

Hydrogen interstitial defects in acceptor-type CuO-doped PbTiO₃—Uptake and dissolution of water vapor and formation of (CuTi^{'''}–(OH)O•)['] defect complexes

Peter Jakes, Hans Kungl, Roland Schierholz, Josef Granwehr, and Rüdiger-A. Eichel

Citation: *Applied Physics Letters* **109**, 122904 (2016); doi: 10.1063/1.4962816

View online: <http://dx.doi.org/10.1063/1.4962816>

View Table of Contents: <http://scitation.aip.org/content/aip/journal/apl/109/12?ver=pdfcov>

Published by the AIP Publishing

Articles you may be interested in

[Tuning the formation of p-type defects by peroxidation of CuAlO₂ films](#)

J. Appl. Phys. **114**, 033712 (2013); 10.1063/1.4816044

[Interactions of defect complexes and domain walls in CuO-doped ferroelectric \(K,Na\)NbO₃](#)

Appl. Phys. Lett. **102**, 242908 (2013); 10.1063/1.4811268

[Native p-type transparent conductive CuI via intrinsic defects](#)

J. Appl. Phys. **110**, 054907 (2011); 10.1063/1.3633220

[Modeling the polaronic nature of p-type defects in Cu₂O: The failure of GGA and GGA + U](#)

J. Chem. Phys. **131**, 124703 (2009); 10.1063/1.3231869

[Effects of the MnO additives on the properties of Pb \(Fe^{2/3} W^{1/3} \) – Pb Ti O₃ relaxors: Comparison of empirical law and experimental results](#)

J. Appl. Phys. **101**, 054117 (2007); 10.1063/1.2709876



NEW Special Topic Sections

NOW ONLINE
Lithium Niobate Properties and Applications:
Reviews of Emerging Trends

AIP | Applied Physics
Reviews

Hydrogen interstitial defects in acceptor-type CuO-doped PbTiO₃—Uptake and dissolution of water vapor and formation of $(\text{Cu}_{\text{Ti}}'' - (\text{OH})_{\text{O}}^{\bullet})'$ defect complexes

Peter Jakes,¹ Hans Kungl,¹ Roland Schierholz,¹ Josef Granwehr,^{1,2}
 and Rüdiger-A. Eichel^{1,3,a)}

¹Forschungszentrum Jülich, Institut für Energie- und Klimaforschung (IEK-9), D-52425 Jülich, Germany

²Institut für Technische und Makromolekulare Chemie, RWTH Aachen University, D-52074 Aachen, Germany

³Institut für Physikalische Chemie, RWTH Aachen University, D-52074 Aachen, Germany

(Received 2 June 2016; accepted 2 September 2016; published online 22 September 2016)

The defect structure of CuO-doped PbTiO₃ has been analyzed using the Hyperfine Sublevel Correlation Experiment to identify hydrogen interstitials. The formation of $(\text{Cu}_{\text{Ti}}'' - (\text{OH})_{\text{O}}^{\bullet})'$ defect complexes has been observed, which exist in addition to the $(\text{Cu}_{\text{Ti}}'' - V_{\text{O}}^{\bullet})^{\times}$ complexes. On this basis, modified reorientation characteristics are proposed due to a change in hopping mechanism from an oxygen-vacancy mediated migration mechanism to a proton hopping process. Furthermore, mobile hydrogen interstitials are generated that increase conductivity in terms of a “Grotthuss”-type charge-transport mechanism. Published by AIP Publishing.

[<http://dx.doi.org/10.1063/1.4962816>]

Ferroelectric devices based on lead zirconate titanate ($\text{Pb}[\text{Zr}_x\text{Ti}_{1-x}]\text{O}_3$, PZT) range from thin-film non-volatile memory applications (ferroelectric random-access memory) to “bulk” piezoelectric actuators or multilayer capacitors. Across the various fields of application, a primary issue is the incorporation of atomistic defects during processing that may lead to device degradation.^{1,2} Gaining insight into the defect structure is thus an essential step to develop strategies for improved materials and to prevent materials degradation.

Hydrogen-related defects represent a class of defects of particular interest. For PbTiO₃, the existence of interstitial hydrogen defects has been predicted based on “*ab-initio*” calculations.³ Their impact on device degradation is mainly two-fold: first, thin-film devices are typically subjected to a forming-gas anneal during fabrication in order to passivate the interface defects. This anneal injects hydrogen, leading to a loss of switchable polarization.^{4–6} Second, in devices fabricated from “bulk” piezoelectrics that are processed under ambient atmosphere, humidity can increase the leakage current, inducing an insulator–semiconductor transition.^{7–11}

To investigate the interplay between hydrogen-related defects and defects resulting from aliovalent acceptor doping, CuO-doped PbTiO₃ has been investigated. As a sensitive spectroscopic tool, electron paramagnetic resonance (EPR) has already been providing detailed information,^{12,13} in particular, on the defect structure at the first coordination sphere.^{14–18} By employing the pulsed hyperfine sublevel correlation experiment (HYSCORE), also magnetically active nuclei at more distant coordination spheres may be probed.^{19,20}

0.25 mol% CuO-doped PbTiO₃ powders were prepared by a standard mixed-oxide route,²⁰ where calcination was performed at 850 °C for 2 hours, starting from ambient atmosphere, i.e. humid conditions to a certain extent.

The X-band pulse EPR measurements were performed at 9.7 GHz on a Bruker ElexSys 680 spectrometer at a temperature of 10 K. The field-swept free induction decay (FID) induced EPR spectrum was obtained using highly selective microwave pulses of 500 ns duration. HYSCORE spectra were recorded using a standard four-pulse sequence $(\frac{\pi}{2} - \tau - \frac{\pi}{2} - t_1 - \pi - t_2 - \frac{\pi}{2} - \tau - \text{echo})$ and an eight-step phase cycle.²¹ Pulse lengths of $t_{\pi/2} = t_{\pi} = 16$ ns and a delay time of $\tau = 240$ ns were employed.

The theoretical description of EPR and HYSCORE spectra for an unpaired $3d^9$ electronic configuration with spin $S = \frac{1}{2}$, as representative for Cu^{2+} , interacting with a nuclear spin $I = \frac{1}{2}$ such as ^1H , is based on the spin Hamiltonian

$$\mathcal{H} = \beta_e \mathbf{B}_0 \cdot \mathbf{g} \cdot \mathbf{S} - \beta_n g_n \mathbf{B}_0 \cdot \mathbf{I} + h \mathbf{S} \cdot \mathbf{A} \cdot \mathbf{I}, \quad (1)$$

where g_n is the nuclear g -factor, and β_e , β_n are the Bohr and nuclear magneton, respectively, and h is Planck’s constant. The first and second term are the electronic and nuclear Zeeman interaction, respectively, where \mathbf{B}_0 denotes the

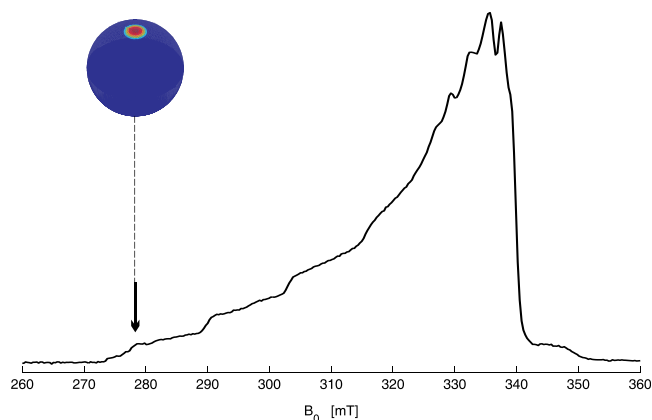


FIG. 1. FID-detected X-band EPR spectrum of 0.25 mol% CuO-doped PbTiO₃ recorded at 10 K.¹⁹ The orientation-selective observer position for ^1H -HYSCORE is indicated by an arrow.

^{a)} Author to whom correspondence should be addressed. Electronic mail: r.eichel@fz-juelich.de

external magnetic field. The last term corresponds to the hyperfine interaction with a nearby magnetic nucleus. The hyperfine tensor \mathbf{A} as well as the external field \mathbf{B}_0 are given in the principal axes system of the \mathbf{g} -matrix of the electron spin. The copper nuclear quadrupole interaction was not resolved in the EPR spectra (cf. Figure 1) and thus has been neglected.

The hyperfine interaction \mathbf{A} can generally be expressed as $\mathbf{A} = a_{\text{iso}} + \mathbf{A}'$, where a_{iso} is the isotropic hyperfine coupling constant, and the tensor \mathbf{A}' describes the anisotropic dipole-dipole interactions between the electron spin S and the nuclear spin I . Because the second-rank tensor \mathbf{A}' is traceless and symmetric, there is always a coordinate system in which \mathbf{A}' is diagonal with the elements A'_\perp and $A'_\parallel = -2A'_\perp$ where, by convention, A'_\parallel is taken to be the principal value with the largest magnitude.

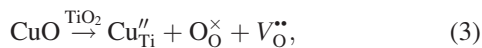
To transform the spin Hamiltonian parameters into structural information, a point-dipole approximation can be assumed with the dipolar hyperfine coupling constant

$$A'_\perp = \frac{\mu_0 g g_n \beta_e \beta_n}{4\pi r^3 h}. \quad (2)$$

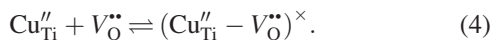
This equation provides an estimate for the distance r between the paramagnetic Cu^{2+} center and the coupling ^1H nucleus.

By using EPR, oxidation state and site of incorporation of the copper functional center can be obtained. The corresponding FID-induced EPR spectrum is displayed in Figure 1. The axially symmetric g -matrix with diagonal elements $g_\parallel = 2.332 > g_\perp = 2.049 > g_e = 2.0023$ and ^{63}Cu -A-hyperfine tensor with diagonal elements $^{63}\text{Cu}A'_\parallel = 395 \text{ MHz}$ and $^{63}\text{Cu}A'_\perp = 20 \text{ MHz}$ is characteristic for Cu^{2+} -centers in octahedral coordination, distorted along one of the pseudocubic axes.^{22–24} This assignment is in line with recent *ab-initio* calculations.¹⁹

Accordingly, the incorporation reaction of CuO , replacing TiO_2 , is

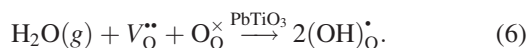


where, for charge compensation, each Cu_{Ti}'' is compensated by an oxygen vacancy ($V_{\text{O}}^{\bullet\bullet}$) as nearest neighbor, forming a charge neutral $(\text{Cu}_{\text{Ti}}'' - V_{\text{O}}^{\bullet\bullet})^\times$ defect complex^{19,25}



Defects that may result from a trapping of conduction electrons, such as singly charged V_{O}^{\bullet} ²⁷ or reduced Ti_{Ti}' -centers,²⁸ were not observed.

Considering now the dissolution of hydrogen from either forming-gas atmosphere or from humid conditions into the PbTiO_3 lattice, the following dissolution reactions take place:



Because in oxidic environments protons cannot substitute other cations and, furthermore, hydrogen interstitials (H_i^\bullet) are always bonded to oxide ions, they will form hydroxide $(\text{OH})_{\text{O}}^\bullet$ -complexes. The $[\text{OH}]^-$ defects in turn are proposed

acting as a fixed charged dipole that may pin ferroelectric domain walls.³⁰

The existence of hydroxide $(\text{OH})_{\text{O}}^\bullet$ -complexes in perovskite oxides is experimentally supported by findings from barium titanate, where hydrogen atoms act as donor centers,³¹ and where the hydrogen interstitial then combines with an O^{2-} ion and forms a hydroxide-ion $(\text{OH})_{\text{O}}^\bullet$, whose existence has been proved by its Raman signature.^{32,33} Electronically, interstitial hydrogen in PbTiO_3 was proposed to act as a shallow donor impurity.³ Note that as a fundamental difference in the dissolution reactions under forming gas and water vapor conditions, for the latter case the existence of oxygen vacancies describes a necessary prerequisite for the uptake and dissolution of water into the perovskite lattice.

For steric reasons, $(\text{OH})_{\text{O}}^\bullet$ -defects are expected to be located more likely close to Cu_{Ti}'' rather than $\text{Ti}_{\text{Ti}}^\times$ -sites. To probe $(\text{OH})_{\text{O}}^\bullet$ -defects in coordination spheres of the paramagnetic Cu_{Ti}'' -site, orientation-selective HYSORE has been performed. The ^1H -HYSORE spectrum, taken on an observer position of 278.5 mT that coincides with the g_\parallel orientation, is depicted in Figure 2. Assuming the \mathbf{g} -matrix main axes being determined by the tetragonal PbTiO_3 crystal distortion, the g_\parallel -orientation is assumed to be collinear with the orientation of spontaneous polarization, $P_S \parallel g_\parallel$.¹⁷

The spectrum is dominated by a correlation that appears as off-diagonal cross-peak ridges shifted by $\Delta\nu_s = 2.19(5) \text{ MHz}$ with respect to the proton nuclear Larmor frequency (ν_{H}), thus showing that the coordinated nuclear spin belongs to a ^1H -nucleus. To determine the distance between Cu_{Ti}'' and H_i^\bullet , the value for A'_\perp is estimated from the frequency shift $\Delta\nu_s$ as $|A'_\perp| = \frac{4}{3}(2^{\frac{1}{2}}\nu_{\text{H}}\Delta\nu_s)^{\frac{1}{2}} = 8.08(9) \text{ MHz}$.²⁶ Adopting the point-dipole approximation (2), the distance between the Cu^{2+} -ion

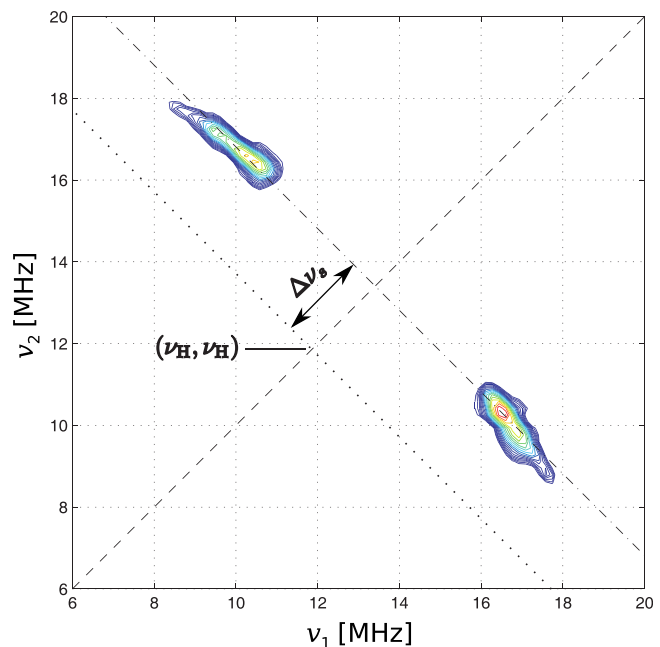
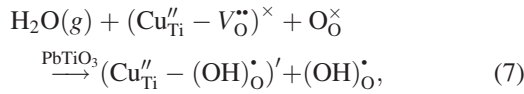


FIG. 2. X-band ^1H -HYSORE spectrum (high-frequency part of (+, +) quadrant) recorded at 10 K and an observer position of 278.5 mT. The dashed lines show the frequency diagonal axis $\nu_1 = \nu_2$; the anti-diagonal (dotted line) crosses the diagonal at $(\nu_{\text{H}}, \nu_{\text{H}})$. The maximum vertical shift $\Delta\nu_s = 2.2 \text{ MHz}$ of the cross-peak ridges from the anti-diagonal is illustrated by a dashed-dotted line.

and the ^1H -nucleus is estimated to be 225(2) pm. On the basis of this distance, the above made assumption that the hydroxide defect should form a defect complex with the Cu_{Ti}'' -functional center could be validated. The observed coupling is assigned to a ^1H nucleus in the first coordination sphere. From the position and shape of the cross-peak ridges, which are approaching the maximum distance from the antidiagonal through point $(\nu_{\text{H}}, \nu_{\text{H}})$, it can be inferred that the dipolar interaction is tilted from the direction of spontaneous polarization by approximately $\theta = 30(5)^\circ$. Based on the distance between Cu and O of approximately 223 pm,¹⁹ and the length of a bond between O and H in a hydroxide defect of about 98 pm,^{3,29} this suggests that the O–H bond is approximately perpendicular to the direction of P_{S} .

Based on this assignment, the hydrogen dissolution reaction (6) under humid conditions of the “pure” perovskite can be modified for CuO-doped PbTiO_3 according to



where the oxygen vacancy of the $(\text{Cu}_{\text{Ti}}'' - V_{\text{O}}'')^\times$ -defect complex is annihilated and replaced by a hydroxide defect, and the two defects formed mutually compensate according to the following charge-neutrality condition:

$$[(\text{Cu}_{\text{Ti}}'' - (\text{OH})_{\text{O}}^\bullet)'] \approx [(\text{OH})_{\text{O}}^\bullet]. \quad (8)$$

Furthermore, the obtained results are in favor of only one well defined site for the hydrogen interstitial adjacent to the Cu^{2+} , because only one set of proton correlation peaks was observed in the ^1H -HYSCORE spectrum (cf. Figure 2). If H_i^\bullet -sites would exist at remote coordination spheres, i.e., neighboring unit cells, additional (weaker) proton hyperfine couplings should exist in the spectrum. The absence of such additional features rules out the existence of additional $(\text{OH})_{\text{O}}^\bullet$ -defects in the vicinity of the Cu_{Ti}'' -functional center. Accordingly, we propose a defect-structural arrangement as schematically illustrated in Figure 3, with the $(\text{Cu}_{\text{Ti}}'' - (\text{OH})_{\text{O}}^\bullet)'$ defect complex oriented along the direction of spontaneous polarization.

Considering the reorientation of the $(\text{Cu}_{\text{Ti}}'' - V_{\text{O}}'')^\times$ defect complex under a sufficiently strong applied external field, an oxygen vacancy has to exchange its position with

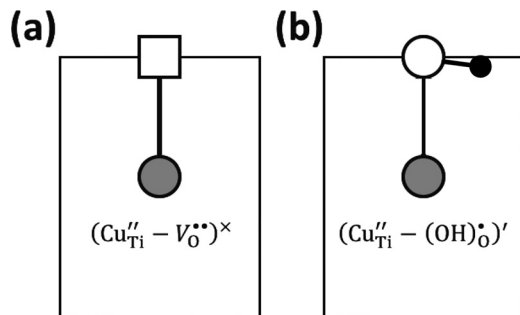


FIG. 3. Schematic illustration of defect structure in CuO-doped PbTiO_3 with $(\text{Cu}_{\text{Ti}}'' - V_{\text{O}}'')^\times$ (a) and $(\text{Cu}_{\text{Ti}}'' - (\text{OH})_{\text{O}}^\bullet)'$ (b) defect complexes. The tetragonal unit cell is represented by a bold square, the Cu_{Ti}'' -center as a gray circle, the oxygen vacancy V_{O}'' as an open square, an oxygen ion $\text{O}_{\text{O}}^\times$ as an open circle and the hydrogen interstitial H_i^\bullet as a bold circle.

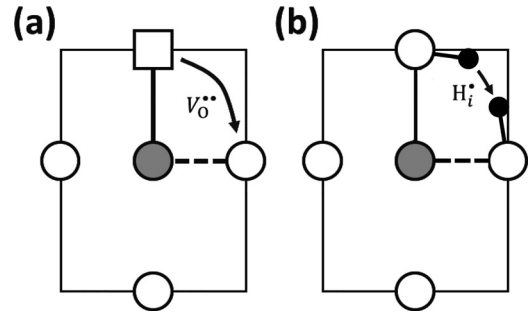
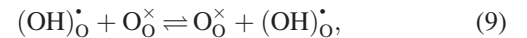


FIG. 4. Schematic illustration of defect-complex reorientation in CuO-doped PbTiO_3 . (a) Hopping mechanism of an oxygen vacancy (V_{O}'') for the reorientation of the $(\text{Cu}_{\text{Ti}}'' - V_{\text{O}}'')^\times$ defect complex. (b) Hopping mechanism of a hydrogen interstitial (H_i^\bullet) for the reorientation of the $(\text{Cu}_{\text{Ti}}'' - (\text{OH})_{\text{O}}^\bullet)'$ defect complex.

a lattice oxygen in the first coordination sphere about the Cu_{Ti}'' -functional center,^{13,36–38} as schematically illustrated in Figure 4(a). In contrast, reorientation of the $(\text{Cu}_{\text{Ti}}'' - (\text{OH})_{\text{O}}^\bullet)'$ defect complex involves a H_i^\bullet -hopping process from one oxygen site to another oxygen site (cf. Figure 4(b)). The former process involves a hopping of a double charged oxygen ion as compared to the hopping of a singly charged proton for the latter case. Additionally, since $r_{\text{O}^{2-}} \gg r_{\text{H}^+}$, the energy needed for the reorientation process will be considerably lower for the $(\text{Cu}_{\text{Ti}}'' - (\text{OH})_{\text{O}}^\bullet)'$ as compared to the $(\text{Cu}_{\text{Ti}}'' - V_{\text{O}}'')^\times$ defect complex.

The fundamental change in reorientation mechanism, from oxygen-vacancy migration to hydrogen-interstitial hopping, implies a variation of the rate at which defect complexes reorient. The diffusion coefficient of oxygen at ambient temperature is comparatively small (in BaTiO_3 at room temperature $D_{\text{O}} = 1.1 \times 10^{-15} \text{ cm}^2/\text{s}$), whereas hydrogen diffusion is 10^3 times as large.⁷ Correspondingly, the variation from V_{O}'' -migration to H_i^\bullet -hopping comes along with a markedly reduced activation energy barrier for defect complex reorientation. Tentatively, a reduction in materials “hardening” can be expected from the anticipated variation in defect complex reorientation.

Exploiting the charge neutrality condition (8), in addition to the hydroxide defect forming $(\text{Cu}_{\text{Ti}}'' - (\text{OH})_{\text{O}}^\bullet)'$ defect complexes, also hydroxide defects in remote areas to $(\text{Cu}_{\text{Ti}}'' - V_{\text{O}}'')^\times$ defect complexes will be present. These contribute to the electrical conductivity by means of an ionic charge-transport mechanism



where the bond of the hydrogen to one lattice oxygen ion is broken and subsequently forming a new bond to a nearest-neighbor lattice oxygen. This so-called “Grotthuss-mechanism” effectively promotes migration of protons in an external field. Although a major pathway of the H_i^\bullet -diffusion is typically expected along grain boundaries,⁸ the results obtained here demonstrate that hydrogen interstitials also diffuse into the grain core, forming defect complexes.

The impact of local mobility of the protons on the mobility of the dipoles has been discussed in context with Figures 3 and 4. The lower energy required for the hopping of the protons compared to a hopping of the oxygen vacancies favors

switching of domains, because non-reorienting dipoles provide no longer an obstacle to domain reorientation. Thus, the proton hopping will result in an enhanced performance with respect to polarization and strain under applied electric fields. However, the overall effects of the presence of protons in the material require a consideration of the long distance mobility as well. A consequence of long range mobility of charge carriers is conductivity. In materials for devices such as capacitors or actuators that should ideally be insulators, conductivity is a loss mechanism which decreases the performance. Moreover, diffusion of charged carriers, such as the protons, over distances of several hundreds of nanometers to domain- or grain boundaries may result in internal bias fields by formation of space charges,^{2,39–41} which provide mechanisms for the charge compensation that counteract polarization reversal and induce aging. The presence of protons thus may enhance mobility of domains via reducing the energy required for switching of the dipoles, but most likely will promote pinning effects via the space charge mechanisms.

In summary, the theoretically predicted existence of hydrogen interstitials³ has been experimentally proved. In particular, the impact of hydrogen interstitials on the defect structure of CuO-doped PbTiO₃ has been characterized. The main experimental observation consists in the formation of $(\text{Cu}_{\text{Ti}}'' - (\text{OH})_{\text{O}}^{\bullet})'$ defect complexes that exist in addition to the $(\text{Cu}_{\text{Ti}}'' - V_{\text{O}}^{\bullet})^{\times}$ complexes. Compared to $(\text{Cu}_{\text{Ti}}'' - V_{\text{O}}^{\bullet})^{\times}$ complexes, modified reorientation characteristics are proposed due to a change in hopping mechanism from an oxygen-vacancy mediated migration mechanism to a proton hopping process. Second, exploiting the charge-neutrality condition (8), only half of the hydrogen interstitials form $(\text{Cu}_{\text{Ti}}'' - (\text{OH})_{\text{O}}^{\bullet})'$ defect complexes, and the remaining part generates mobile hydrogen interstitials according to a “Grotthuss”-type charge-transport mechanism that impacts the conductivity of the material and could explain the observed transition from a ferroelectric *insulating*, to a *semi-conducting* compound.

Tentatively, both mechanisms are expected to affect the ferroelectric properties. These properties are usually discussed in terms of interactions with domain walls.^{34–36} Corresponding interpretations have been suggested and a significant impact can be expected, which should be investigated in more detail.

¹R.-A. Eichel, H. Kungl, and P. Jakes, *Mater. Technol.* **28**, 241–246 (2013).

²Y. A. Genenko, J. Glaum, M. J. Hoffmann, and K. Albe, *Mater. Sci. Eng.* **192**, 52–82 (2015).

³C. H. Park and D. J. Chadi, *Phys. Rev. Lett.* **84**, 4717 (2000).

⁴Y. Shimamoto, K. Kushida-Abdelghafar, H. Miki, and Y. Fujisaki, *Appl. Phys. Lett.* **70**, 3096 (1997).

⁵J. P. Han and T. P. Ma, *Appl. Phys. Lett.* **71**, 1267 (1997).

⁶H. J. Joo, S. H. Lee, J. P. Kim, M. K. Ryu, and M. S. Jang, *Ferroelectrics* **272**, 149–154 (2002).

⁷H. Y. Huang, W. Y. Chu, Y. T. Su, K. W. Gao, J. X. Li, and L. J. Qiao, *J. Am. Ceram. Soc.* **90**, 2062–2066 (2007).

⁸N. J. Donnelly and C. A. Randall, *J. Am. Ceram. Soc.* **92**, 405–410 (2009).

⁹I. P. Lipscombe, P. M. Weaver, J. Swingle, and J. W. McBride, *Sens. Actuators, A* **151**, 179–186 (2009).

¹⁰M. Wu, H. Y. Huang, W. Y. Chu, L. Q. Guo, L. J. Qiao, J. Y. Xu, and T. Y. Zhang, *J. Phys. Chem. C* **114**, 9955–9960 (2010).

¹¹F. Chen, W. P. Chen, Y. Wang, Y. M. Hu, Z. J. Shen, and H. L. W. Chan, *Physica B* **406**, 683–686 (2011).

¹²R.-A. Eichel, *Phys. Chem. Chem. Phys.* **13**, 368–384 (2011).

¹³P. Jakes, H. Kungl, R. Schierholz, and R.-A. Eichel, *IEEE Trans. Ultrason. Ferroelectr. Freq. Control* **61**, 1447–1455 (2014).

¹⁴E. Erüenal, P. Jakes, S. Körbel, J. Acker, H. Kungl, C. Elsässer, M. J. Hoffmann, and R.-A. Eichel, *Phys. Rev. B* **84**, 184113 (2011).

¹⁵E. Erdem, P. Jakes, S. K. S. Parashar, K. Kiraz, M. Somer, A. Rüdiger, and R.-A. Eichel, *J. Phys.: Condens. Matter* **22**, 345901 (2010).

¹⁶E. Erüenal, R.-A. Eichel, S. Körbel, C. Elsässer, J. Acker, H. Kungl, and M. J. Hoffmann, *Funct. Mater. Lett.* **3**, 19–24 (2010).

¹⁷R.-A. Eichel, H. Mestric, K. P. Dinse, A. Ozarowski, J. van Tol, L. C. Brunel, H. Kungl, and M. J. Hoffmann, *Magn. Reson. Chem.* **43**, S166–S173 (2005).

¹⁸R.-A. Eichel, K.-P. Dinse, H. Kungl, M. J. Hoffmann, A. Ozarowski, J. van Tol, and L. C. Brunel, *Appl. Phys. A* **80**, 51–54 (2005).

¹⁹R.-A. Eichel, P. Erhart, P. Träskelin, K. Albe, H. Kungl, and M. J. Hoffmann, *Phys. Rev. Lett.* **100**, 095504 (2008).

²⁰R.-A. Eichel, H. Kungl, and M. J. Hoffmann, *J. Appl. Phys.* **95**, 8092–8096 (2004).

²¹C. Gemperle, G. Aebli, A. Schweiger, and R. R. Ernst, *J. Magn. Reson.* **88**, 241 (1990).

²²W. L. Warren, B. A. Tuttle, F. C. Rong, G. J. Gerardi, and E. H. Poindexter, *J. Am. Ceram. Soc.* **80**, 680 (1997).

²³H. T. Langhammer, T. Müller, R. Böttcher, and H.-P. Abicht, *Solid State Sci.* **5**, 965 (2003).

²⁴R.-A. Eichel, E. Erüenal, M. D. Drahush, D. M. Smyth, J. van Tol, J. Acker, H. Kungl, and M. J. Hoffmann, *Phys. Chem. Chem. Phys.* **11**, 8698–8705 (2009).

²⁵R.-A. Eichel, M. D. Drahush, P. Jakes, E. Erüenal, E. Erdem, S. K. S. Parashar, H. Kungl, and M. J. Hoffmann, *Mol. Phys.* **107**, 1981–1986 (2009).

²⁶A. Pöpl and L. Kevan, *J. Phys. Chem.* **100**, 3387 (1996).

²⁷R.-A. Eichel, E. Erdem, P. Jakes, A. Ozarowski, J. van Tol, R. Hoffmann, and J. J. Schneider, *Funct. Mater. Lett.* **6**, 1330004 (2013).

²⁸E. Erdem, P. Jakes, R.-A. Eichel, D. C. Sinclair, M. Pasha, and I. M. Reaney, *Funct. Mater. Lett.* **3**, 65–68 (2010).

²⁹K. Xiong and J. Robertson, *Appl. Phys. Lett.* **85**, 2577–2579 (2004).

³⁰D. Dimos, W. L. Warren, M. B. Sinclair, B. A. Tuttle, and R. W. Schwartz, *J. Appl. Phys.* **76**, 4305 (1994).

³¹R. Waser, *J. Am. Ceram. Soc.* **71**, 58 (1988).

³²S. Kapphan and G. Weber, *Ferroelectrics* **37**, 673–676 (1981).

³³S. Aggarwal, S. R. Perusse, C. W. Tipton, R. Ramesh, H. D. Drew, T. Venkatesan, D. B. Romero, V. B. Podoedov, and A. Weber, *Appl. Phys. Lett.* **73**, 1973–1975 (1998).

³⁴P. V. Lambeck and G. H. Jonker, *J. Phys. Chem. Solids* **47**, 453 (1986).

³⁵H. Neumann and G. Arlt, *Ferroelectrics* **76**, 303 (1987).

³⁶R.-A. Eichel, E. Erüenal, P. Jakes, S. Körbel, C. Elsässer, H. Kungl, J. Acker, and M. J. Hoffmann, *Appl. Phys. Lett.* **102**, 242908 (2013).

³⁷W. L. Warren, K. Vanheusden, D. Dimos, G. E. Pike, and B. A. Tuttle, *J. Am. Ceram. Soc.* **79**, 536 (1996).

³⁸L. X. Zhang, E. Erdem, X. Ren, and R.-A. Eichel, *Appl. Phys. Lett.* **93**, 202901 (2008).

³⁹G. Arlt and H. Neumann, *Ferroelectrics* **87**, 109–120 (1988).

⁴⁰K. Carl and K. H. Härdtl, *Ferroelectrics* **17**, 473–486 (1978).

⁴¹Y. A. Genenko, *Phys. Rev. B* **78**, 214103 (2008).