():
413         for stack in self.Stacks:
414             par[k]=par[k]+stack.resolveLayerParameter(k)
415         if cap_steps>0:
416             if k=='d':
417                 par[k][-1]=par[k][-1]-cap_step_height*cap_steps/2.
418                 par[k]=par[k]+[cap_step_height]*cap_steps
419             elif k=='dens':
420                 dens=par[k][-1]
421                 x=linspace(-2.*cap_sigma, 2.*cap_sigma, cap_steps)
422                 sigma_asym=2.*cap_sigma/(1+exp(cap_center*x))

```

```
420     Pfac=exp(-0.5*x**2/sigma_asym**2)
421     Pfac/=Pfac.sum()
422     factors=[1.-Pfac[:i+1].sum() for i in range(cap_steps)]
423     par[k]=par[k]+[dens*fi for fi in factors]
424     elif k=='sigma':
425         par[k][-1]=cap_step_height
426         par[k]=par[k]+cap_steps*[par[k][-1]]
427     else:
428         par[k]=par[k]+cap_steps*[par[k][-1]]
429     par[k]=par[k]+[self.Ambient.__getattr__(k)+0.0]
430     return par
431
432 Sample.resolveLayerParameters=sample_resolveLayerParameters
```

## B.3 Spin model and neutron diffraction calculation for

$\text{Tl}_{18/3} \times 20$

```

1  from numpy import *
2  import matplotlib.pyplot as plt
3  from scipy.signal import fftconvolve
4
5  def get_XY(steps, interpolations):
6      # Get xy-grid for the simulation
7      r=arange(-steps/2.,steps/2.+1./interpolations,1./interpolations)
8      return meshgrid(r,r)
9
10 def get_Z(X,Y):
11     # create a periodic structure with limited coherence
12     LX=1./(1.+(X/correlation_a)**2)
13     LY=1./(1.+(Y/correlation_b)**2)
14     Zf=(a1*cos(2.*phi_a1*pi*X)+a2*cos(2.*phi_a2*pi*X))*cos(2.*phi_b*Y*pi)*LX*LY
15     return where((X%0.5==0.)*(Y%0.5==0.), Zf, 0.)
16
17 def get_Z_reset(X,Y):
18     # create a periodic structure with limited cohrennce with
19     # a specific phase at the beginning of each layer
20     LX=1./(1.+(X/correlation_a)**2)
21     LY=1./(1.+(Y/correlation_b)**2)
22     Zf=(a1*cos(2.*phi_a1*pi*X)+a2*cos(2.*phi_a2*pi*X))*cos(2.*phi_b*((Y%
23         bilayer_period)*pi))*LX*LY
24     return where((X%0.5==0.)*(Y%0.5==0.), Zf, 0.)
25
26 def get_I(Z):
27     # calculate scattered intensity from a given spin structure
28     S=fft.fft2(Z)
29     I=abs(S**2)
30     return I
31
32 def get_resolution(X,Y,sigmax, sigmay):
33     # calculate gaussian resolution function at 0,0
34     G=exp(-0.5*X**2/sigmax**2)*exp(-0.5*Y**2/sigmay**2)
35     G/=G.sum()
36     return G
37
38 def make_layers(Y,Z):
39     # crop spins from \la layers
40     return where((Y%bilayer_period)<=layer_thickness,Z, 0.)
41
42 def fill_layers(X,Y,Z):
43     # set spins at \la layers to 1.
44     return where((Y%bilayer_period)<=layer_thickness,Z, where((X%0.5==0.)*(Y
45         %0.5==0.), 0.33/(1.+(X/correlation_a)**2),0.))
46
47 def export_for_gnuplot(X,Y,Z, file_name):
48     # export a dataset as x.y.z columns to a text file
49     # scans are separated by empty lines for gnuplot
50     fhander=open(file_name, 'w')
51     for xi,yi,zi in zip(X,Y,Z):
52         zone=array([xi,yi,zi]).transpose()
53         zonestr="\n".join(
54             map(lambda line: " ".join(
55                 map(str, line)
56             ), zone))
57         fhander.write(zonestr+'\n\n')
58     fhander.close()
59
60 def export_directios_for_gnuplot(X,Y,M1,M2,C, file_name):
61     # export the spin directions to a 5 column textfile
62     # the 5th column denotes the layer where the spin is situated

```

```

62     fhandler=open(file_name, 'w')
63     for xi,yi,m1i,m2i,ci in zip(X,Y,M1,M2,C):
64         ids=where((xi%0.5==0.)*(yi%0.5==0.))
65         zone=array([xi[ids],yi[ids],m1i[ids],m2i[ids],ci[ids]]).transpose()
66         zonestr="\n".join(
67             map(lambda line: " ".join(
68                 map(str, line)
69             ), zone))
70         fhandler.write(zonestr+'\n\n')
71     fhandler.close()
72
73     ##### define constants and simulate the structure #####
74
75     bilayer_period=17.5+3.5      # \la+\tb thickness
76     layer_thickness=17.5        # \tb thickness
77     phi_a1=2.                   # Phase for periodicity in c-direction
78     phi_a2=1.                   # Phase for periodicity in c-direction
79     phi_b=5/layer_thickness     # Phase in b-direction
80     a1=0.5                      # Amplitude for first periodicity
81     a2=0.52                     # Amplitude for second periodicity
82
83     # Define the grid and resolution function
84     X,Y=get_XY(200, 4) # 200x200 unit cells with 4 steps/UC
85     Qx=X/50.+2.         # Corresponding reciprocal space vectors
86     Qy=Y/50.
87     G=get_resolution(Qx-2.,Qy,0.03, 0.02) # Gaussian resolution
88
89     # Calculate ions for the non spin-flip channel
90     correlation_a=1.       # Correlation length in c-direction
91     correlation_b=1e4      # Correlation length in b-direction
92     Z=get_Z_reset(X,Y)    # Coupled magnetic structure to layers
93     Z=fill_layers(X,Y,Z)  # Ferromagnetic spins in \la
94     Znsf=Z
95     I=get_I(Z)            # Calculate intensity
96
97     # Interactive plotting and export of the data
98     plt.figure(1)
99     plt.subplot(211)
100    plt.pcolormesh(Y,X,Z)
101    plt.subplot(212)
102    Insf=fftconvolve(I,G,mode='same')
103    export_for_gnuplot(Qy, Qx, Insf/Insf.max(), 'Insf.out')
104    plt.pcolormesh(Qy,Qx,Insf)
105
106    # Calculations for the spin-flip channel
107    #a1=0.
108    #a2=1.
109    #phi_b=0.
110    #correlation_a=1e10
111    #correlation_b=1e10
112    #Z=get_Z(X,Y)
113    #Znew=zeros_like(Z)
114
115    ## Averidge the intensities of sets with random integer numbers of SDWs in
116    ## each layer
117    for i in range(-1,int(200/bilayer_period)):
118        #periodicity=random.randint(1,7)
119        #Znew+=cos((Y%bilayer_period)*pi*periodicity/layer_thickness+pi/2.)*(Y<(
120            bilayer_period*(i+1)-bilayer_period*int(100/bilayer_period)))*(Y>=(i*
121            bilayer_period-bilayer_period*int(100/bilayer_period)))*Z
122    #Z=Znew
123    #Z=make_layers(Y,Z)
124    #I=get_I(Z)
125    for i in range(5):
126        #Z=get_Z(X,Y)
127        #Znew=zeros_like(Z)
128        for i in range(-1,int(400/bilayer_period)):
129            #periodicity=random.randint(1,7)

```



```

127     #Znew+=cos((Y%bilayer_period)*pi*periodicity/layer_thickness+pi/2.)*(Y<(
        bilayer_period*(i+1)-bilayer_period*int(100/bilayer_period)))*(Y>=(i*
        bilayer_period-bilayer_period*int(100/bilayer_period)))*Z
128     #Z=Znew
129     #Z=make_layers(Y,Z)
130     #I+=get_I(Z)
131     #I/=6.
132
133     ## Interactive plotting and export of the data
134     #plt.figure(2)
135     #plt.subplot(211)
136     #plt.pcolormesh(Y,X,Z)
137     #plt.subplot(212)
138     #Isf=fftconvolve(I,G,mode='same')
139     #export_for_gnuplot(Qy, Qx, Isf/Isf.max(), 'Isf.out')
140     #export_directios_for_gnuplot(Y,X,Znsf,Z,fill_layers(X,Y,zeros_like(Z)), '
        spins.out')
141     #plt.pcolormesh(Qy,Qx,Isf)
142
143     plt.show()

```

# Appendix C

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# Appendix G

## List of Symbols and Abbreviations

### G.1 Symbols

|   | Mathematic Symbols  |
|---|---|
| $\vec{v}$   | Vector  |
| $\hat{v}$   | Unit vector parallel to $\vec{v}$   |
| $\underline{M}$   | Matrix  |
| $\underline{M}^T$   | Transposed matrix   |
| $\begin{pmatrix} \vec{i} & \vec{j} \end{pmatrix}$         | A matrix, where the columns are the vectors $\vec{i}$ and $\vec{j}$   |
| $a \otimes b$   | Convolution of $a$ and $b$  |
| $\mathfrak{F}(f)$   | Fourier transform of function $f$   |
| $\mathfrak{F}^{-1}(F)$                                    | Fourier back transform  |
| $\mathcal{P} \int$  | Cauchy principal value of an integral (removing singularities by e.g. replacing with a limes)   |
| $\Re(x)$  | Real part of complex number $x$   |
| $\Im(x)$  | Imaginary part of complex number $x$  |
| $(n+1)_{mod 3}$   | The modulo operation on the number $(n+1)$ to the quotient 3  |
| $\xrightarrow{[53]}$                                      | The derivation is explained in the according publication  |
| $\langle A \rangle$                                       | Average value/expectation value of quantity $A$   |
|   | Physical Nomenclature   |
| $\langle t_{2g}^2 \rangle t_{2g\uparrow}^2 e_{g\uparrow}$ | An electronic state with two paired electrons in a $t_{2g}$ , two additional unpaired spin-up electrons in a $t_{2g}$ and one unpaired spin-up electron in a $e_g$ orbital. |
| $MnL_{III}$   | Manganese resonance at the $L_{III}$ absorption edge  |
| UC  | One unit cell   |
| TEY   | Total electron yield  |
| TFY   | Total fluorescence yield  |
| $\mu_B$   | Bohr magnetron ( $9.27 \cdot 10^{-24} \text{ A} \cdot \text{m}^2$ )   |
| $r_e$   | Classical electron radius ( $2.81 \cdot 10^{-15} \text{ m}$ )   |
| $\vec{\sigma}$  | Vector of the three Pauli matrices $\sigma_x$ , $\sigma_y$ and $\sigma_z$   |
| $\vec{P}_n$   | Neutron polarization  |
| $T_{N_{SDW}}$   | Transition temperature to spin density wave magnetic order  |
| $T_{N_C}$   | Transition temperature to cycloidal magnetic order  |
| $T_{N_{Tb}}$  | Transition temperature of Tb sublattice   |
| $T_C$   | Transition temperature to ferromagnetic order   |

**Physical Nomenclature** (continued)

|                                   |   |
|-----------------------------------|---|
| $a_{\text{TbMnO}_3}^*$            | Length of the reciprocal lattice vector $a^*$ of $\text{TbMnO}_3$   |
| $\langle f ,  i\rangle$           | Quantum mechanical initial (i) and final (f) states   |
| $\lambda$                         | Wavelength  |
| $\vec{k}_{i/f}$                   | Incident and outgoing wave vector with $k = \frac{2\pi}{\lambda}$   |
| $\vec{Q} = \vec{k}_f - \vec{k}_i$ | Scattering vector   |
| $\hat{e}_{i/f}$                   | Photon polarization vector of incident and outgoing beams   |
| $\vec{r}$                         | Real space vector   |
| $I_\sigma$                        | Intensity measured with $\sigma$ -polarized incident beam, measurements with other polarization (x-ray/neutron) are denoted accordingly |
| $f(\vec{Q})$                      | Atomic form factor  |
| $V(\vec{r})$                      | Scattering potential  |
| $S_z/L_z/T_z$                     | Spin/orbit momentum / magnetic dipole operator  |
| $\mathcal{H}$                     | Hamilton operator   |
| $n$                               | Refractive index  |
| $m_{\text{red}}$                  | Reduced mass of a two body system   |
| $\rho$                            | Density   |
| $\sigma$                          | Depending on context: Scattering cross-section – Photon polarization perpendicular to scattering plane – Root mean square roughness     |
| $b$                               | Neutron nuclear scattering length   |
| $\chi$                            | Susceptibility  |
| $\Phi$                            | Wave function   |
| $\vec{m}_i/\vec{M}$               | Single magnetic moment/magnetization distribution   |

**Sample Parameters in Models**

|            |  |
|------------|--|
| $\delta$   | Scattering power density (scattering length density for neutrons) of a layer |
| $d_i$      | Thickness of layer i   |
| $\delta d$ | Variation of the thickness over the whole sample surface                     |
| $D$        | Bilayer thickness in a multilayer  |
| $N_X$      | Number of unit cells in layer X  |
| $M$        | Multilayer repetitions   |
| $\sigma$   | Root mean square roughness standard deviation                                |
| $f_i$      | Atomic form factor of atom i   |
| $P(x_i)$   | Probability of occurrence for parameter $x_i$                                |

**Sample Emblems**

|                                |   |
|--------------------------------|---|
| $\text{T}_x^{\text{PLD}}$      | x nm $\text{TbMnO}_3$ thin film created with pulsed laser deposition                                  |
| $\text{T}_x^{\text{SD}}$       | x nm $\text{TbMnO}_3$ thin film created with sputter deposition                                       |
| $\text{D}_x$                   | x nm $\text{DyMnO}_3$ thin film created with pulsed laser deposition                                  |
| $\text{L}_x$                   | x nm $\text{LaCoO}_3$ thin film created with pulsed laser deposition                                  |
| $\text{TL}_{x \times x}^{y/z}$ | x repetitions of y UC $\text{TbMnO}_3$ and z UC $\text{LaCoO}_3$ created with pulsed laser deposition |
| $\text{EB}_{x \times x}^{y/z}$ | x repetitions of y UC $\text{EuTiO}_3$ and z UC $\text{BaTiO}_3$ created with pulsed laser deposition |



## G.2 Abbreviations

| <b>Instruments</b> |   |
|--------------------|---|
| DNS                | Diffuse neutron scattering experiment for neutron polarization analysis in Garching |
| D17                | Polarized neutron reflectometer at ILL, Grenoble                                    |
| D7                 | Neutron polarization analysis instrument at ILL, Grenoble                           |
| D8                 | Bruker laboratory x-ray reflectometer   |
| P09                | Resonant scattering and diffraction beamline at PETRA-III, Hamburg                  |
| TREFF              | Temporary reflectometer in Garching for polarized neutron reflectometry             |
| UE46-PGM-1         | Soft x-ray resonant magnetic scattering beamline at BESSY-II, Berlin                |
| 4-ID               | Soft x-ray XMCD experiment at APS, Argonne  |
| 4-circle           | Huber laboratory 4-circle diffractometer  |
| <b>Methods</b>     |   |
| AFM                | Atomic force microscope   |
| PNR                | Polarized neutron reflectometry   |
| PND                | Polarized neutron diffraction   |
| PLD                | Pulsed laser deposition   |
| RBS                | Rutherford backscattering spectrometry  |
| SD                 | Sputter deposition  |
| SHG                | Second harmonic generation  |
| SQUID              | Superconducting quantum interferometric device magnetometer                         |
| XMCD               | X-ray magnetic circular dichroism   |
| XRD                | X-ray diffraction   |
| XRMS               | X-ray resonant magnetic scattering, also called x-ray resonant exchange scattering  |
| XRR                | X-ray reflectometry   |

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