

Abstract

Convective gravity wave (GW) sources are spatially localized and emit at the same time waves with a wide spectrum of phase speeds. Any wave analysis therefore comprises between spectral and spatial resolution. Future satellite borne limb imagers will for a first time provide real 3d volumes of observations. These volumes will be however limited which will impose further constraints on the analysis technique. In this study a three dimensional few-wave approach fitting sinusoidal waves to limited 3-D volumes is introduced. The method is applied to simulated GWs above typhoon Ewiniar and GW momentum flux is estimated from temperature fluctuations. Phase speed spectra as well as average profiles of positive, negative and net momentum fluxes are compared to momentum flux estimated by Fourier transform as well as spatial averaging of wind fluctuations. The results agree within 10–20 %. The few-wave method can also reveal the spatial orientation of the GWs with respect to the source. The relevance of the results for different types of measurements as well as its applicability to model data is discussed.

1 Introduction

Gravity waves (GWs) are atmospheric waves conveying momentum and energy from the lower into the mid and upper atmosphere. They are the main driver of the mesospheric circulation and the main reason for the cold summer mesopause (e.g. McLandress, 1998) and contribute 50 % or more to the driving of the QBO (Dunkerton, 1997; Ern and Preusse, 2009; Alexander and Ortland, 2010). Climate modeling indicates that they provide a significant portion of the predicted acceleration of the Brewer-Dobson circulation in response to CO₂ increase (McLanress and Shepherd, 2009; Butchart et al., 2010). These and many other effects make GWs to be one of the most important coupling processes in the atmosphere.

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The acceleration or deceleration of the background wind (frequently called GW drag) is given by the vertical gradient of the pseudomomentum flux (Fritts and Alexander, 2003). This gradient is caused, in general, by GW dissipation and is particularly strong below a critical level where the phase speed of the wave matches the background wind speed. In order to understand the interaction of GWs with the background wind one therefore has to determine both the spatial distribution of GW sources and the phase speed distribution of pseudomomentum flux associated with these sources (Preusse et al., 2006; Alexander et al., 2010).

The vertical flux of horizontal pseudomomentum associated with a GW is given by (Fritts and Alexander, 2003)

$$(F_{\rho x}, F_{\rho y}) = \left(1 - \frac{f^2}{\hat{\omega}^2}\right) \bar{\rho} \left(\overline{u' w'}, \overline{v' w'}\right) \quad (1)$$

where f is the Coriolis parameter, $\hat{\omega}$ is the intrinsic frequency, $\bar{\rho}$ is the background density and u' , v' and w' are the wind fluctuations in zonal, meridional and vertical direction associated with the wave. The overline over the fluctuation quantities denotes a suited average, e.g. over one or several wave periods or one or several full wave-lengths. However, measurements may not have access to these quantities and therefore equivalent expressions are deduced based on the dispersion relation and polarization relations. For instance, satellite-borne infrared emission sounders can measure snap-shots of temperatures. As shown by Ern et al. (2004) the pseudomomentum flux then can be calculated from the temperature amplitudes \hat{T} and the three-dimensional wave vector (k, l, m) by

$$(F_{\rho x}, F_{\rho y}) = \frac{1}{2} \bar{\rho} \frac{(k, l)}{m} \left(\frac{g}{N}\right)^2 \left(\frac{\hat{T}}{\bar{T}}\right)^2. \quad (2)$$

N is the buoyancy frequency, g the gravity acceleration, $\bar{\rho}$ the background atmosphere density and \bar{T} the background atmosphere temperature. Spectral properties of the

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wave are therefore not only important for the interpretation, but also essential to determine the pseudomomentum flux, in particular from temperature measurements.

To determine the spectral wave parameters is a challenging task. Gravity waves are highly intermittent and maxima in momentum flux are located close to the sources.

5 Over small distances momentum flux may vary 1–2 orders of magnitude. On the other hand the wave spectrum consists of a superposition of a number of wave components. Any method for analyzing GWs therefore is necessarily a compromise between spectral and spatial resolution. In addition, different data sets and, in particular, measured data provide additional limitations.

10 Fourier transform is a mathematically well-founded method for the analysis of regularly gridded model data. The underlying assumptions are periodicity as well as spatial homogeneity and temporal stationarity of the data. Homogeneity means that all spatial variations are explained in terms of the superposition of waves, i.e. all wave components are present in all regions of the analyzed volume with the same amplitude. In this view, regions of higher or lower variance express a constructive or destructive interference of the waves. Stationarity is the temporal analogon. This is an approximation which is not fully consistent with our understanding of localized GW sources.

15 By the Parseval theorem the Fourier components are linked to the variance. Therefore the net momentum flux (i.e. the sum of all negative and positive components) calculated from the whole spectrum is mathematically equivalent to the net momentum flux calculated directly from the wind variance. However wind fluctuations due to gravity waves are difficult to measure. In particular, direct estimation from horizontal and vertical wind variances cannot be applied to many atmospheric measurements (e.g. satellite data and radiosondes) and do not provide insight in the spectral properties.

25 New detector technology will allow in future to obtain three dimensional temperature distributions from satellite observations in a volume along the orbital track. For instance, the infrared limb imager of the PRocess Exploration through Measurements of Infrared and millimetre wave Emitted Radiation (PREMIER) satellite proposed for

effect. These waves, however, would not be observable by infrared limb emission sounders and hence the present simulation provides a suited test case for these kind of observations. Comparisons to nadir viewing satellites have revealed good agreement (Kim et al., 2009).

The paper is organized as follows. Section 2 gives a brief introduction about the data and the selected analysis methods. The results for average positive, negative and net momentum flux in terms of vertical profiles are discussed in Sect. 3, spectra deduced from Fourier transform as well as statistical combination of many events analyzed with a few-wave approach are compared in Sect. 4, and spatio-temporal variations are considered in Sect. 5. In the conclusions the findings are summarized and the relevance for PREMIER and other measurements are discussed. Further, possible implications also for model data are pointed out.

In addition to the new class of satellite instruments the results discussed in this investigation are also relevant for other novel measurements characterizing 3-D atmospheric structures (e.g. new radar systems) as well as for existing climatologies of absolute values of GW momentum flux from infrared limb sounders. Additionally, the method may be used as a complementary approach to model data analysis, as will be discussed in the conclusions section.

2 Description of the typhoon modeling

This study is based on simulated gravity waves generated by typhoon Ewiniar 2006. The simulation was realised by Kim et al. (2009) using the Advanced Research WRF (Weather Research and Forecasting) modeling system (Skamarock et al., 2005). Three dimensional simulations are performed with a horizontal grid spacing of 27 km in a horizontal domain with 187×187 grid points. The vertical domain extends from the surface to 0.1 hPa (~ 65 km) with a damping layer of the uppermost 20 km. Hence the physical domain of the simulation is from the surface to $z = \sim 45$ km with a grid spacing of ~ 500 m in the stratosphere. The time step used in the simulation is 20 s. Modeling is

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performed for the period from 7 July 2006, 00:00 UTC to 10 July 2006, 18:00 UTC. This period is split into three periods of 30 h each in order to adjust the typhoon position in the mesoscale model to the real typhoon position derived from global analysis data. The model output consists of wind and temperature fields.

2.1 Spectral analysis by Fourier transform

We here make the approach of a scale separation between the global-scale fields \bar{u} , \bar{v} , \bar{w} and \bar{T} and the fluctuations caused by GWs u' , v' , w' and T' and remove the background by subtracting a running mean over 21×21 points (567×567 km) in the model domain.

The spectral analysis uses wind and temperature fields which are saved every 10 minutes. These fields are spectrally analyzed for each altitude independently by means of a 3-D Fourier transform (two dimensions for the horizontal coordinates and one dimension for time). This results in spectra dependent on horizontal wavenumbers k and l and ground-based frequency ω . From $\mathbf{k}_h = (k, l)$ and ω the ground based phase speed can be calculated

$$c_h = \frac{\omega \mathbf{k}_h}{|\mathbf{k}_h|^2}. \quad (3)$$

Momentum flux is calculated from the co-spectra of horizontal and vertical winds, i.e. only the in-phase contribution is used. If $U(k, l, \omega)$ and $W(k, l, \omega)$ are the complex Fourier components then the co-spectrum is defined as

$$\text{Co}(UW) = \text{Re}(UW^*) \quad (4)$$

where Re is the real-part and $*$ denotes the complex conjugate. For a detailed discussion of the cospectrum method see Alexander et al. (e.g. 2004).

Spectra of momentum flux in ω , k and l are binned according to direction and phase speed $|c_h|$. This is the physically most interesting way of display as the phase speed and direction governs the interaction with the background wind.

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2.2 Analysis by few-wave decomposition (S3D)

The few-wave analysis operates on single time snap-shots of the model simulations. The whole analyzed domain is divided into sub-volumes of 10 km vertical extent and 350 km × 350 km horizontal domain. The sub-volume size is arbitrary but in this study orientated on the PREMIER measurement geometry.

For each volume subsequent least-square fits are performed. For each wave component i the algorithm minimizes the squared deviations

$$\chi^2 = \sum_j \frac{(y_j - f(x_j, y_j, z_j))^2}{\sigma_j^2} \quad (5)$$

of the function

$$f(x_j, y_j, z_j) = \sum_j A_j \sin(k_j x_j + l_j y_j + m_j z_j) + B_j \cos(k_j x_j + l_j y_j + m_j z_j) \quad (6)$$

where (k_j, l_j, m_j) is the wave vector for the j -th wave component and A_j and B_j are the according amplitudes. y_j are the individual measurements and are in our case the wind or temperature fluctuations, that is u' , v' , w' or T' . As for a given wave vector the least-square problem in A_j and B_j can be solved analytically, a variational method to minimize χ^2 is required only for the wave vector. As a first approach we have used nested intervals and an initial wave vector provided from 3-D Fourier transform (maximum amplitude of the FT) is used. After determining the optimal solution for wave component j this is subtracted from the temperature fluctuations and the least-square fit for component $j + 1$ is performed. Please note that in this way for each wave component the solution is selected which describes most of the remaining variance.

Please note also, that waves with wavelength longer than the extent of the fitting cube have wavenumbers between zero (constant component) and the smallest wavenumber in the respective direction. Using a least square approach has the advantage that the determination of horizontal wavenumbers is not limited to the fixed set of wavenumbers

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resulting from a standard Fourier analysis. In particular, low wavenumbers corresponding to wavelengths longer than the 3-D cube used for the analysis can be recovered.

The few-wave approach has been tested systematically by superpositions of two sinusoids. It was possible to identify both amplitudes with an accuracy better than 95 % (deviations less than 5 %) even in cases where one of the waves had wavelengths larger than the cube size in all three spatial dimensions.

For comparison with the Fourier transform the domain will be covered by non-overlapping cubes. Momentum flux is calculated according to Eq. (2), intrinsic phase speed according to the GW polarization relation, and ground based phase-speed by Doppler-shifting using the background wind. Spectra are generated by binning the data into intervals of phase-speed and direction and the total gravity wave momentum flux is calculated in each bin. In this way the number of wave events in a certain bin is as important as the momentum flux of these events. The same phase-speed bins as for the Fourier-transform are used, but only 16 directions.

3 Vertical profiles of average momentum flux

In this section vertical profiles of the average momentum flux for the three periods of the WRF model simulations (see Sect. 2) were investigated. The wind tendencies, i.e. the (positive or negative) acceleration of the background wind, is given by the vertical derivative of the momentum flux. In order to determine the wind tendencies the net momentum flux, i.e. the sum of negative and positive wave components, is necessary. In order to confine e.g. a GW parameterization scheme or GW ray-tracer that can be used to simulate GW drag in the mesosphere at altitudes where high spatial resolution observations are not available, it is even more important to quantify the positive and negative contributions separately. Therefore in this chapter all three quantities, positive, negative and net momentum flux, each for the zonal and meridional direction are considered.

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For the Fourier transform the positive momentum flux is the superposition of all spectral components with positive momentum flux, which homogeneously fill the analysis space; for the sinusoidal fits (S3D method) the positive momentum flux is the sum of all discrete, spatially and spectrally localized wave events with positive intrinsic phase speeds.

As mentioned in the introduction, it is not trivial that the S3D method also captures the weaker flux components. These are often due to gravity waves propagating into the direction parallel to the background wind (Warner et al., 2005). Furthermore, the Fourier transform is calculated based on time series of individual altitude levels. The S3D method does not have this temporal information, but uses 10 km vertical intervals to determine the vertical wavelength and hence the temperature-based momentum flux values. This is expected to result in a smoothing of the vertical profiles. It also means that only those results are reliable which are solely based on values above the tropopause. The tropopause marks a sharp gradient in the vertical profile of the buoyancy frequency. At this sharp gradient partial reflection occurs (Kim et al., 2012) and trapped waves in a wave guide are generated. For these the usual equations for vertically propagating waves must not be applied. In addition, below the tropopause some of the wind and temperature perturbations are caused by the strong convection itself.

This is illustrated by Fig. 1 showing vertical profiles of momentum flux from the second period of the model simulations. Below the tropopause (~ 17 km) momentum flux values are huge and more than one order of magnitude larger than above the tropopause. The blue profiles result from the spectral analysis of wind fluctuations. Positive and negative values peak at different altitudes resulting in an S-curve shaped profile. The same is valid in the net momentum flux (red curve) calculated from the spectral analysis of the model temperatures which is in discrepancy to the wind results in direction, magnitude and peak altitude. Only above 18 km the curves are in reasonable agreement. This suggests that only S3D results above 23 km are reliable for this case study and a 10 km vertical analysis window. Above 40–45 km the sponge layer

starts which reduces reliable altitudes for the S3D method to 25–40 km. In order to visualize also the influence from the tropopause included in the vertical analysis window we will plot profile comparisons in the range 20–40 km.

Figure 2 compares profiles for all three periods and both zonal and meridional momentum flux. Long-dashed curves give the negative components, dashed curves the positive components and solid curves the net momentum flux. The S3D analyses of temperatures and winds are represented by the red and dark-blue lines, the Fourier transform by magenta and blue lines. All these curves assume that waves are propagating upward. However, partial reflections at buoyancy gradients and above 45 km cause reflected waves with about 5 % of the momentum flux of the upward propagating waves. Using the FT results of winds and temperatures these contributions can be identified and the correct eastward and westward (respectively northward and southward) momentum fluxes can be determined (Kim et al., 2012). Such corrected results from temperature data are shown as green curves.

Due to wind filtering by prevailing stratospheric easterlies, the zonal momentum flux is dominated by positive momentum from eastward propagating waves. The negative momentum flux is very small. This relation is well represented by all analysis methods. Positive and net momentum flux agree within 20 % or better among the different methods for altitudes of 25 km and above. It is curious to note that at these altitudes the largest deviations are found for the Fourier-Transform analyses of temperatures. As expected the error increases for the S3D results at 20 km.

For the meridional momentum flux positive and negative momentum flux are of comparable size and can be quantified with an accuracy of better than 25–30 % for all altitudes above 25 km. In particular in period 2 positive and negative momentum flux are almost equal. Still, the sign and profile shape of the net momentum flux can be retrieved. For periods 1 and 3 net momentum flux from S3D temperatures and FT winds are in very good agreement.

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4 Momentum flux spectra

The propagation direction and ground-based phase speed of GWs determines the vertical wavelength, saturation amplitude and critical level of a GW. (There are some slight dependencies on the frequency or horizontal wavelength which vanish in mid frequency approximation, which is valid for the waves considered in this case study.) Therefore GW spectra are frequently given in terms of ground based phase speed and propagation direction.

Figures 3 and 4 show momentum flux spectra for the three periods and altitude levels of 25 km and 40 km height obtained by Fourier Transform from winds (Fig. 3) and temperatures (Fig. 4). Spectra are calculated in terms of horizontal wavenumbers k , l and ground based frequency ω . From these the ground based phase speed $(c_{h,x}, c_{h,y}) = (\omega/k, \omega/l)$ and propagation direction ϕ ; $l/k = \tan(\phi)$ are calculated and the momentum flux values are binned accordingly.

The spectra are influenced by variations in the source as well as the filtering by the background winds. This is described in detail by Kim and Chun (2010) and here only salient patterns in the spectra are discussed. The effects of the background winds are similar in all three periods. Due to the background easterlies in the subtropical jet, part of the waves reaches a critical level around the tropopause. Downstream (westward) propagating waves with low phase speeds are removed from the spectrum. Some waves with south-west or north-west propagation direction and some with phase speeds larger than 40 ms^{-1} remain, but are weaker than the upstream (eastward) propagating waves. The effect intensifies at 40 km altitude where only waves in the right-hand side of the plots (i.e. preferentially upstream propagating GWs) remain.

One further interesting pattern is a little “pig tail” of westward propagating GWs with close to zero phase speeds. If the waves propagating upward from the source meet the background winds from about -10 to -40 m s^{-1} , i.e. do not meet zero wind, critical-level filtering occurs for wave components between the two critical lines resulting in the pig-tail shape spectrum. The variation among the periods is mainly due to differences

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in the wave excitation. In the first period the typhoon propagates north-westward, in the second period northward and in the third period north-eastward. In the second period the typhoon emits GWs with a slight northward preference, in the third period there is a strong north-east preference in the wave excitation.

The corresponding spectra from the S3D analysis are shown in Figs. 5 and 6. The momentum flux is the absolute value $F_p = \sqrt{F_{p,x}^2 + F_{p,y}^2}$. The phase speed and direction are calculated from the wave vector and background winds (cf. Sect. 2.2).¹ The S3D method was applied to the data at the full hour only (FT was applied to 10 min sampling). Therefore there are too few points to obtain as fine a spectral grid as used for the FT results. This also results in different absolute values per spectral bin and we therefore will focus on the relative structures. It should be further noted that Figs. 5 and 6 are plotted using a logarithmic color scale and resolve smaller momentum flux values than the color scales used in Figs. 3 and 4.

In comparing the spectra, all salient structures described above are well reproduced by the S3D method. Both the wind filtering between the two levels as well as the change of wave excitation between the different periods can be observed. The predominant phase speeds are well captured. Also the little “pig tail” is reproduced.

5 Spatio-temporal variations

Strong convection is a localized source. GWs are expected to be radiated away from this source, i.e. eastward propagating waves are observed predominately east of the convection and westward propagating waves are observed predominately west of the

¹For the wind spectra the zonal momentum flux (respectively the meridional momentum flux) is directly calculated from the zonal and vertical wind amplitudes \hat{u} and \hat{w} and the phase difference ψ : $F_{p,x} = \hat{u}\hat{w}\cos\psi$. In this way we obtain for each wave solution also a direction of the momentum flux ϕ_F ; $F_{p,y}/F_{p,x} = \tan(\phi_F)$. However, as we need also the phase speed, we bin according to the propagation direction determined from the wave vector ϕ ; $l/k = \tan(\phi)$.

convection (e.g. Piani et al., 2000; Alexander et al., 2004). However, a typhoon is a very complex system encompassing strong convection in the eye-wall as well as in the spiral bands. Therefore the relative location of the observed GWs with respect to the storm center can give further insight in the details of the generation mechanism.

Also of interest is the temporal development. From the spectra it can be seen that the typhoon changes its GW radiation characteristic between the three periods with a distinct preference of generating north-eastward propagating waves (in the same direction as the propagation direction of the typhoon) during period 3. Is it also possible to achieve a finer temporal resolution?

Figures 7 and 8 show a series of maps at 25 and 40 km altitude, each representing a six hour interval. The upper row shows the first period, the middle row the second period and the lower row the third period. Each panel gives a model domain of 2500 km \times 2500 km in model x and y direction, minor axis ticks indicating 100 km distance, major ticks indicating 500 km distance. The thin arrows give the single values for both fitted components of the S3D method every hour. The direction of the arrows indicates the direction of the momentum flux, the color gives the absolute value. The thick arrows show the sum of the two components and the average over the six hours, that is the average total momentum flux for every spatial analysis volume of 360 km \times 360 km \times 10 km. The red asterisks mark the position of the typhoon center. The small panel below the color bar indicates the center positions of the analysis volumes (crosses) and the typhoon track with respect to the total model domain for the three periods. In this panel color indicates time.

In particular for the 25 km maps the first column displays obviously smaller values than all other panels. This could indicate that at the beginning of each period GWs are not fully developed, which is likely an effect of the model simulation and not a real feature of the typhoon. Therefore only results from the second to fifth column will be discussed physically. To confirm the interpretation Fig. 11 shows the accumulated precipitation of the last hour before the mid of each period. The white frame indicates the analysis region and the white asterisk the typhoon center.

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Physical interpretation of results

Comparing the thin arrows which show the individual fits, i.e. single wave events, with the thick arrows which give the sum of both spectral components and the averages over 6 h, i.e. the average total momentum flux in Figs. 7 and 8, regional differences are found. In regions with low momentum flux the direction is often almost arbitrary resulting in arrows pointing in all directions. For the regions of large momentum flux also the single events are more coherent though some variations exist.

Even better spatial resolution can be reached, if the size of the analysis volumes is reduced to 189 km × 189 km × 10 km. These results are shown in Figs. 9 and 10. The magnitude of the momentum flux values as well as the salient features are the same as in Figs. 7 and 8, but finer detail is resolved and the patterns can be interpreted more easily.

First the distributions at 25 km altitude (Figs. 7 and 9) are considered. In the beginning of period 1 (first row, second column) the largest momentum fluxes are arc oriented around the typhoon center and with the highest values close to the center. It should, however, be noted that the direction of the arrows is not away from the storm center but stronger W-E oriented and extends rather far to the south. This is consistent with a large region of precipitation observed in Fig. 11, left panel, which acts also as a wave source and is located in the south of the typhoon center.

Period 2 is similar to period 1, but at the end some northward propagating waves north of the typhoon start to develop. The direction points clearly to a source close to the typhoon center (i.e. the arrow bases are all oriented towards the typhoon center). In this period also the precipitation (Fig. 11, center panel) is related with the typhoon center. A band of precipitation in the north seems to be connected to a large area of moderate momentum flux (about 0.5 mPa).

In period 3 these north and north-eastward propagating waves become the dominant features. The waves are clearly connected to the typhoon center. Towards the end of period 3 the intensity of the storm decreases (two rightmost panels, lower row). In

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accordance, the momentum flux considerably weakens. Again this can also be seen in Fig. 11, where the accumulated precipitation decreases.

At 40 km altitude (Figs. 8 and 10) the waves have, in general, propagated away from the storm center and upstream. This effect is best noticeable in the third period. In the very last panel the maximum of gravity wave momentum flux seems to extend outside the analysis region, which was chosen to match the region of the FT. Relative maxima in momentum flux occur somewhat later which is compatible to a non-zero group velocity of the GWs.

In summary, the S3D method reveals strong spatial variations which are related to the position of the waves with respect to the storm center. The spatial variations are plausible in terms of waves radiating away from a common source. Such spatial inhomogeneities are at odds with the theoretical basis of a FT postulating a homogeneous wave field.²

Compared to a mere variance analysis the S3D method could also provide such parameters as phase speed and group velocity as well as a full wave characterization allowing ray-tracing experiments.

6 Summary and discussion

Our case study demonstrates that inside a range of 10–20 % or better the two different approaches, that is (1) a FT spectral decomposition of an assumed-to-be homogeneous region and (2) spatially varying few-wave superpositions are consistent. This is very comforting, since a single true approach that can serve as a kind of “silver bullet” does not exist, and compromises have always to be made. Both approaches have their strengths (+) and weaknesses (–).

²Note that by definition the spatial and temporal variation is fully described and that the mathematical assumption rather influences the interpretation of the spectra.

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Fourier transform

- o is a multi-spectral approach assuming spatial homogeneity
- + has a long tradition and well founded theoretical background
- + describes the variance completely (Parseval theorem)
- 5 + provides well resolved spectra for
 - o the parts of the wave spectrum which are small compared to the analysis region or period
 - o fine and regular sampling
- is prone to leakage if the wavelength is of the same order of size as the analysis region
- 10 – maps spatial variation into spectral features

Few-wave decomposition

- + assumes spatial homogeneity over a small volume only
- + has a simple mathematical background
- 15 + can describe a superposition of a few waves and characterize them completely
- + provides solutions for any wavelengths, even those which are larger (at least in one or two dimensions) than the analysis volume
- + can provide spectra by superposition of the single volume solutions
- may map superpositions of many waves or waves of similar frequency into spatial variations (cf. beat frequency effects may occur)
- 20

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The essential advantage of the few-wave decomposition (S3D) for evaluation of measurements is that it can be performed with good results on relatively small volumes. Currently, there are a few instruments which can provide 3-D data sets: nadir viewing satellites, though with very limited vertical resolution, and novel radar systems. In future, limb imaging satellite instruments, if funded, also will provide 3-D data. In all these cases the measurement volume is limited. Though a single measurement may not fully characterize the spectrum, in a statistical sense all important quantities such as characteristic phase speeds, preferential propagation directions and the relative contribution of positive and negative zonal and meridional fluxes can be achieved.

The S3D method may also be an interesting tool for analyzing model data. Global high-resolution model data are commonly only saved at time-steps much too sparse for a space-time analysis. While momentum flux and its direction can be directly calculated from the wind fields by spatial averaging, the chosen spatial region influences the result, superpositions of waves are not decomposed and spectral information is missing. Few-wave decomposition may be an alternative, here.

In particular, the full 3-D wave vector together with background winds allows S3D results to be used as launch parameters for ray-tracing and thus opens a large potential for improved interpretation of measurements and model data alike.

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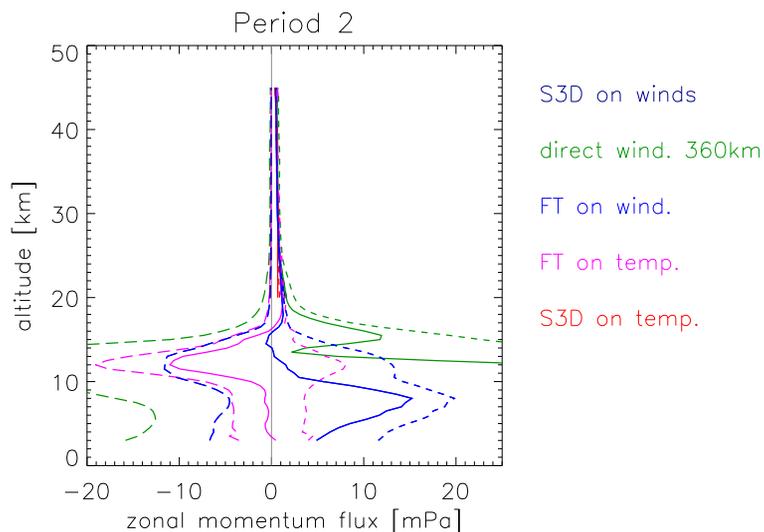


Fig. 1. Comparison of zonal momentum flux for period 2. Long-dashed lines indicate negative, dashed lines positive and solid lines net momentum fluxes. Below the tropopause momentum flux values are approx. a factor 20 larger than in the stratosphere and momentum flux values deduced from winds and temperatures are in discrepancy.

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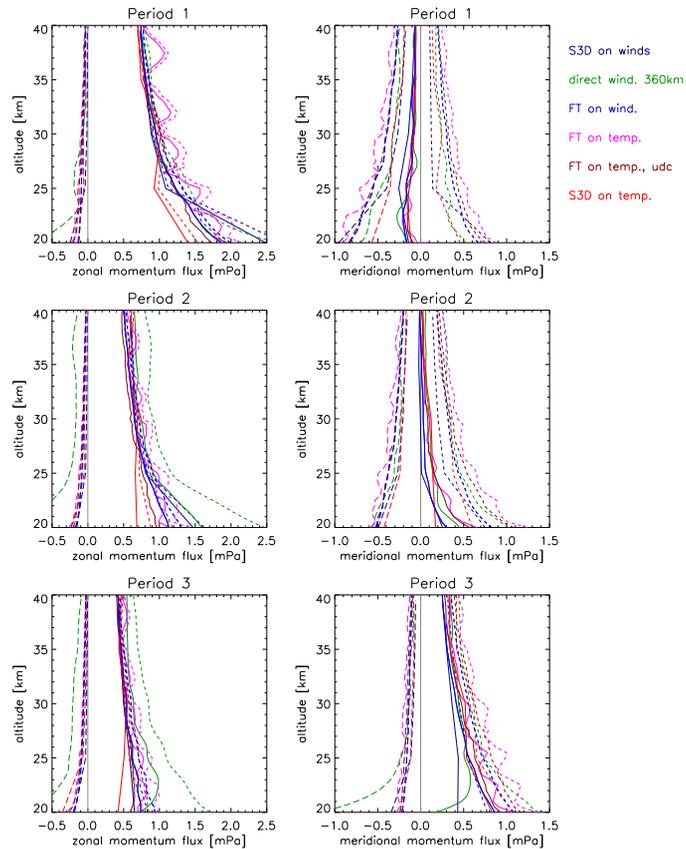


Fig. 2. Comparison of different methods to infer the momentum flux. Shown are results for the three periods and both zonal and meridional momentum. Long-dashed lines indicate negative, dashed lines positive and solid lines net momentum fluxes. Please note that the S3D results are reliable only above 25 km.

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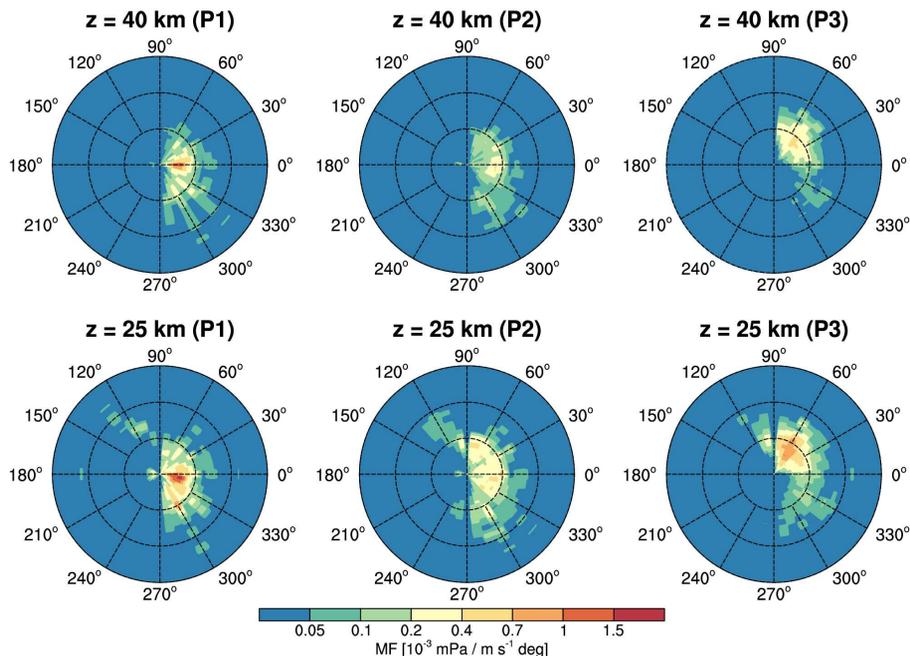


Fig. 3. Momentum flux spectra calculated from model winds for 25 km and 40 km altitude. Spectra are calculated in terms of k , l and ground based frequency ω_{gb} and binned according to ground based phase speed and propagation direction. Momentum flux is determined from co-spectra of vertical and horizontal winds. Note the quasi-logarithmic color scale.

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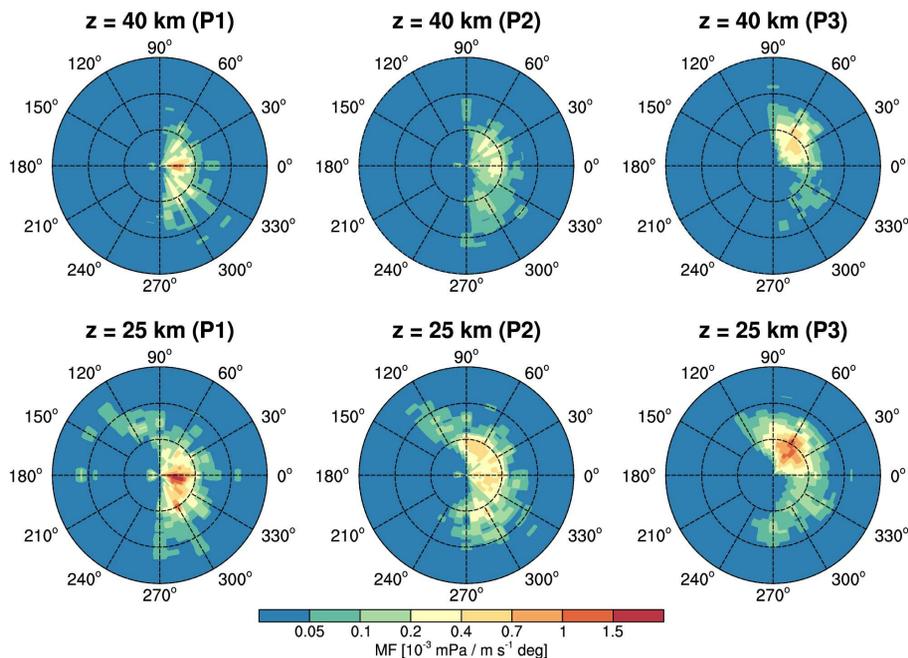


Fig. 4. As Fig. 3 but for model temperatures. Polarization relations are employed to calculate the momentum flux from the temperature amplitudes.

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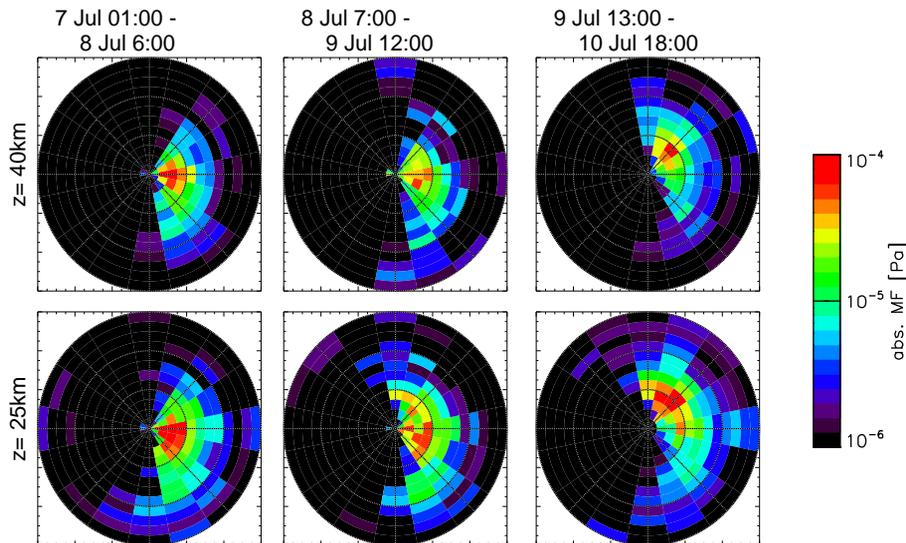


Fig. 5. Momentum flux spectra from the S3D analysis method applied to model winds. The ground-based phase speed is determined from the vertical wavelength and background winds. Color scale is logarithmic.

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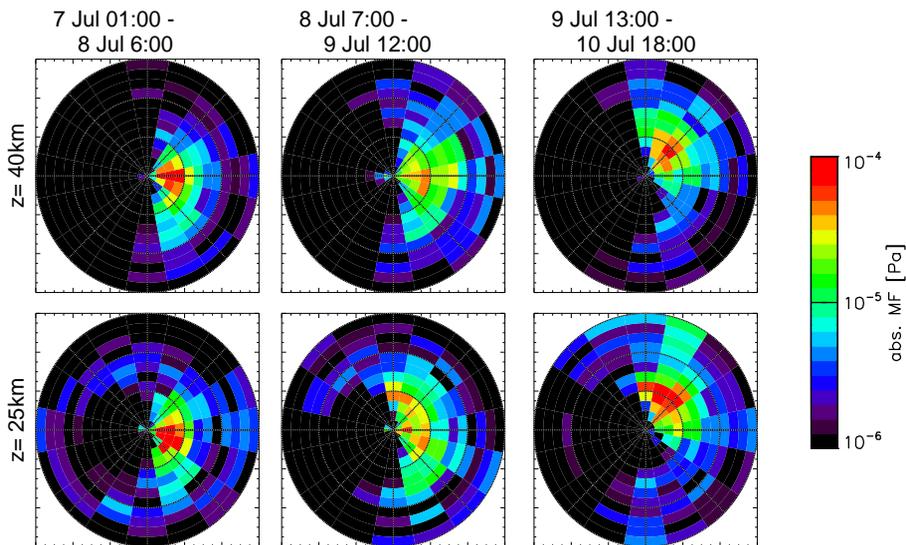


Fig. 6. As Fig. 5, but for temperatures.

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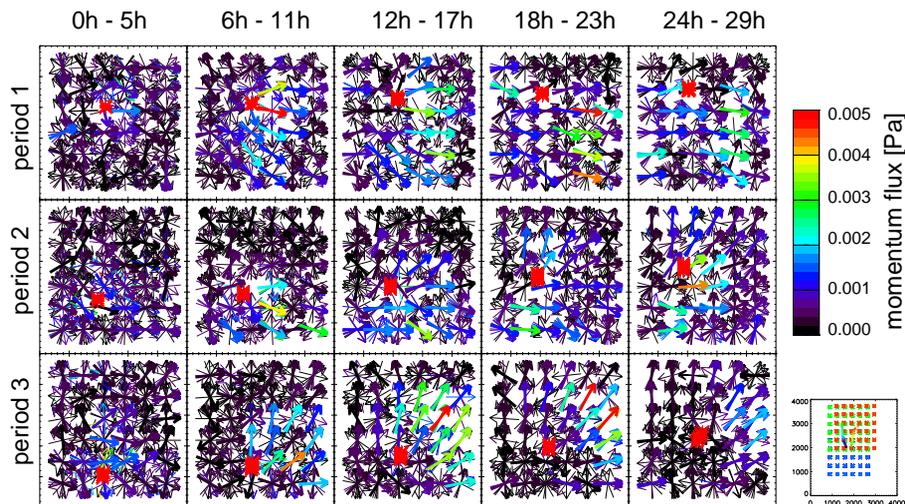


Fig. 7. Spatio-temporal evolution of the the momentum flux over the typhoon at 25 km altitude for $360 \text{ km} \times 360 \text{ km} \times 10 \text{ km}$ analysis volume. Thin arrows indicate single events and components, thick arrows the average total momentum flux. Each panel shows a six hourly interval, time proceeds from left to right and up to bottom. Please note that the position of a momentum flux value corresponds to the center of an arrow (not the base!).

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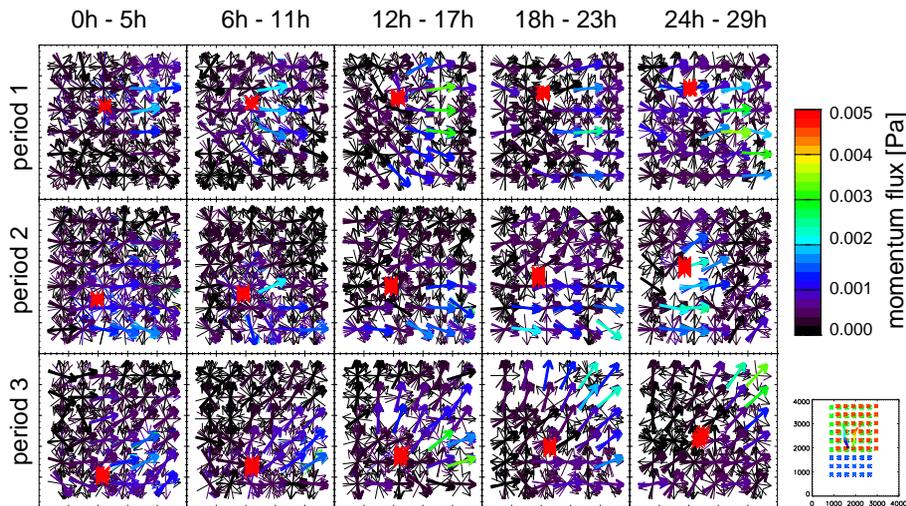


Fig. 8. As for Fig. 7 but for 40 km altitude.

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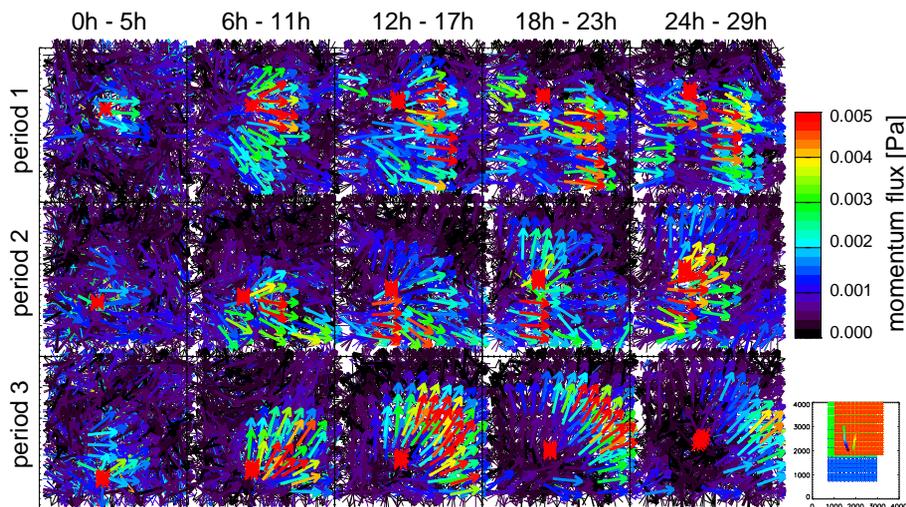


Fig. 9. As for Fig. 7 but for $189 \text{ km} \times 189 \text{ km} \times 10 \text{ km}$ analysis volume. Please note that the position of a momentum flux value corresponds to the center of an arrow (not the base!).

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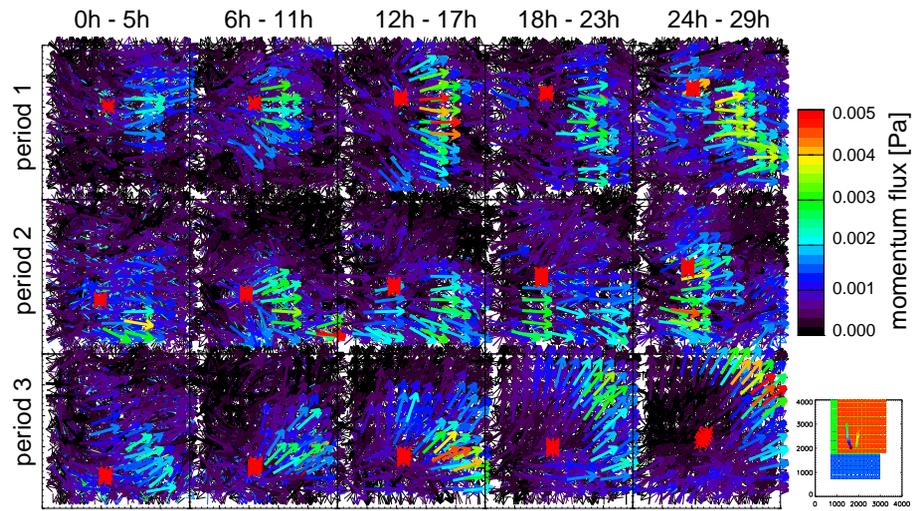


Fig. 10. As for Fig. 8 but for 189 km × 189 km × 10 km analysis volume.

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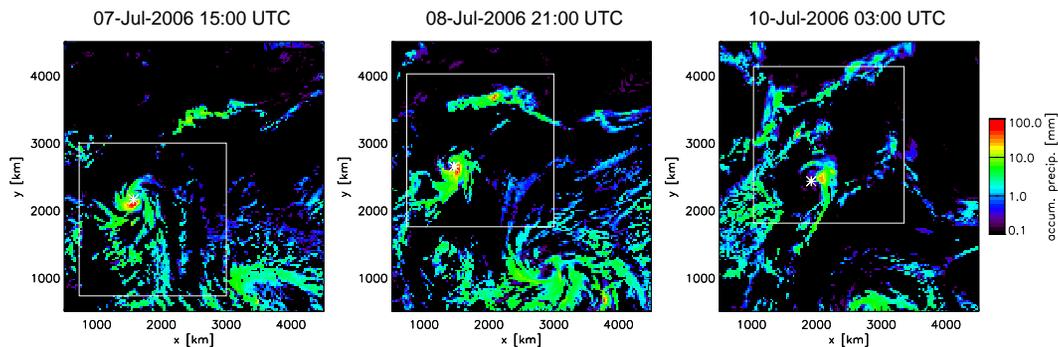


Fig. 11. Accumulated precipitation of the last hour before the center time of each simulation period. The white frame indicates the analysis region and the white asterisk the typhoon center.

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