

# Explaining soil moisture variability as a function of mean soil moisture: A stochastic unsaturated flow perspective

H. Vereecken,<sup>1</sup> T. Kamai,<sup>2</sup> T. Harter,<sup>2</sup> R. Kasteel,<sup>1</sup> J. Hopmans,<sup>2</sup> and J. Vanderborght<sup>1</sup>

Received 24 August 2007; revised 5 October 2007; accepted 15 October 2007; published 21 November 2007.

[1] Understanding soil moisture variability and its relationship with water content at various scales is a key issue in hydrological research. In this paper we predict this relationship by stochastic analysis of the unsaturated Brooks-Corey flow in heterogeneous soils. Using sensitivity analysis, we show that parameters of the moisture retention characteristic and their spatial variability determine to a large extent the shape of the soil moisture variance-mean water content function. We demonstrate that soil hydraulic properties and their variability can be inversely estimated from spatially distributed measurements of soil moisture content. Predicting this relationship for eleven textural classes we found that the standard deviation of soil moisture peaked between 0.17 and 0.23 for most textural classes. It was found that the  $\beta$  parameter, which describes the pore-size distribution of soils, controls the maximum value of the soil moisture standard deviation. **Citation:** Vereecken, H., T. Kamai, T. Harter, R. Kasteel, J. Hopmans, and J. Vanderborght (2007), Explaining soil moisture variability as a function of mean soil moisture: A stochastic unsaturated flow perspective, *Geophys. Res. Lett.*, 34, L22402, doi:10.1029/2007GL031813.

## 1. Introduction

[2] Soil moisture is a key variable controlling hydrological and energy fluxes in soils. Due to the heterogeneity of soils, atmospheric forcing, vegetation, and topography, soil moisture is spatially variable. Understanding and characterizing this spatial variability is one of the major challenges within hydrological sciences. Especially the relationship  $\sigma_\theta(\langle\theta\rangle)$  between mean soil moisture content,  $\langle\theta\rangle$ , and its standard deviation  $\sigma_\theta$ , has received considerable attention in the hydrological community. This relationship is important to understand the contribution of soil moisture variability at smaller scales towards the effective soil moisture observed at larger scales or its role in the parametrization of, e.g., climate and watershed models (upscaling/downscaling [e.g., Famiglietti *et al.*, 1999; Crow *et al.*, 2005; Ryu and Famiglietti, 2005]). Some studies report an increase in  $\sigma_\theta$  with decreasing  $\langle\theta\rangle$  [e.g., Bell *et al.*, 1980; Famiglietti *et al.*, 1998; Oldak *et al.*, 2002], while others report the opposite behaviour [Famiglietti *et al.*, 1999; Choi and Jacobs, 2007]. Re-examination of recent experimental work [Ryu and

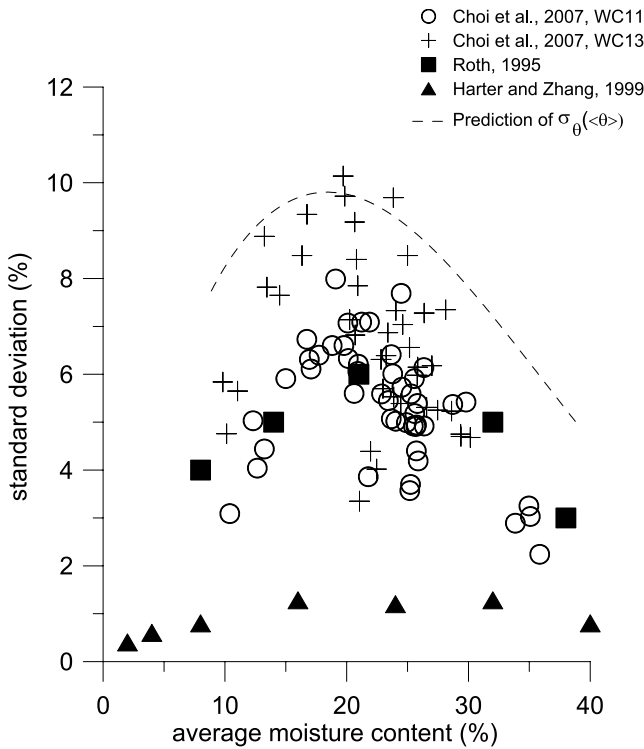
Famiglietti, 2005; Choi and Jacobs, 2007; Choi *et al.*, 2007] and of results from simulations and stochastic analysis of water flow in heterogeneous soils [Roth, 1995; Harter and Zhang, 1999] shows that  $\sigma_\theta(\langle\theta\rangle)$  increases during drying from a very wet stage, reaches a maximum value at a specific or critical mean moisture content, and then decreases during further drying (Figure 1). The observed unimodal shape of  $\sigma_\theta(\langle\theta\rangle)$  has been explained mostly based on empirical [Hu and Islam, 1998] and/or statistical analysis of field data [e.g., Famiglietti *et al.*, 1998; Ryu and Famiglietti, 2005; Choi and Jacobs, 2007]. To date, an explicit mathematical analysis of  $\sigma_\theta(\langle\theta\rangle)$  is lacking. In this letter, we use analytical stochastic work by Zhang *et al.* [1998], to show that  $\sigma_\theta(\langle\theta\rangle)$  is directly related to the soil hydraulic properties and their statistical moments and that inverse modelling can be used to estimate these properties from moisture data. Our results show that the relationship between soil moisture variability and mean moisture content is controlled by soil hydraulic properties, their statistical moments and their spatial correlation. The unimodal shape of  $\sigma_\theta(\langle\theta\rangle)$  observed in the field and in simulation data is well explained by existing stochastic theories.

## 2. Stochastic Theory

[3] Over the past thirty years, various stochastic theories of unsaturated water flow have been developed to predict effective water fluxes, state variables, and hydraulic parameters for heterogeneous soils [e.g., Yeh *et al.*, 1985; Zhang, 2002]. Briefly, across a field site, the variability in soil hydraulic parameters leads to an ensemble of moisture retention curves,  $\theta(h)$ , where  $h$  is the pressure head, that typically show the largest variation of  $\theta$  in the medium range of logarithmic pressure head values. Stochastic perturbation theory predicts that when soil gets drier the variance of both, pressure head and moisture content increase [Harter and Zhang, 1999]. Given the fact that  $\theta(h)$  is bounded between  $\theta_r$ , the residual moisture content and  $\theta_s$ , the saturated moisture content,  $\sigma_\theta(\langle\theta\rangle)$  is also bounded even when the variance of the pressure head increases to large values. This is demonstrated by numerical simulations and stochastic analysis of water flow in heterogeneous unsaturated porous media [Roth, 1995; Zhang *et al.*, 1998; Harter and Zhang, 1999]. Zhang *et al.* [1998] derived closed form equations for the variances and covariances of  $h$  and  $\theta$  and the cross-covariances between  $h$  and hydraulic parameters in the Brooks-Corey (BC) and Gardner-Russo equations for the case of 1D gravity dominated unsaturated flow in mildly heterogeneous flow domains. These equations are derived assuming stationarity in saturated hydraulic conductivity and pressure

<sup>1</sup>Agrosphere, Institute of Chemistry and Dynamics of the Geosphere, Forschungszentrum Jülich, Jülich, Germany.

<sup>2</sup>Department of Land, Air and Water Resources, University of California, Davis, California, USA.



**Figure 1.** Soil moisture variability with respect to mean soil moisture content for the measurements made by Choi *et al.* [2007] on field sites WC11 and WC13. Symbols demonstrate results obtained with numerical simulations [Roth, 1995; Harter and Zhang, 1999]. The dashed line represents the theoretical  $\sigma_{\theta}(\langle\theta\rangle)$  (1) based on Table 2 values for the soil of Choi *et al.* [2007]. Actual  $\sigma_{\alpha}^2$  and  $\sigma_{\beta}^2$  at the field site may be smaller than estimated from Table 2 leading to the high values for the theoretical  $\sigma_{\theta}(\langle\theta\rangle)$ .

head, joint-Gaussian spatial distribution of hydraulic parameters with exponential covariance functions and negligible correlation between the hydraulic parameters. Despite these restrictions, the derived equation provides an excellent tool to analyze the relationship between  $\langle\theta\rangle$  and  $\sigma_{\theta}$ . Using the BC equation for  $\theta(h)$  and the hydraulic conductivity function [Zhang *et al.*, 1998] the variance of effective moisture content for 1D vertical flow is written as:

$$\sigma_{\theta_e}^2(\langle\theta_e(x_3)\rangle) = b0^2 \left\{ \frac{b2^2 \sigma_{\ln K_s}^2 \lambda_{\ln K_s}^2}{(1 + a2 \lambda_{\ln K_s}^2) a2} + \frac{b1^2 \sigma_{\alpha}^2}{(1 + a2 \lambda_{\alpha})} + b3^2 \sigma_{\beta}^2 \left[ 1 + \frac{b2 \lambda_{\beta} (6a2 + 9b2)}{(1 + a2 \lambda_{\beta}) a2} \right] \right\} \quad (1)$$

The parameters  $a1$ ,  $a2$ ,  $a3$ ,  $b0$ ,  $b1$ ,  $b2$ ,  $b3$  are functions of  $\ln K_s(x_3)$ ,  $\alpha(x_3)$ ,  $\beta(x_3)$ ,  $h(x_3)$ .  $\alpha(x_3)$  is the air entry value,  $\beta(x_3)$  is the pore size distribution index characterizing the shape of the moisture retention characteristic,  $K_s(x_3)$  is the saturated hydraulic conductivity, and  $x_3$  the vertical coordinate.  $\theta_e(x_3)$  is the effective moisture content equal

to  $\theta(x_3) - \theta_r$ . Further,  $\sigma_{\ln K_s}^2$  is the variance of  $\ln K_s(x_3)$ ,  $\sigma_{\beta}^2$  the variance of  $\beta$ ,  $\sigma_{\alpha}^2$  the variance of  $\alpha$ , and  $\lambda_i$ , the correlation length of  $\ln K_s(x_3)$ ,  $\alpha(x_3)$ ,  $\beta(x_3)$ . In the subsequent we will drop the coordinate symbol  $x_3$  and use  $\sigma_{\theta}(\langle\theta\rangle)$  rather than  $\sigma_{\theta e}(\langle\theta_e\rangle)$  for convenience.

### 3. Methods

[4] First, we use four typical soils (Table 1) to demonstrate the effect of soil texture on  $\sigma_{\theta}(\langle\theta\rangle)$ . Values of the BC parameters,  $\langle\alpha\rangle$ ,  $\langle\beta\rangle$ , and  $\langle\ln K_s\rangle$ , for the sandy loam were obtained from Zhang *et al.* [1998]. The values for the other soils were derived from soil texture data using pedotransfer functions, PTF (“Rosetta” [Schaap *et al.*, 1998]), and then fitting the BC-equation to the Van Genuchten model obtained from Rosetta. We assumed that  $CV_{\alpha}$  (CV: coefficient of variation) and  $CV_{\beta}$  were 30%,  $\sigma_{\ln K_s}^2 = 1$  and correlation scales were equal to 25 cm based on field data [e.g., Russo and Bresler, 1981; Mallants *et al.*, 1996; Schaap *et al.*, 1998].  $\theta_r$  and  $\theta_s$  were assumed to be constant. Second, the sensitivity of  $\sigma_{\theta}(\langle\theta\rangle)$  to the variability in soil hydraulic parameters in (1) was investigated. Third, we used (1) to estimate  $\langle\alpha\rangle$ ,  $\langle\beta\rangle$ ,  $\sigma_{\alpha}^2$ ,  $\sigma_{\beta}^2$  and  $\sigma_{\ln K_s}^2$  from an artificial, computer-generated  $\sigma_{\theta}(\langle\theta\rangle)$  data via inverse modelling. The inverse model was based on least-squares optimization with the Levenberg-Marquardt algorithm (MATLAB, 2007). Assumptions about  $\theta_r$ ,  $\theta_s$ ,  $\lambda_{\alpha}$ ,  $\lambda_{\beta}$  and  $\lambda_{\ln K_s}$  were as above. The inverse modelling was performed using the loamy sand (Table 1) and by generating synthetic datasets of  $\sigma_{\theta}(\langle\theta\rangle)$ . White noise ( $N(0, 1)$ ) was added to the computed value of  $\sigma_{\theta}(\langle\theta\rangle)$ . Six noise levels were used: 0%, 1%, 2%, 3%, 4% and 5%. For each level, ten realizations were obtained, inverse modelling was performed, and average parameter estimates and estimation variances were calculated. The 0% noise case was used to test the algorithm. Fourth, we calculate  $\sigma_{\theta}(\langle\theta\rangle)$  using BC-data for eleven textural classes (Table 2) according to Rawls *et al.* [1982] and Cosby *et al.* [1984] to find the relation between moisture content and  $\sigma_{\max}$ , the max. standard deviation. Fifth, we show an application to field data of  $\sigma_{\theta}(\langle\theta\rangle)$  [Choi *et al.*, 2007]. Again,  $\theta_r$  and  $\theta_s$  were obtained based on available soil texture data using PTF. Values of  $\langle\alpha\rangle$ ,  $\langle\beta\rangle$ ,  $\sigma_{\alpha}^2$ ,  $\sigma_{\beta}^2$  and  $\sigma_{\ln K_s}^2$  were estimated by applying field texture data to Table 2.

### 4. Results and Conclusions

#### 4.1. Effect of Soil Texture on $\sigma_{\theta}(\langle\theta\rangle)$

[5] Finer textured soils (silt loam, clay loam) have a clear peak in  $\sigma_{\theta}(\langle\theta\rangle)$  whereas the sandy loam soil and the loamy

**Table 1.** Brooks-Corey Parameters of the Example Soils<sup>a</sup>

	Sandy Loam	Loamy Sand	Silt Loam	Clay Loam
$\theta_r$ [cm <sup>3</sup> cm <sup>-3</sup> ]	0	0.057	0.067	0.095
$\theta_s$ [cm <sup>3</sup> cm <sup>-3</sup> ]	0.5	0.41	0.45	0.41
$\alpha$ [cm <sup>-1</sup> ]	0.022	0.177	0.026	0.025
$\beta$	1.738	1.07	0.394	0.292
$\sigma_{\ln K_s}^2$	1 (0.1, 0.5, 1)			
$\lambda_{\alpha}$ , $\lambda_{\beta}$ , $\lambda_{\ln K_s}$ [cm]	25 (10, 40, 80)			

<sup>a</sup>The variance of  $\alpha$  and  $\beta$  was calculated for a CV of 0.3. Values used for the sensitivity analysis are given in parentheses.

**Table 2.** Brooks-Corey Parameter for Different Textural Classes<sup>a</sup>

	$\theta_s$	$\theta_r$	$\alpha, \text{cm}^{-1}$	$\sigma_\alpha^2$	$\beta$	$\sigma_\beta^2$	$\sigma_{\ln K_s}^2$
Sand	0.437	0.02	0.5599	8.7071	0.694	0.163	0.152
loamy sand	0.437	0.035	0.3966	3.5986	0.553	0.102	0.260
sandy loam	0.453	0.041	0.0886	0.0330	0.378	0.057	0.449
Loam	0.463	0.027	0.1425	0.1379	0.252	0.028	0.397
silt loam	0.501	0.015	0.0709	0.0282	0.234	0.017	0.303
Sandyclayloam	0.398	0.068	0.0494	0.0123	0.319	0.058	0.292
clay loam	0.464	0.075	0.0511	0.0117	0.242	0.029	0.348
siltyclayloam	0.471	0.04	0.0463	0.0085	0.177	0.019	0.372
sandy clay	0.43	0.109	0.0508	0.0152	0.223	0.031	0.109
silty clay	0.479	0.056	0.0400	0.0078	0.15	0.012	0.476
clay loam	0.475	0.09	0.0371	0.0069	0.165	0.016	0.384

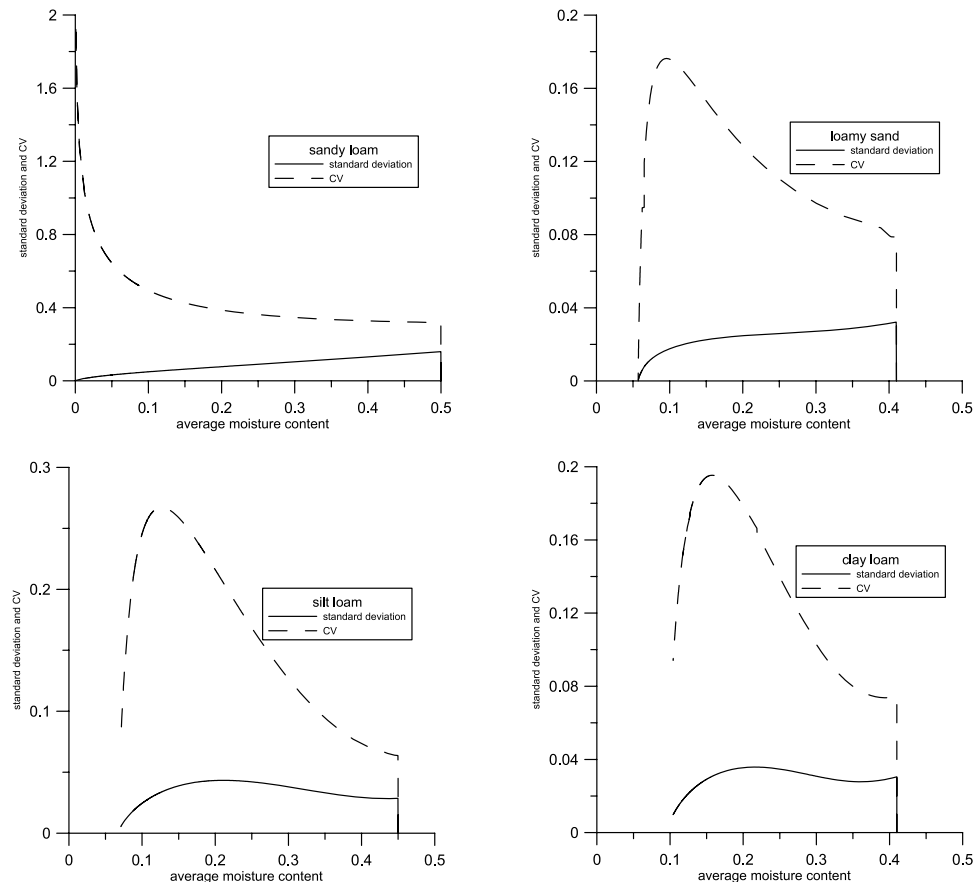
<sup>a</sup>Parameters as given by *Rawls et al.* [1982]. The variance of  $\ln K_s$  is obtained from *Crosby et al.* [1984]. The  $\alpha$  values given by *Rawls et al.* [1982] were statistically transformed to represent its inverse value used in equation (1).

sand soil show a steady decrease in  $\sigma_\theta(\langle\theta\rangle)$  from wet to dry (Figure 2). Therefore, we may observe different behavior in  $\sigma_\theta(\langle\theta\rangle)$  depending on mean soil moisture status and on soil hydraulic properties. The  $CV_\theta(\langle\theta\rangle)$  of the sandy soil increases as the soil dries and reaches its maximum value near the residual moisture content (Figure 2). The other soils show a more unimodal shape in  $CV_\theta(\langle\theta\rangle)$ .

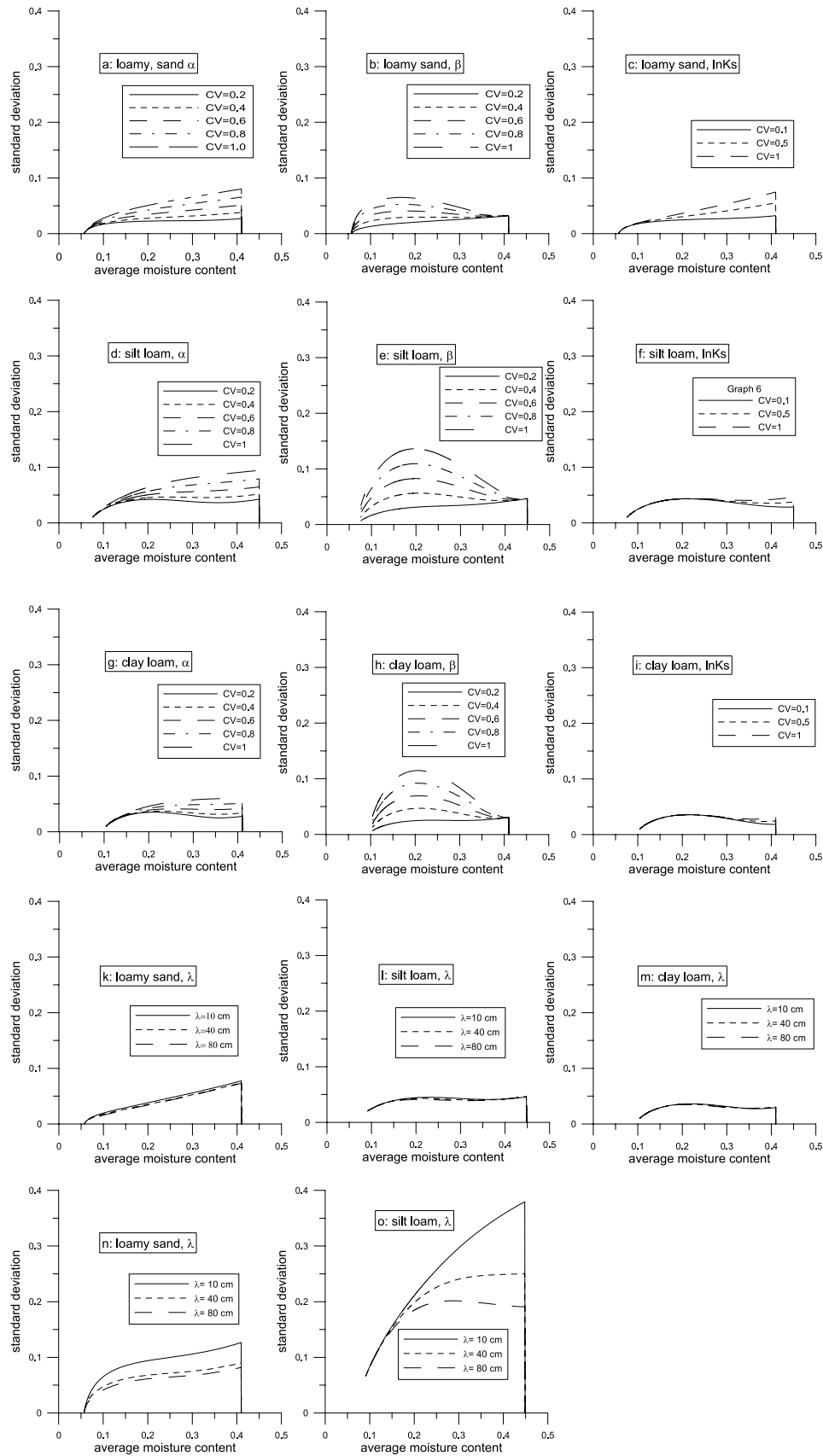
#### 4.2. Sensitivity of $\sigma_\theta(\langle\theta\rangle)$ to Soil Hydraulic Properties

[6] Variability in  $\alpha$  affects  $\sigma_\theta(\langle\theta\rangle)$  mainly at high soil moisture regardless of soil type (Figures 3a, 3d and 3g).

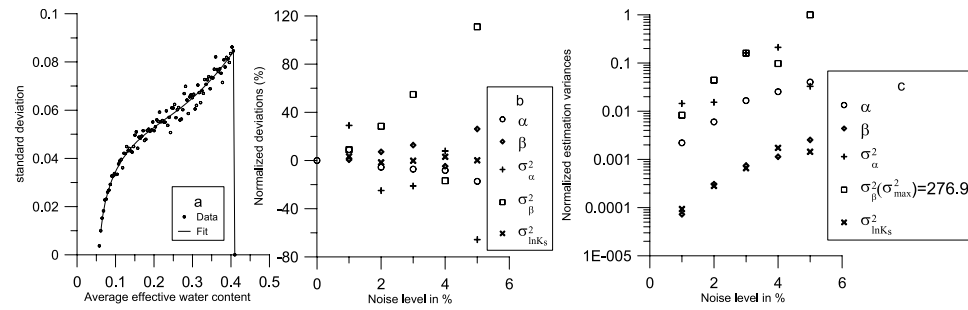
However, the sensitivity is smaller for the finer textured clay loam soil. The pronounced sensitivity of  $\sigma_\alpha^2$  at high soil moisture suggests that soil moisture data under a wet regime are important for estimating this parameter. All three soils show that  $\sigma_\theta(\langle\theta\rangle)$  is very sensitive to  $\sigma_\beta^2$  at moderate soil moisture content, with the largest sensitivity found for the silt loam soil (Figures 3b, 3e and 3h). The effect can be explained by the fact that  $\beta$  is a measure of the pore size distribution of the soil. It therefore affects the shape of the entire moisture retention characteristic, particularly in the moisture range where most variation in soil



**Figure 2.** The  $\sigma_\theta(\langle\theta\rangle)$  and the corresponding CV for four different textural classes using equation (1). Parameter specifications are given in Table 1.



**Figure 3.** (a, d, g) The effect of variability in  $\alpha$  on soil moisture variability for the loamy sand, silt loam, and clay loam soil using five different values for the CV. Similar analysis is shown for the parameter (b, e, h)  $\beta$ , (c, f, i)  $\ln K_s$ , and (k, l, m) vertical correlation length of the Brooks-Corey parameters. (n, o) The effect of an increased coefficient of variation for  $\sigma_\alpha^2$  and  $\sigma_\beta^2$  (CV = 0.9) on the sensitivity of  $\sigma_\theta(\theta)$  for the correlation scale.



**Figure 4.** (a) Fit to the data with 5% measurement noise. (b) Normalized deviations from optimal parameter values. (c) Normalized estimation values with respect to  $\sigma_\beta^2$ .

moisture occurs. The impact of  $\beta$  on  $\sigma_\theta(\theta)$  at moderate soil moisture was indirectly observed by *Famiglietti et al.* [1998] who found a strong correlation between the variability in surface soil moisture content and clay content under dry conditions. *Cosby et al.* [1984] also showed that clay content and  $\beta$  are strongly correlated. The sensitivities of  $\sigma_\theta(\theta)$  to  $\sigma_\alpha^2$  and  $\sigma_\beta^2$  are complementary: Near saturation, the sensitivity to  $\sigma_\alpha^2$  is larger and diminishes as the soil dries out whereas the sensitivity of  $\sigma_\theta(\theta)$  to  $\sigma_\beta^2$  is small near saturation and increases as the soil dries out (e.g., Figures 3d and 3e). Upon further drying, however, the effect of  $\sigma_\beta^2$  decreases as soil moisture is approaching residual moisture content. Variability in  $\sigma_{\ln K_s}^2$  mainly affects the wet part of  $\sigma_\theta(\theta)$  (Figures 3c, 3f and 3i). This effect was also observed by *Famiglietti et al.* [1998] who found that variability in soil moisture content is controlled strongly by porosity and hydraulic conductivity under wet conditions but not under drier conditions. This is supported by our calculations, which show a decrease in the sensitivity of  $\sigma_\theta(\theta)$  to variability in  $\sigma_{\ln K_s}^2$  as the soil is drying. In general, the sensitivity of  $\sigma_\theta(\theta)$  to variability in  $\ln K_s$  seems smaller compared to its sensitivity to  $\sigma_\alpha^2$  and  $\sigma_\beta^2$ . The sensitivity of  $\sigma_\theta(\theta)$  with respect to the correlation scale is low (Figures 3k, 3l and 3m). Moreover, the sensitivity of  $\sigma_\theta(\theta)$  to correlation scale seems to be related to the magnitude of  $\sigma_\alpha^2$  and  $\sigma_\beta^2$  (Figures 3n and 3o). The larger  $\sigma_\alpha^2$  and  $\sigma_\beta^2$ , the more pronounced is the effect of correlation scale on the soil moisture variability. The largest effect is observed in the wet part of the soil moisture range.

#### 4.3. Inverse Estimation of Soil Hydraulic Parameters From $\sigma_\theta(\theta)$

[7] For zero noise, the estimated soil hydraulic parameters from the synthetic  $\sigma_\theta(\theta)$  were in perfect agreement with their “true” values (not shown). Excellent agreement of estimated with “true” parameters was also found for low noise levels (Figure 4a). At all noise levels, good estimates of  $\alpha$ ,  $\beta$  and  $\sigma_{\ln K_s}^2$  were obtained from the synthetic  $\sigma_\theta(\theta)$  data. Maximum deviations from “true” values range between 10% and 25% (Figures 4b and 4c). Higher order moments  $\sigma_\alpha^2$  and  $\sigma_\beta^2$  show deviations larger than 30% at 2% noise and quickly increase with noise level. Estimation variances of the parameters also rapidly increase with noise level (Figure 4c).

#### 4.4. Relation Between Mean Moisture Content and $\sigma_{\max}$

[8] The largest observed moisture variability is a function of soil texture (Table 3).  $\sigma_\theta(\theta)$  is typically largest in the mid-range of soil moisture content for all textural classes except “sand”, for which the maximum of  $\sigma_\theta$ ,  $\sigma_{\max}$ , value is at air entry. For the finer textured soils,  $\sigma_{\max}$  occurs at mean soil moisture values ranging from 0.18 to 0.23 (Table 3). This theoretical result based on mechanistic soil-physical analysis corresponds well with *Ryu and Famiglietti* [2005] who experimentally found that  $\sigma_\theta(\theta)$  tends to peak around a value of 0.2.

#### 4.5. Comparison of Predicted and Measured $\sigma_\theta(\theta)$

[9] An application of this approach to field data shows good agreement between measured  $\sigma_\theta(\theta)$  and the theoretical  $\sigma_\theta(\theta)$  curve (Figure 1) obtained by applying field texture data to Table 2. These results demonstrate that measured  $\sigma_\theta(\theta)$  may be used to derive soil hydraulic parameters. Further in-depth analysis and field testing is needed to evaluate the full potential of this approach, particularly when including the forcing through precipitation and vegetation. Also, it is generally accepted that the BC model has limited value in the field, particularly near saturation. Improved stochastic theories based on the Van Genuchten model or similar more realistic descriptions of the soil moisture characteristic might be valuable in improving estimation of hydraulic parameters from measured  $\sigma_\theta(\theta)$  curves.

**Table 3.** Maximum Standard Deviation in Function of Soil Type and Moisture Content<sup>a</sup>

	$\sigma_{\max}$	$\theta$ at $\sigma_{\max}$	$\sigma$ at Air Entry, $1/\alpha$
Sand	0.203	0.41	0.191
loamy sand	0.056	0.153	0.041
sandy loam	0.089	0.168	0.042
Loam	0.103	0.172	0.032
silt loam	0.098	0.196	0.029
Sandy clay loam	0.089	0.179	0.024
clay loam	0.100	0.210	0.025
Silty clay loam	0.123	0.200	0.022
sandy clay	0.092	0.223	0.011
silty clay	0.114	0.211	0.021
clay loam	0.108	0.231	0.018

<sup>a</sup>Maximum standard deviation,  $\sigma_{\max}$ ; moisture content,  $\theta$ .

## References

- Bell, K. R., B. J. Blanchard, T. J. Schmugge, and M. W. Witzak (1980), Analysis of surface moisture variations within large-field sites, *Water Resour. Res.*, *16*(4), 796–810.
- Choi, M., and J. M. Jacobs (2007), Soil moisture variability of root zone profiles within SMEX02 remote sensing footprints, *Adv. Water Res.*, *30*(4), 883–896.
- Choi, M., J. M. Jacobs, and M. H. Cosh (2007), Scaled spatial variability of soil moisture fields, *Geophys. Res. Lett.*, *34*, L01401, doi:10.1029/2006GL028247.
- Cosby, B. J., G. M. Hornberger, R. B. Clapp, and T. R. Ginn (1984), A statistical exploration of the relationships of soil-moisture characteristics to the physical properties of soils, *Water Resour. Res.*, *20*(6), 682–690.
- Crow, W. T., et al. (2005), Upscaling of field-scale soil moisture measurements using distributed land surface modeling, *Adv. Water Res.*, *28*(1), 1–14.
- Famiglietti, J. S., et al. (1998), Variability in surface moisture content along a hillslope transect: Rattlesnake Hill, Texas, *J. Hydrol.*, *210*(1–4), 259–281.
- Famiglietti, J. S., J. A. Devereaux, C. A. Laymon, T. Tsegaye, P. R. Houser, T. J. Jackson, S. T. Graham, M. Rodell, and P. J. van Oevelen (1999), Ground-based investigation of soil moisture variability within remote sensing footprints during the Southern Great Plains 1997 (SGP97) Hydrology Experiment, *Water Resour. Res.*, *35*(6), 1839–1851.
- Harter, T., and D. X. Zhang (1999), Water flow and solute spreading in heterogeneous soils with spatially variable water content, *Water Resour. Res.*, *35*(2), 415–426.
- Hu, Z. L., and S. Islam (1998), Effects of subgrid-scale heterogeneity of soil wetness and temperature on grid-scale evaporation and its parametrization, *Int. J. Climatol.*, *18*(1), 49–63.
- Mallants, D., et al. (1996), Spatial variability of hydraulic properties in a multi-layered soil profile, *Soil Sci.*, *161*(3), 167–181.
- Oldak, A., et al. (2002), Using GIS in passive microwave soil moisture mapping and geostatistical analysis, *Int. J. Geogr. Inf. Sci.*, *16*(7), 681–698.
- Rawls, W. J., et al. (1982), Estimation of soil-water properties, *Trans. ASAE*, *25*(5), 1316–1320.
- Roth, K. (1995), Steady-state flow in an unsaturated, 2-dimensional, macroscopically homogeneous, Miller-similar medium, *Water Resour. Res.*, *31*(9), 2127–2140.
- Russo, D., and E. Bresler (1981), Soil hydraulic-properties as stochastic-processes. 1: An analysis of field spatial variability, *Soil Sci. Soc. Am. J.*, *45*(4), 682–687.
- Ryu, D., and J. S. Famiglietti (2005), Characterization of footprint-scale surface soil moisture variability using Gaussian and beta distribution functions during the Southern Great Plains 1997 (SGP97) hydrology experiment, *Water Resour. Res.*, *41*, W12433, doi:10.1029/2004WR003835.
- Schaap, M. G., et al. (1998), Neural network analysis for hierarchical prediction of soil hydraulic properties, *Soil Sci. Soc. Am. J.*, *62*(4), 847–855.
- Yeh, T. C. J., L. W. Gelhar, and A. L. Gutjahr (1985), Stochastic-analysis of unsaturated flow in heterogeneous soils. 1: Statistically isotropic media, *Water Resour. Res.*, *21*(4), 447–456.
- Zhang, D. (2002), *Stochastic Methods for Flow in Porous Media*, 350 pp., Academic Press, San Diego, Calif.
- Zhang, D. X., T. C. Wallstrom, and C. L. Winter (1998), Stochastic analysis of steady-state unsaturated flow in heterogeneous media: Comparison of the Brooks-Corey and Gardner-Russo models, *Water Resour. Res.*, *34*(6), 1437–1449.

---

T. Harter, J. Hopmans, and T. Kamai, Department of Land, Air and Water Resources, University of California, Davis, 113 Veihmeyer Hall, Davis, CA 95616-8628, USA.

R. Kasteel, J. Vanderborght, and H. Vereecken, Agrosphere (ICG-4), Institute of Chemistry and Dynamics of the Geosphere (ICG), Forschungszentrum Jülich GmbH, D-52425 Jülich, Germany. (h.vereecken@fz-juelich.de)