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## Optical band gap of BiFeO<sub>3</sub> grown by molecular-beam epitaxy

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BiFeO<sub>3</sub> thin films have been deposited on (001) SrTiO<sub>3</sub> substrates by adsorption-controlled reactive molecular-beam epitaxy. For a given bismuth overpressure and oxygen activity, single-phase BiFeO<sub>3</sub> films can be grown over a range of deposition temperatures in accordance with thermodynamic calculations. Four-circle x-ray diffraction reveals phase-pure, epitaxial films with  $\omega$  rocking curve full width at half maximum values as narrow as 29 arc sec (0.008°). Multiple-angle spectroscopic ellipsometry reveals a direct optical band gap at 2.74 eV for stoichiometric as well as 5% bismuth-deficient single-phase BiFeO<sub>3</sub> films. © 2008 American Institute of Physics. [DOI: 10.1063/1.2901160]

BiFeO<sub>3</sub> is the only known material that is both ferroelectric ( $T_C \sim 1083$  K) and antiferromagnetic ( $T_N \sim 625$  K) at room temperature.<sup>1</sup> Recent reports of a large spontaneous polarization ( $\sim 100 \mu\text{C}/\text{cm}^2$ ) in thin films,<sup>2</sup> bulk ceramic,<sup>3</sup> and single crystals<sup>4</sup> of BiFeO<sub>3</sub> have led to an explosion of interest in its growth and properties.

The ferroelectric and multiferroic properties of BiFeO<sub>3</sub> are of interest for a number of applications including devices that utilize heterojunction effects where knowledge of the BiFeO<sub>3</sub> band gap is crucial for device design. To date, there is limited and conflicting information on the band gap and optical properties of BiFeO<sub>3</sub>, with existing reports limited to polycrystalline films<sup>5–7</sup> or nanowires.<sup>8</sup>

We have previously reported the deposition of BiFeO<sub>3</sub> films via adsorption-controlled reactive molecular-beam epitaxy (MBE) on (111) SrTiO<sub>3</sub> substrates.<sup>9</sup> In this letter, we report the adsorption-controlled growth of BiFeO<sub>3</sub> on (001)-oriented SrTiO<sub>3</sub> and the resulting crystalline quality, microstructure, optical dielectric functions, and band gap.

Single-crystalline, TiO<sub>2</sub>-terminated<sup>10</sup> SrTiO<sub>3</sub> substrates aligned within  $\pm 0.5^\circ$  of (001) were used as substrates. Films were grown under conditions described previously.

The parameter space for the adsorption-controlled growth of BiFeO<sub>3</sub> was calculated through the CALPHAD method<sup>11</sup> and was empirically established using *in situ* reflection high-energy electron diffraction (RHEED) and confirmed by *ex situ* four-circle x-ray diffraction (XRD). Figure 1 shows a calculated Ellingham diagram representing the phase stability regions of (I) BiFeO<sub>3</sub> +  $\gamma$ -Fe<sub>2</sub>O<sub>3</sub>, (II) BiFeO<sub>3</sub>, and (III) BiFeO<sub>3</sub> + Bi<sub>2</sub>O<sub>2.5</sub> as a function of substrate temperature and O<sub>2</sub> overpressure. Analogous phase stability diagrams have been calculated from thermodynamic data for the adsorption-controlled growth of III-V compounds,<sup>12–15</sup> MgB<sub>2</sub>,<sup>16</sup> PbTiO<sub>3</sub>,<sup>17</sup> and Bi<sub>4</sub>Ti<sub>3</sub>O<sub>12</sub>.<sup>12</sup> In the case of BiFeO<sub>3</sub>

and Bi<sub>2</sub>O<sub>2.5</sub>, the Gibbs energies of formation have not been reported. The boundaries between regions I, II, and III were calculated with the Gibbs energy functions of the gas phase containing various Bi and Bi–O species and the stable and metastable iron and bismuth oxides, all taken from the SGTE database.<sup>18</sup> We consider two scenarios for Bi<sub>2</sub>O<sub>2.5</sub> and BiFeO<sub>3</sub>. The enthalpy of formation of Bi<sub>2</sub>O<sub>2.5</sub> is assumed to be +100 or +4500 J/mol of Bi<sub>2</sub>O<sub>2.5</sub> with respect to the Bi–Bi<sub>2</sub>O<sub>3</sub> tie line. The enthalpy of formation of BiFeO<sub>3</sub> is assumed to be –1000 or –5000 J/mol with respect to the Bi<sub>2</sub>O<sub>3</sub>–Fe<sub>2</sub>O<sub>3</sub> tie line. The phase stability region was calculated using THERMOCALC (Ref. 19) with the partial pressure of bismuth fixed at  $6.7 \times 10^{-10}$  atm, which corresponds to the pressure at the plane of the substrate for an incident bismuth flux of  $1.4 \times 10^{14}$  Bi/cm<sup>2</sup> s.<sup>20</sup> The solid lines in Fig. 1 bound

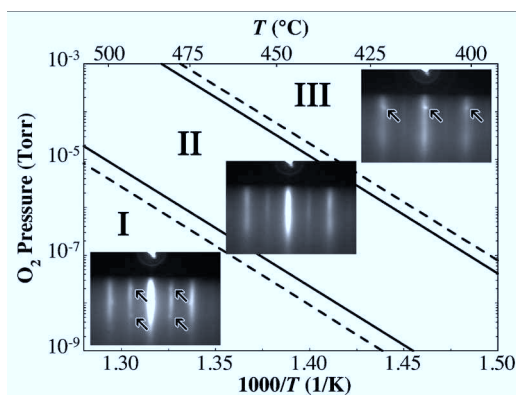


FIG. 1. Calculated Ellingham diagram and RHEED patterns collected along the  $\langle 110 \rangle$  azimuth of SrTiO<sub>3</sub> during Bi–Fe–O deposition at different temperatures and Bi<sub>x</sub>O<sub>y</sub> gas overpressures. Solid lines represent phase boundaries using +100 and –1000 J/mol formula unit free energies for Bi<sub>2</sub>O<sub>2.5</sub> and BiFeO<sub>3</sub>, respectively, specifying the narrowest growth window possible, and dashed lines for +4500 and –5000 J/mol formula unit, indicating the approximate uncertainty in width of the growth window. Phase stability between Bi<sub>x</sub>O<sub>y</sub> gases and BiFeO<sub>3</sub> +  $\gamma$ -Fe<sub>2</sub>O<sub>3</sub>, BiFeO<sub>3</sub>, and BiFeO<sub>3</sub> + Bi<sub>2</sub>O<sub>2.5</sub> condensed phases is represented by Regions I, II, and III, respectively.

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the BiFeO<sub>3</sub> region with formation enthalpies of +100 and −1000 J/mol for Bi<sub>2</sub>O<sub>2.5</sub> and BiFeO<sub>3</sub>, respectively, specifying the narrowest growth window possible, while the dashed lines represent the stability for +4500 and −5000 J/mol, indicating the approximate uncertainty in the growth window due to the lack of relevant free energy data.

The thermodynamic predictions were verified by investigating a horizontal slice through this diagram at constant bismuth (Bi flux =  $1.4 \times 10^{14}$  Bi/cm<sup>2</sup>s) and oxygen (O<sub>2</sub> + ~10% O<sub>3</sub> background pressure =  $1 \times 10^{-6}$  Torr) overpressure during the deposition of Bi–Fe–O over a temperature range of 375–475 °C and a fixed Bi:Fe flux ratio of 8:1. The *in situ* RHEED patterns collected along the ⟨110⟩ azimuthal direction of (001)-oriented SrTiO<sub>3</sub> delineating the three regions are superimposed in Fig. 1. Above 460 °C, RHEED streaks associated with BiFeO<sub>3</sub> and additional spots are observed. These spots can be indexed to diffraction from (111)-oriented γ-Fe<sub>2</sub>O<sub>3</sub>, the presence of which was verified by *ex situ* XRD. For these growth parameters, this temperature represents the boundary between regions I and II. Many authors have observed iron oxide inclusions in BiFeO<sub>3</sub> films grown by other techniques, e.g., α-Fe<sub>2</sub>O<sub>3</sub> by off-axis rf sputtering<sup>21</sup> and γ-Fe<sub>2</sub>O<sub>3</sub> by pulsed laser deposition at low oxygen pressures.<sup>22,23</sup> Between 415 and 460 °C, phase-pure films can be grown indicative of region II. At a temperature below 415 °C, additional spots form, which have been indexed by *ex situ* XRD as (001)- and (110)-oriented Bi<sub>2</sub>O<sub>2.5</sub>. The occurrence of these spots corresponds to the phase boundary separating regions II and III. A change of the bismuth flux or the oxygen activity results in a shift of the growth window for single-phase BiFeO<sub>3</sub>, as indicated by the Ellingham boundaries of the adsorption-controlled growth window in Fig. 1. The O<sub>2</sub> overpressures calculated compare well with what is expected given the enhanced activity of O<sub>3</sub> and our directed gas inlet that locally increases the oxygen pressure at the substrate surface.<sup>20</sup>

It has been reported that the single-phase field of BiFeO<sub>3</sub> grown by MBE is broad, with single-phase films as much as 8% Bi-deficient being grown.<sup>9</sup> Two films were grown at different points in region II to investigate the growth temperature dependence on composition. One sample was grown in the middle of region II and the second was grown near the phase boundary between regions II and III. For a Bi:Fe flux ratio of 7:1, substrate temperatures of 405 and 375 °C, respectively, corresponded to these points in the Ellingham diagram. The sample grown at ~375 °C had a stoichiometric composition within the 3% measurement accuracy of Rutherford backscattering spectroscopy and displayed a minimum channeling yield ( $\chi_{\min}$ ) of 11%. The film grown at 405 °C was Bi-deficient with a 0.95 (±0.03):1.00 Bi:Fe ratio and a  $\chi_{\min}$  of 16%. Our results indicate that stoichiometric single-phase BiFeO<sub>3</sub> films may be prepared at the Bi-rich end of region II, i.e., near the boundary with region III.

An XRD scan of the 30 nm thick BiFeO<sub>3</sub>/(001) SrTiO<sub>3</sub> stoichiometric sample is shown in Fig. 2(a). The film is phase-pure (10 $\bar{1}2$ )-oriented BiFeO<sub>3</sub> (hexagonal indices are used throughout this letter for BiFeO<sub>3</sub>). Figure 2(b) shows a high-resolution scan of the 10 $\bar{1}2$  peak exhibiting clear thickness fringes indicative of a smooth film with high crystalline quality. A  $\omega$  rocking curve from the same film is shown in Fig. 2(c). The full width at half maximum (FWHM) of the BiFeO<sub>3</sub> film, 29 arc sec (0.008°), is identical to that of the

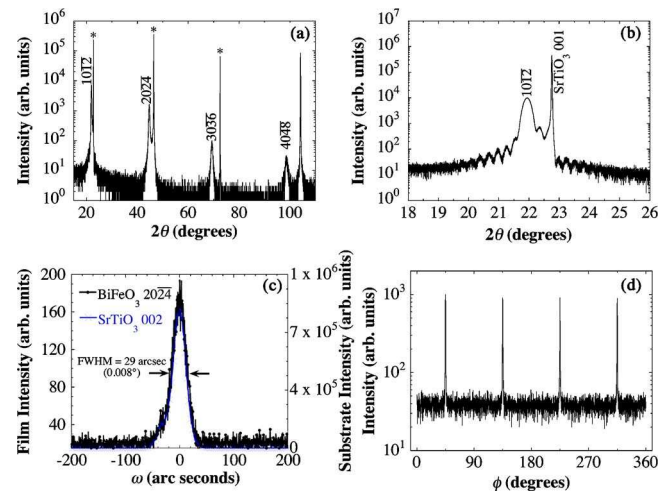


FIG. 2. (Color online) (a)  $\theta$ - $2\theta$  X-ray diffraction pattern of a 30 nm thick (10 $\bar{1}2$ )-oriented BiFeO<sub>3</sub> film grown on (001) SrTiO<sub>3</sub>. (b) Shows a close-up of the 10 $\bar{1}2$  peak and thickness fringes. (c) Superimposed  $\omega$ -rocking curves of the 20 $\bar{2}4$  film and 002 substrate peaks. (d) Azimuthal  $\phi$  scan of 11 $\bar{2}3$  ( $\chi=64.7^\circ$ ) diffraction peaks.  $\chi=90^\circ$  aligns the diffraction vector to be perpendicular to the plane of the substrate.  $\phi=0^\circ$  corresponds to the projection of the substrate [100] in-plane direction.

underlying substrate indicating that the film crystallinity is substrate limited and is comparable to the narrowest recorded for a BiFeO<sub>3</sub> film.<sup>9</sup> Figure 2(d) shows a  $\phi$  scan of the 11 $\bar{2}3$  family of peaks. Four separate peaks are seen, demonstrating that the film is epitaxial with rhombohedral or lower symmetry. Films of cubic or tetragonal symmetry would not exhibit diffraction at these peak positions.<sup>21</sup>

Cross-sectional transmission electron microscopy (TEM) specimens were imaged within a JEOL 3011 high-resolution TEM (HRTEM) that has 0.17 nm point-to-point resolution. Dark-field and HRTEM imaging (not shown) reveals 71° and 109° domain walls, as have been previously observed in films grown by other techniques on nonvicinal (001) SrTiO<sub>3</sub> substrates.<sup>24,25</sup> HRTEM verifies the 10 $\bar{1}2$  orientation and reveals an atomically abrupt interface.

As stoichiometry can play a strong role in material properties, we investigated the optical properties and band gaps for the two films grown in different locations within region II. Room temperature ellipsometric spectra (in  $\Delta$ ,  $\psi$ ) were collected *ex situ* at three angles of incidence,  $\Theta_i=55^\circ$ ,  $70^\circ$ , and  $85^\circ$ , using a variable-angle rotating-compensator multichannel spectroscopic ellipsometer<sup>26,27</sup> over a spectral range from 0.75 to 6.5 eV for the stoichiometric BiFeO<sub>3</sub> film and at  $\Theta_i=45^\circ$ ,  $60^\circ$ , and  $75^\circ$  over a spectral range from 0.75 to 5.0 eV for the Bi-deficient film. The dielectric function spectra ( $\epsilon_1$ ,  $\epsilon_2$ ) shown in Fig. 3 were extracted using a least squares regression analysis and a weighted root mean square function<sup>28</sup> to fit the experimental ellipsometric spectra to a four-medium optical model consisting of a semi-infinite SrTiO<sub>3</sub> substrate/bulk film/surface roughness/air ambient structure where free parameters correspond to the bulk and surface roughness thicknesses of the BiFeO<sub>3</sub> film and a parameterization of the BiFeO<sub>3</sub> dielectric function. The dielectric function parameterization of BiFeO<sub>3</sub> consists of four Tauc–Lorentz oscillators<sup>29</sup> sharing a common Tauc gap and a constant additive term to  $\epsilon_1$  represented by  $\epsilon_\infty$ . The optical properties of the surface roughness layer are represented by a Bruggeman

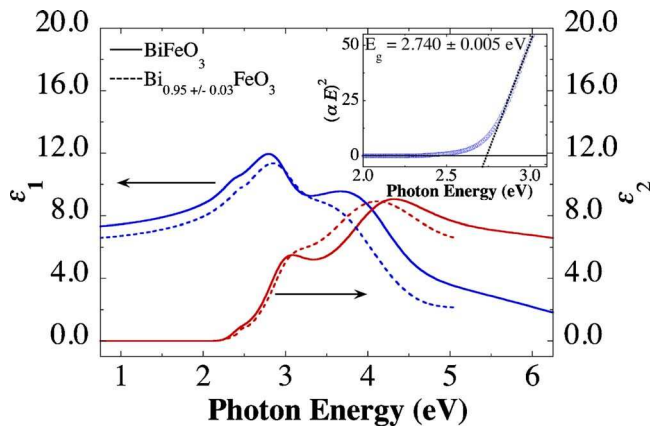


FIG. 3. (Color online) Dielectric function spectra obtained from spectroscopic ellipsometry analysis of stoichiometric (solid lines) and Bi-deficient (dashed lines) 30 nm thick  $\text{BiFeO}_3/(001)$   $\text{SrTiO}_3$  over a spectral range from 0.75 to 6.5 eV for the stoichiometric film and from 0.75 to 5.0 eV for the Bi-deficient film.

effective medium approximation<sup>30</sup> consisting of a 50% bulk film/50% void mixture. Although  $\text{BiFeO}_3$  is rhombohedral and exhibits uniaxial optical anisotropy, these thin films may be treated as isotropic due to their mixed domain structure (i.e., the four twin variants in these films distribute the optic axes along the four  $\langle 111 \rangle$  pseudocubic  $\text{BiFeO}_3$  directions within the macroscopic region sampled in the spectroscopic ellipsometry measurement). The experimental real and imaginary dielectric spectra are a combination of the ordinary and extraordinary dielectric functions but, due to the distribution in optical axis orientation, it is impossible to separate the respective contributions.

The onset of optical absorption is observed at  $2.07 \pm 0.14$  eV and  $2.11 \pm 0.06$  eV for the bismuth-deficient and stoichiometric  $\text{BiFeO}_3$  films, respectively. The direct band gap, obtained from a linear extrapolation of  $(\alpha E)^2$  (inset, Fig. 3 for the stoichiometric film) is invariant at 2.74 eV. Band gap measurements on five different MBE-grown  $\text{BiFeO}_3$  films on (001)  $\text{SrTiO}_3$ , (001)  $(\text{LaAlO}_3)_{0.3}(\text{SrAl}_{0.5}\text{Ta}_{0.5}\text{O}_3)_{0.7}$  (LSAT), and (111)  $\text{SrTiO}_3$  (Ref. 31) revealed a direct band gap in all cases with  $E_g = 2.77 \pm 0.04$  eV. The invariance of the band gap energy with films of differing strain states suggests that the band gap is relatively insensitive to these effects. This value is consistent with predictions.<sup>32</sup> Previous reports have suggested an indirect gap at lower energies in addition to the direct gap.<sup>5,6</sup> In our data, the lack of the characteristic shape of the  $(E\alpha)^{1/2}$  versus energy plot indicating the required phonon participation argues against an indirect gap.<sup>33</sup> It is prudent to consider the optical absorption onset as a joint density of states effect that is very small and likely insignificant in ac conductivity. While the two films studied exhibit stoichiometry differences, the dielectric function spectra show similar absorption onsets and direct band gaps. This is to be expected, as the identical crystal structure and, thus, bonding is present resulting in minute variations in the density of states and band gap. A shift in the resonance energies to lower energy is observed in the dielectric function for the nonstoichiometric film.

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