Corrigendum to:

Soft Matter, 2014, 10, 1987 by J.K.G. Dhont and K. Kang.

We made an error in the calculation of the rod-rod interaction potential V_Q in Ref.[1], "The origin of an electric-field induced dynamical state in dispersions of highly charged colloidal rods", where a mechanism is suggested and a theory is presented for a dynamical state as found experimentally in Ref.[2]. This error changes values of constants in the equation of motion for the orientational order parameter, but does not change any of the conclusions in Ref.[1].

The error we made is concerned with the interaction potential between two charged rods. For thick double layers the interaction potential can be written as a pair-wise sum of beadbead interactions (see eq.(11) in Ref.[1]). This sum can be written as a double contour integral, extending the integration ranges to infinite, which is allowed as long as the Debye length κ^{-1} is much smaller than the length L of the rods,

$$V_Q(\mathbf{R}, \hat{\mathbf{u}}_1, \hat{\mathbf{u}}_2) = \frac{\exp\{\kappa d\}}{4\pi\epsilon (1 + \kappa a)^2} \nu_1 \nu_2 \int_{-\infty}^{+\infty} dl_1 \int_{-\infty}^{+\infty} dl_2 \frac{\exp\{-\kappa \mid l_1 \hat{\mathbf{u}}_1 - l_2 \hat{\mathbf{u}}_2 + \mathbf{r} \mid\}}{\mid l_1 \hat{\mathbf{u}}_1 - l_2 \hat{\mathbf{u}}_2 + \mathbf{r} \mid},$$

where d is the rod core-diameter, a = d/2 the radius, ϵ the dielectric constant of the solvent, and ν_1 and ν_2 are the local line-charge densities at the points on the contour of the rods 1 and 2 for which the distance between the points is minimum, respectively. The minimum distance between the center lines of the two rods is equal to,

$$\mathbf{r} \; = \; \mathbf{R} \cdot \left(\hat{\mathbf{u}}_1 \times \hat{\mathbf{u}}_2 \right) / \mid \hat{\mathbf{u}}_1 \times \hat{\mathbf{u}}_2 \mid \, , \label{eq:reconstruction}$$

where \mathbf{R} is the distance between the mid-points of the two rods. It is erroneously stated in Ref.[1] that the integral can not be evaluated explicitly. In fact this integral can be evaluated analytically, as already stated in Ref.[3], and is equal to,

$$\int_{-\infty}^{\infty} dl_1 \int_{-\infty}^{+\infty} dl_2 \, \frac{\exp\left\{-\kappa \mid l_1 \hat{\mathbf{u}}_1 - l_2 \hat{\mathbf{u}}_2 + \mathbf{r} \mid\right\}}{\mid l_1 \hat{\mathbf{u}}_1 - l_2 \hat{\mathbf{u}}_2 + \mathbf{r} \mid} = \frac{2\pi}{\kappa} \, \frac{\exp\left\{-\kappa r\right\}}{\mid \hat{\mathbf{u}}_1 \times \hat{\mathbf{u}}_2 \mid}. \tag{1}$$

For a uniformly charged rod (without field-induced polarization) the interaction potential is therefore (in the notation of Ref.[1], and with $\beta = 1/k_BT$),

$$\beta V_{\bar{Q}\bar{Q}}(\mathbf{R}, \hat{\mathbf{u}}_1, \hat{\mathbf{u}}_2) = \frac{K_Q}{|\hat{\mathbf{u}}_1 \times \hat{\mathbf{u}}_2|} \exp\left\{-\kappa r |\mathbf{R} \cdot (\hat{\mathbf{u}}_1 \times \hat{\mathbf{u}}_2)| / |\hat{\mathbf{u}}_1 \times \hat{\mathbf{u}}_2|\right\},$$
(2)

where the erroneous factor in $1/\kappa r$ that we had in Ref.[1] is absent, and where (with l_B the Bjerrum length),

$$K_Q = \frac{2\pi Z^2 \exp\{\kappa d\}}{(1+\kappa a)^2} \frac{l_B}{\kappa L^2}.$$
 (3)

This expression for K_Q differs by a factor $\pi/2$ from the expression that we had in Ref.[1]. In the same way, in the potential V_{EE} due to E-field induced charges in eq.(21) in Ref.[1], the factor $1/\kappa r$ should be omitted, while the correct value for the constant K_E is also different by a factor $\pi/2$ from eq.(22) in Ref.[1],

$$K_E = \frac{\pi \left(\kappa_c/\kappa\right)^2 \exp\{\kappa d\}}{8 \left(1 + \kappa a\right)^2 \left(1 + 2\kappa_c a \mathcal{K}(\kappa a)\right)^2} \frac{\kappa d^2}{l_B}, \tag{4}$$

where $\kappa_c = 2 \pi l_B \bar{c}$ is the inverse "condensate length", with \bar{c} the number surface concentration of condensed ions in the absence of the electric field, and (with K_0 the modified Bessel function of the second kind of zeroth order),

$$\mathcal{K}(\kappa a) \equiv \frac{1}{2\pi} \int_0^{2\pi} d\varphi \, K_0 \left(\kappa a \sqrt{2 \left(1 - \cos \varphi \right)} \right) \,. \tag{5}$$

Although the error made in determining the potential between two rods is admittedly quite fundamental, it has a minor effect on the equation of motion of the orientational order parameter, in the sense that it slightly changes the values of coefficients, but does not affect the structure of the equation of motion.

As a consequence of the erroneous factor $1/\kappa r$ in the potentials in eqs.(21) and (26) in Ref.[1], the asymtotic behaviour of the integral,

$$I(A) \equiv -\kappa d + \int_0^\infty d\alpha l \left[1 - \exp\left\{a A \exp\left\{-\alpha\right\}\right\}\right] , \qquad (6)$$

needs to be evaluated instead of the similar integral, evaluated in appendix A in Ref.[1], where $\exp\{-\alpha\}$ is replaced by $\exp\{-\alpha\}/\alpha$ (the extra erroneous $1/\alpha$ is due to the factor $1/\kappa r$ in the interaction potential). The asymptotic form of this integral has been evaluated in Ref.[4],

$$I(A) = -\kappa d + \ln\{A\} + \gamma_E , \qquad (7)$$

where $\gamma_E = 0.5772 \cdots$ is Euler's constant. This should be compared with the incorrect result in eq.(55) in Ref.[1], which reads; $I(A) = -\kappa d + \ln\{A\} + C$, with C = -3/4. Correct results are thus obtained by simply replacing C by γ_E in all expressions in Ref.[1]. In particular, the effective diameter is equal to,

$$\frac{d_{\text{eff}}}{d} = \frac{1}{\kappa d} \left[\ln\{K_Q\} + \gamma_E \right] , \tag{8}$$

which is essentially identical to the expression given in Ref. [5]

In effect, the use of an erroneous potential amounts to changing the values of the constants K_Q , K_E , and the expression for d_{eff} in the otherwise correct equation of motion for the orientational order parameter. A publication is in preparation where experiments at different ionic strengths as well as various rod-concentrations is compared with theory, using the correct numerical values of these parameters.

References

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