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# Realization of electron vortices with large orbital angular momentum using miniature holograms fabricated by electron beam lithography

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Free electron beams that carry high values of orbital angular momentum (OAM) possess large magnetic moments along the propagation direction. This makes them an ideal probe for measuring the electronic and magnetic properties of materials, as well as for fundamental experiments in magnetism. However, their generation requires the use of complex diffractive elements, which usually take the form of nano-fabricated holograms. Here, we show how the limitations of the current fabrication of such holograms can be overcome by using electron beam lithography. We demonstrate experimentally the realization of an electron vortex beam with the largest OAM value that has yet been reported to the first diffraction order ( $L = 1000\hbar$ ), paving the way for even more demanding demonstrations and applications of electron beam shaping. *Published by AIP Publishing.*

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Similar to its optical counterpart,<sup>1</sup> an electron vortex beam (EVB) possesses one or more phase singularities at the center of its helical wavefront and is an eigenstate of the component of orbital angular momentum (OAM) along its propagation direction with eigenvalue  $\ell\hbar$  (where  $\ell$  is an integer and  $\hbar$  is the reduced Planck constant).<sup>2–5</sup> As an electron is a charged particle, an EVB has a magnetic moment of  $\ell\mu_B$ , where  $\mu_B$  is the Bohr magneton. Both its magnetic moment and its angular momentum allow for coupling to materials and for intriguing applications, including magnetic and shape dichroism measurements,<sup>6–9</sup> chiral crystal structure characterization,<sup>10</sup> nanoparticle manipulation,<sup>11</sup> and electron spin polarization.<sup>12</sup> EVBs are also of fundamental interest as they are characterized by a discrete quantum number that can form the basis of quantum experiments.<sup>13</sup> For values of  $\ell$  of a few units, the resulting magnetic effects are of the same order of magnitude as spin effects. However, the magnetic moment increases linearly with  $\ell$  and can in principle be orders of magnitude larger, since there is no fundamental upper bound for  $\ell$ .

The realization of high OAM values is of great importance for the amplification of subtle physical effects. For example, a magnetic component of transition radiation has been predicted for large OAM beams.<sup>14</sup> They have also been proposed for the measurement of out-of-plane magnetic fields in nanostructures using transmission electron microscopy (TEM) through the Larmor/Zeeman interaction.<sup>15,16</sup>

Moreover, large EVBs are interesting quantum objects in their own right. Whereas the TEM electron wavelength is typically on the order of 2 pm, a single highly twisted wavefront winds up with a step length of up to a few nanometers.

Finally, EVBs can be coupled to Landau states in the magnetic lens of a TEM (a longitudinal magnetic field). Landau states possess a functional similarity to the class of EVBs that are termed Laguerre-Gaussian beams and are characterized by a spiraling phase corresponding to  $L = \ell\hbar$  with a radial index  $p$ .<sup>13,17,18</sup> The transverse energies of such states can be written as  $\varepsilon = \hbar\Omega(2p + \ell + |\ell| + 1)$ , where  $\Omega = eB/2m$  is the Larmor frequency,  $B$  is the magnetic field, and  $m$  and  $e$  are the electron mass and charge, respectively. Neglecting for the moment the large spread over the  $p$  degree of freedom of most electron beams (e.g., in Ref. 19 we have shown an extreme case of dispersion in  $p$  decomposition), for a typical magnetic field  $B$  of 2 T inside an electron microscope the discrete transverse energy of an excited state corresponding to a few  $1000\hbar$  can be as high as 0.5–1 eV and can therefore potentially be coupled to infrared/visible light.

Unfortunately, the experimental realization of large OAM EVBs has been hindered technically by the approaches to nano-fabrication that have been used. Since EVBs were predicted theoretically,<sup>2</sup> several different methods have been used to generate them, involving the use of spiral phase plates,<sup>3,20–22</sup> pitch-fork holograms,<sup>4,5,19,23,24</sup> spiral zone plates,<sup>25,26</sup> Hilbert phase plates coupled to quadrupole lenses,<sup>27</sup> multipole lenses in aberration correctors,<sup>28</sup> and both magnetic<sup>29,30</sup> and electrostatic<sup>31</sup> phase plates. From these options, off-axis phase holograms<sup>5,19,23,24,32</sup> are still the method of choice. In such

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holograms, phase changes are introduced in proportion to their local thickness. EVBs have been reported with values for  $\ell$  of 100–200  $\hbar$  in high diffraction orders<sup>5</sup> and a first-order value for  $\ell$  of 200  $\hbar$  with higher efficiency.<sup>19</sup> In a very recent paper, one of the authors (V. Grillo), together with a group from the University of Oregon, demonstrated a superimposed set of vortices reaching up to  $L = 4000 \hbar$  in the 5th order.<sup>33</sup> This beam is potentially useful in coupling with Landau states to reach 1 eV energy but not in magnetic experiments where well-separated EVBs are necessary.<sup>15,16</sup>

Such phase holograms can be fabricated with different groove profiles to produce different intensity distributions in their diffraction orders.<sup>23</sup> For example, a blazed triangular profile can potentially be used to convey all of the transmitted intensity into a single diffracted beam.<sup>23,34</sup> Other less challenging and more popular groove profiles take sinusoidal and rectangular forms. For a perfectly tuned thickness, a rectangular shape is superior to a sinusoidal shape, as it inhibits all even diffraction orders, including the 0th order.

The limited resolution of focused ion beam (FIB) milling, which has been used to fabricate the holograms in these examples, prevents the realization of higher OAM beams since the primary grating periodicity  $P$  must be decreased to achieve an increasing OAM in order to avoid the superposition of electron vortices of different diffraction orders. For definiteness, a top-hat cutoff of the hologram generates an EVB with size  $r_K \approx \ell/R$ , where  $R$  is the radius of the cutoff in the hologram. The first diffraction order is centered at the main frequency  $1/P$  of the hologram. Therefore, the first order is only well sampled if  $P \ll \frac{R}{2\ell}$ . Since  $R$  is typically limited to  $\sim 100 \mu\text{m}$ , high spatial resolution is needed in the fabrication of large vortices. Limited resolution can also mean that an intended rectangular groove profile can end up being nearly sinusoidal. Moreover, it is demanding to maintain the same groove profile and a uniform response over both high and low spatial frequencies. Additional problems include the total patterning time and the total number of addressable pixels.

Here, we overcome these limitations by using electron beam lithography (EBL) to achieve a vortex with a topological charge as high as 1000  $\hbar$ . EBL is a technique that is used widely to produce patterns based on the selective electron irradiation of an electron sensitive material. We use a Zeiss  $\Sigma$  scanning electron microscope equipped with a Schottky field emitter and a Raith Elphy Quantum pattern generator.

In order to optimize the spatial resolution of EBL patterning, we tested both positive and negative resists. We used square 50-nm-thick SiN membranes, on which the electron-transparent region had a width of 80  $\mu\text{m}$ . The membranes were covered with evaporated Au (typically 200 nm thick), which was removed only in the hologram region. The procedure required 2 steps of lithography. A first step was used to create an electron transparent aperture in the Au mask in the active region of the hologram. A second step involved patterning the holograms with appropriate phase modulations. The pattern thickness was defined according to the formula (see [supplementary material](#))

$$t = \frac{1}{2} t_0 (1 + \text{sign}(\sin(\ell\theta + \rho k_{\text{carrier}} \cos(\theta)))) \quad (1)$$

where  $\rho, \theta$  are polar co-ordinates in the hologram plane,  $k_{\text{carrier}} = 2\pi/P$  is the carrier frequency in the off-axis hologram, and  $\text{sign}[\cdot]$  is the sign function, which is  $\pm 1$  for positive and negative arguments, respectively. The thickness  $t_0$  was chosen to provide a phase difference close to  $\pi$ . The rectangular groove shape defined by Eq. (1) conveniently allowed the use of EBL to produce holograms with 2 discrete thickness levels.

To first order, the separation  $d$  between two hologram lines is related to the argument of the sin function, i.e.,  $f = \ell\theta + \rho k_{\text{carrier}} \cos(\theta)$ , through the expression to the first order  $\frac{1}{d} \approx \frac{|\nabla_{\rho,\theta}(f)|}{\pi} + \dots$ . When the function  $f$  is stationary (i.e., when  $\nabla_{\rho,\theta}(f) = 0$ ), the separation between the lines increases. This condition is realized when  $\rho = \ell/k_{\text{carrier}}$ ,  $\theta = \frac{\pi}{2}$ . A detailed analysis shows that the  $f$ -stationary point is a saddle point for  $f$ . Such a saddle point is present in our previous work for  $\ell = 200$ , taking the form of a cross close to the center of the hologram.<sup>19</sup> The lines in the hologram have a much higher frequency in the center and opposite the  $f$ -stationary point. As in our previous paper, we decided here to exclude the central region of the hologram from patterning.<sup>5,19</sup> For all patterning, a bitmap image was created using the STEM\_CELL software<sup>35</sup> and converted to a data format that was readable using the EBL pattern generator.

We made a first series of holograms by using poly-methyl methacrylate (PMMA) for patterning and reactive ion etching (RIE) to transfer the pattern onto the SiN membrane (see [supplementary material](#)). This process was not able to provide a high enough carrier frequency. In contrast, Figure 1 shows the process that gave the best results in terms of resolution. In this case, we used hydrogen silsesquioxane (HSQ), which transformed into a silica-like structure after baking on a hot plate.

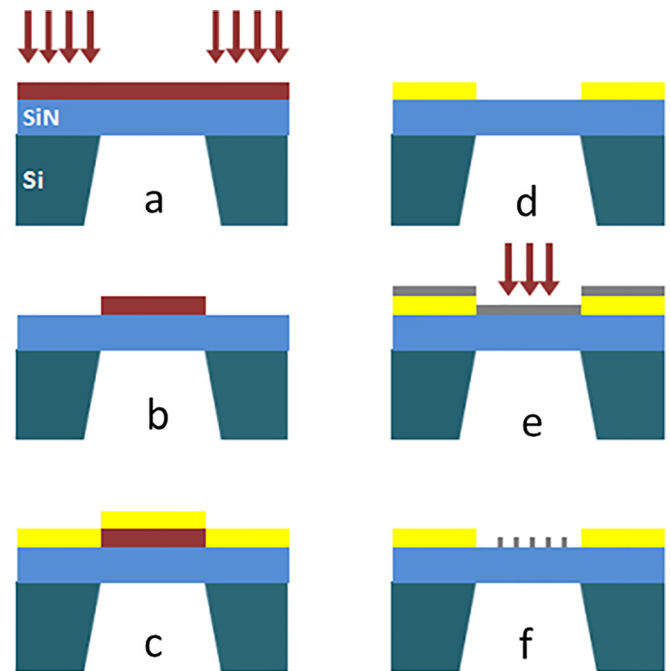


FIG. 1. Schematic diagrams showing (1) spin coating of PMMA and EBL; (2) developing the resist; (3) Au evaporation; (4) lift-off; (5) hydrogen silsesquioxane (HSQ) spin coating and EBL; and (6) developing the HSQ.

The EBL was carried out at an accelerating voltage of 20 kV using a 7.5  $\mu\text{m}$  aperture, an exposure dose of 700 pC/cm, and a beam current of 11 nA. After exposure, the sample was developed in tetramethylammonium hydroxide (TMAH) 2% for 90 s and rinsed in distilled water for 30 s followed by nitrogen drying.

Baked HSQ, which is resistant to electron beam irradiation, was the material used to impart a phase difference to the electron wave in the TEM. The use of such a negative resist provided considerable advantages in terms of ease of fabrication and well known superior resolution. The only disadvantage was the insulating nature of the HSQ, which resulted in charging during TEM examination. Each hologram was therefore coated with a few nm of evaporated Cr, which solved most of the charging problems. The result of this patterning is shown in the form of a TEM image of a hologram in Figure 2(a). The patterned area is clearly visible, as is the large central hole. On the top-left, a region of stationary phase is visible (indicated by a circle). Although the image appears to show other stationary points, these are artifacts resulting from digital reproduction due to undersampling of the TEM image (further TEM and SEM images are also visible in the [supplementary material](#)). Figure 2(b) shows a TEM image of part of the hologram, which confirms that different spatial frequencies are reproduced correctly. Figure 2(c) shows a thickness map, calculated using energy-filtered TEM,<sup>19</sup> of part of a pattern, in which line widths of 35 nm are present and the average periodicity is below

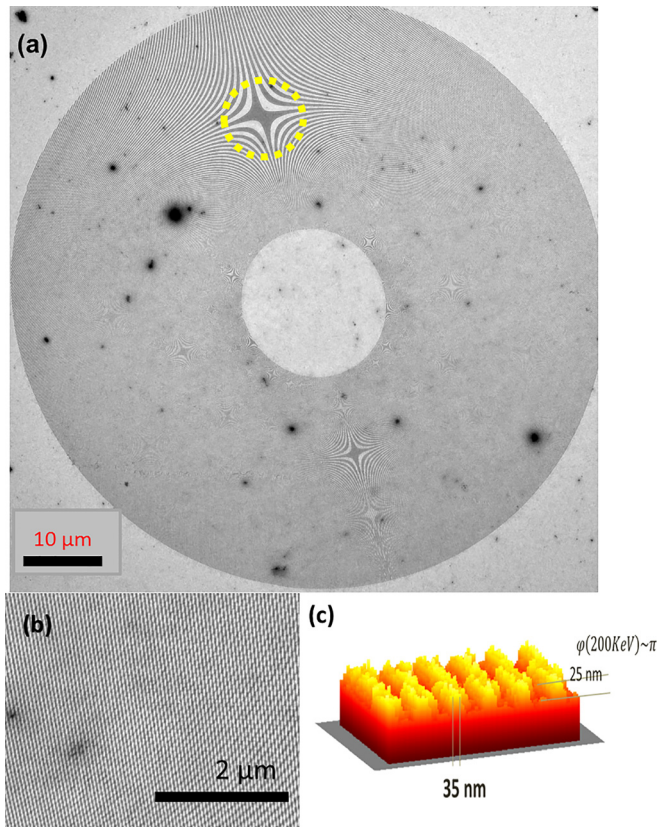


FIG. 2. (a) TEM image of an HSQ-based hologram for  $\ell = 1000\hbar$ . (b) Higher magnification TEM image of a region of the hologram, showing both low and high spatial frequencies in the pattern. (c) 3D rendering of an energy-filtered-TEM-based thickness map of a region of one of the holograms, showing detail on the order of 35 nm.

65 nm. The map and simulations in the [supplementary material](#) indicate that, even at such a scale, the lateral definition of the trench is good, that the vertical step is nearly perfect, and that the trench thickness is uniform.

Figure 3(a) shows a nearly-in-focus image of a Fraunhofer diffraction pattern of the hologram recorded at 300 keV using an FEI Titan equipped with a Schottky FEG and operated in LowMag mode. The two opposite vortices take the form of rings with uniformly bright intensities, confirming the very high resolution of our EBL pattern, i.e., that both high and low spatial frequencies are diffracted with the same intensity. We also observe only a very faint trace of second order diffraction, providing confirmation that the grooves are sharp and almost rectangular (as suggested by the thickness map). We achieved a first order efficiency of up to 20% but a second order efficiency of only 3.5%. This inhibition of the second order is very important for applications and is a consequence of the highly rectangular profile of the gratings (see [supplementary material](#)).

We now address measurement of the OAM value of the vortex. In a previous article,<sup>19</sup> the authors measured a thickness map in the hologram plane. Here, considering the large size of the pattern with respect to those fabricated previously,<sup>23</sup> we are not able to make a reasonable thickness map of the entire hologram (we would need a digital image with a size of at least a  $4 \times 10^8$  pixels). Therefore, we cannot check the exact OAM spectrum of the vortex in this way. Instead, inspired by a suggestion in the literature,<sup>36–38</sup> we used the selected area diffraction (SAD) aperture to block half of the vortex. We then systematically varied the excitation of the diffraction lens, which is located immediately after the aperture. In this way, we observed the rotation of the Fresnel diffraction image. A simplified way to calculate this rotation angle makes use of the expression

$$\theta = \left( \frac{eB}{2m} \pm \frac{L}{mr^2} \right) \frac{\Delta z}{v}, \quad (2)$$

where  $\Delta z$  is the propagation distance,  $v$  is the electron velocity, and the quantity  $r$  is a “semi-classical” value of the radius, whose correct quantum interpretation depends on the shape of the beam.<sup>38</sup> The expression for the rotation angle contains two terms. The first is the Larmor rotation, which depends on the magnetic field of the diffraction lens. The second is referred to as the Gouy rotation and is associated with the phase gradient of the vortex. As the Gouy rotation goes to zero at large distances  $r$  from the rotation center, we can separate the Larmor contribution by checking the rotation of the shadow of the aperture far from the center. For our large OAM vortex, as a result of the use of a weak diffraction lens, this contribution is small (10% of the overall rotation), while the dominant contribution to the rotation originates from the phase gradient of the vortex itself.

For an exact evaluation of the Gouy rotation, instead of using Eq. (2) we evaluated the Fresnel propagation numerically for different values of  $\ell$ . We calibrated the defoci by comparing simulations and experimental images recorded without an aperture, since the absolute  $z$  positions of both the SAD aperture and the Fraunhofer diffraction pattern were unknown. We define the parameter

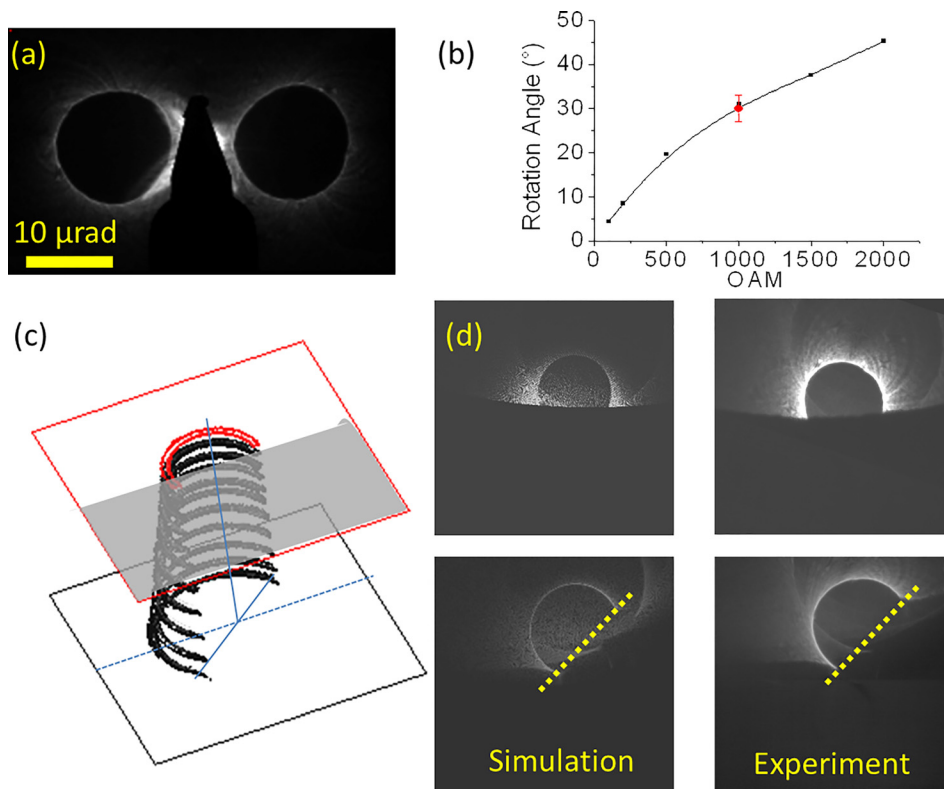


FIG. 3. (a) Experimental image of a diffraction pattern of the hologram nearly in focus. A beam stop was used to block the transmitted beam. (b) Plot of the expected rotation as a function of OAM quantum number, shown together with our experimental measurement. (c) Schematic diagram illustrating the use of a knife edge to measure beam rotation. The half circles are the silhouette of the EVB after the knife edge (here in gray). (d) Experimental results and simulations for  $\ell = 1000$  before (upper figures) and after (lower figures) propagation. The simulations (left) and the experiment (right) are compared. The important parameter is the rotation, which is highlighted by the dashed line.

$$z_R = \pi \frac{r_{rim}^2}{1000 \times \lambda}, \quad (3)$$

which would be the Rayleigh range for an ideal Laguerre-Gauss beam with  $p=0$  and an equivalent apparent rim radius  $r_{rim}$  (with the radius corresponding to maximal intensity). We find that the aperture is located at  $z/z_R = 0.5$  and that we analyzed the rotation after  $z/z_R = 2$ . Figure 3(b) shows the expected rotation according to simulations for beams with different values of  $L$  and for a realistic hologram structure. The best match for  $\langle L \rangle$  is  $(960 \pm 120) \hbar$  and is consistent with the nominal value. Figure 3(c) shows a comparison between a simulation for  $L = 1000 \hbar$  and our experimental results, demonstrating good agreement in the rotation angle (Minor details depend on the exact shape of the aperture).

To conclude, we have demonstrated that by using EBL we can overcome previous intrinsic limitations of holograms, in terms of (1) the maximum OAM that can be reached; (2) the minimum detail that can be reproduced (at least 35 nm; in the [supplementary material](#) we reach 18 nm); (3) improved uniformity of the frequency response; and (4) better suppression of higher order diffraction due to a nearly perfect rectangular groove profile. We believe that EBL will be the fabrication technique of choice for future complex diffractive optics with electrons. One of the most interesting perspectives is to use holograms to shape beams that have very well defined and stable properties, in order to increase the precision of TEM measurements. A very extended and precise grating can be used for electron interferometry, while by using an extended version of a conical hologram<sup>32</sup> it will be possible to create a nearly ideal Bessel beam potentially useful for interferometry or for measurements of small deflections.

See [supplementary material](#) for: (S1) how to calculate the hologram, (S2) alternative EBL, (S3) imaging of the hologram, and (S4) discussions on efficiency vs groove shape.

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