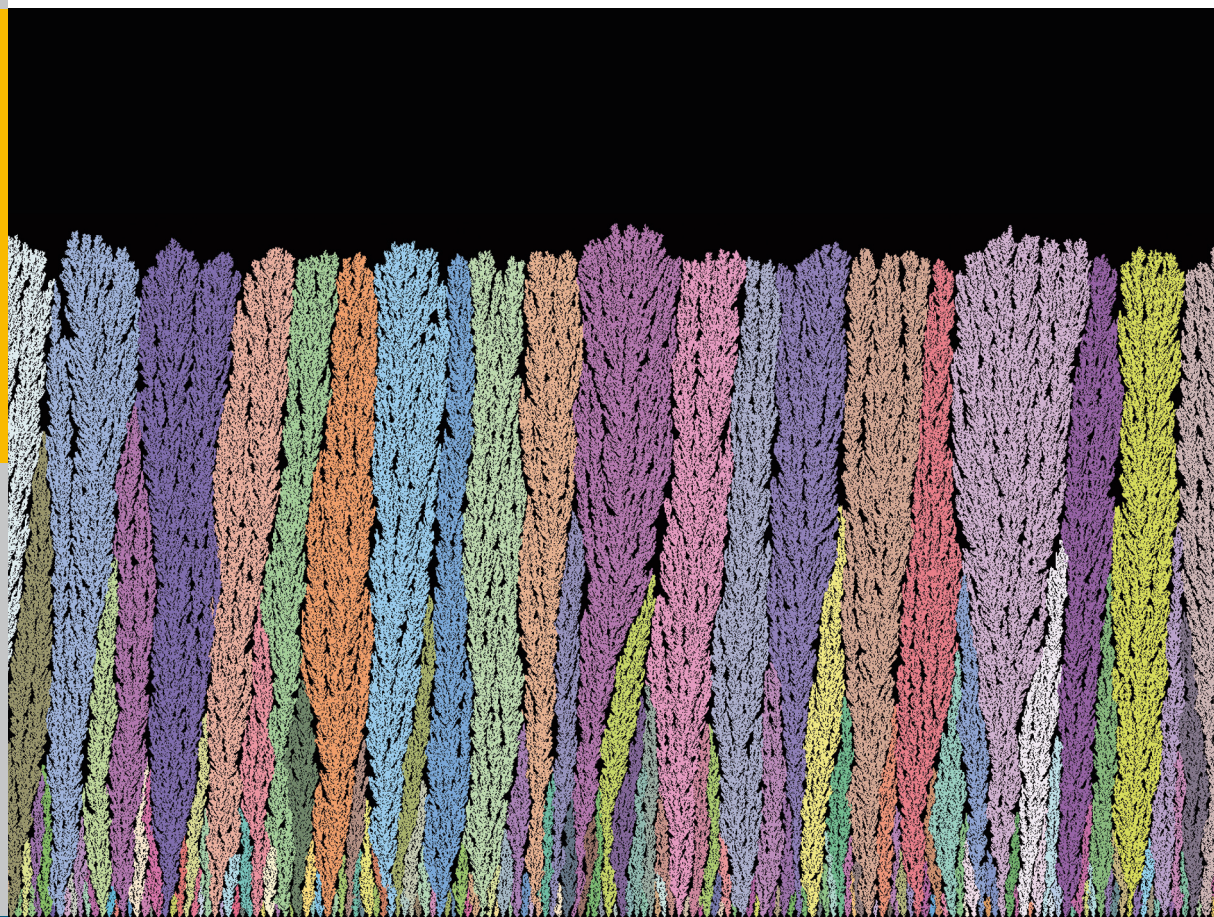


Numerical Simulation of Plasma Spray-Physical Vapor Deposition

Panpan Wang



Member of the Helmholtz Association

Energie & Umwelt /
Energy & Environment
Band / Volume 401
ISBN 978-3-95806-282-5

Forschungszentrum Jülich GmbH
Institute of Energy and Climate Research
Materials Synthesis and Processing (IEK-1)

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Schriften des Forschungszentrums Jülich
Reihe Energie & Umwelt / Energy & Environment

Band / Volume 401

ISSN 1866-1793

ISBN 978-3-95806-282-5

Bibliographic information published by the Deutsche Nationalbibliothek.
The Deutsche Nationalbibliothek lists this publication in the Deutsche
Nationalbibliografie; detailed bibliographic data are available in the
Internet at <http://dnb.d-nb.de>.

Publisher and
Distributor: Forschungszentrum Jülich GmbH
Zentralbibliothek
52425 Jülich
Tel: +49 2461 61-5368
Fax: +49 2461 61-6103
Email: zb-publikation@fz-juelich.de
www.fz-juelich.de/zb

Cover Design: Grafische Medien, Forschungszentrum Jülich GmbH

Printer: Grafische Medien, Forschungszentrum Jülich GmbH

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Schriften des Forschungszentrums Jülich
Reihe Energie & Umwelt / Energy & Environment, Band / Volume 401

D 294 (Diss., Bochum, Univ., 2017)

ISSN 1866-1793
ISBN 978-3-95806-282-5

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Abstract

The modeling of the plasma spray process is driven by the intention of further increasing the understanding the growth mechanisms of columnar thermal barrier coatings (TBC). The major parameters associated with the deposition process in the experiment are the power input, plasma gas composition, and chamber pressures resulting in distinct microstructures.

Therefore, the objective of this study was to simulate the plasma jet and the growth of columnar TBCs. Five main topics were examined: (1) thermodynamic and transport properties for different plasma mixtures (35Ar-60He, 35Ar-60He-10H₂, and 100Ar-10H₂) depending on the pressure and the temperature; (2) vacuum plasma spray (VPS); (3) plasma-spray physical vapor deposition (PS-PVD); (4) built-up of columnar coatings using the Monte-Carlo method; (5) validation by experiments.

Investigations of thermodynamic and transport properties gave the basis for the understanding of the plasma process and provide data of the following plasma jet modeling. The plasma jet modeling used three types of plasma mixture (35Ar-60He at pressures ranging from 200 Pa-10000 Pa, 35Ar-60He-10H₂ at a pressure of 200 Pa, and 100Ar-10H₂ at a pressure of 200 Pa) was carried out by ANSYS Fluent 17, the results were compared to photographs of the plasma jets. Taking into account the influence of non-equilibrium, the plasma composition and spectral line intensities were calculated. Results of the measured and calculated intensities proved that non-equilibrium exists. Finally, a two-dimensional Monte Carlo simulation was used to investigate the formation of columnar growth in plasma spray-physical vapor deposition process (PS-PVD). The surface diffusion in the coating was neglected because of the high deposition rate. The detailed examination of the morphology, the orientation, the porosity level of the columns is given, which is compared to the microstructures produced by a PS-PVD process.

Kurzfassung

Die Modellierung des Plasmaspritzverfahrens wird von der Absicht angetrieben, das Verständnis der Wachstumsmechanismen von kolumnaren Wärmedämmschichten (TBC) weiter zu verbessern. Die Hauptparameter, die mit dem Abscheidungsprozess in dem Experiment assoziiert sind, sind die Eingangsleistung, Plasmagaszusammensetzung, und Kammerdrücke, die zu unterschiedlichen Mikrostrukturen führt.

Daher war das Ziel dieser Studie, den Plasmastrahl und das Wachstum von säulenförmigen TBCs zu simulieren. Fünf Hauptthemen wurden untersucht: (1) thermodynamische und Transporteigenschaften für verschiedene Plasmamischungen (35Ar-60He, 35Ar-60He-10H₂ und 100Ar-10H₂) in Abhängigkeit vom Druck und der Temperatur; (2) Vakuumplasmaspray (VPS); (3) physikalische Dampfabscheidung im Plasma (PS-PVD); (4) Aufbau von Säulenüberzügen unter Verwendung der Monte-Carlo-Methode; (5) Validierung durch Experiment.

Untersuchungen der thermodynamischen Eigenschaften und der Transporteigenschaften bildeten die Grundlage für das Verständnis des Plasmaprozesses und lieferten Daten der folgenden Plasmastrahlmodellierung. Die Plasmastrahlmodellierung verwendete drei Arten von Plasmamischungen (35Ar-60He bei Drücken im Bereich von 200 Pa-10000 Pa, 35Ar-60He-10H₂ bei einem Druck von 200 Pa und 100Ar-10H₂ bei einem Druck von 200 Pa). ANSYS Fluent 17 wurden mit Fotografien der Plasmastrahlen verglichen. Unter Berücksichtigung des Einflusses von Nichtgleichgewicht wurden die Plasmazusammensetzung und die Spektrallinienintensitäten berechnet. Die Ergebnisse der gemessenen und berechneten Intensitäten zeigten, dass ein Nichtgleichgewicht existiert. Schließlich wurde eine zweidimensionale Monte-Carlo-Simulation verwendet, um die Bildung von säulenförmigem Wachstum im Plasmasprühphysik-Abscheidungsverfahren (PS-PVD) zu untersuchen. Die Oberflächendiffusion in der Beschichtung wurde wegen der hohen Abscheidungsrate vernachlässigt. Die detaillierte Untersuchung der Morphologie, der Orientierung, des Porositätsniveaus der Säulen ist gegeben, die mit den durch einen PS-PVD-Prozess erzeugten Mikrostrukturen verglichen wird.

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Nomenclature

APS	Atmospheric Plasma Spray
VPS	Vacuum Plasma Spray
PS-PVD	Plasma Spray Physical Vapor Deposition
SPS	Suspension Plasma Spray
OES	Optical Emission Spectroscopy
EB-PVD	Electron Beam Physical Vapor Deposition
TGO	Thermally Grown Oxide
BC	Band Coat
YSZ	Yttria-Stabilized Zirconia
TBCs	Thermal Barrier Coatings
DC	Direct Current
LTE	Local Thermodynamic Equilibrium
LCE	Local Chemical Equilibrium
NLTE	Thermal Non-equilibrium Plasma
NLCE	Chemical Non-equilibrium Plasma
DNS	Direct Numerical Simulation
LESs	Large Eddy Simulations
RANS	Reynolds-averaged Navier–Stokes Equations
SZM	Structure Zone Model
CEA	NASA Lewis Research Center’s Chemical Equilibrium and Applications Program
SST	Shear-Stress Transport
T_h	heavy particle temperature, K
l_e	mean free path of the electrons, m
P	Pressure, Pa
T_e	electron temperature, K
m_e	Electron mass, kg
m_h	heavy particle mass, kg
κ_{tot}	Total thermal conductivity, $\text{W m}^{-1}\text{K}^{-1}$
κ_h	heavy particle transition, $\text{W m}^{-1}\text{K}^{-1}$

κ_{int}	internal thermal conductivity, $\text{W m}^{-1}\text{K}^{-1}$
κ_r	reaction thermal conductivity (ionization and dissociation) , $\text{W m}^{-1}\text{K}^{-1}$
κ_e	electron translation, $\text{W m}^{-1}\text{K}^{-1}$
m	Mass, kg
T	Temperature, K
Q	the collision integral
θ	Non-equilibrium parameter
k	turbulence kinetic energy
ω	the specific dissipation rate
α	Angle of incident vapor
β	Orientation of column
n_e	concentrations of electrons, m^{-3}
n_i	concentrations of ions, m^{-3}
n_a	concentrations of atoms, m^{-3}
$Z_i(T_e)$	the internal partitions functions of ions
$Z_a(T_e)$	the internal partitions functions of atoms
E_i	the ionization energy, J
ΔE_i	the ionization potential lowering
k	the Boltzmann constant
g_m	the statistical weight
h	Planck's constant
c	the speed of light, m/s
A_{mn}	the transition probability
λ_{mn}	the wavelength between the upper level m and lower level n , m
E_m	the energy of the upper level, J
n_j	the total concentration of the species j , m^{-3}
$Z_j(T_e)$	the internal partition function
M	Mach number
μ	Viscosity, $\text{kg m}^{-1}\text{s}^{-1}$

1 Overview

1.1 Introduction

Yttria-stabilized zirconia (YSZ) coatings are widely used in gas turbines to insulate superalloy components from the heat generated during the jet engine operation. Thermal barrier coatings (TBCs) are commonly produced through plasma spray processes or the electron beam physical vapor deposition (EB-PVD). In the case of atmospheric plasma spray (APS) processes, plasma heating of YSZ powders produces completely or partially melted particles that subsequently deposit on the substrate. This technique is commonly used to accelerate and melt feedstock particles to obtain splat-like coatings for multiple applications: solid oxide fuel cells [1, 2], gas separation membranes [3] and thermal barrier coatings [4]. The reduced pressure plasma spray processes includes vacuum plasma spray (VPS) or plasma spray physical vapor deposition (PS-PVD) processes. The plasma jet at a controlled chamber pressure allows the formation of coatings from material in a molten, semi-molten or vapor state that lead to distinct coating microstructures [5]. Using the deposition from a vapor state, the resultant columnar coatings can be used as TBC characterized by enhanced strain tolerance.

Intensive researches have been conducted through both experimental measurements and the modeling as follows: (1) the plasma formation and dynamics of the arc leading to jet instabilities [6-8]; (2) melting and evaporation of feedstock particles [9]; (3) the coating formation [10]. However, detailed studies on a long plasma jet according the influence of plasma composition and chamber pressures, and the validations by the experiment are still missing.

Thermodynamic and transport properties of Ar-He-H₂ gas mixtures depending on the pressure and the temperature are examined to understand the benefits of gas mixtures in contrast to pure gas. Literatures related to the modeling of the plasma jet including the plasma generation in the torch and the plasma jet expanding in a chamber are summarized in this work. The influence of the non-equilibrium state on the thermodynamic and transport properties is also investigated. In the simulation of the plasma jet, most literatures focus on atmospheric plasma spray process and its coupling

with feedstock particles injection outside of the nozzle. This work focused on the plasma jet expanding in a low and very low chamber pressure.

A Monte Carlo simulation, which depends on the impingement of a oblique incident vapor as a straight line onto the substrate surface, is used to model the deposition of columnar TBCs. These simulation sights describe electron beam physical vapor deposition (EB-PVD) and plasma spray-physical vapor deposition (PS-PVD).

1.2 Objectives of the Thesis

The modeling of the plasma jet at pressures ranging from 200 Pa-10000 Pa has been done by Fluent using a SST $k - \omega$ turbulence model to describe the flow field of the plasma spray. At a chamber pressure of 200 Pa, PS-PVD processes utilizing distinct plasma mixtures (35Ar-60He, 35Ar-60He-10H₂, and 100Ar-10H₂) cause columnar or splat-like microstructures. To analyze the melting or evaporated capability of plasma gas mixtures to YSZ particles, the thermodynamic and transport properties of gas mixtures depending on the pressure and the temperature at equilibrium are investigated.

To verify the simulated results, the photographs of the plasma jets at pressures ranging from 200 Pa-10000 Pa for a 35Ar-60He plasma are compared to the temperature profile in the radial and axial direction. The instabilities of the plasma jet are examined by comparing between the turbulent Reynolds number and the images. To evaluate the thermal non-equilibrium parameters of PS-PVD process at a pressure of 200 Pa for 35Ar-60He plasma, the plasma composition and the atomic and ionic spectral line intensities are calculated in contrast to the integrated spectral line intensities of optical emission spectroscopy (OES) measurement. The measured intensities also highlight the evaluation of the temperature.

A Monte-Carlo method is used to model the built-up of columns depending on the self-shadowing effect to understand the formation of columns in the PS-PVD process [11]. In this simulation, the columns grow, because oblique incoming atoms or molecules impinge on the substrate surface. The modeling and the experiment are compared with respect the columns growth.

1.3 Structure of the Thesis

Chapter 2 summarizes literature reviews of the plasma spray, coating deposition, and related modeling publications, and then brings about main issues. The relationship between plasma spray parameters and columnar microstructures will be discussed. Parameters that influence the modeling of columnar microstructures are summarized. Chapter 3 covers the theoretical methods, including the modeling of the plasma jet, the calculation of plasma compositions of a plasma in non-equilibrium characterized of ion temperatures, and the procedure of Monte Carlo simulation of columns growth. The relationship between the modeling assumptions according to the plasma spray parameters and the characteristics of the plasma spray process will be shown in Chapter 3. Experimental methods will be presented in Chapter 4, whereas Chapter 5 shows and interpretes the results. In this Chapter, the first section discusses the thermodynamic and transport properties of different plasma gas mixtures. Details of the modeling of VPS and PS-PVD processes will be presented in the second section. In the third section, interpretations of results of Monte Carlo simulations of physical vapor deposition will be reviewed. Finally, summary and remarks will conclude in Chapter 6 of the thesis.

2 Fundamentals and State-of-the-art

2.1 Thermal Plasma

A plasma consists of electrons, ions, and neutral atoms. Ions and neutrals are noted as the heavy species. Some of these heavy species may be in an excited state due to the high energy of plasmas. Particles in an excited state can return to ground state by photon emission, which is partially responsible for the luminosity of plasma. Plasmas, consisting of electrons as well as ions and neutrals in excited or ground state, are overall electrically neutral, which is also known as quasi-neutrality.

Many collisions (high collisional frequency) are required to eliminate energy (temperature) differences between electrons and heavy species due to a big mass difference and then to reach thermal equilibrium [12]. The equilibrium condition realizes in the condition where temperatures are between 8000~15000 K with electron densities ranging from $10^{21} \sim 10^{24} \text{ m}^{-3}$ [13].

2.1.1 Thermal Excitation and Ionization

The Maxwell-Boltzmann equation establishes the basis of the kinetic theory of gases. It describes distributions of speeds for ideal gases at specific temperatures. At lower temperatures, the molecules have less energy. Therefore, the speeds of the molecules are lower and the distribution has a smaller range. As the temperature of the molecules increases, the Maxwell-Boltzmann distribution is shifted to higher speeds and is broadened. The Maxwell-Boltzmann distributions also depend on the molecule mass. Heavier molecules move more slowly than lighter molecules. Therefore, heavier molecules have a smaller speed distribution, while lighter molecules have a speed distribution that is more spread out. The Maxwell-Boltzmann probability distribution at thermodynamic equilibrium is written [12]

$$f(v) = \sqrt{\left(\frac{m}{2\pi kT}\right)^3} 4\pi v^2 e\left(-\frac{mv^2}{2kT}\right) \quad (2.1)$$

where v is the particle velocity, m is the particle mass, and kT is the product of Boltzmann's constant and absolute temperature.

The distribution of a Maxwell-Boltzmann distribution among the particles in a plasma depends strongly on the interaction between the particles, i.e. on the collisional frequency and energy exchange during a collision. The collisional frequency decreases if the rarefaction degree increases. Conservation of both momentum and translational kinetic energy happens.

In addition to elastic collisions, inelastic collisions occur leading to chemical reaction (excitation, dissociation, and ionization). The degree of ionization of a plasma depends on the temperature. At sufficiently high temperature, high-speed electrons collide with atoms and remove electrons from atomic orbits. A general relation between the degree of ionization and temperature can be obtained from a statistical description of the plasma in thermodynamic equilibrium.

The Saha ionization equation, also known as Saha-Langmuir equation, describes the ionization state of a gas. It relates the temperature, concentration, and ionization energies of atoms. In the case of ionization reactions, this may be corrected for the lowering of the ionization energy due to the effects of electric or magnetic fields. These mass action laws allow, taking into account species conservation and Dalton's law, the calculation of the plasma composition at equilibrium.

For a monatomic gas, the Saha equation is written:

$$n_e \left(\frac{n_i}{n_a} \right)^{1/\theta} = \frac{2Z_i(T_e)}{Z_a(T_e)} \left(\frac{2\pi m_e k T_e}{h^2} \right)^{3/2} \exp \left(- \frac{E_i - \Delta E_i}{k T_e} \right) \quad (2.2)$$

where n_e , n_i , and n_a are, respectively, the electron, ion and atom concentration. $Z_i(T_e)$ and $Z_a(T_e)$ are the internal partitions functions of ions and atoms. T_e is the electron temperature. E_i is the ionization energy and ΔE_i accounts for the lowering of the ionization potential.

However, in thermal plasmas, especially those produced by arcs, regions exist where steep gradients of temperature, composition and velocity are present. Electrons diffuse faster than heavy species even if this diffusion is slowed down by the electric field created between ions and electrons. If diffusion processes are faster than ionization by electron impact, the Saha balance is no longer satisfied.

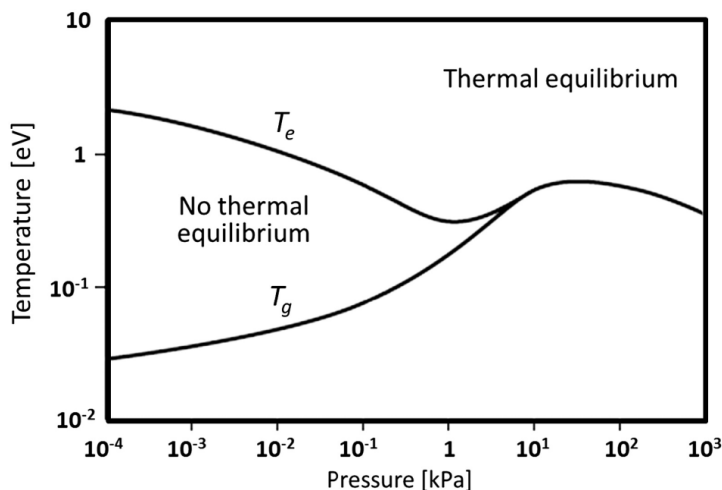


Figure 2-1. Evolution of the temperature of the electrons (T_e) and the heavy particles (T_g) as a function of the total pressure in the plasma [14].

Figure 2-1 shows that at atmospheric pressure a plasma should be at thermal equilibrium. An increase in the mean free path of the pressure decrease results in a decrease of the number of collisions. This will lead to an increase of thermal non-equilibrium.

The spectrum from typical thermal plasma generated from a monatomic gas reveals continuous as well as line radiation. Electronic transitions of excited atoms or ions from higher to lower energy states cause the emission of spectral lines. The total energy transport by line radiation is frequently only a small fraction of the total radiation energy from plasma; the energy transport depends on the number and wavelength of the emitted lines, which in turn depend on the characteristics of the plasma fluid, in particular, on the number of possible species at a given temperature. The plasma of a given gas may be a "strong" or "weak" line radiator, depending on the plasma density and composition,

which are functions of pressure and temperature. In general, absorption effects become more pronounced as the pressure increases. Plasmas at very high pressures become optically thick and may approach the radiation intensity of a blackbody radiator if the temperature is sufficiently high [12].

2.1.2 Generation of Thermal Plasmas

Plasmas occur over a wide range of pressures, they are typically classified in terms of electron temperature and electron densities. Methods for producing thermal plasmas include the most widely used direct current (DC) high-intensity arcs, radio frequency (RF) induced, and microwave induced plasmas [15]. DC high-intensity arcs consist of free burning arcs, transferred arcs, and non-transferred arcs [6, 16, 17].

The modeling of the plasma torch comprises arc-cathode interactions, arc column and arc-anode interactions that are published in [17-24]. The arc column takes up a large part of the gas computational domain and can be considered in local thermodynamic equilibrium (LTE). Departure from thermal equilibrium has been taken into account in the regions where the cold gas and plasma interact, as well as close to the electrodes. Its operation is controlled by dynamic, thermal, electromagnetic, acoustic and chemical phenomena that are not fully addressed yet by the current models and several further steps are needed to achieve calculations with a high level of predictability: arc-anode interactions, arc-cathode interactions, arc column, and plasma-electrode interfaces.

A schematic representation of the flow and modeling of arc reattachment process inside a SG100 DC arc plasma torch is illustrated in Figure 2-2. The dynamics of the arc inside the torch can be discerned through two main features: the movement of the arc-anode attachment and the process of formation of a new position of the arc-anode attachment, that what is called the arc reattachment process [16]. The dynamic nature of the arc is evidenced by the temporal variation of the voltage drop between the electrodes, as well as by fluctuations in the temperature, pressure and velocity at the torch exit [25].

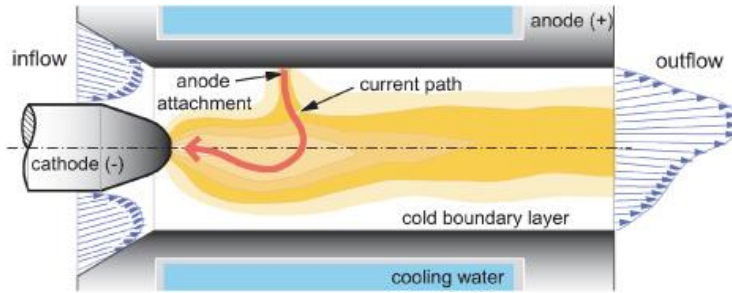


Figure 2-2. Schematic representation of the flow and modeling of arc reattachment process inside a SG100 DC arc plasma torch [6].

Two major forces acting on the arc are the gas dynamic drag force in the downstream direction and the Lorentz force acting in a direction depending on the curvature of the attachment column to the anode. The force on the curved attachment root is due to the asymmetric interaction between the arc current and the self-magnetic field generated by the current, and acts away from the center of curvature. For a stable attachment situation, the drag force and magnetic forces on the arc root must balance. Deviations from the attachment position must result in an imbalance, which will return the attachment to its original location.

Many plasma processes use argon-hydrogen mixtures because argon and hydrogen improve the momentum and energy transfers, respectively [26, 27]. A higher argon flow rate stabilizes the arc which also explains why arc dynamic behaviors in the nozzle are neglected [28]. A rather high viscosity due to high ionization energy also characterizes argon gas plasma, and argon gas keeps a relatively low thermal conductivity. Argon-helium is also widely used because, on one hand, helium increases the plasma enthalpy and, on the other hand, the mixture exhibits a higher viscosity over 10000 K at equilibrium due to its high ionization energy. Enthalpy of these monoatomic gases is substantially lower in contrast to the diatomic ones, as shown in Figure 2-3. However, transition into the plasma is simpler than diatomic gas, they produce stable electric arc, and they require lower operating voltage. The temperature of their plasmas reaches higher values in comparison to diatomic plasma inside the nozzle.

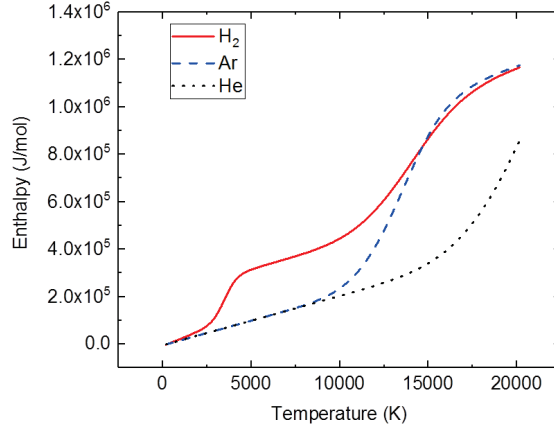


Figure 2-3. Temperature dependence of the enthalpy of hydrogen, argon and helium, at atmospheric pressure and equilibrium.

2.1.3 Thermodynamic and Transport Properties

Pateyron et al [29] calculated the enthalpy variation versus temperature for various mixtures of Ar-H₂ and Ar-He gases at atmospheric pressure. It can be concluded that the addition of H₂ to Ar increases the enthalpy of the mixture, especially at the temperatures when the dissociation of the H₂ molecules and the first ionization of Ar occur. But due to the high mass of argon compared with that of hydrogen, the increase in enthalpy is not as drastic for concentrations less than 30 vol% H₂ for what compared to pure H₂. The addition of He drastically increases the mixture enthalpy for temperatures higher than 17000 K, but here again the mass of helium is small compared with that of argon, and thus the modification becomes very significant for He concentrations higher than 70%. Compared to pure argon plasma at 12000 -14000 K, the enthalpy of the mixture is doubled with either with 80% He or 30% H₂ [29].

Contributions from translational and internal partition functions as well as relevant ionization energies are included in the calculation of enthalpy. Temperatures below 6000 K give the same values for different pressures. The mean free path of a molecule in a gas is the average distance of travel between its collisions with other particles. This is inversely proportional to the pressure. More collisions will take place at a higher pressure.

Collisions reduce the electrons' energy and make it more difficult for it to ionize. In contrast to higher pressures, it is easier to ionize at the lower pressures.

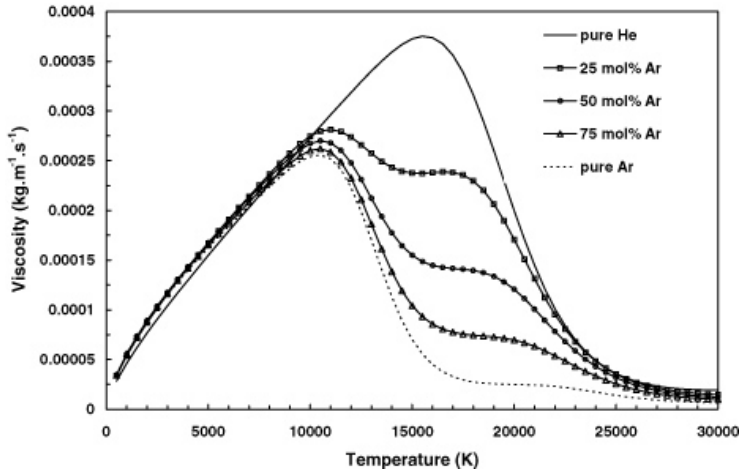


Figure 2-4. Temperature dependence of the viscosity of an argon-helium mixture for different values of molar percentages of argon, at atmospheric pressure and at equilibrium [30].

The transport coefficients are calculated by using the Chapman-Enskog method [31]. Figures 2-4 and 2-5 show the temperature dependence of the viscosity and the total thermal conductivity of argon-helium mixture for different molar percentages at equilibrium, respectively. From Figure 2-4, we see that below 6000 K, it is known that the viscosity is proportional to \sqrt{mT}/Q , where m , T , Q are, respectively, the mass, the temperature and the collision integral. The viscosity is dominated by neutral-neutral interactions and gives roughly the same results for argon as for helium. The combination of collision integrals and mass of results in roughly the same viscosity for argon as for helium. However, when ionization becomes efficient, interactions between charged particles occur, resulting in a regime dominated by Coulomb collision integrals, which are higher than those of neutral-neutral interactions, therefore resulting in a decrease in the viscosity. The viscosity of pure helium is much higher than that of pure argon, because the helium ionization starts at higher temperatures.

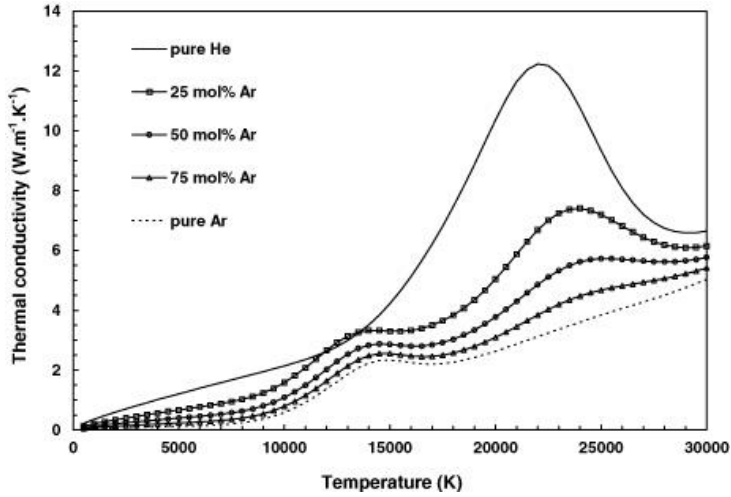


Figure 2-5. Temperature dependence of the thermal conductivity of an argon–helium mixture for different values of molar percentages of argon, at atmospheric pressure and at equilibrium [30].

It can be observed in Figure 2-5 that the thermal conductivity of helium is generally higher than that of argon due to the mass difference as well as to the collision integrals between argon species which are higher than those of helium species. Below 6000 K, this statement is confirmed by the fact that the thermal conductivity is proportional to $\sqrt{T}/(Q\sqrt{m})$, which explains that the thermal conductivity of helium is about nine magnitude higher than that of argon. Moreover, the first peak corresponds to the ionization of argon while the second one is related to the ionization of helium atom and Ar^+ ion.

The temperature dependence of the viscosity of argon-hydrogen mixtures in three different proportions is compared in Figure 2-6 with that of pure argon and pure hydrogen. The viscosity of argon is much greater than that of hydrogen, because of its much larger mass of argon (m); this outweighs the influence of the generally smaller collision integrals for interactions between hydrogen species. Furthermore, the addition of 25% hydrogen to argon plasmas does not significantly affect the viscosity.

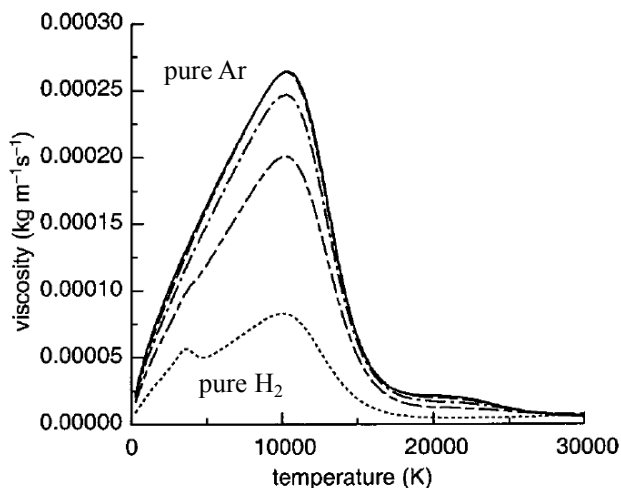


Figure 2-6. Temperature dependence of the viscosity of an argon-hydrogen mixture for different values of molar concentrations of argon, at atmospheric pressure and at equilibrium. Legend of the concentration from top to bottom: pure argon; 75% argon; 50% argon; 25% argon; pure hydrogen [32].

The thermal conductivity of argon-hydrogen mixtures is shown in Figure 2-7. The thermal conductivity of hydrogen is very much greater than that of argon. Factors that contribute to this are the $m^{-1/2}$ dependence of the translational thermal conductivity, the existence of a large reaction thermal conductivity peak associated with the dissociation of molecular hydrogen, and the generally smaller collision integrals for interactions between hydrogen species. The presence of a small amount of hydrogen makes a strikingly large difference to the thermal conductivity at temperatures around 3800 K.

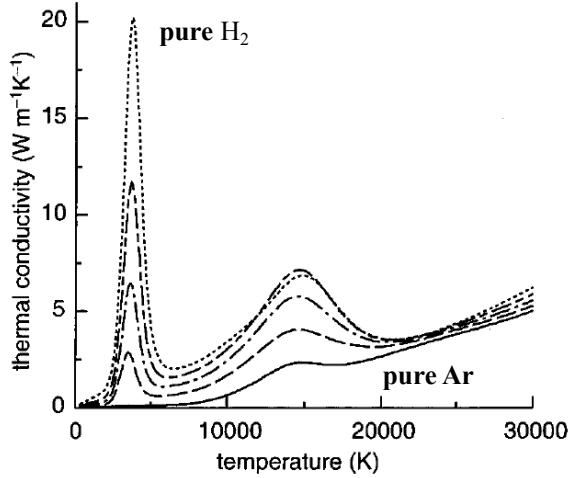


Figure 2-7. Temperature dependence of the thermal conductivity of an argon-hydrogen mixture for different values of molar percentages of argon, at atmospheric pressure and at equilibrium. Legend of the concentration from top to bottom: pure argon; 75% argon; 50% argon; 25% argon; pure hydrogen [32].

Contrary to LTE plasmas, the two-temperature plasma compositions are calculated by different models and use different relations to describe the ionization and dissociation reactions. The plasma composition is determined by the modified equilibrium constant method of van der Sanden [33]. Collision integrals are required to calculate transport coefficients by Rat [34].

Two-temperature transport coefficients are calculated for different values of the non-equilibrium parameter θ . It characterizes the departure from thermal equilibrium and corresponds to $\theta = T_e/T_h$. It can be even higher than 10 in a DC plasma torch, as shown by the calculations of Trelles et al [35]. In this work, the calculations are focused on $\theta = 1, 1.1, 1.3, 1.6$ and 2 , whereas is $\theta = 3$ an extreme value which can be observed, at atmospheric pressure, as soon as the plasma interacts with a cold wall or when a cold gas is injected for chemical reactions or as a particle carrier gas. Besides, it has to be noted that the approach of Rat et al [34] does not limit the value of θ , since it is assumed in the derivation of two-temperature transport coefficients that the distribution function of species depends on T_e and θ without any constraint on the non-equilibrium parameter θ .

In order to illustrate the influence of the non-equilibrium parameter on the plasma composition, we show in Figure 2-8 the dependence of the number densities of electrons of an argon-helium mixture (25 mol% Ar) on electron temperature for different values of non-equilibrium parameter. It can be observed that the electron density becomes almost constant over 15000 K, and slightly increases, at fixed T_e as θ increases. The non-equilibrium values are always higher than those obtained at equilibrium. Furthermore, the plasma composition is dominated by the modified Saha equations calculated at T_e , which favor the ionization of species.

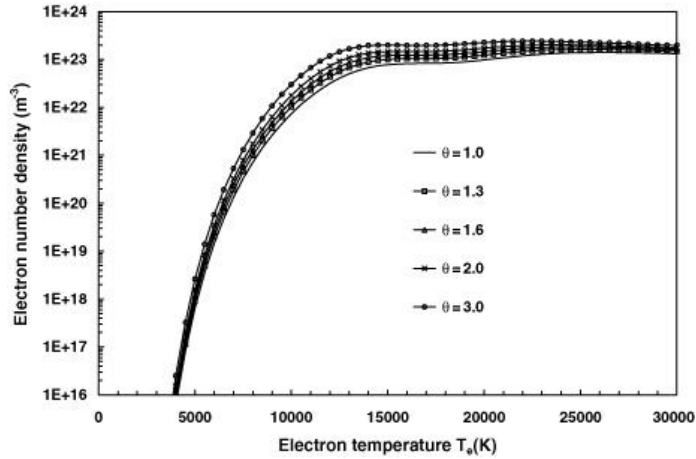


Figure 2-8. Electrons concentration of Ar-He mixture as a function of electron temperature (25 mol% Ar), for different values of θ , at atmospheric pressure [30].

The dependence of the viscosity on θ is pronounced, as shown in Figure 2-9, which depicts the viscosity of an argon-helium mixture (25 mol% of argon) as a function of the heavy species temperature, for different values of the non-equilibrium parameter θ , at atmospheric pressure. The viscosity has been plotted as a function of heavy species temperature because it is governed by heavy species. The part of the non-equilibrium curves which overlap the equilibrium one corresponds to the neutral-neutral interaction regime before efficient ionization. The study of plasma composition shows that ionization is especially favored as θ increases. The significant change in the slope corresponds to ionization, i.e. the collision integrals of charged species are dominant which drastically

reduces the viscosity because the collision integrals of charged species are three orders of magnitude higher than those of neutral species.

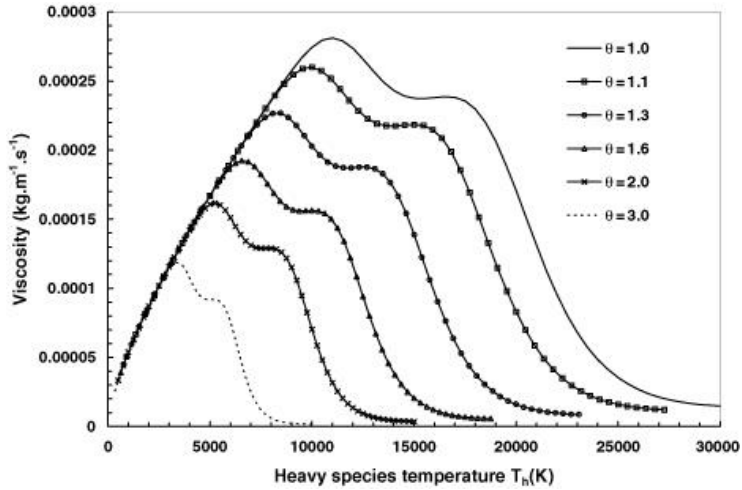


Figure 2-9. Viscosity of Ar-He mixture as a function of heavy species temperature (25 mol% of argon), for different values of the non-equilibrium parameter θ , at atmospheric pressure [30].

Figure 2-10 shows the electron temperature dependence of the thermal conductivity of an argon-helium mixture (25 mol% of argon), for different values of the non-equilibrium parameter θ , at atmospheric pressure. The main contributions to the total thermal conductivity are the electron translation thermal conductivity as well as the reaction thermal conductivity, which depends on ionization reactions (obtained with the modified Saha equation). As a result, the total thermal conductivity is plotted as a function of T_e .

At low temperatures, the translational contribution of heavy species is dominant. Below 10000 K, it can be seen that, at fixed T_e , the thermal conductivity, depending mainly on the heavy species temperature, decreases as θ increases due to a shift of curves plotting.

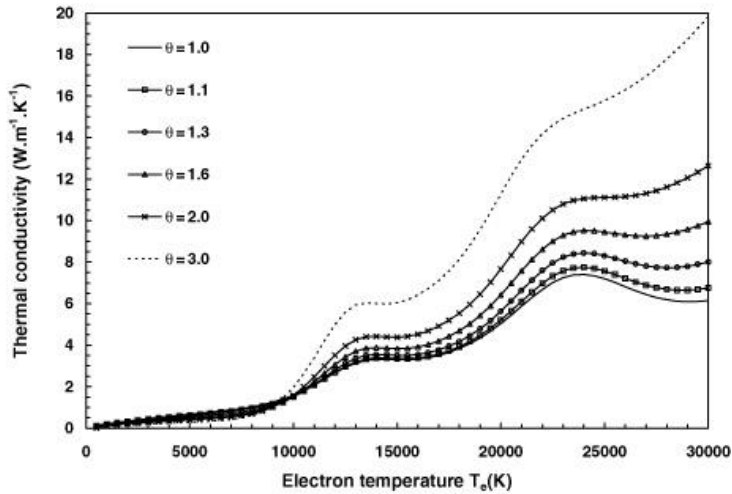


Figure 2-10. Electron temperature dependence of the thermal conductivity of an argon–helium mixture (25 mol% of argon), for different values of the non-equilibrium parameter θ , at atmospheric pressure [30].

2.2 Plasma Spraying

2.2.1 Plasma Spraying Processes

Plasma spraying has been developed since 50 years ago. Praxair, Plasmadyne, Metco and Plasma Technik, and Thermal Dynamics Corporation are examples of the company to develop the commercial plasma spraying device [36-38]. The plasma spray process utilizes a high energy to melt or evaporate feedstock particles, which are injected to penetrate the plasma torch. Using different spray technology, gas compositions, the efficient power, the pressure of the process environment, and the feedstock rate yield different microstructures of coatings deposited.

In the APS process, the feedstock particles are injected into the plasma plume outside the plasma gun by a carrier gas. An APS coating is deposited by completely or partially molten particles that impinge on a substrate, spread across the surface, and solidify into disc-like structures referred to as lamellae. During droplets spreading, the liquid may not yet wet completely the underlying surface, which will result in inter-lamellar pores. Adhesion in APS coatings is a result of the interaction of the melted powders with

previously deposited layers. SPS differs from APS primarily in that a liquid replaces the powder carrier gas. This change makes deposited coatings from nanometer-scale feedstock powders; further details are published [39, 40]. Latest researches of plasma spraying to control splats coating formation can be found in publications [41]. Two main parameters control the splat formation: the in-flight treatment of particles behavior and their interaction with the substrate surface on which they impinge [42-57].

In addition to splats deposition processes, physical vapor deposition methods such as electron beam physical vapor deposition (EB-PVD) are used to manufacture thermal barrier coatings [58]. EB-PVD is a process in which a focused high-energy electron beam is directed to evaporate particles in a high vacuum chamber (~ 0.05 Pa). The evaporated material condenses on the surface of the substrate [59]. During deposition, external heating is used to heat the substrate up to 1500 K for enhancing metallurgical bonding between the coating and the substrate [60]. EB-PVD is primarily a line-of-sight process; therefore, continuous rotation of the substrate is applied to deposit coatings of complex parts like turbine airfoils.

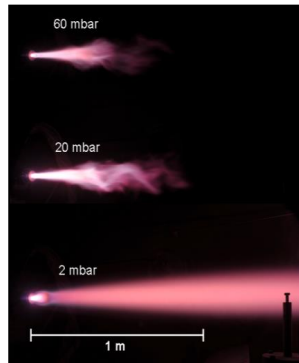


Figure 2-11. The influence of a chamber pressure on the plasma jet [61].

As shown in Figure 2-11, when the plasma spray operates under a reduced chamber pressure environment of 5-20 kPa, it is known as vacuum plasma spray (VPS). The combination of further reduced pressure (50-200 Pa) with high gun currents has led to the development of the plasma spray physical vapor deposition process (PS-PVD).

Figure 2-12 presents a schematic of PS-PVD process and a typical resulting columnar microstructure. PS-PVD is a process in which the feedstock powders are injected into the inside of plasma torch and are partially or completely evaporated. The evaporated materials are transported in the plasma jet to deposit columnar structured coatings on the substrate.

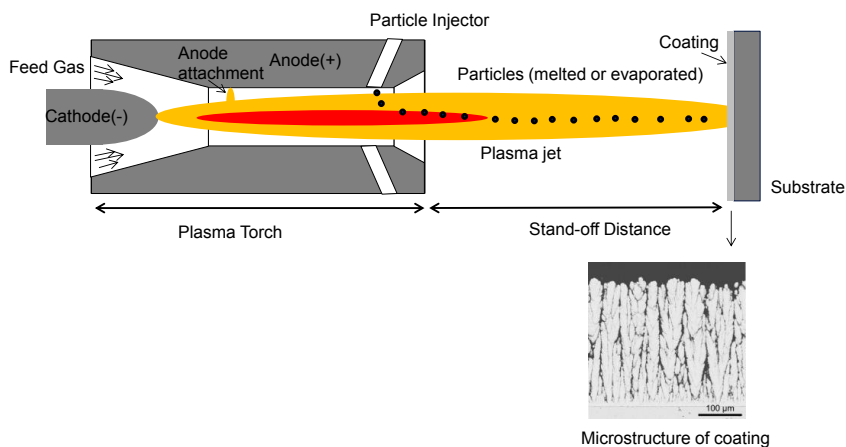


Figure 2-12. Schematic of plasma spray physical vapor deposition process, microstructure of coatings shown in [62].

The PS-PVD equipment used was developed by Oerlikon Metco AG (Switzerland) based on F4 or O3CP torch with internal power injections. In comparison to atmospheric plasma spray and vacuum plasma spray up to 90 kW, the PS-PVD process uses a high energy (up to 180 kW) torch operated at a working pressure below 200 Pa. Under these conditions, the plasma jet extends in the vacuum chamber reaching lengths up to 2 m and having a maximum visible diameter of 400 mm. The characteristics of PS-PVD such as gas compositions and stand-off distance of the sample provide the possibility to deposit a coating by melting the feedstock particles from liquid splats, but also from vaporized materials [61]. However, the effect of spray parameters on the microstructure of the columnar structures is not yet well understood.

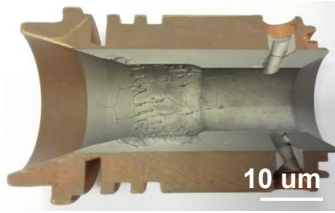


Figure 2-13. Cross-sectioned nozzle of an O3CP gun.

Using the converging-diverging O3CP nozzle in the experiments, as shown in Figure 2-13, the chamber pressure is significantly below the nozzle exit pressure. The plasma jet exits the nozzle at a supersonic speed. The pressure difference between the nozzle exit and the chamber pressure leads to the formation of shock diamonds in the flow. In the downstream direction, the jet adapts to have the same pressure with the chamber. At low chamber pressure, the environments influence on the plasma jet significantly decreases. Therefore, the high-energy distribution and different transport properties in the plasma plume allows the deposition of distinct microstructures of coatings.

2.2.2 Simulations of Plasma Spraying

The modeling of plasma spraying has to consider three main aspects: (1) influences of carrier gas on the jet dynamics, (2) particles' melting and diffusion, (3) particles' evaporation, and (4) coating formation.

The common computational flow dynamics (CFD) approach approximate the fluid conservation equations of continuity, momentum, species, and energy. The diffusion phenomena are considered by introducing relations between heat flux and temperature gradient, or between stress tensor and velocity, respectively. The strategy of CFD is to replace the continuous simulated domain with a control volume. The control volume should small enough to capture all relevant local values of the fluid characteristics, as well as large enough to make the continuum assumption meaningful.

2.2.2.1 Modeling of Plasma Flow Formation

The modeling of the plasma torch is highly nonlinear and characterized by its strong gradients in physical properties. The non-transferred direct current (DC) plasma torch involves the electrodes, cathode and anode regions, and arc column. The simulations of the plasma torch have been developed with many assumptions dealing with local thermal and chemical equilibrium (LTE and LCE). Their predictions give accurate and detailed results: transient behavior of the arc, prediction of the temperature distribution. However, the developing of thermal and chemical non-equilibrium (NLTE and NLCE) plasma torch combined with electrode sheaths are believed necessary for further advances in the prediction [35, 63, 64].

Near electrodes, the departure from ionization equilibrium and quasi-neutrality can be modeled by using sheath models to avoid artificial boundary conditions at electrode walls. Such approach requires at least two-temperature model, characterized by the ratio $\theta = T_e/T_h$.

The arc-cathode interactions behavior is calculated with imposing the arc current and the temperature at the rear face of the cathode; then the heat and current density distribution in the cathode region is calculated; a cathode sheath model is included that predicts the electron and ion density and temperature at the outer boundary of the sheath as well as the cathode voltage drop.

The description of the arc column is based on the coupling of fluid and electromagnetic equations and requires the thermodynamic (density, enthalpy, and specific heat) and transport properties (thermal and electrical conductivities, viscosity, and diffusion coefficients) of the gas mixture as well as its radiative properties [35].

The modeling of the plasma formation inside the torch with the surrounding anode has to address three main issues: (1) the displacement of the arc-anode attachment; (2) the arc reattachment process; (3) the phenomena at the plasma-anode interface [64].

2.2.2.2 Modeling of Plasma Jets

The plasma jet is distinguished into three different areas. The first region corresponds to the plasma jet core, i.e. the hottest zone which extends depending on a chamber pressure and in which the ambient penetration is low. In the second region, it acts as the transition zone toward the turbulence marked by the fast decrease of the plasma temperature because of the penetration of a chamber gas within the jet. The third region is where the temperature keeps decreasing as the plasma gas mixes more and more with the surrounding gas.

The vast majority of plasma jets are turbulent, such as in vacuum plasma spray and atmospheric plasma spray. Turbulent flows with a wide range of time and length scales exhibit irregular, random, and chaotic. The turbulence increases the exchange of momentum in boundary layers. The larger length scale of eddies are in the order of the flow geometry. The friction forces are larger the smaller eddies. Approximately 90% of the kinetic energy from larger scales is finally dissipated into eddies of smaller scales [65]. The turbulence enhances the uniform distribution of the temperature close to the boundary layer.

The simulation of plasma spray processes requires solving the Navier-Stokes equations for the continuum flow. Alternatively, the occurring vortices can be calculated using direct numerical simulation (DNS) that is commonly used to simulate Low-to-medium Reynolds-number turbulence typical of wind tunnel laboratory experiments [66]. However, it is less accurate and time-consuming. Large-eddy simulation (LES) is a numerical technique that describes a high-Reynolds number time-evolving and cuts off the high frequency or small-scale part of the turbulence spectrum [66]. The computational complexity of the LES models is 20 times higher than that of RANS simulations and substantially lower than that of DNS.

However, it is difficult to implement microscopic interactions into the macroscopic Navier-Stokes equation. In the other side, plasma jets with particles injection refer to one of the most complex flows, namely for its multiphase character during spraying. This includes interface instability, wetting dynamics, interfacial slip, and evaporation of particles [67]. Simulating these kinds of flows has always been a challenge to

conventional CFD because of the moving and deformable interfaces between phases or components originating from the specific interactions among the flow. The lattice Boltzmann method (LBM) is considered versus classical approaches to solve complex problems of heat and fluid flow. Its time-dependent scheme is in accordance with unsteady plasma jet [68, 69]. In LBM, the particulate kinetics provides a relatively easy way to incorporate the microscopic interactions by modifying the collision operator. Plasma jet and plasma spraying for a multiphase/multicomponent flow can be done by LBM simulation and modeling [70, 71]. It is generated automatically from the particle dynamics and no special treatment is needed to manipulate the interfaces as in traditional CFD methods. The LBM scheme is also employed for simulating the turbulent plasma flow in coupling with the mass, momentum and energy conservation equations [72, 73]. Moreover, LBM contains more physical connotation than Navier-Stokes due to the application of a mesoscopic discrete Boltzmann equation to describe the flow. However, an introduction of sound speed reduction is treated by LBM model is needed to simulate a compressible flow [74].

Three-dimensional simulation of plasma torch with asymmetric temperature and velocity distributions at the nozzle exit, which are obtained from the plasma arc model, to clarify the three-dimensional effect of nozzle exit profiles on the plasma jet characteristics [75]. Standard K- ϵ model is used to account the turbulent characteristics of the plasma jet. It is concluded that plasma jet velocity shows stronger three-dimensional effect than temperature.

K. Bobzin et al [76] has shown the flow characteristics of atmospheric plasma jets generated by means of a three-cathode spraying system. Among all RANS models investigated in this study, the SST turbulence model yielded the best agreement with LES. SST turbulence and k- ω revealed similar results for free flows. At wall-boundaries, k- ω models showed a satisfactory accuracy. The focus was placed on to the turbulence and diffusion/demixing modeling. The author also has shown that the significance of diffusion-driven mixing is negligibly small in comparison with that of turbulence-driven mixing for plasma spraying. Numerical calculations related to the comparisons of between turbulent and laminar plasma jet have been published [77-87]. It can be

summarized that the entrainment of surrounding cold gas into the plasma jet is detrimental in terms of particle melting as well as particle acceleration.

2.2.2.3 Modeling of the Particles Treatment in Plasma Jets

The modeling of the plasma jet has advanced greatly in the last 15 years due to a better understanding of the underlying physics, development of computational fluid dynamics software and access to high performance and cloud computing. The fluid dynamics and properties of the plasma jet is controlled by the plasma formation, dynamic behaviors of the arc, melting, evaporation and vaporization of feedstock particles and the coating formation [88, 89], while the interactions between the feedstock particles and the plasma are not completely understood yet. Particularly, in the PS-PVD process, feedstock particles are introduced to the inner side of the torch.

The particle trajectory within the high-energy plasma jet depends on its acceleration of jet flow on it. This acceleration is proportional to the flow velocity and viscosity, but inversely related to the specific mass and diameter of the particle. The heat transfer mechanisms between the hot flow and a single particle is determined by convective heating and radiative losses of the particle. To obtain completely evaporation of a particle, the energy transferred by the plasma onto the particle during the residence time must be larger than the energy required for heating, melting and evaporating the particle. There are reveal possibilities to increase the heat transfer to the particle [90]: (1) enhanced heat transfer coefficient (higher thermal conductivity), (2) increased residence time of the particle in the plasma, (3) raised plasma temperature, (4) reduced particle diameter. Hong-Bing Xiong et al [91] has shown the melting behavior of in-flight particles in plasma spray process.

Coatings applied via atmospheric or vacuum plasma spraying are composed of splats which emerge when semi-molten and molten powder particles which are deposited on the substrate, while coatings produced by PS-PVD consists of columnar structures. Characteristic of particles state involved in the coating formation, i.e., their temperatures, velocities, diameters, and melting or evaporation index, determine the performances of the coatings. The above-mentioned properties of particles greatly depend on the heat and momentum transfer between plasma jet and feedstock particles. Comprehensive recently

literature reviews on the modeling of the plasma spraying have been published [76, 92-101].

The computation of particles' velocities, temperatures, and trajectories without consideration of evaporation is shown in [102]. The only viscous drag force acting on a particle was considered as the only driving force. The motion of particles is governed by Newton's second law, which, after integration, gives the trajectory. Due to the consideration of carrier gas influence, the particles are more dispersed.

P. Fauchais [103] presents developments in direct current plasma spraying of suspensions. It explains the interactions between the liquid feedstock with sub-micrometric particles and plasma jet, and concludes by linking the coating microstructure with the liquid processing the plasma jet. K. Pourang [104] studied suspension plasma spray both experimentally and numerically. A two-way coupled Eulerian-Lagrangian approach was solved by ANSYS Fluent software. The suspension was modeled as a multi-component droplet that undergoes break up and evaporation. At the standoff distance of 50 mm, plasma axial velocity was found to be around 800 m/s and plasma temperature was calculated to be about 3500 K. A large body of literature published related to suspension plasma spraying since 2010 [39, 40, 105-113].

2.3 Coating Deposition

2.3.1 Thermal Barrier Coatings

Thermal barrier coatings (TBCs) are increasingly being applied to the surfaces of metallic parts in the hottest part of gas-turbine engines [114, 115]. Yttria-stabilized zirconia (YSZ) is still the state-of-the-art ceramic material for TBC applications. While the coating provides a thermal barrier, it does not block oxidation of the underlying metal, because ZrO_2 is a fast oxygen-ion conductor at high temperatures. As a result, an oxide (termed thermally grown oxide, TGO) gradually grows at the interface between the metal and the coating. Indeed, the bond coat is applied to the metal prior to the deposition of the thermal barrier coating. It promotes the formation of a highly stable, protective aluminum oxide phase during oxidation. Figure 2-14 illustrates the structure of TBCs. The

application of TBCs increases the working environment temperature of the turbine by 400 K, including the development of single-crystal Ni-based superalloys.

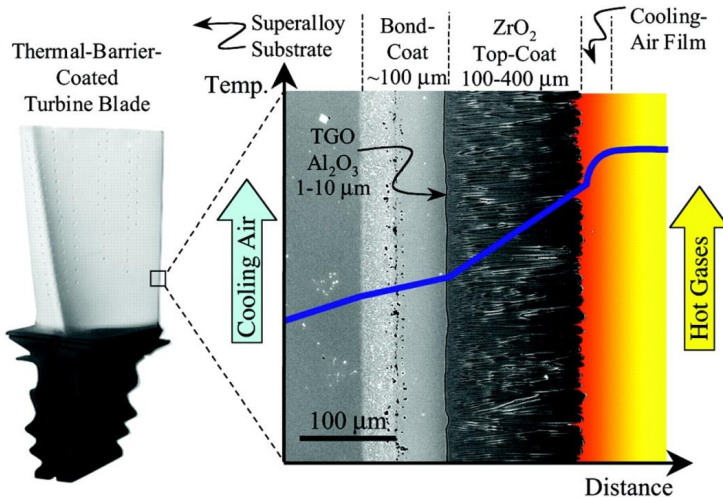


Figure 2-14. The structure of turbine blade with thermal barrier coatings. The left turbine blade contains internal hollow channels for air-cooling, the right is the detailed structure of thermal barrier coatings [116].

Thermally sprayed ceramic deposits are characterized by lamellar microstructure produced by APS resulting in a low thermal lifetime due to a sensitive thermal expansion mismatch. The porosity is up to 20%, which results from incomplete wetting of molten liquid on the rough substrate surface. The voids in the coating have greatly influence on mechanical (elastic modulus and stress at failure) and physical (thermal conductivity) properties. TBCs produced by APS with economical benefits and better insulation are applied in the intermediate temperatures environment. Further application of thermally sprayed ceramics are applied to solid oxide fuel cell (SOFC) [117, 118] and membranes [119].

Coatings of columnar structure can be produced by, suspension plasma spraying (SPS), plasma spray physical vapor deposition (PS-PVD) process and electron beam physical vapor deposition (EB-PVD) process. PS-PVD process produces fully or incomplete evaporated vapor condensed onto the surface of the substrate, while EB-PVD is an

atomistic deposition process. As to SPS, particles are dispersed in the solvent to decrease the size of the original particles, and then are injected into the plasma jet. After the solvent vaporization, melted particles spread over the substrate in the same way as for APS. Nevertheless, SPS requires lower stand-off distances (for example 50 mm) to void re-solidification of nanoparticles.

2.3.2 Growth Mechanisms of Columnar Microstructures

In SPS process, a higher proportion of smaller splats (average diameter $\sim 3.3 \mu\text{m}$) facilitate the deposition of columnar YSZ coatings described by Chen et al [120]. High-magnification SEM images indicate that SPS YSZ intra-columns have a similar microstructure to conventional APS coatings, but with much thinner lamellar thickness. The substrate surface roughness has a strong influence on the SPS coatings. The rougher the substrate surface, the less uniform the coating that could change from free of vertical cracks and columns to deep vertically cracked (DVC), and even to columnar. A rougher substrate surface lead to a higher drag force level by the plasma gas flow, which make fine SPS droplets with a higher lateral impinging velocity resulting in a high potential to develop columnar structures on the substrate with a roughness [121]. As shown in Figure 2-15(a), SPS coating porosity presents a uniform distribution in space within the layer thickness compared to EB-PVD coating for which porosity is mainly located in the fringe of the columns.

The diameter of the columns of EB-PVD YSZ coatings starts from less than $2\text{-}3 \mu\text{m}$ on the substrate surface and increases at the column tip to $10\text{-}20 \mu\text{m}$ [122]. These columns are mainly separated by inter-columnar gaps. Inter-columnar gaps are a few nanometers width close to the substrate and can be large as $1 \mu\text{m}$ at the coating tip. The high thermal shock-resistance of the EB-PVD processed TBCs is a result of the presence of these inter-columnar gaps. Most of the open porosity originates from the voids present between nano-sized secondary columns, so-called feather-arms, growing at the column edges, as shown in Figure 2-15(b). These are formed mainly by shadowing, depending on the rotation speed, the substrate temperature and the angle between the substrate and incident vapor. Due to the interruption of the vapor deposition during rotation, intra-columnar voids are created in form of channel-like pores. It should be mentioned that EB-PVD

generally produces quasisingle crystalline columns with a predominantly $\langle 100 \rangle$ orientation [120].

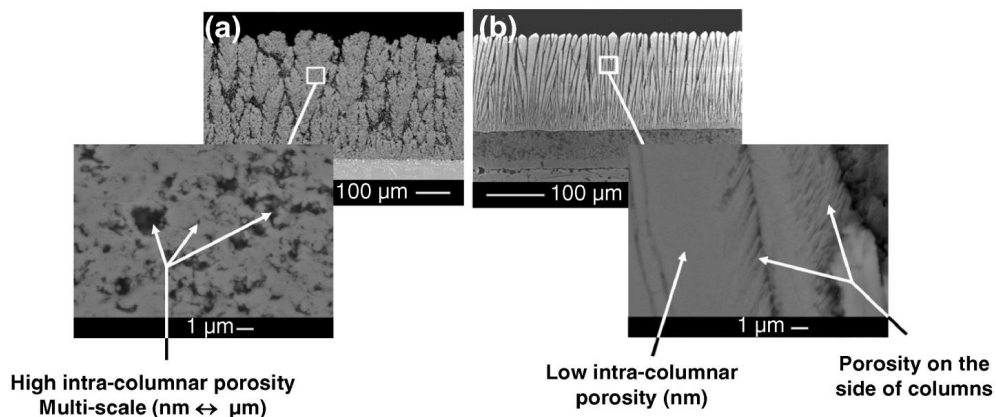


Figure 2-15. Intra-columnar porosity in SPS (a) and EB-PVD (b) coatings [121].

2.3.3 Microstructures Produced by Plasma Spray Physical Vapor Deposition

The PS-PVD coatings are commonly splat-like or columnar, deposited from molten feedstock particles and feedstock vapors, respectively [4, 123-127]. These two types of microstructures are related to different plasma energies and compositions. Heat transfer to particles injected in the flow occurs mainly by conduction through the boundary layer surrounding particles. The heat flux, of course, follows the same trend as the thermal conductivity of the plasma [128]. If the heat transfer is much higher with appropriate plasma gas mixtures, for example 35Ar-60He, zirconia can efficiently evaporate, and the structure of the deposited coating is columnar that is similar to columns produced by EB-PVD [60]. Figure 2-16 shows the microstructure deposited by PS-PVD. The vaporization degree of the powder can be controlled by the plasma gas composition and the powder feed rate [129, 130].

100Ar-10H₂ plasma yield a very low degree of vaporization due to low temperature, as shown in the top graph of Figure 2-16. Consequently, a high powder feed rate can result in splat-deposition. Hydrogen dissociation consumes a remarkable portion of energy that will lead to a significantly lower maximum temperature of the plasma jet. The slight

increase of the temperatures at the substrate surface are associated to the release of the dissociation energy.

Hot ^{35}Ar - ^{60}He plasma combining with a low feedstock rate yield a high degree of vaporization, which leads to a real vapor deposition which is comparable to the coatings by EB-PVD, as shown in bottom graph of Figure 2-16. The middle graph of Figure 2-16 shows that a high feedstock rate results incompletely evaporated particles (clusters).

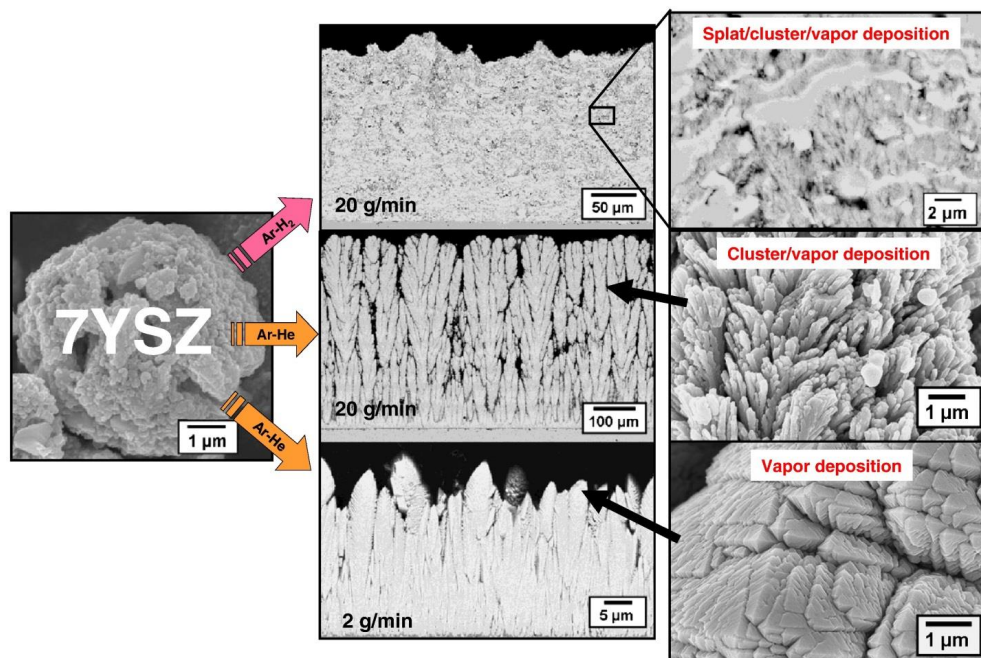


Figure 2-16. SEM images produced by PS-PVD at different parameters, the left is morphology of YSZ particles, the middle is the resultant microstructures for different feeding rate, and the right is the detailed microstructures corresponding to the middle [129].

Optical emission spectroscopy (OES) is used to verify the influence of specific plasma parameters with the injected ceramic materials on the resulting microstructures. Figure 2-17(a) shows the spectrum of the plasma jet with injected YSZ powders that produce splat-like coatings. The intensity of the spectral lines coming from the YSZ species is low,

which presents that only a minor amount of the coating material is evaporated. In Figure 2-17(b), the spectrum shows an increased overall intensity of the spectral YSZ lines which cover the full-wavelength bandwidth of the spectrometer (350-900 nm). The spectral lines correspond to the different species contained within the YSZ, namely, zirconium and yttrium. Here, the injected material could be vaporized which allows the growth of columnar-structured coatings.

A typical EB-PVD 7YSZ TBC microstructure in polished cross section can be seen in Figure 2-18(a). EB-PVD produced coatings consist of a quite homogeneous columnar structure composed of compact single columns. The bulk structure is characterized by inter-columnar gaps and voids between feathery structures. In contrast, PS-PVD produced coatings consist of many fine needles with a high amount of internal porosity, as shown in Figure 2-18(b).

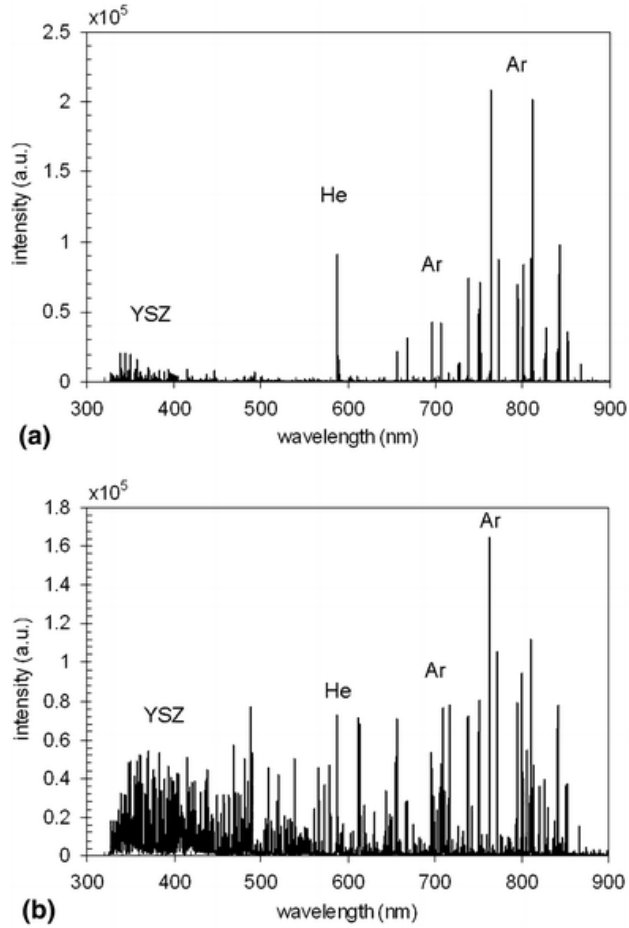


Figure 2-17. Optical spectrum of the plasma jet (Ar/He) with 7YSZ corresponding to coatings having (a) no columnar structure and (b) with columnar structure [5].

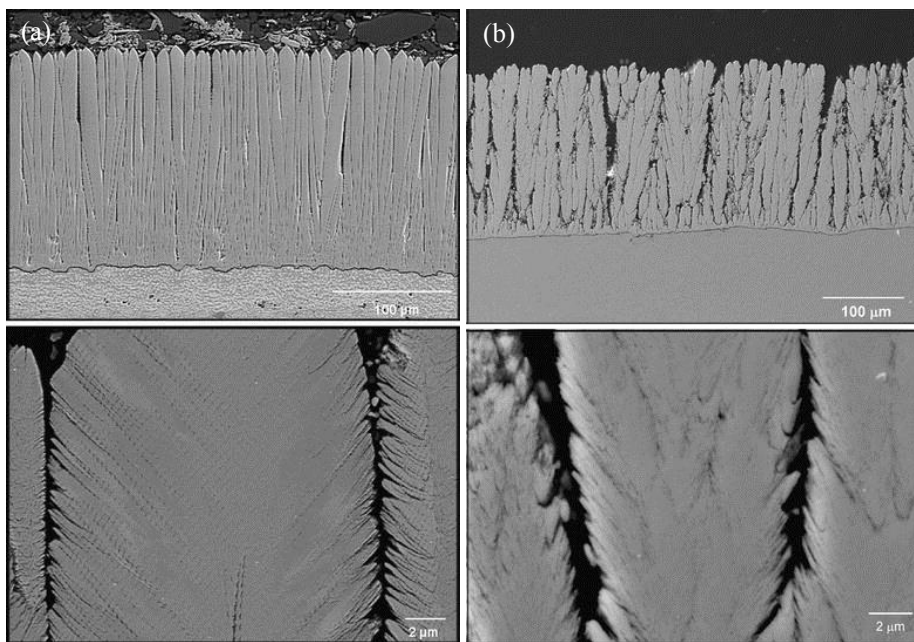


Figure 2-18. Typical EB-PVD 7YSZ TBC microstructure in cross section (a) and columnar TBC top layer deposited with PS-PVD on a MCrAlY bond coat (b) [131].

2.4 Modeling of Columnar Microstructure Formation

Monte Carlo methods start with random inputs from a probability distribution then perform a deterministic computation on the inputs to obtain numerical results. An overview on the Monte Carlo model for simulating microstructural evolution can be found in [132-139].

The morphology of the depositing film is determined by the characteristics of the incident vapor or droplets, the surface roughness, and the surface mobility of the deposited atoms, the presence of geometrical shadowing and surface diffusion [140]. The EB-PVD coatings with preferential crystal orientation deposit from atomically dispersed vapor plume at a very low deposition rate [141, 142]. Deposition rates up to 240 $\mu\text{m}/\text{min}$ of PS-PVD process result in no prominent crystal orientation, except for at specified high temperature near the substrate [61]. Two-dimensional Monte Carlo simulations have been

conducted to provide insight on the evolution of columns [143, 144]. This model is implemented on a molecular scale that incorporates the effect of self-shadowing.

The respective columnar microstructures forming in PVD layers are controlled by self-shadowing, surface diffusion, and bulk diffusion as substrate temperature increases [145]. This porous columnar structures form when the incident vapor phase particles impinge on a substrate and insufficient diffusion does not overcome the influence of the self-shadowing [146]. As the substrate temperature increases surface diffusion is activated. The columns evolution from densely, well-defined microstructure to equiaxed grains with recrystallization occur as the further increase of temperature to activate the possibility of bulk diffusion [147, 148].

Y.G. Yang [137] utilized a kinetic Monte Carlo (KMC) method to simulate void evolution of a zig-zag coatings. The pore morphology strongly depends on the incident vapor flux distribution. Theron M. Rodgers [136] quantifies the simulation of nickel coatings with those from experimental depositions. The author investigates high vacuum physical vapor deposition to predict variations in coating thickness, columnar growth angle, and porosity during both stationary and substrate rotated deposition.

Deposition rates by the PS-PVD process are two scales higher than those that of EB-PVD process [123, 149]. When the deposition rate is low, particles (gases, molecules or clusters) migration is possible. The probability of diffusion to the shadowed areas occurs when the jump attempt time is smaller than the time interval between particles arrivals at low deposition rate, or when at high substrate temperatures the energy barrier is low for possible diffusion. Even though a numerical simulation of columnar microstructures in EB-PVD process by Monte Carlo technique with consideration of self-shadowing and kinetic diffusion [136, 137, 150], the simulation of columnar microstructures in PS-PVD process including self-shadowing is rare. The PS-PVD process has also been proved to deposit coatings on the shadowed areas of the substrate [129].

2.4.1 Effect of Adatom Surface Mobility

Typically, the film near the interface is influenced by the substrate and or interface material and it takes an appreciable thickness before the film establishes a particular

growth mode. After a growth mode has been established, the film morphology can be described by a structure zone model (SZM), as shown in Figure 2-19. The SZM was first applied to vacuum-deposited coatings by Movchan and Demchishin (MD) in 1969 [136]. Later, the SZM was extended to sputter-deposited films by Thornton [151], and later modified by Meissner [145] to include point defect agglomeration and void coarsening with thickness.

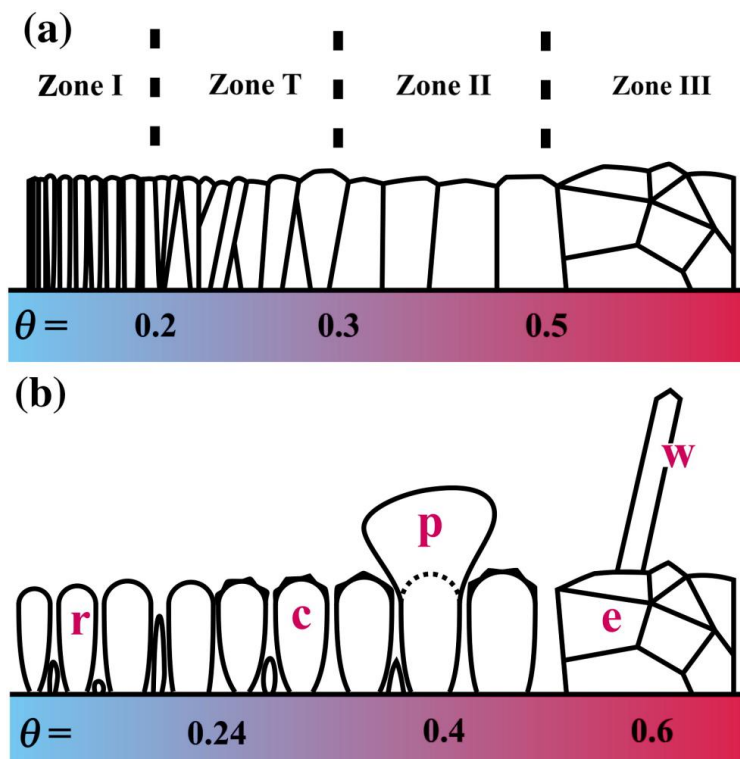


Figure 2-19. (a) Structure zone model for thin films deposited by physical vapor deposition [151, 152]. The x-axis shows the deposition temperature $\theta = T_s/T_m$. (b) Corresponding schematic for layers deposited by glancing angle deposition, showing rods (r), columns (c), protrusion (p), equiaxed grain (e), and whiskers (w) [153].

Shadowing controls the film microstructure and texture in Zone I, and the film is columnar with tapered voids between columns. In Zone II, surface diffusion is the

leading process that controls the morphological evolution, and the film consists of columnar grains with defined dense grain boundaries, faceted top surfaces, and an increased grain width. In Zone III, the microstructure is governed by bulk diffusion, and the microstructure exhibits equiaxed grains.

2.4.2 Effect of Angle-of-incidence

The columnar growth also depends on the angle-of-incidence of the atom flux. The more off-normal the deposition is, the more prominent is the columnar growth. As the nuclei form, the shadowing effect will quickly become a dominant factor in the film growth. Shadowing leads to the formation of columns inclined towards the source. It has been conclusively demonstrated that the column tilt angle is less than the deposition angle, as shown in Figure 2-20 and 2-21. The shadowing effect is highlighted if the vapor flux is off-normal so that the valleys are in “deeper shadows” compared to the situation when the flux is normal to the surface.

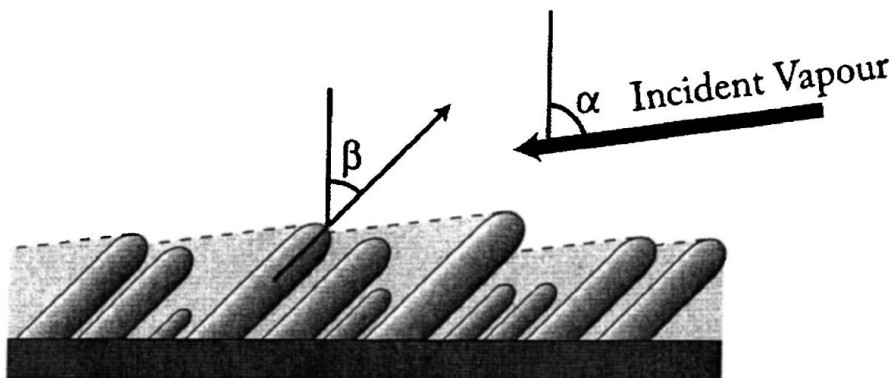


Figure 2-20. Columns will grow oriented toward the source, forming an angle β with the substrate normal ($\beta < \alpha$) [146].

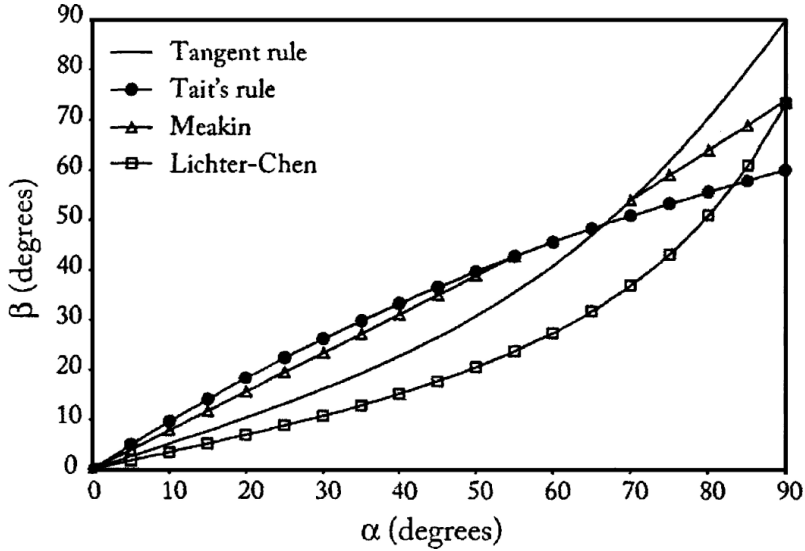


Figure 2-21. Plot of four different analytic curves relating the column tilt angle β and the deposition angle α [146].

2.4.3 Effect of Substrate Parameters

2.4.3.1 Diffusion and Surface Temperature

Surface diffusion counteracts the effect of shadowing. Fick's law, moving adatoms from the columns tips toward the shadowed areas, governs the diffusion. Surface diffusion can be considered as a thermally activated Arrhenius-type process. The displacement of the adatoms over the substrate surface is proportional to \sqrt{Dt} (D the diffusion coefficient, t the diffusion time). Surface diffusion is linked to the substrate temperature and the deposition rate. Higher temperatures and slow deposition rate (EB-PVD) will increase the diffusion distance, whereas lower temperatures and rapid deposition (PS-PVD) will limit diffusion.

2.4.3.2 Roughness of the Substrate Surface

VanEvery et al [108] proposed that the column size of column formation in SPS YSZ coatings is strongly influenced by the surface topography. Small droplets of 1 μm , their

deposition trajectory will follow the parallel flow to the surface for some distance before they impact a surface asperity. Thus, the individual columns form by progressive built up of particulates on surface peaks. Smoother surfaces tend to generate a higher density of columns. When the surface is rough, the peaks receive the adatom flux from all directions and, if the surface mobility of the adatoms is low, the peaks grow faster than the valleys due to geometrical shadowing.

Park et al [154] reported that the roughness of the substrate affected the growth behavior of the EB-PVD YSZ coatings, but has not found any evident influence on the width of columns. Smooth surface areas lead to regular and uniform columns. Dense and inclined columns are deposited at a rough area due to non-uniform distribution of atomic vapor flux resulting from diffusion. Therefore, the film growth behavior can be different at different location of the surface.

3 Theoretical Methods

3.1 The Plasma Jet Modeling

3.1.1 Assumptions

The simulation of the plasma jet is based on the following assumptions:

- The jet can be represented by a 2D axis-symmetrical flow field;
- The plasma is in chemical and the thermodynamic equilibrium;
- The condition of quasi-neutrality holds;
- The plasma is optically thin, the emission coefficients and the observed intensities are directly proportional;
- The plasma gas and chamber gas have the same composition;
- Gravitational effects are considered to be negligible;
- Arc dynamics influence on the plasma jet is not considered, therefore, the amplitude of the temperature and velocity at the nozzle exit is a 2D time-averaged value and validated by net power.

3.1.2 Mathematical Modeling

The computational domain is displayed in Figure 3-1. The plasma jet is treated as a compressible, reacting with temperature-dependent thermodynamic and transport properties with the assumption of local thermodynamic equilibrium. The plasma jet is described as a symmetrical, two-dimensional geometry. Detailed descriptions of the governing equations for the mass, momentum and energy conservation equations for the plasma mixture can be found in literature [140].

Plasma gas leaves the plasma torch at the nozzle outlet at high temperatures and velocities. The temperature is verified by the efficient power. In the laminar flow, the flow is dominated by the object shape and dimension (large scale). In the turbulent flow, the flow is dominated by the object shape and dimension and by the motion and evolution of small eddies (small scales). Turbulent flow is chaotic, random, and irregular.

Particularly, the boundary layers and the wakes around and after the substrate are turbulent.

The continuity equation for the mass, momentum and energy conservation equations for the flow used to model the plasma jet is based on Navier-Stokes equations. Two-equation models Shear-Stress Transport (SST) k - ω model are used that shows a satisfactory accuracy to model the walls. It was developed by Menter [155]. The simulation of the plasma jets in the steady-state are solved by pressure-based coupled solver [156]. In the case of slip flow, Dmitrii Ivchenko et al has shown the continuum breakdown of the flow at very low pressure plasma spray conditions [157].

The temperature and pressure dependent thermodynamic properties of the plasma gas are required in the literatures [158]. The transport property (viscosity and thermal conductivity) data is used in the NASA Lewis Research Center's Chemical Equilibrium and Applications Program (CEA). It complements transport property coefficients are independent of pressure.

3.1.3 Geometry and Boundary Conditions

The computational domains with its geometrical dimensions are composed of nozzle (torch region) and chamber where the plasma jets extend, as illustrated in Figure 3-1. Table 3.1 summarizes boundary conditions of the computational domains. The boundary conditions include the nozzle wall and a chamber wall. Nozzle wall represents the wall of the water-cooled anode, defines as a no-slip wall at a constant temperature of 350 K. Nozzle inlet means plasma forming gas inlet where the composition of feedstock gases are obtained from [159], and is defined as mass flow inlet with a high constant temperature adjusted to the efficient power in the nozzle exit of 60 kW [160]. Pressure outlet at a constant value means boundaries of a chamber ranging from 200 Pa to 10,000 Pa are used according to the case studied. The plasma spray operating parameters are summarized in Table 3.2.

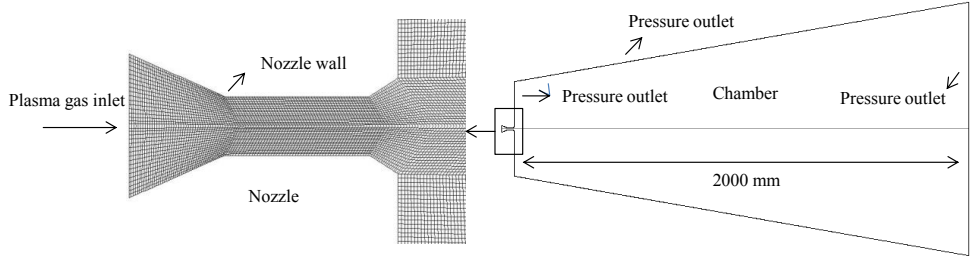


Figure 3-1. The computational domain.

Table 3.1. Boundary conditions

Boundary conditions	
Nozzle wall	No-slip wall
Nozzle inlet	Mass flow inlet
Chamber wall	Pressure outlet

3.2 Plasma Composition

Compositions of two-temperature plasmas in local chemical equilibrium (LCE) were derived following by the minimization of Gibbs free energy [161-163], or by Potapov's method [164, 165], or by kinetic calculation [166], or by Van de Sanden et al [33, 164].

The plasma is considered to be in local thermodynamic equilibrium (LTE) when the Maxwell-Boltzmann distribution describes the kinetic energies of each species, the Boltzmann distribution describes the excited states, mass action laws describe the species densities. LTE allows the conservation equations (of mass, momentum, and energy), provided the thermodynamic state of the plasma and the transport coefficients.

The plasma is assumed to be in chemical equilibrium; therefore, according to the assumptions in section 3.1, its composition is determined by the minimization of Gibbs free energy, the quasi-neutrality condition and Dalton's law of partial pressures [12]. For an Ar-He-H₂ plasma and the temperatures considered in this study, the plasma is primarily composed of eight species (i.e. He, He⁺, H₂, H, H⁺, Ar, Ar⁺, and e⁻). In PS-PVD

process, 35Ar-60He plasma is used in contrast to non-equilibrium studies of thermal plasmas.

Minimization of Gibbs free energy leads to the derivation of Van de Sanden et al equations [12]. Even though two alternative forms of non-equilibrium Saha equations have commonly been used in the literatures [167-169]. Saha equations of the following form is used by lack of the exponent $1/\theta$, in the left hand side of equation 3.1.

$$\frac{n_e n_i}{n_a} = \frac{2Z_i(T_e)}{Z_a(T_e)} \left(\frac{2\pi m_e k T_e}{h^2} \right)^{3/2} \exp \left(-\frac{E_i}{k T_e} \right) \quad (3.1)$$

The following equation is generalized by Dalton's law of partial pressures

$$n_i + n_a + \theta n_e = \frac{p}{k T_h} \quad (3.2)$$

The quasi-neutrality condition is stated as

$$n_i = n_e \quad (3.3)$$

Where n_e , n_i , and n_a , are the concentrations of electrons, ions, and atoms, respectively. $Z_i(T_e)$ and $Z_a(T_e)$ are the internal partitions functions of ions and atoms as a function electron temperature T_e , respectively. E_i is the ionization energy. k is the Boltzmann constant, m_e is the electron mass. θ is non-equilibrium parameter.

Equations 3.1 to 3.3 allow the calculation of the plasma composition for different non-equilibrium parameter at a pressure of 200 Pa in PS-PVD process. The plasma composition in the local thermal equilibrium (LTE) model is given by $\theta=1$. Calculations of the plasma compositions and the spectral line intensities are used to investigate the non-equilibrium parameter of plasma jets.

3.3 Spectral Line Intensities

Once the plasma composition is known, the spectral line intensity of the monatomic species (atoms and ions) is calculated by

$$I(\lambda_{mn}) = \frac{1}{4\pi} \frac{hc}{\lambda_{mn}} A_{mn} g_m \frac{n_j}{Z_j(T_e)} e^{-E_m/kT_e} \quad (3.4)$$

Where h is the Planck's constant, c is the speed of light, A_{mn} is the transition probability, λ_{mn} is the wavelength between the upper level m and lower level n , g_m is the statistical weight, E_m is the energy of the upper level, n_j is the total concentration of the species j , and $Z_j(T_e)$ is the internal partition function calculated at electron temperature T_e . These parameters are taken from the NIST atomic spectra database [170].

3.4 Monte Carlo Simulation of Columns Growth

3.4.1 Assumptions

Two-dimensional Monte Carlo simulation of columns growth in the PS-PVD process is based on the following approximations:

1. Surface and bulk diffusion is neglected due to the fast deposition rate;
2. Particle coagulation is neglected;
3. No collisions between incident vapor particles;
4. The effect of self-shadowing on the columns growth is considered;

3.4.2 Two-dimensional Computational Procedure

A Monte Carlo algorithm is used to simulate the deposition of particles in two dimensions [143]. The modeling is conducted using a 5000×1000 ($x \times y$ pixels) grid with periodic boundary conditions. The modeling include two steps to investigate the formation of columnar microstructures: Firstly, the incoming particle deposits on the substrate surface considering shadowing, Then, the newly deposited particle relaxes to a stable site.

A sketch of the deposition process explains the computational procedure, which is shown in Figure 3-2. Each square represents one particle position. It is possible to grow in the x -direction and y -positive direction. Particles are allowed to deposit at free site. The bottom represents the surface of substrate, α represents the incident angle of the vapor flux

relative to the substrate normal. The pair of seeds is used to make sure that a newly deposited particle has at least two neighborhoods.

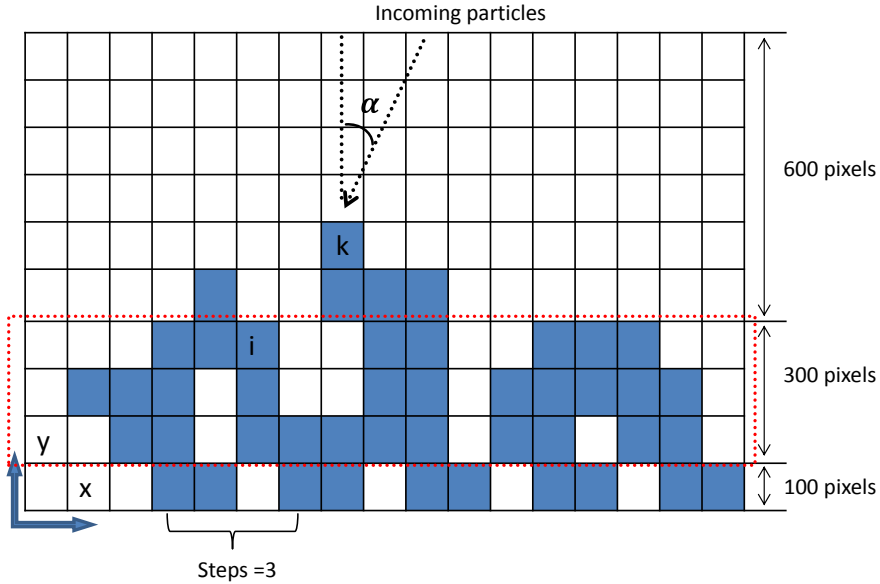


Figure 3-2. A sketch of the deposition process. The width and height of mesh are 5000×1000 ($x \times y$ pixels). The bottom represents the surface of substrate. The marked area (analyzed area) in red dash line is used to calculate porosity. “Steps = 3” means that one free sites at the beginning of simulation. The arrow is the direction of incoming particles. Self-shadowing refers to along the trajectory of incoming particles position particle (i) can not grow due to a previously deposited particle (k) blocks the incoming flux.

Before the deposition begins, a pair of seeds occupy the substrate sites of the simulation cell for different seed distances (steps are assumed as 2 or 10, if substrate is planar, $y = 0$), whereas the rest of the lattice is empty; each particle is dropped from a randomly chosen y position at a height 1000 with a random traveling angle α relative to the substrate normal following the normal distribution (μ, σ) in Figure 3-3. Injecting vapor particle travels along a straight line (assuming no collisions occur with other gas atoms) towards the substrate in the direction of the vapor flux (varying between -90° and 90°). Subsequently, particles are allowed to deposit on any of the exposed surface of an already

deposited particle. All new particles are assumed to bind with the other already deposited particles after checking the surrounding neighbors to establish the newly deposited particle having at least two neighboring sites along the direction of the incoming particle. The diagonal neighbors are considered so that a deposited particle can have maximum 8 neighboring sites. As shown in Figure 3-2, we use already deposited particle k as an example, if a newly traveling particle with a angle α relative to the substrate normal, it deposits on the top position of the particle k, then checking it neighbors and finding a position at the left of the particle k with two neighbors, finally the newly coming particle will deposit in the left position of the particle k.

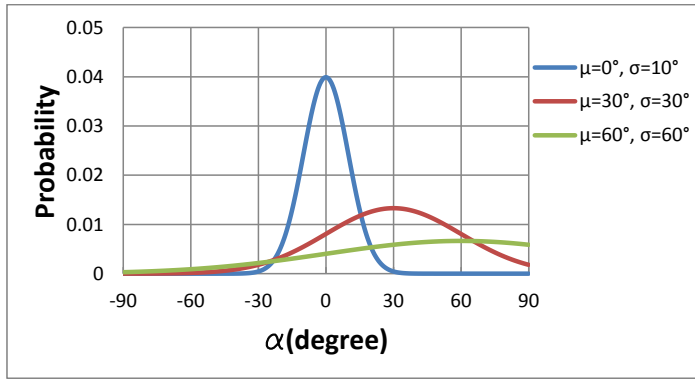


Figure 3-3. Normal distributions of incoming vapor flux ranging from -90° to 90° .

The averaged porosity is calculated in the marked area of the deposition process. The influence of distance of seeds and top free-space are ignored. It refers to only the bulk area of columns considered. The orientation of columns is analyzed by averaged-angle of different titled columns.

4 Experimental Methods

4.1 PS-PVD Equipment

Plasma spraying was employed on a Oerlikon Metco PS-PVD Multicoat System with the O3CP gun (Switzerland). Images of plasma jets were taken depending on chamber pressures ranging from 200 Pa to 10,000 Pa to compare to my simulated results and a power input of 120 kW were used in the experiment. The net power was 60 kW.

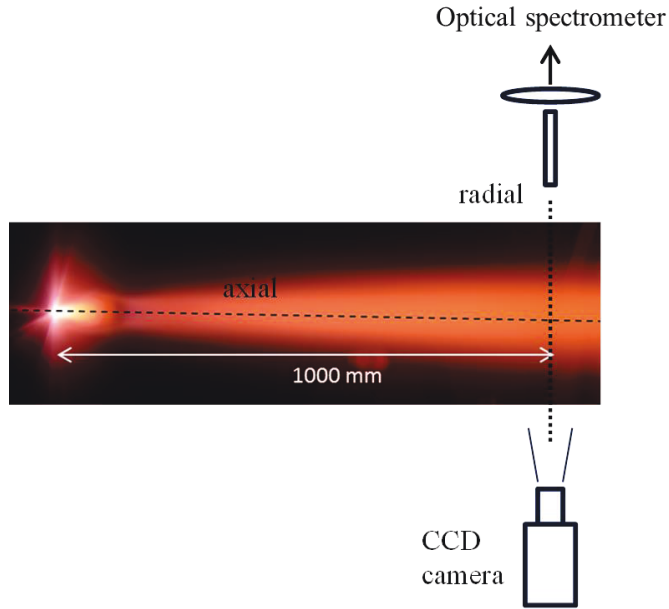


Figure 4-1. The process of optical emission measurement.

4.2 Plasma Jet Characterization

In order to validate the calculated spectral line intensities, Optical Emission Spectroscopy (OES) that has been done by the peer PhD-candidate Wenting He, they are compared it to the measured integrated spectral line intensities. OES is used as a common technique to determine the relative spectral line intensities for atoms and ions in the UV/visible range.

For plasma characterization, the spectrometer applied for plasma characterization was an ARYELLE 200 (Laser Technik Berlin (LTB), Berlin, Germany) scanning a wavelength range of 381-786 nm. Plasma radiation was collected through a borosilicate glass window and an achromatic lens, transferred by an optical fiber to the 50 μm entrance slit and detected by a 1024x1024 CCD array. The system was equipped with an Echelle grating and the spectral resolution obtained is 15.9-31.8 pm [160]. In the experiment of the OES measurement, the integrated relative intensity was measured as a function of radial distance (0 mm -100 mm) at the axial stand-off distance of 1 m at a chamber pressure 200 Pa, as shown in Figure 4-1.

Table 4.1. The plasma spray operating parameters

Plasma gun operating conditions	
Nozzle exit diameter, mm	20
Current, A	2750
Effective power, kW	60
Plasma gas flow rate Ar/He, slpm	35/60
Plasma gas flow rate Ar/He/H ₂ , slpm	35/60/10
Plasma gas flow rate Ar/H ₂ , slpm	100/10
Chamber pressure, Pa	200-10000
Spray distance, mm	1000

slpm (stand liter per minute)

4.3 Coating Characterization

The PS-PVD process for a 35Ar-60He plasma mixture with YSZ powder injected operates at a chamber pressure of 200 Pa. The net power of the process is 60 kW. Two types of coatings were produced by PS-PVD, in which two orientations (horizontal and vertical) towards the axial center of the plasma jet are used at the stand-off distance of 1m. Cross-sections of the PS-PVD coatings were observed by a scanning electron microscope

(TM3000, Hitachi High Technologies Europe GmbH, Krefeld) and surface morphology was investigated with Lasermicroscope-Cyberscan (VK9700, Keyence Germany GmbH, Neu-Isenburg, Germany). The main aim of the two substrate orientations is to evaluate the deposited coating structures.

5 Results and Discussions

5.1 Thermodynamic and Transport Properties

The thermodynamic (specific heat, enthalpy, and entropy) and transport (viscosity and thermal conductivity) property data provided with the CEA program are given as functions of temperature as high as 20000 K in the form of least-squares coefficients [158]. The minimization-of-free-energy formulation is used to describe the chemical equilibrium in the CEA program [171]. Zeleznik [172] presents equations based on minimization of Gibbs energy.

For the monatomic gases (Ar and He), when temperature increases, first the density of argon or helium decreases following the ideal gas law, and then progressively ionization takes place. Figure 5.1 presents the compositions for 35Ar-60He-10H₂ plasma at the pressure of 200 Pa. At 5000 K for Ar the ion density is four orders of magnitude lower than that of the neutral species, and it becomes higher than that of neutral species only at about 10000 K. No Ar²⁺ ions show up for T<20000 K while the density of Ar is 1×10^{16} against $1 \times 10^{20} \text{ m}^{-3}$ for Ar⁺ at 20000 K. For helium, due to the higher ionization potential (24.5 eV against 15.8 eV for Ar), the same phenomena ($n_{\text{He}} = 10^4 n_{\text{He}^+}$ and $n_{\text{He}} = n_{\text{He}^+}$) occur at 11000 K and 16000 K, respectively. Hydrogen behaves differently: first the molecule has to be dissociated (dissociation energy 4.6 eV), which is completed at 5000 K, before ionization of the atomic species occurs. As the ionization energy is close to that of Ar (13.6eV against 15.8 eV for Ar), ionization is completed at about the same temperature as for Ar.

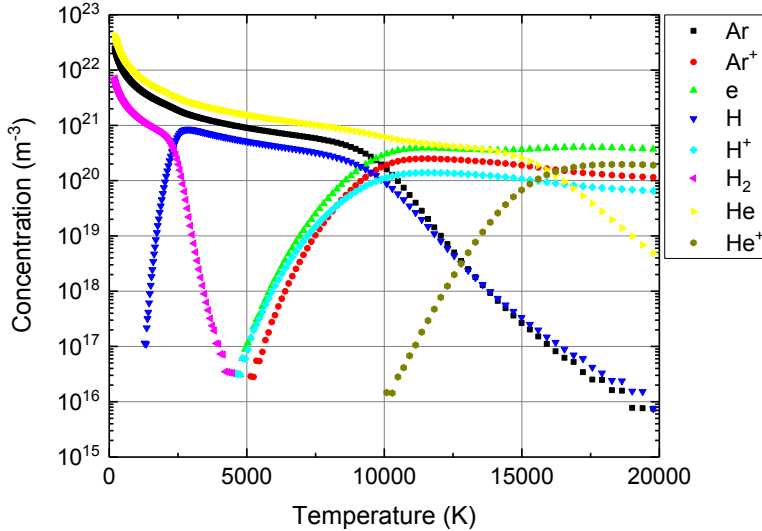


Figure 5-1. Evolution of molar densities of a 35Ar-60He-10H₂ plasma versus temperature at the pressure of 200 Pa.

5.1.1 Ar-He Plasma Mixture at High Pressures

The thermodynamic and transport property are calculated based on CEA program, which uses the minimization-of-free-energy formulation for assigned temperature and pressure. Temperature and pressure follow the kinetic theory. The interaction among species is neglected.

Figure 5-2 and 5-3 show the enthalpy and specific heat capacity of 35Ar-60He plasma mixture at different pressures. At a given temperature, the enthalpy of a gas increases as the pressure decreases due to the lower ionization temperatures; a great deal of energy is needed to ionize a gas, and thus the energy content is higher at temperatures exceeding the ionization level. It can be seen that when the pressure increase, the successive peaks of specific heat capacity corresponding to argon ionization, helium ionization, and ionization is shifted to higher temperatures. The maximum values of the peaks decreases with the increase of the pressures.

Figure 5-4 and 5-5 present the viscosity and thermal conductivity of 35Ar-60He plasma mixture at different pressures. In this theory, viscosity is independent of pressure. The apparent paradox of the independence of viscosity with the pressure can be explained as follows. If the concentration of atoms is halved, a half concentration of atoms available to transport momentum, but the mean free path of each atom is doubled, therefore it can transport this momentum twice efficiency, and thus the net rate of momentum transfer is unchanged. When the temperature increases, the viscosity is first controlled by atoms. When the ionization happens, the viscosity decreases with increasing temperatures. The thermal conductivity is also independent of pressure and depends only on the square root of temperature. Peaks of thermal conductivity shift to lower temperatures due to the ionization of argon.

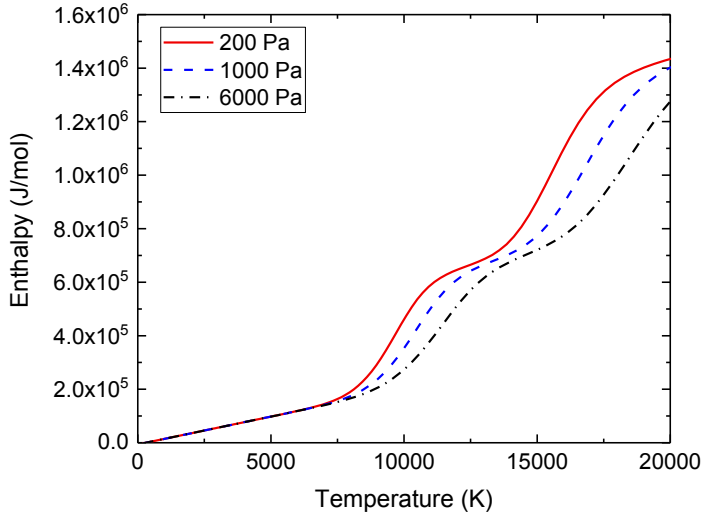


Figure 5-2. Enthalpy of 35Ar-60He plasma mixture at different pressures.

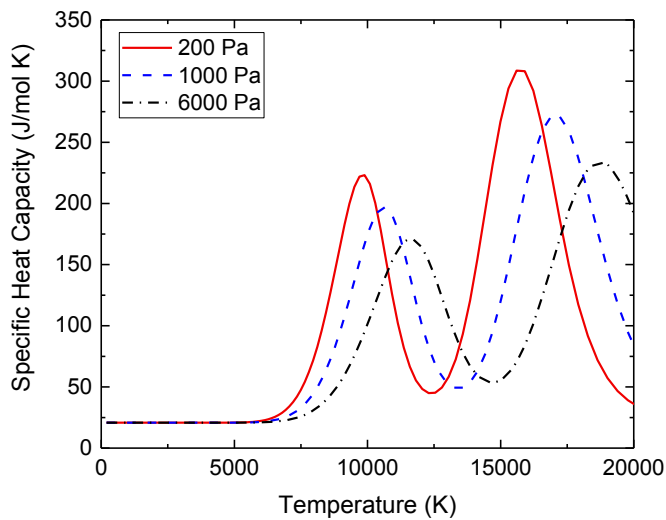


Figure 5-3. Specific heat capacity of 35Ar-60He plasma mixture at different pressures.

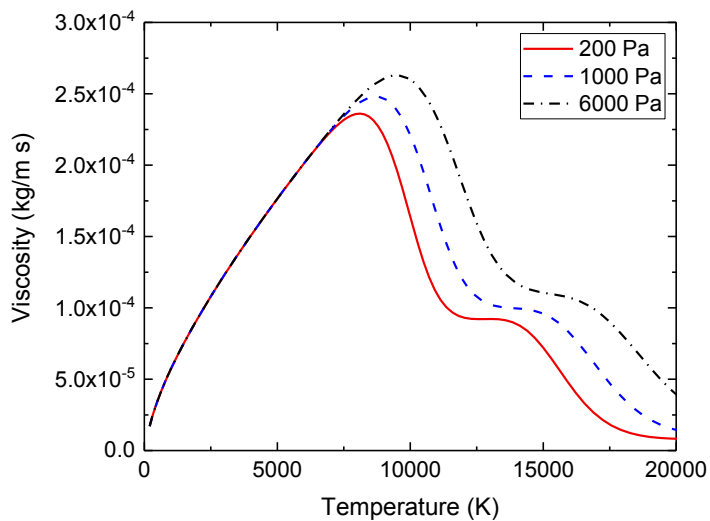


Figure 5-4. Viscosity of 35Ar-60He plasma mixture at different pressures.

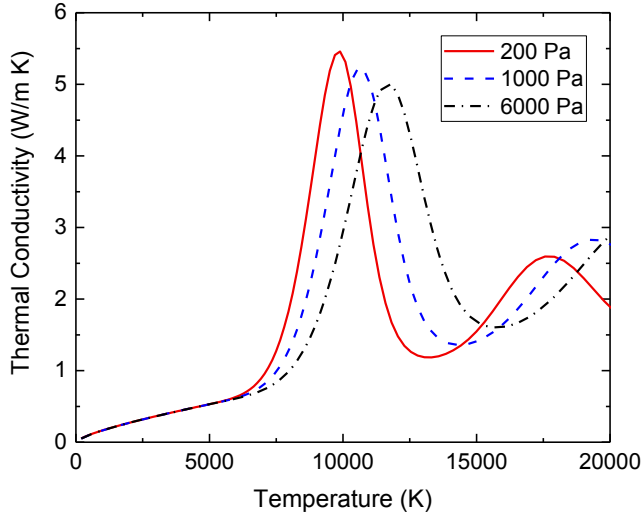


Figure 5-5. Thermal conductivity of 35Ar-60He plasma mixture at different pressures.

5.1.2 Ar-He-H₂ Plasma Mixture at a Pressure of 200 Pa

Three plasma (35Ar-60He, 35Ar-60He-10H₂, and 100Ar-10H₂) are very commonly in the PS-PVD process to obtain completely different microstructures of coatings [61]. Figure 5-6 and 5-7 show the enthalpy and specific heat capacity for three different plasma mixtures at a chamber pressure of 200 Pa, respectively. The variations of enthalpy are mainly due to the heat of the dissociation of hydrogen and the ionization of argon. The steep variations in enthalpy are essentially due to the heat of reaction (dissociation and ionization). The very high enthalpy of H₂ is also because of its low mass. For a given specific enthalpy as long as $T < 17000$ K, the temperature of 35Ar-60He mixtures is the highest.

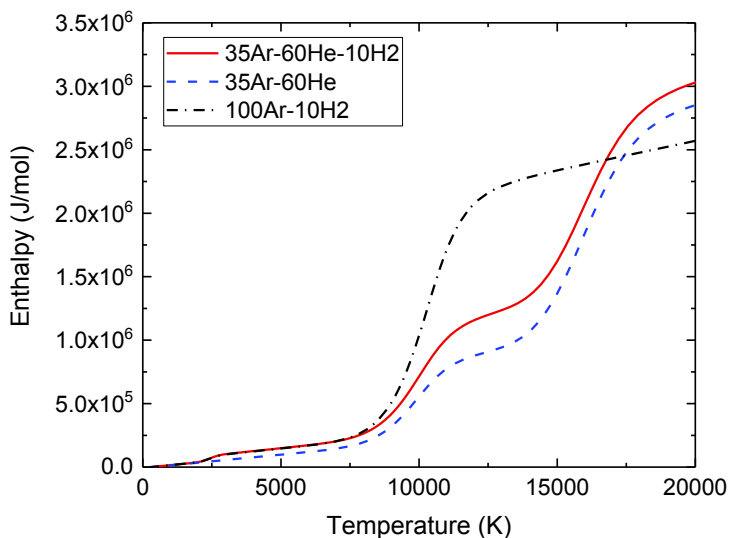


Figure 5-6. Enthalpy of different plasma mixtures at a pressure of 200 Pa.

Figure 5-8 and 5-9 shows thermal conductivity and viscosity of the different plasma mixture at a pressure of 200 Pa, respectively. The peaks of the curves respond to the dissociation of the hydrogen molecules and the ionization of atoms. The increase of helium percentage raises significantly the viscosity of the mixture at round 15000 K. At a temperature of 10000 K, the argon ions start to be significantly compared to atoms. The thermal conductivity and viscosity of 35Ar-60He and 35Ar-60He-10H₂ mixture peak at the temperature ranging from 15000 K to 20000 K. This refers to the greater heat capacity to evaporate the particles compared to 100Ar-10H₂ mixtures.

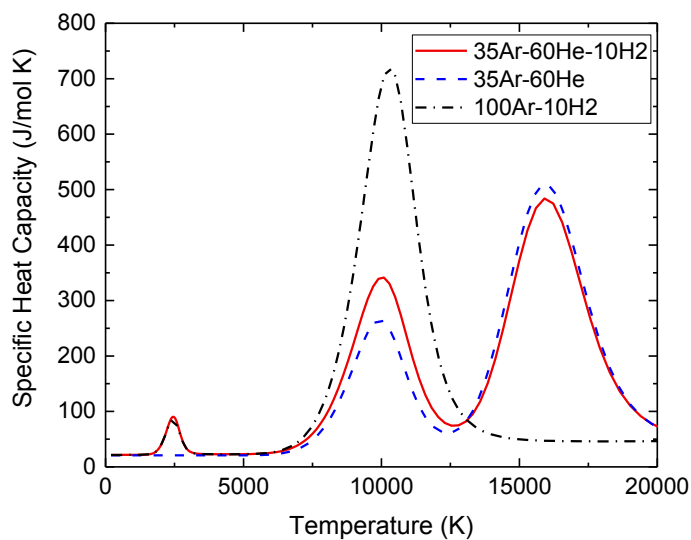


Figure 5-7. Specific heat capacity of different plasma mixture at a pressure of 200 Pa.

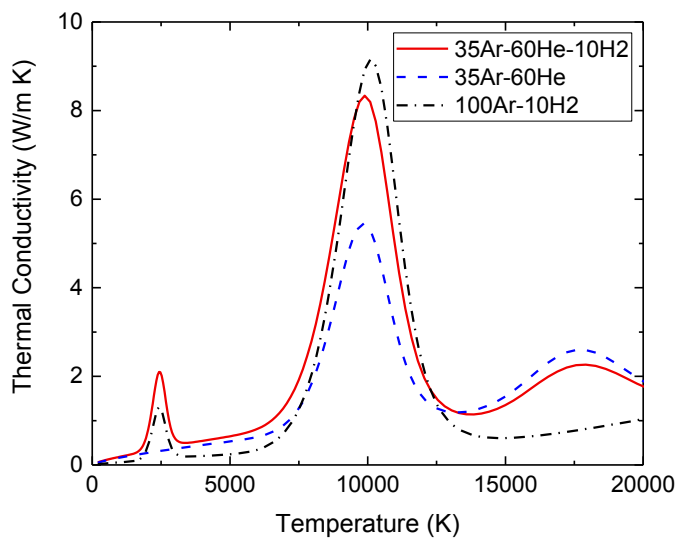


Figure 5-8. Thermal conductivity of different plasma mixture at a pressure of 200 Pa.

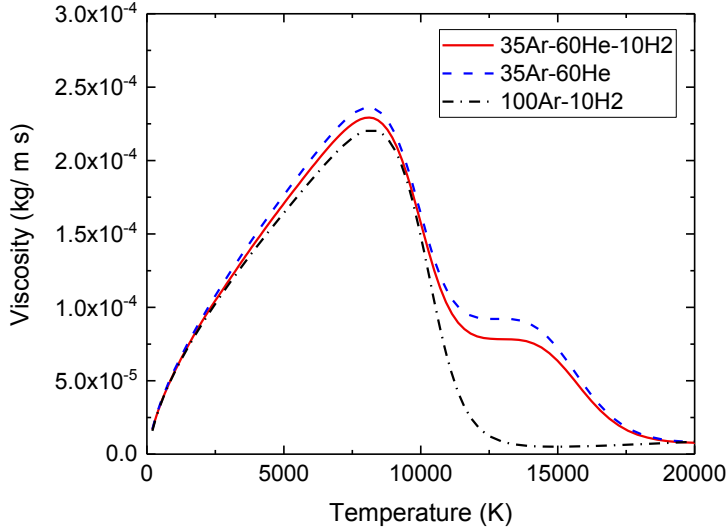


Figure 5-9. Viscosity of different plasma mixture at a chamber pressure of 200 Pa.

5.2 The Plasma Jet Modeling

Based on the thermodynamic and transport properties of 35Ar-60He plasma (200 Pa-10000 Pa), 35Ar-60He-10H₂ (200 Pa), and 100Ar-10H₂ (200 Pa) assuming local thermodynamic equilibrium (LTE), the fluid dynamic simulation of the plasma jet were conducted by ANSYS Fluent 17.1 to interpret the very low and low-pressure plasma spraying process.

5.2.1 Vacuum Plasma Spray

The flow field of a supersonic under-expanded jet issuing from a converging-diverging nozzle (pressure of inner nozzle up to 10^4 - 10^5 Pa) into a chamber domain at rest theoretically and experimentally to validate the model was investigated. Correspondingly, different series of expansion and compression waves appear in the jet, and they change the jet pressure that it finally matches itself with chamber pressure.

The flow pattern in the initial region of a supersonic under-expanded jet and images of plasma jets are presented in Figure 5-10. The plasma jet that accelerates from subsonic, sonic to supersonic in the nozzle, then a supersonic under-expanded jet expands in the large chamber.

The conditional jet boundary corresponds to the Mach number $M = 1$. The condition of the pressure constancy along the boundary of an expanding supersonic jet leads to the curving of the boundary and the formation of compression waves directed inward the jet. The intersection of the compression waves forms a barrel-shaped shock. It is reflected from the axis of the axisymmetric jet with the formation of a normal shock. The interaction of the reflected shock with the constant pressure region results in the formation of expansion waves and a new jet “barrel”. It should be noted that the main amount of the plasma issuing from the nozzle passes through the region enclosed between the submerging shock and the jet boundary. The flow ahead of the Mach disk is characterized by a high flow velocity and a small density. As the flow pass across the normal shock, the flow velocity decreases jump-wise, while the concentration increases. The submerging and reflected shocks are visible only slightly.

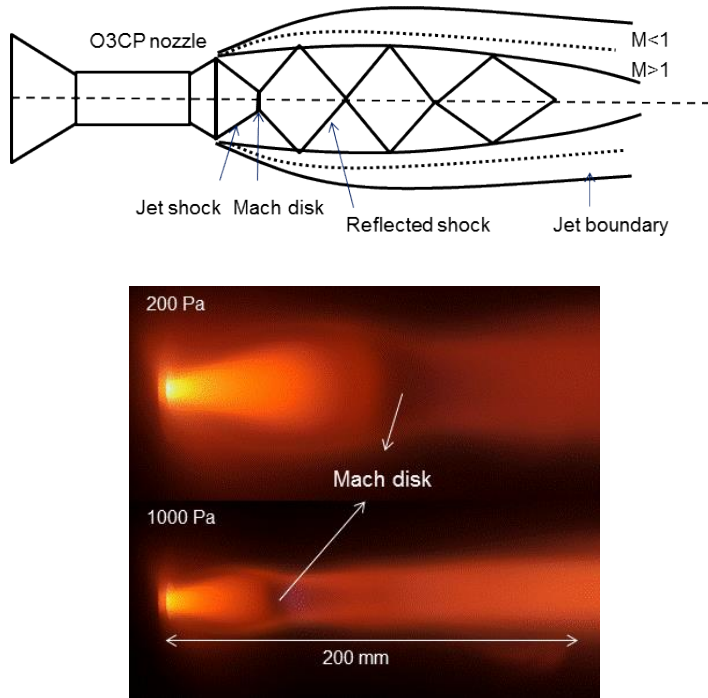


Figure 5-10. A schematic sketch of a supersonic free jet [173] and images of ^{35}Ar - ^{60}He plasma jets at different chamber pressures.

Jet shock diamonds in the moderately under-expanded plasma jet, each initial oblique shock impinges on the opposite edge of the jet, turning the flow away or towards the centerline. The shock or expansion fan reflects off the edge, and propagates back to the other side, repeating the cycle until the jet dissipates. These flow patterns are known as shock diamonds, which are often visible in the flow that is corresponding to the temperature distribution in Figure 5-14.

5.2.1.1 Temperature

The plasma jets at chamber pressures ranging from 200 Pa to 10000 Pa are investigated. In particular, the flow behind the highly under-expanded region is of great interest, because it is a long laminar jet, including experimental and theoretical studies of the structure of the jet flow.

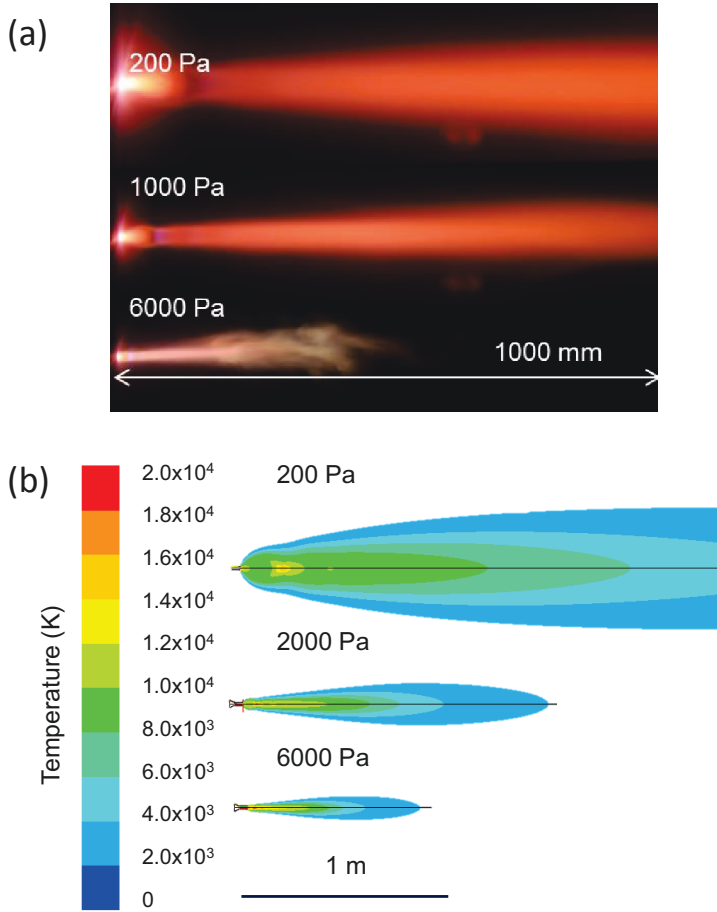


Figure 5-11. Comparisons between the jet photographs (a) and simulated temperature distribution for different pressures (b).

Figure 5-11 to 5-14 present comparisons between the jet images and temperature distribution for different pressures. Since the chamber pressure in this computation is varied from 200 Pa to 10,000 Pa while the nozzle exit pressure is around 10^4 - 10^5 Pa, and the plasma jet is clearly observed from highly under-expanded to moderately under-expanded state. The images of the luminous plasma jets were obtained using detected by a 1024x1024 CCD array camera. From the images, the width and length of the jet are examined.

Figure 5-11 describes the jet photographs and a simulated averaged-temperature contour depending on a chamber pressure. As a chamber pressure increases, the width and length of the plasma jet of the 35Ar-60He mixture greatly decrease. Figure 5-12 demonstrates the simulated temperature distribution along the axial direction vs the chamber pressure. The discrete scale x-axis is used to note the axial distance from the nozzle exit. Y-axis represents the static temperature, which is corresponding to the total temperature that considers the influence of the velocity.

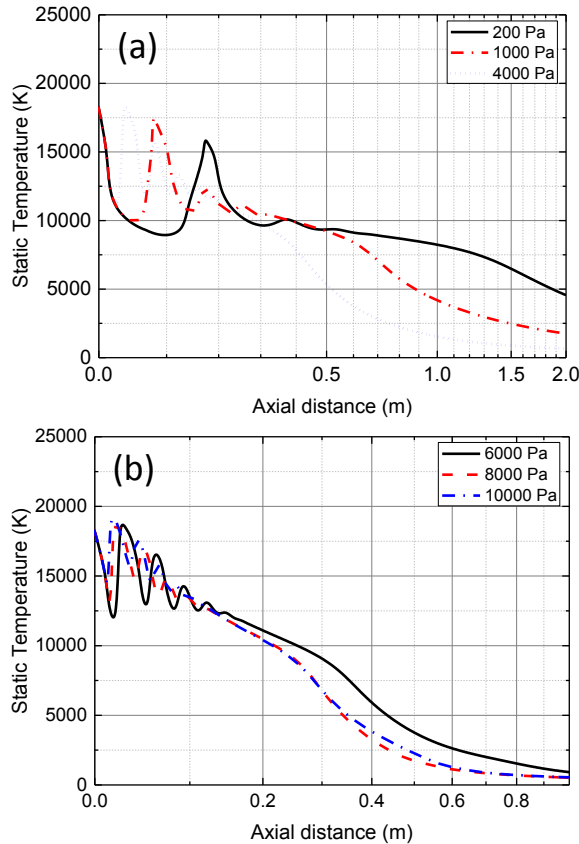


Figure 5-12. Axial direction dependence of temperature on varied chamber pressures of the plasma jet of 35Ar-60He.

For a chamber pressures less than 1000 Pa, the temperature can remain quite high and homogeneous over a long distance. The jet shock length was found to be comparable with the jet photographs. Temperature decreases along the downstream of the plasma jet. Figure 5-13 shows that the jet shock length from the nozzle exit is 100 mm and 50 mm for chamber pressure 200 Pa and 1000 Pa, respectively. This result means the simulation of pressure and velocities in the simulation are predictive. Pan et al [78] shows that the temperature gradients of laminar plasma jets with long plasma plumes in the axial direction are about two orders lower than those of turbulent plasma jets, and temperature distribution in radial direction is more concentrated.

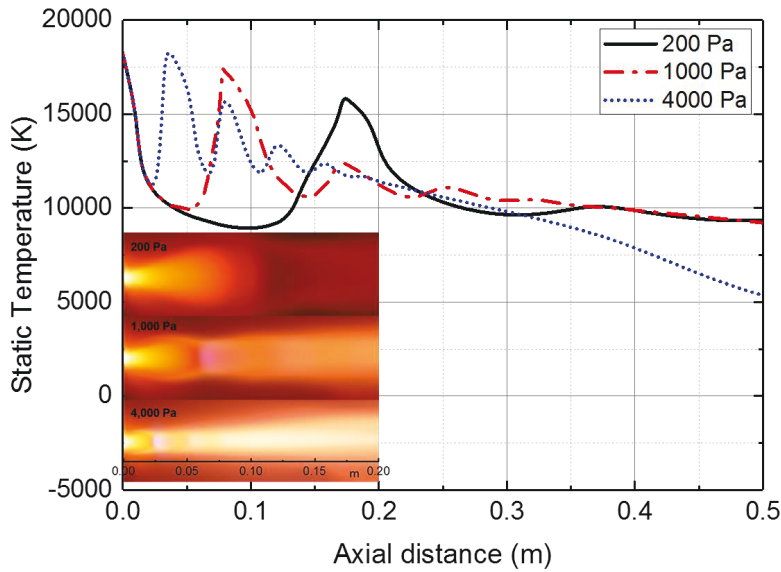


Figure 5-13. Comparisons of shock diamonds between the jet photographs and temperature distribution for different pressures (200 Pa, 1000 Pa, 4000 Pa).

Figure 5-14 presents comparisons of shock diamonds between the jet image and temperature distribution for higher pressures (6000 Pa, 8000 Pa, 10000 Pa). The images show large-scale structures in the mixing layer of the jet. Mixing between the plasma downstream and cold chamber gas generates vorticities. As the chamber pressures increase from 6000 Pa to 10000 Pa, the resultant size of shock diamonds decreases.

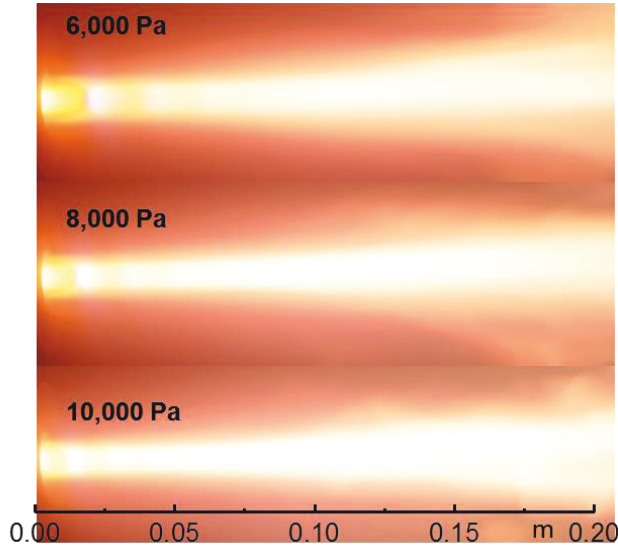
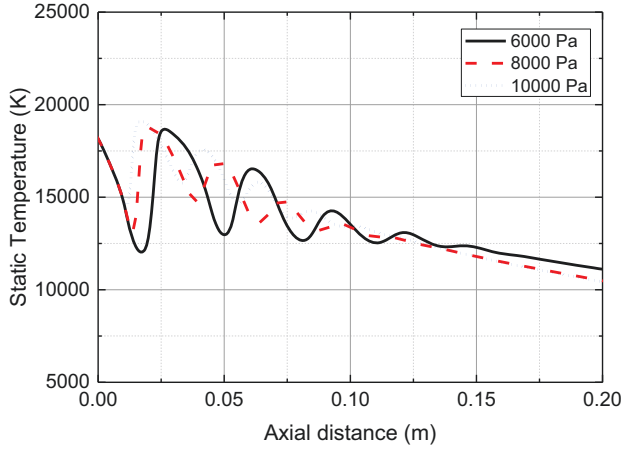


Figure 5-14. Comparisons between the jet photographs and temperature distribution for higher pressures (6000 Pa, 8000 Pa, 10000 Pa).

The analysis in the experiment of the plasma jet indicates three major flow types [173]: (1) subsonic jet $P_{exit}/P_{\infty} = 1$, (2) moderately under-expanded jet, (3) highly under-expanded jet. In these discussions, moderately under-expanded jet exhibits the familiar oblique shock pattern (shock diamonds) as shown in Figure 5-10, and in highly under-

expanded condition, a normal shock (Mach disk) forms as shown in Figure 5-9. Particularly, as P_{exit}/P_{∞} further increases the jet shock increases in size [174, 175].

5.2.1.2 Pressure

Figure 5-15 presents the pressure distribution along the axial direction for different chamber pressure. When the nozzle exit pressure is close to the chamber pressure, the pressure variation decreases. This has a great influence on the plasma jet length and supersonic properties. The relations of pressure, velocity, and Mach number are as follows: (1) when the jet accelerates the pressure drops, (2) the pressure is reduced across expansion and increases through compressed zone. In the main region, the plasma jet becomes isobaric. The plasma jet, correspondingly from low chamber pressure to high chamber pressure, can change from laminar to turbulent, respectively. In the plasma jet, a mixing layer develops along the jet boundary of a high chamber pressure.

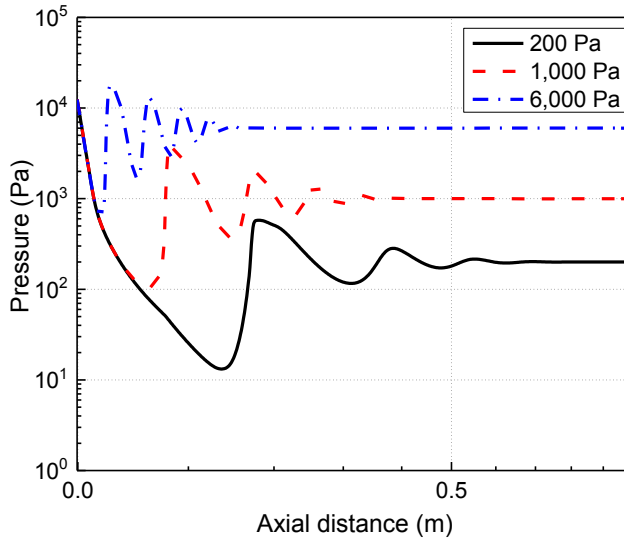


Figure 5-15. Axial direction dependence of pressure of the 35Ar-60He plasma jet on varied chamber pressures (200 Pa, 1000 Pa, and 6000 Pa).

5.2.1.3 Velocity

Figure 5-16 shows the axial distribution dependence of velocity for varied pressures. At the nozzle exit, the velocity is about 5000 m/s. Along the downstream of the plasma jet, the velocity sharply increases to 10000 m/s and then greatly decreases for a chamber pressure of 200 Pa. At a chamber pressure of 6000 Pa, the length of the plasma jet is about 0.5 m where the velocity decreases almost to zero, which is also comparable to Figure 5-8. The length of plasma jet is around 2 m (200 Pa), 1 m (1,000 Pa) and 0.5 m (6,000 Pa).

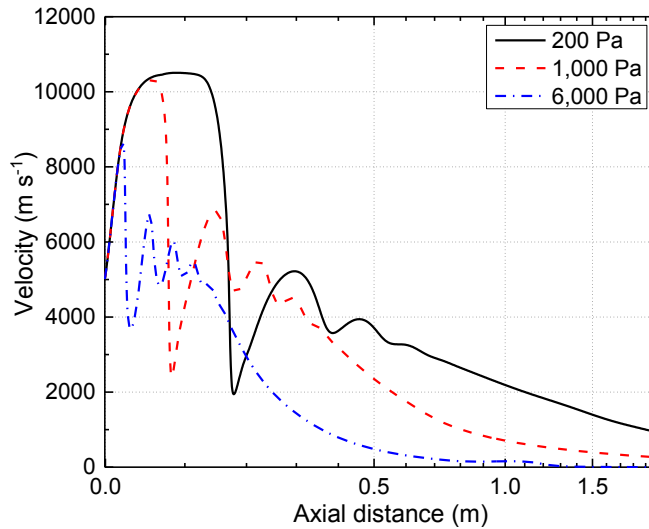


Figure 5-16. Axial direction dependence of the velocity of the 35Ar-60He plasma jet for varied chamber pressures (200 Pa, 1,000 Pa, and 6,000 Pa).

5.2.1.4 Speed of Sound

Figure 5-17 shows the speed of sound along the axial direction of the 35Ar-60He plasma mixture at different chamber pressures. The speed of sound is proportional to the square root of the temperature. At a pressure of 200 Pa, the plasma jet is a long laminar jet and can keep homogenous and high temperature at a great distance along the downstream.

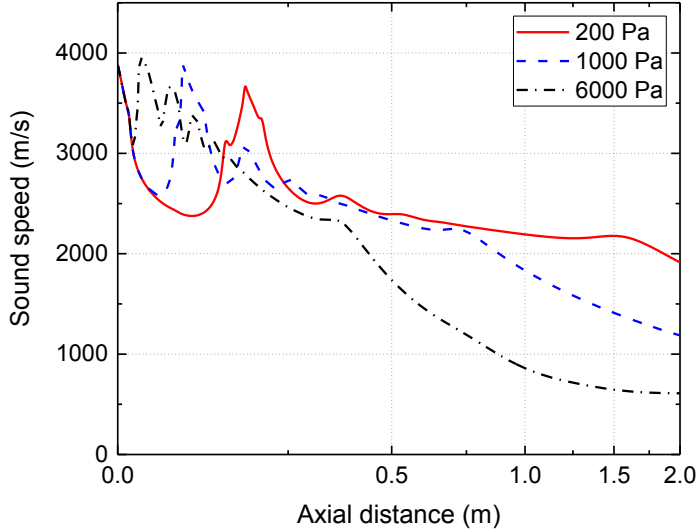


Figure 5-17. Axial direction dependence of sound speed of the 35Ar-60He plasma jet for varied chamber pressures (200 Pa, 1,000 Pa, and 6,000 Pa).

5.2.1.5 Mach number

Figure 5-18 presents the evolution of Mach number along the axial direction of the plasma jet depending on varied chamber pressures. The Mach number is the ratio of velocity of the jet to the speed of sound. The plasma jet changes its flow regime from supersonic to transonic and then to subsonic. At a chamber pressure of 200 Pa, the supersonic flow of the plasma jet reaches a long distance after exhausting from the torch exit. If it is subsonic flow, eddies grow rather much fast and the cold gas mix with the jet more efficiently. The flow tends to be laminar at higher Mach numbers [176]. In addition, the flow behaves laminar downstream for pressures lower than 1000 Pa. Furthermore, the flow appears transitional over greater distance from the nozzle exit.

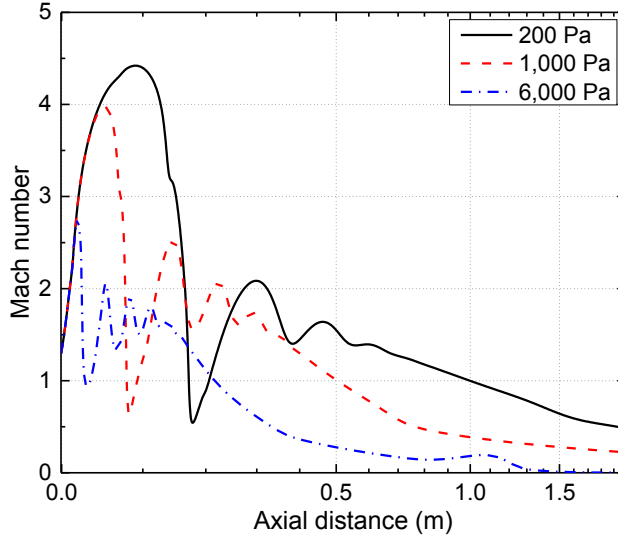


Figure 5-18. Axial direction dependence of Mach number of the 35Ar-60He plasma jet for varied chamber pressures (200 Pa, 1,000 Pa, and 6,000 Pa).

5.2.1.6 Turbulence

Figure 5-19 depicts the predicted turbulent Reynolds number developments of the plasma jet along the radial direction at the axial stand-off distance of 500 mm for different chamber pressures. At a chamber pressure of 1000 Pa, the turbulent Reynolds number peaks at the radial distance of 0.175 mm. Therefore, the plasma jet is turbulent at the edge. Turbulent Reynolds number increases as the chamber pressure increases. The degree of turbulence not only describes the quantity of cold gas entrained into the jet and thus the volume of useful plasma, but it also affects heat transfer rates to particles travelling through the jet. The maximum turbulent Reynolds number at a chamber pressure of 1,000 Pa is less than 1,000; while at 6,000 Pa the largest value is 6,000. It can be concluded that the flow is laminar for chamber pressure less than 1000 Pa.

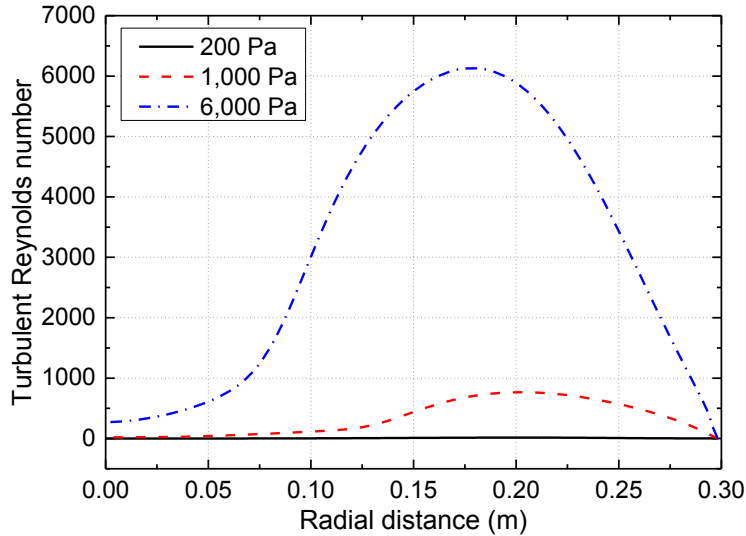


Figure 5-19. Radial direction dependence of the turbulent Reynolds number of the plasma jets for varied chamber pressures (200 Pa, 1,000 Pa, and 6,000 Pa) at the axial stand-off distance of 500 mm of the 35Ar-60He plasma jet.

Turbulent Reynolds number peaks of the jet locate along the radial direction on the fringe of the plasma jet. These peaks occur at the radial distance of 0.2 m for an axial stand-off distance of 500 mm shown in Figure 5-19. The layer becomes full turbulent. The evolution of flow from laminar to turbulent extends over a Reynolds number range from 350 to 2×10^5 which was labeled as “the transitional shear layer flow” [177].

5.2.2 Plasma Spray Physical Vapor Deposition

The soft vacuum plasma spraying methods often involve entrainment of the surrounding cold gas into the turbulent plasma jet core and result in coatings with relatively high porosity and low adhesive strength. Coatings produced by long laminar plasma jet have advantages in aspects such as the adhesive strength at the interface of ceramic coating or bond coat, the surface roughness and microstructure [178].

5.2.2.1 Temperature

Figure 5-20 shows the temperature evolution along the axial direction for different plasma mixture at a pressure of 200 Pa. The temperature of the 35Ar-60He plasma mixture was found to be the highest about 17500 K while the temperature of the 100Ar-10H₂ plasma mixtures is the lowest around 12500 K at the nozzle exit. The temperature of 35Ar-60He-10H₂ plasma at the nozzle exit was found to be 15000 K.

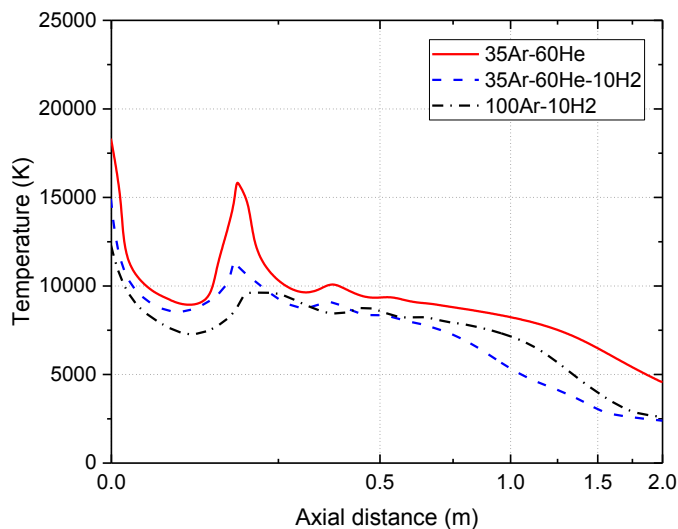


Figure 5-20. Temperature distribution along axial direction for different plasma mixtures, at a chamber pressure of 200 Pa.

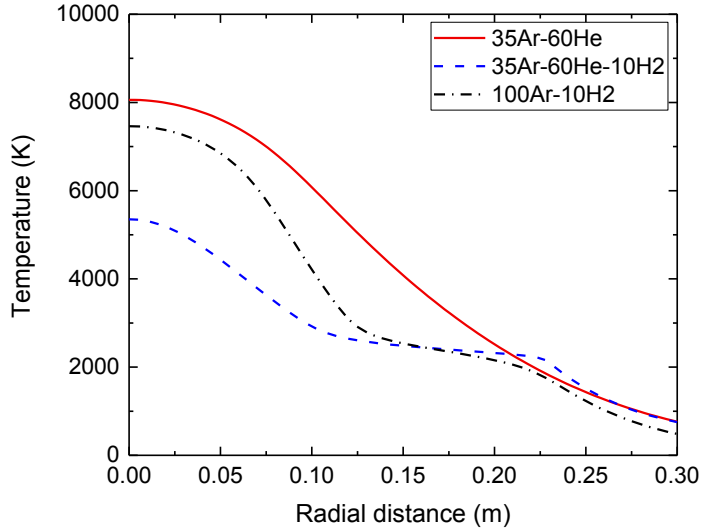


Figure 5-21. Temperature profile along the radial direction for different plasma gases mixture at a stand-off distance of 1m at a chamber pressure of 200 Pa.

Figure 5-21 shows the temperature profile along the radial direction for different plasma mixture at a stand-off distance of 1 m at a chamber pressure of 200 Pa. The width of the plasma jet is around 0.4 m. The value of the temperature of 35Ar-60He plasma mixtures shows a steady decline. The temperature falls slightly first and then maintains at the same level for the 35Ar-60He-10H₂ plasma mixture. In the case of 100Ar-10H₂ plasma mixture, the temperature suffers a gradual fall and levels off at 2500 K. Furthermore, the temperature ended with a slight decrease for all plasma mixture. The width of the red luminosity of 35Ar-60He-10H₂ plasma mixture is larger than that of the 100Ar-10H₂ plasma mixture in the plasma jet.

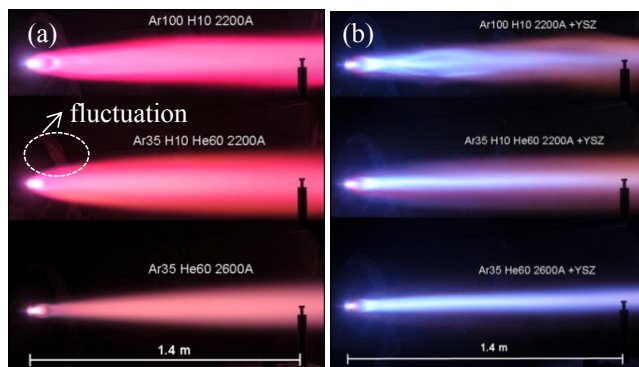


Figure 5-22. Images of the plasma jets expanding at a chamber pressure of 200 Pa for different plasma gas mixture without particle injections (a) and with particle injections (b) [61].

Figure 5-22 shows photographs of the plasma jets expanding at a chamber pressure of 200 Pa for different plasma gas mixtures without particle injections (a) and with particles injection of YSZ powder (b). For H_2 -containing plasma mixtures, the red color in the illuminated jet represents the recombination of hydrogen atoms into molecules. This explains why the width of the plasma jet for 35Ar-60He plasma mixtures is smaller than that of the other two H_2 -containing plasma mixtures. As to the case of consideration of YSZ injections, the white blue color denotes the emission of zirconia. The melting temperature for YSZ powders is 3000 K, which is almost comparable to the temperature of the dissociation of the hydrogen molecule.

5.2.2.2 Velocity

Figure 5-23 shows the velocity profile along the axial direction emerging from the torch nozzle into a big chamber with a pressure of 200 Pa for different plasma mixture. It can be seen clearly that the velocity increases drastically and reaches their peaks. The velocity of 100Ar-10 H_2 plasma is the lowest compared to the other two plasma mixture. At the standoff distance of 0.21 m from the nozzle exit, a slight fluctuation for 35Ar-60He and 35Ar-60He-10 H_2 plasma occur due to the sharp decrease of the velocity, as shown in Figure 5-22. Modeling of the plasma jets shows the comparable results. Figure

5-24 presents the velocity profile along the radial direction at a standoff distance of 1 m. The velocity of 35Ar-60He plasma jet is the highest.

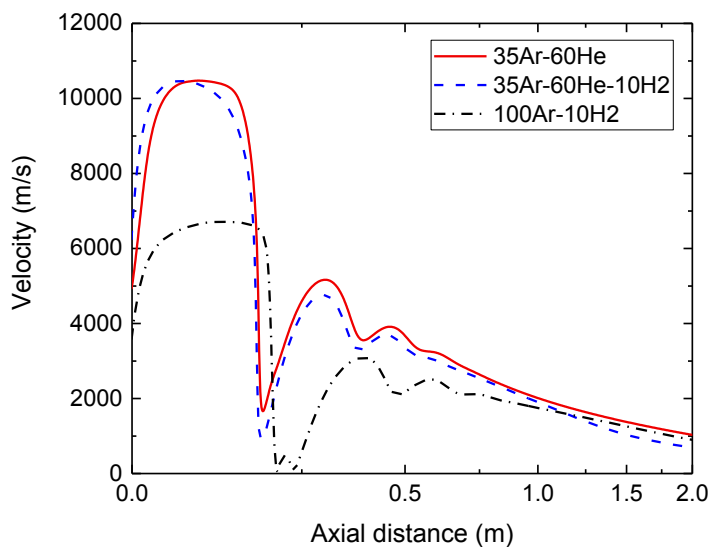


Figure 5-23. Velocity profile along the axial direction for different plasma mixture at a chamber pressure of 200 Pa.

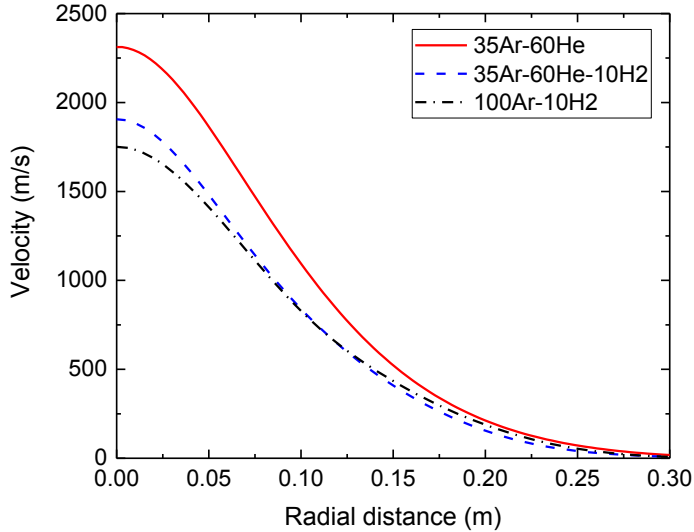


Figure 5-24. Velocity profile along the radial direction for different plasma mixture at the standoff distance of 1m at a chamber pressure of 200 Pa.

5.2.2.3 Speed of Sound

Figure 5-25 shows the speed of sound profile along the axial direction for different plasma mixture at a chamber pressure of 200 Pa. The speed of sound is proportional to the square root of the product of the temperature and the ratio of specific heats. The 100Ar-10H₂ plasma jet is the lowest due to the lowest temperature.

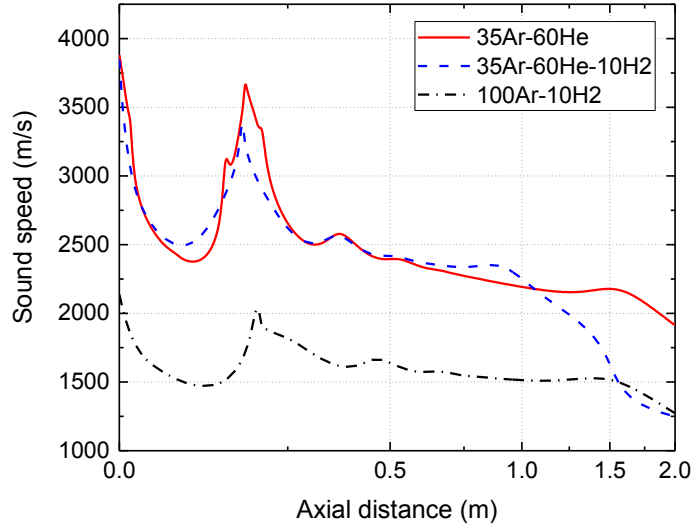


Figure 5-25. Sound speed profile along the axial direction for different plasma mixture at a chamber pressure of 200 Pa.

5.2.2.4 Mach number

Figure 5-26 and 5-27 show the Mach number profile along the axial and radial direction for different plasma mixture at a chamber pressure of 200 Pa, respectively. At the Mach numbers approaches 1, the flow is transonic. When the Mach number exceeds 1, the flow is termed supersonic and contains shocks and expansion fans. The maximum value of the Mach number reaches 4.5. At the standoff distance of 1m, the plasma jet is around transonic.

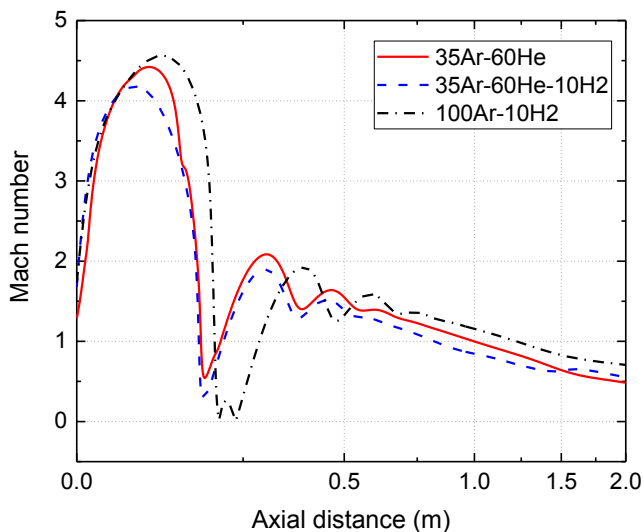


Figure 5-26. Mach number profile along the axial direction for different plasma mixture at a chamber pressure of 200 Pa.

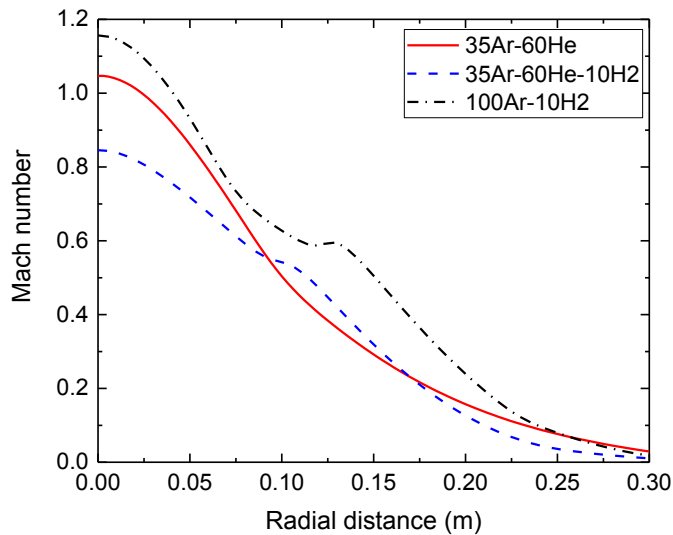


Figure 5-27. Mach number profile along the radial direction for different plasma mixture at the standoff distance of 1m at a chamber pressure of 200 Pa.

5.2.2.5 Effect of the Substrate in the Plasma Jet

Figure 5-28 and 5-29 present the velocity profile around the horizontally and vertically oriented substrates at a standoff distance of 1 m for the 35Ar-60He plasma, respectively. The velocity close to the substrate can reach as large as 1500-2000 m/s for the vertically oriented substrate. For the vertically oriented substrate, the velocity is homogenous; for the horizontally oriented substrate, a big gradient of velocity exists around the substrate surface.

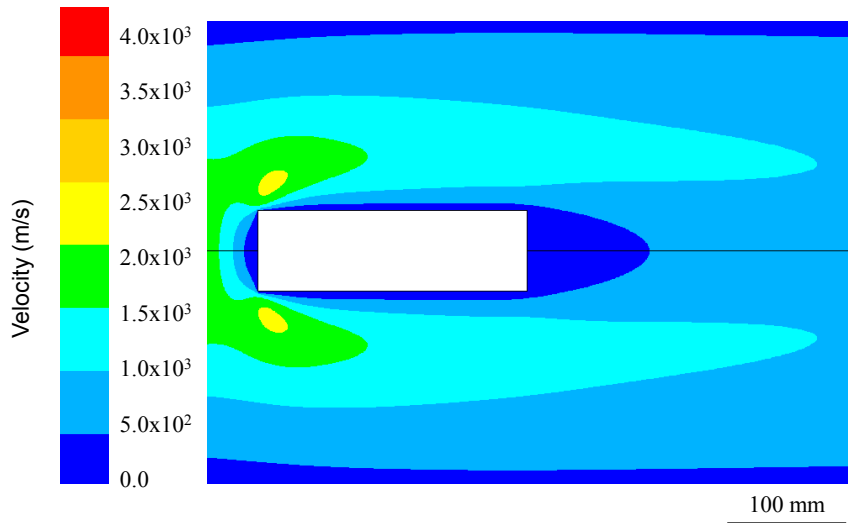


Figure 5-28. Velocity profile around the horizontally oriented substrate at a standoff distance of 1 m for the 35Ar-60He plasma.

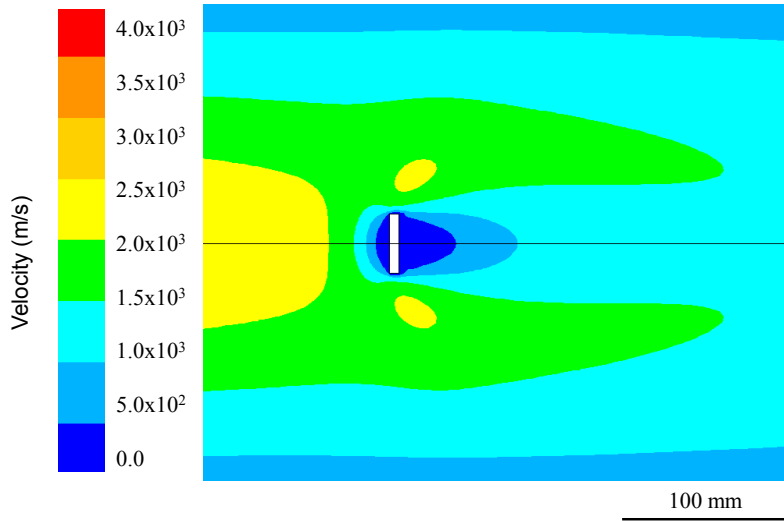


Figure 5-29. Velocity profile around the vertically oriented substrate at a standoff distance of 1 m for the 35Ar-60He plasma.

Figure 5-30 and 5-31 describe the temperature profile around the horizontal and vertical substrate at a standoff distance of 1 m for the 35Ar-60He plasma, respectively. The temperature of the substrate surface reaches up to 9000 K. For the horizontally oriented substrate, the thickness of the boundary layer is proportional to the square root of the distance from the leading edge of the substrate. It can be concluded that a greater difference of temperature and velocity between the leading edge and bottom edge of the substrate surface leads to distinct deposition process at the surface of the horizontally oriented substrate.

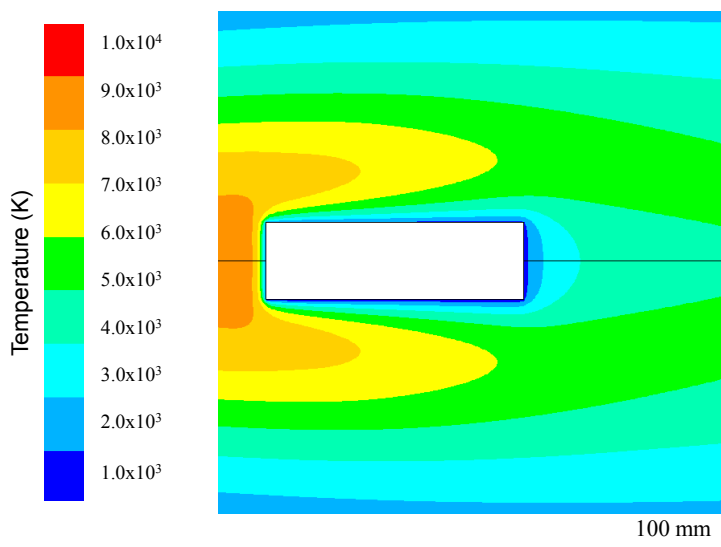


Figure 5-30. Temperature profile around the horizontally oriented substrate at a standoff distance of 1 m for the 35Ar-60He plasma.

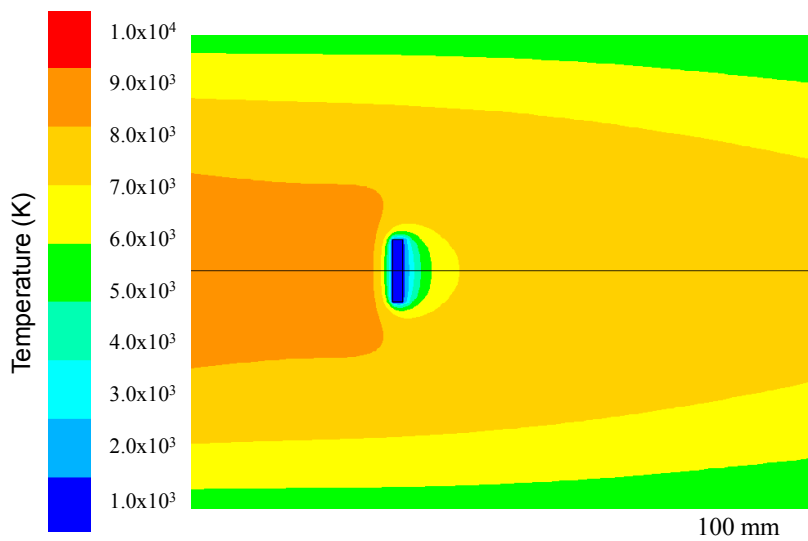


Figure 5-31. Temperature profile around the vertically oriented substrate at a standoff distance of 1 m for the 35Ar-60He plasma.

5.2.2.6 Non-Line-of-Sight Depositions

The flow field behavior, as characterized by the velocity vector surrounding the substrate scaled by pressure, is shown in Figure 5-32. The vapor flux changes its impingement direction towards the substrate inside the boundary layer. The most significant deviations from the normal happen at locations near the edges of the substrate. In reality, the variability of the incident angle could also be associated with fluctuations or instability of the flow field around the substrate as a result of the surface roughness. As a result, the consideration of incident vapor angle at a normal distribution is practical in the Chapter 5.3 to simulate the built-up of columns. Even though the region of the highest deposition rate is within the line of sight of the vapor source, it is possible to deposit coatings in shadowed areas such as in the backside of the substrate. This non-line-of-sight deposition can be validated in the experiment [5]. In the PS-PVD process, the feedstock particles are injected to the plasma gun where it vaporizes and is transported in a laminar supersonic plasma gas stream. Temperature is high enough to ensure vapor or small clusters that can follow the gas flow. Eddies behind the sample lead to impingement of gases of the jet onto the back surface of the sample.

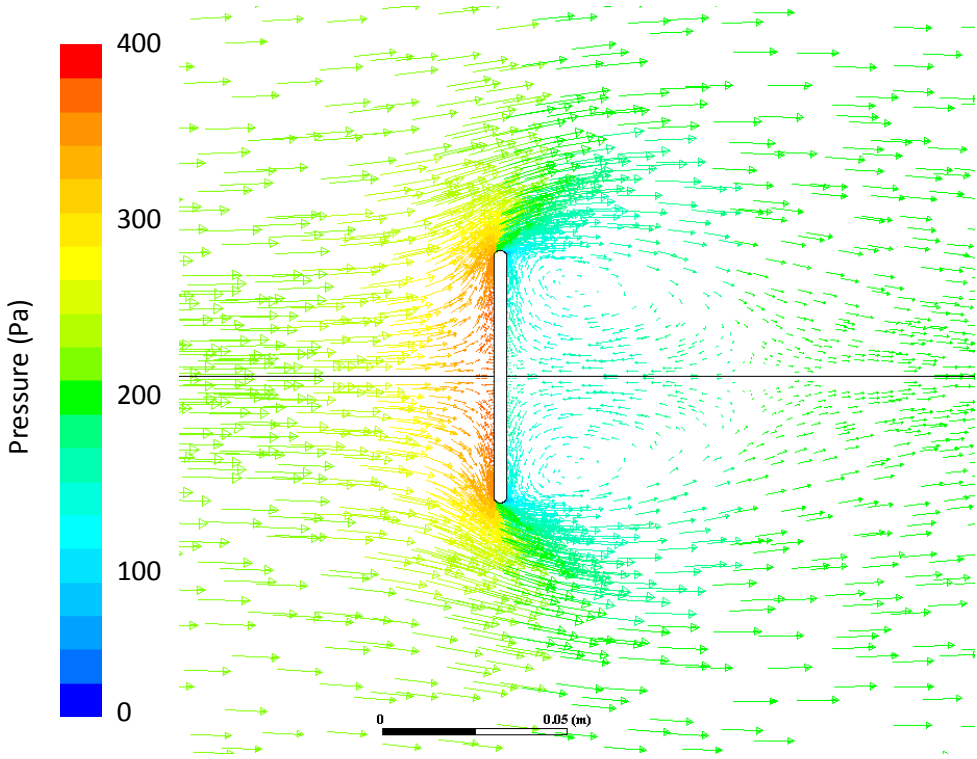


Figure 5-32. Velocity vector field around the substrate color-scaled by the pressure. The substrate is vertical to the center of PS-PVD for 35Ar-60He plasma at a chamber pressure of 200 Pa.

5.2.2.7 Optical Emission Evaluation

Optical emission spectroscopy is used to investigate 35Ar-60He plasma jet at a chamber pressure of 200 Pa. The composition and spectral line intensities are calculated considering non-equilibrium [179]. From the analysis of electrons concentrations of Chapter 5.1, in the temperature ranging from 6000 K to 9000 K, electron densities in the range of 10^{18} - 10^{20} m^{-3} , the probability of non-equilibrium exists, in contrast, the electron densities are over 10^{22} m^{-3} where a local thermodynamic equilibrium exists [180, 181]. These results give us the reasons why we have to analyze the plasma jet compositions out of equilibrium. According to the calculation of the plasma composition, at the

temperature ranging from 4,000 K to 10,000 K, it is not necessarily to consider the ionization of helium.

The plasma jet temperature can be characterized by OES (typically from $8000\text{ K} < T < 14000\text{ K}$) [37]. The thermal plasma spraying process out of equilibrium has been calculated in the literatures [17, 182, 183]. For a very low chamber pressure of 200 Pa, the plasma jet seems to be out of thermal equilibrium because of insufficient transfer of energy between the electrons and heavy species [184]. The challenge is to evaluate the degree of non-equilibrium. Plasma compositions and spectral line intensities for 35Ar-60He plasma are calculated according to the expressions in Chapter 3.2 and 3.3.

An overview of the radial spectrum is shown in Figure 5-33 that is measured by peer PHD candidate W. He, which gives the emission spectrum of a 35Ar-60He plasma jet at an axial stand-off distance of 1 m. The presence of intensive emission lines allows us to analyze the argon ionization. As no helium ions intensities were detected a negligible ionization of helium is assumed. The most intensive emission lines for Ar I are 696.5 nm, 751.5 nm, 763.5 nm and 772.4 nm, for He I are 447.2 nm, 587.6 nm and 667.8 nm, respectively.

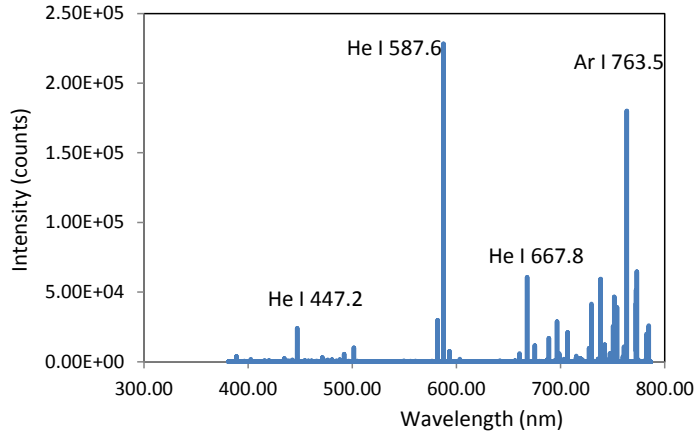


Figure 5-33. Emission spectrum of a 35Ar-60He plasma jet at an axial stand-off distance of 1 m.

Figure 5-34 depicts the dependence of two relative integrated spectral line intensities of atoms and ions as a function of the radial direction at an axial stand-off distance of 1 m. The normalized intensities as a function of the radial distance are shown in Figure 5-35. The maximum values of spectral line intensities of Ar I 763.5 nm is located at a radial distance of around 40 mm due to a big drop of argon atoms concentration. For the intensities of Ar II 487.9 nm, the maximum locates in the center of the plasma jet. Argon ions start to emit considerably at a temperature of around 6,000 K [185]. Furthermore, the intensities of Ar I 763.5 nm are two orders magnitude higher than the intensities of Ar II 487.9 nm.

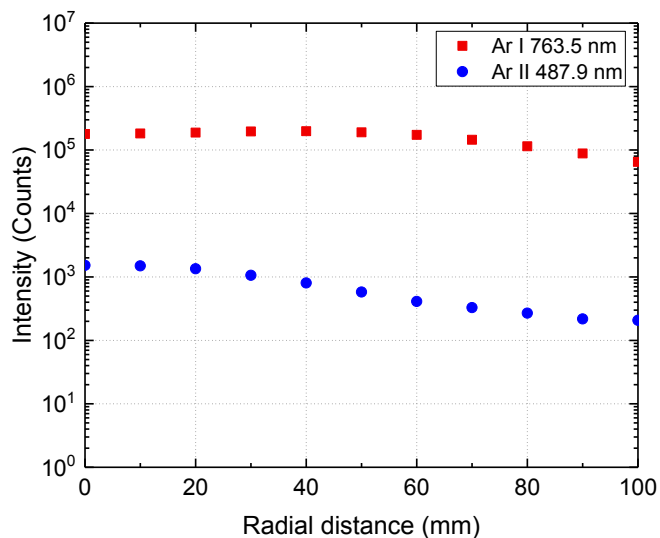


Figure 5-34. Measured dependence of the relative integrated spectral line intensities of Ar I atoms and Ar II ions as a function of the radial direction, at an axial direction stand-off distance of 1 m, compared to [186].

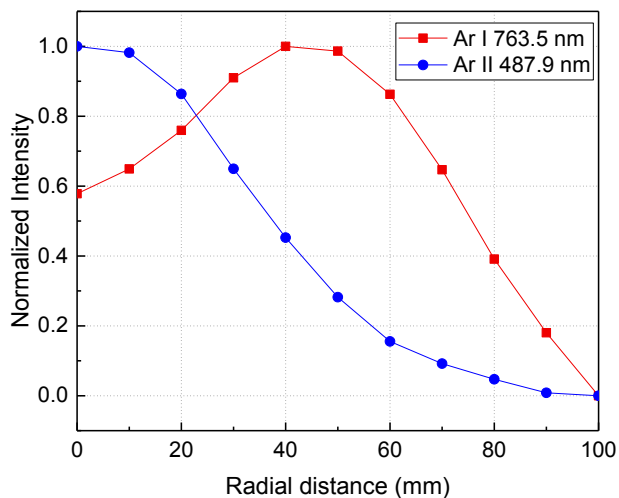


Figure 5-35. Measured dependence of the normalized intensities of Ar I atoms and Ar II ions as a function of the radial direction, at an axial direction stand-off distance of 1 m.

Figure 5-36 shows the simulated results of temperature profile of a 35Ar-60He plasma jet at a pressure of 200 Pa along a radial direction at an axial stand-off distance of 1 m at equilibrium. Under these conditions, the temperature is slightly above 8,000 K in the center of the plasma jet. The temperature decreases with increasing radial distance. As shown in [164, 167], departures from equilibrium dominate at low temperature ($\sim 5,000$ K). Therefore, the probability of non-equilibrium is higher in the fringe of the jet compared to the center of the jet. Figure 5-37 presents the concentrations of atoms and ions along the radial direction at an axial standoff distance of 1 m at equilibrium corresponding to the temperature profile in Figure 5-36.

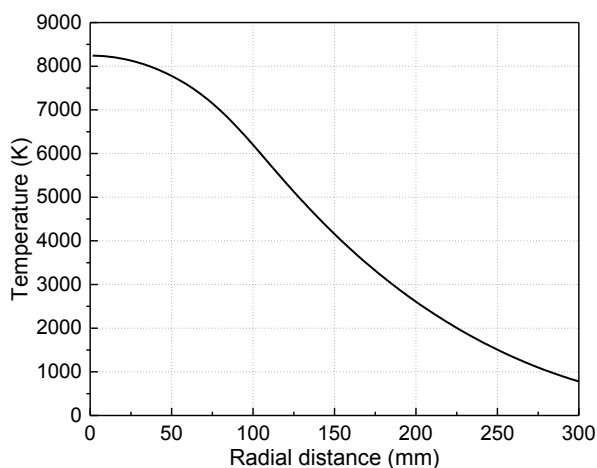


Figure 5-36. Simulated results of temperature profile of a 35Ar-60He plasma jet at a pressure of 200 Pa at an axial stand-off distance of 1 m at equilibrium.

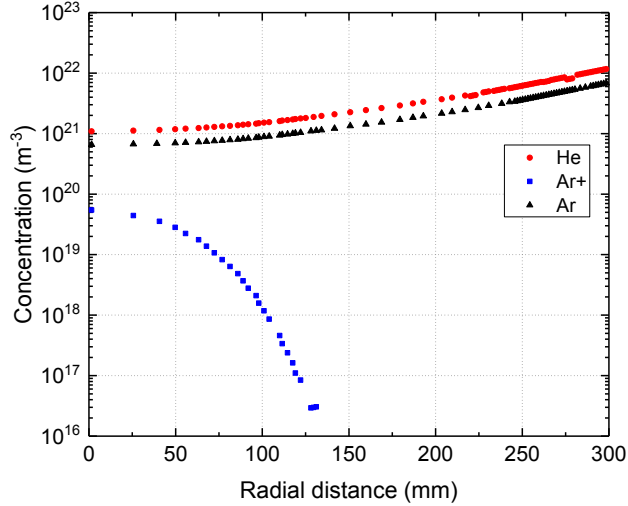


Figure 5-37. Simulated results of compositions of atoms and ions along a radial direction at an axial stand-off distance of 1 m at equilibrium.

Figure 5-38 presents the argon ion and atom concentration as a function of temperature for the heavy species temperature of a 35Ar-60He plasma at a pressure of 200 Pa, calculated for different non-equilibrium parameters θ . As θ increases from 1 to 1.5, the argon ion concentrations level off at the temperature decreasing from 10000 K to 6000 K. At equilibrium, it can be seen in the figure that the concentration of argon atoms start to decrease significantly for temperatures above 10000 K.

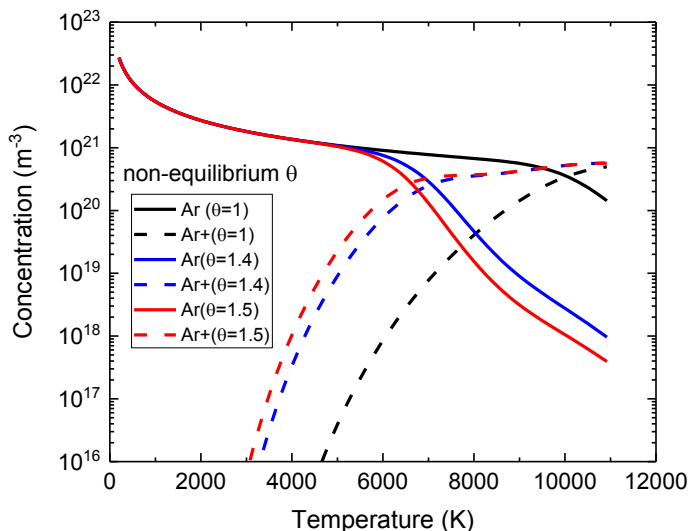


Figure 5-38. Simulated dependence of the argon ions and atoms concentrations for the heavy species temperature of a 35Ar-60He plasma at a pressure of 200 Pa, calculated for different non-equilibrium parameters θ .

Figure 5-39 and 5-40 demonstrate the dependence of Ar I 763.5 nm and Ar II 487.9 nm intensities as a function of the heavy species temperature of a 35Ar-60He plasma at a pressure of 200 Pa, calculated for different non-equilibrium parameters θ . At equilibrium, maximum intensity of Ar I 763.5 nm is located at the center of the plasma jet. As shown in Figure 5-40, the spectral line intensity of Ar II 487.9 nm at equilibrium is calculated around 10^{-4} W/m^3 , which is not high enough to be detected. Comparisons between the peak of plots in Figure 5-35 and 5-39, it can be concluded that the non-equilibrium parameter was found to be around 1.3.

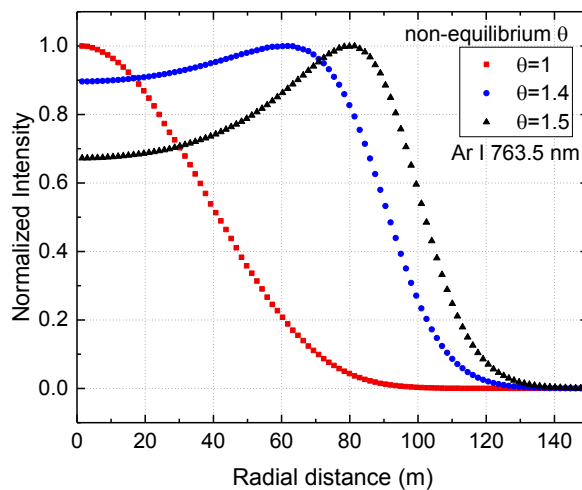


Figure 5-39. Simulated dependence of Ar I 763.5 nm normalized intensities as a function of radial distance of a 35Ar-60He plasma at a pressure of 200 Pa, calculated for different non-equilibrium parameters θ , at an axial stand-off distance of 1 m.

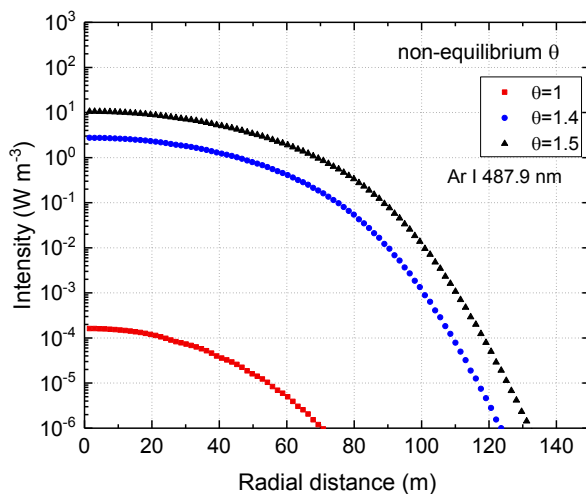


Figure 5-40. Simulated dependence of Ar II 487.9 nm intensities as a function of radial distance of a 35Ar-60He plasma at a pressure of 200 Pa, calculated for different non-equilibrium parameters θ , at an axial stand-off distance of 1 m.

5.3 Monte Carlo Simulation of Plasma Spray-Physical Vapor Deposition

Characteristics of columnar microstructures formation produced by the PS-PVD process have been discussed in the before chapters. Monte Carlo simulation is applied to model the column growth in the process, which is based on the following three main points: the fast deposition rate, no consideration of the preferential crystal orientation of columns, and the neglected surface and bulk diffusion.

5.3.1 Influence of Limited Diffusion

Figure 5-41 shows the influence of limited diffusion on the microstructure evolution. Limited diffusion means when the newly incoming particle firstly makes contact with the already deposited particles, but it is allowed to relax to the nearest free neighbor position. After this relaxation process is completed, the next incident particle is introduced. Where limited diffusion is considered, as shown in Figure 5-41(b), the microstructure has a higher intra-columnar porosity (17%) compared to that of Figure 5-41(a). However, its influence on inter-columnar porosity is negligible. In contrast to PS-PVD coatings shown in Figure 2-17(b), it can be concluded that the consideration of limited diffusion gives results that are more realistic.

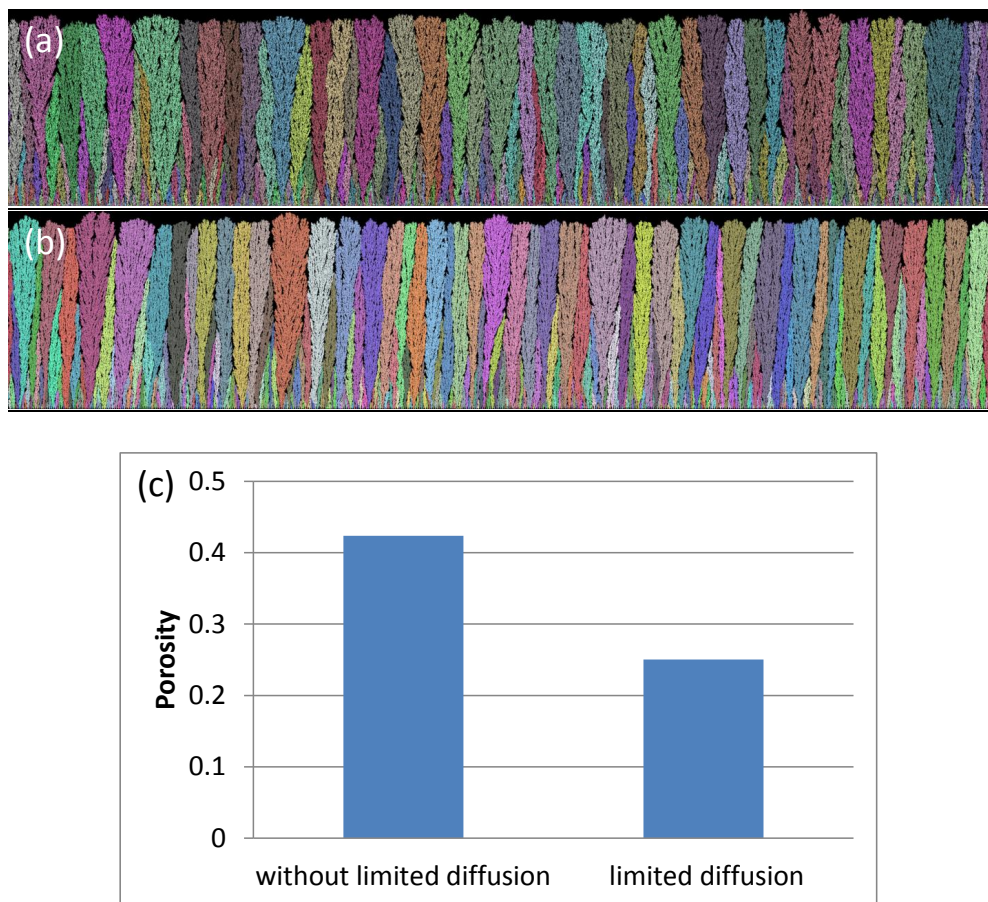


Figure 5-41. Vapor flux distribution (μ, σ) = ($0^\circ, 30^\circ$), (a) without limited diffusion, (b) with limited diffusion, and (c) porosity comparison of (a) and (b).

5.3.2 Morphology of Simulated Columns

5.3.2.1 Deposition of Normal Vapor Incidence

Figure 5-42 shows four simulated column growths under normal vapor incidence ($\mu = 0^\circ$) with standard deviations (σ) corresponding to 10° , 30° , 60° , and 90° , respectively. The different colors (pixels) represent columns originating from different parental seeds. The columns are not perfectly straight. When their height is still small, the difference in

column heights is not large enough to allow blocking of columns, then, the width of the column is also still small, indicating that horizontal growth was limited. As the height increases, the width of the column increases over a broad transition region until the width of column is almost linearly growing with the height. This is due to competitive growth (the width can only increase if other columns stop to grow) [137].

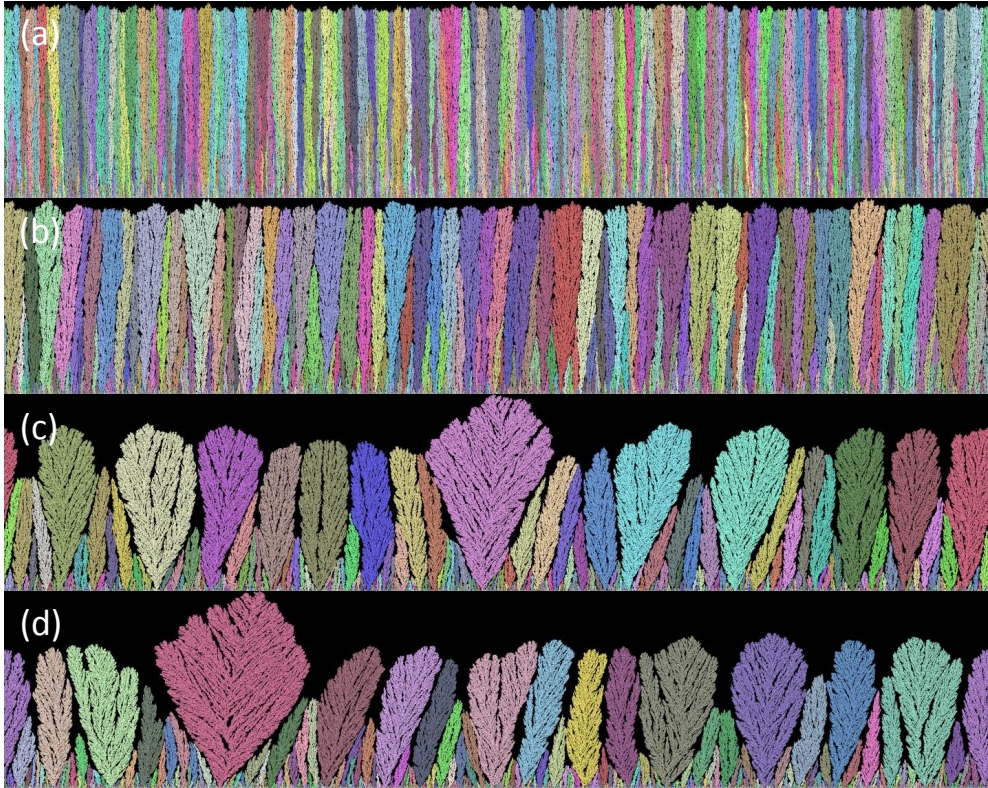


Figure 5-42. Simulated structures deposited under normal vapor incidence, $\mu = 0^\circ$, steps = 3, (a) $\sigma = 10^\circ$, (b) $\sigma = 30^\circ$, (c) $\sigma = 60^\circ$, (d) $\sigma = 90^\circ$.

These graphs show that uniformity of the columns is significantly more pronounced for narrow angle distributions. Furthermore, a broad distribution of incident vapor angle results in an increased inter-columnar porosity. Under these conditions, the inter-columnar gaps are wide, and competitive growth between neighboring is evident.

However, as the incident vapor is orientated parallel to the substrate surface normal, the more deposited structure becomes densely packed. As standard deviation angle (σ) increases from 30° to 60° microstructures can grow from clearly columnar to loosely symmetric cauliflower-shaped structures.

5.3.2.2 Deposition of Oblique Vapor Incidence

Figure 5-43 shows the influence of the value of mean angle (μ) of the vapor flux on the simulated structures. The columnar structure therefore becomes increasingly more noticeable with larger mean angles of vapor incidence. As the mean angle increases, the uniformity of column's size decreases. The most uniformly separated columnar structure is seen in Figure 5-42(b) and Figure 5-43(a), which is the result of a narrowly distributed vapor flux.

Since the incident direction was inclined, the resulting columns are also inclined. Just above the substrate, the columns grow almost perpendicularly irrespective of incident angle of the vapor flux. As the distance from the substrate increases, the columns become gradually more inclined. It can be concluded that when the incident vapor angle is too high (including mean angle and standard deviation angle), the changes of morphology, porosity, orientation of columns are disregarded.

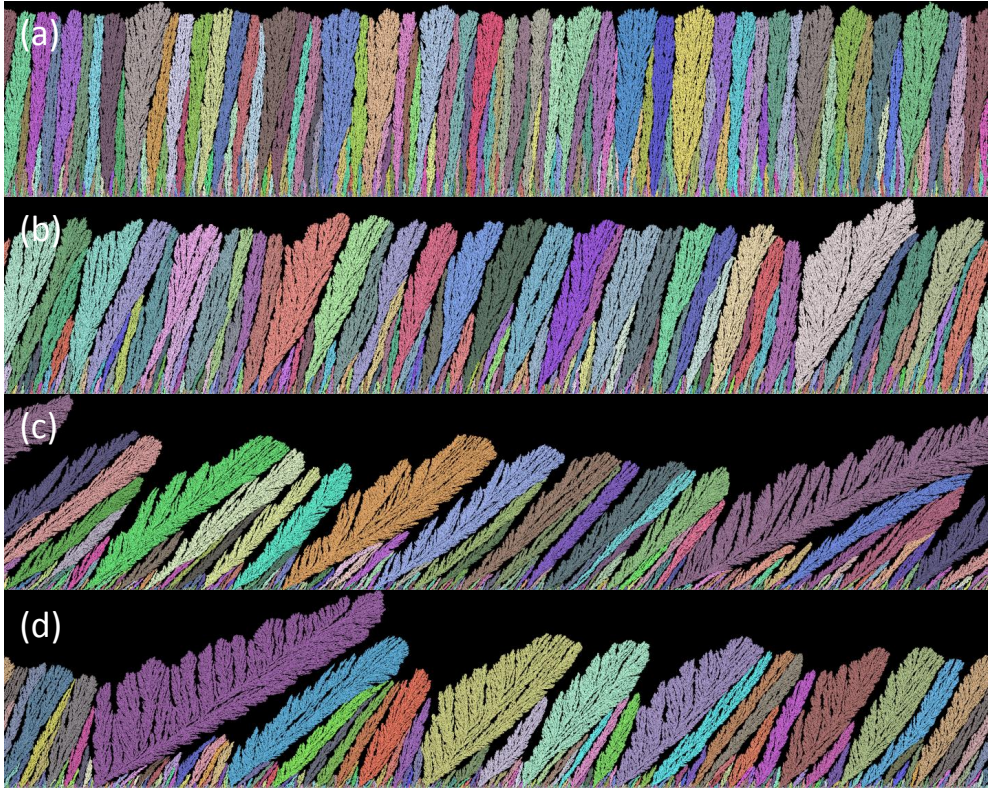


Figure 5-43. Simulated structures deposited at an oblique normal vapor incidence, $\sigma = 30^\circ$, Steps = 3, (a) $\mu = 10^\circ$, (b) $\mu = 30^\circ$, (c) $\mu = 60^\circ$, (d) $\mu = 90^\circ$.

In contrast to Figure 5-42 and 5-43 (steps = 3), Figure 5-44 shows the influence of oblique incidence fluxes on simulated structures for a different seed distance (steps = 10). It can be clearly observed that by increasing seed distance variations of the morphology and orientation of columns structure are negligible. The porosity of growth is sensitive to the initial seed distance of the substrate only during the early stage of depositions. However, a large incident angle contributes to greatly loosely columnar structures, which are easily detached from the substrate in reality.

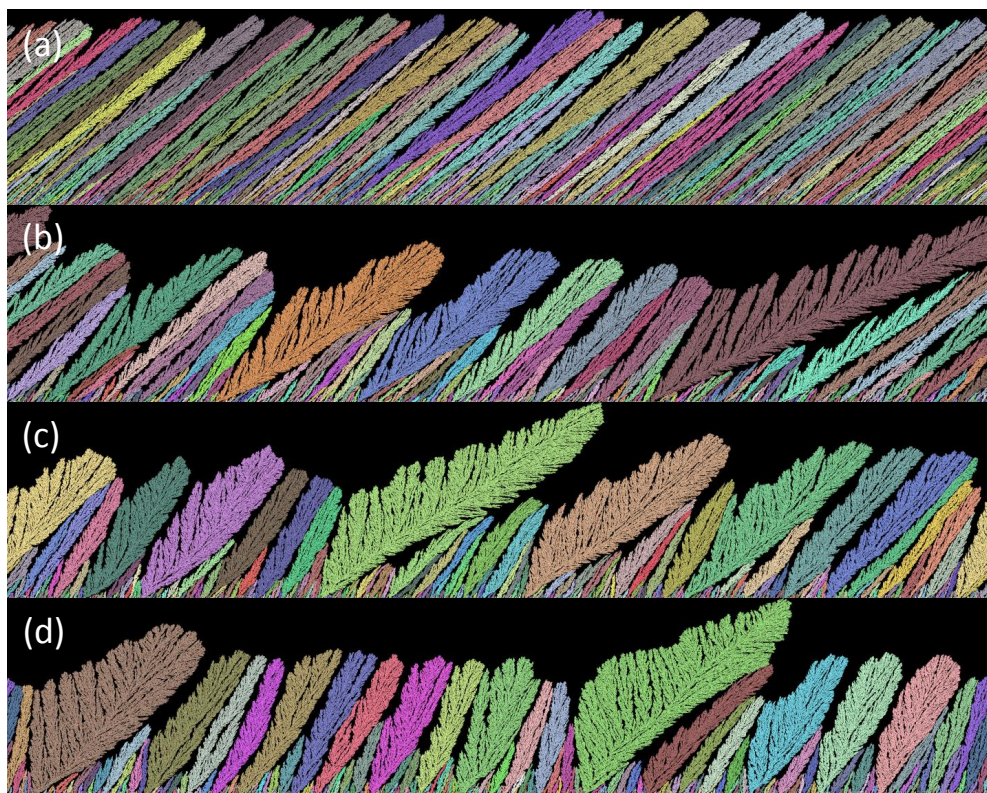


Figure 5-44. Simulated structures deposited at an oblique normal vapor incidence, steps = 10, $\mu = 60^\circ$, (a) $\sigma = 10^\circ$, (b) $\sigma = 30^\circ$, (c) $\sigma = 60^\circ$, (d) $\sigma = 90^\circ$.

According to [146], tapered columns with domed tops and columns separated by voids result from self-shadowing where surface diffusion is not considered. A. Hospach [123] presents PS-PVD coatings with big gaps between columns which is comparable with the simulated columns.

5.3.2.3 Single Column Growth

Figure 5-45 presents the mechanism of a single column growth resulting from an increased lateral component of the incoming vapor. Graphs of three columns indicate that

the feathery structures at the side of the column is formed. Without influence of another column, higher fluctuations of the incident vapor angle lead to wider columns.

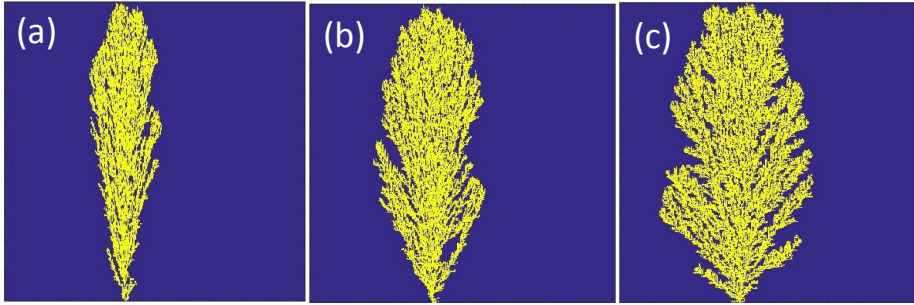


Figure 5-45. One column growth at different distributions, (a) $(\mu, \sigma) = (0^\circ, 5^\circ)$, (b) $(\mu, \sigma) = (0^\circ, 10^\circ)$, (c) $(\mu, \sigma) = (0^\circ, 20^\circ)$.

5.3.3 Porosity Analysis

The pore structure includes inter-columnar voids surrounding $\sim 10 \mu\text{m}$ diameter width of columns and nanoscale pores exist within the columns [136, 187]. In addition to the inter-columnar gaps, TBCs produced by PS-PVD process contain substantial amounts of intra-columnar porosity. The large inter-columnar pores reduce coating strain energy by accommodating mismatches in thermal expansion, the microscale pores provide a significant decrease in coating thermal conductivity in the heat flux propagation direction. Nanoscale pores also decrease coating conductivity by increasing phonon scattering, but are fast removed by sintering during operation of the engine [115, 188, 189]. Internal pores (voids) or microcracks aligned perpendicular to the direction of heat conduction, which provides good thermal insulation [136, 143, 147]. In the boundary of columns, porosity is typically arranged in a “feathery” morphology, comprising thin ribbon-like pores at an angle to the column axis.

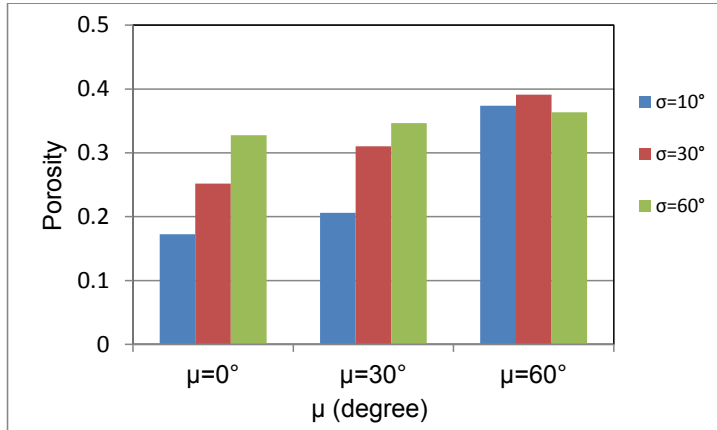


Figure 5-46. Porosity of simulated structures as a function of the different incident vapor angle (μ, σ), steps = 3.

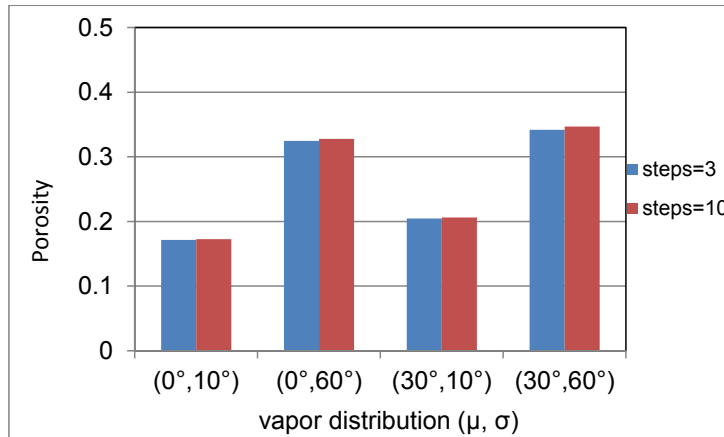


Figure 5-47. The porosity of simulated structures as a function of seeding and different incident vapor angle (μ, σ).

Figure 5-46 shows the influence of the standard deviations (σ) on the porosity of the simulated columns. The results indicate that the porosity decreases when the vapor flux becomes more narrowly distributed. When the mean angle (μ) of the incident vapor angle increases the porosity increases. For very large mean angle and standard deviations, the broadness of the distribution of incoming vapor results in a very large lateral component

of the growth. Figure 5-47 indicates that the effects of the seeding size on the porosity can be neglected.

Typical porosity of TBCs obtained by PS-PVD are about 10-30% , which is slightly smaller than the porosity in simulated results. Two factors account for the discrepancy. Firstly, TBCs produced by PS-PVD contain substantial amounts of intra-columnar porosity. These tiny pores are simply neglected depending on the experimental analysis method and the morphology of the coatings. The second factor relates to the diffusion in the boundary layer of the substrate at a very high substrate temperature and the influence of surface roughness on the vapor flux direction.

5.3.4 Orientation of Columns

Figure 5-48 shows the relationship of the orientation of columns and the vapor incidence angle. The orientation of the columns is smaller than the vapor incidence angle. The inclination angle of the columns (β) can often be well fitted with an vapor incident mean angle (μ)

$$\mu = 2 * \beta \quad (5.1)$$

when the self-shadowing effect from other columns is removed, as shown in Figure 5-45, one column would grow exactly along the direction of the vapor flux. The orientation angle is half the value of the vapor incidence angle. The error of the column orientation angle is $\pm 1^\circ$. At higher mean angles, broader distribution of incoming vapor leads to smaller tilted angle of the columns owing to a higher probability of the lateral growth.

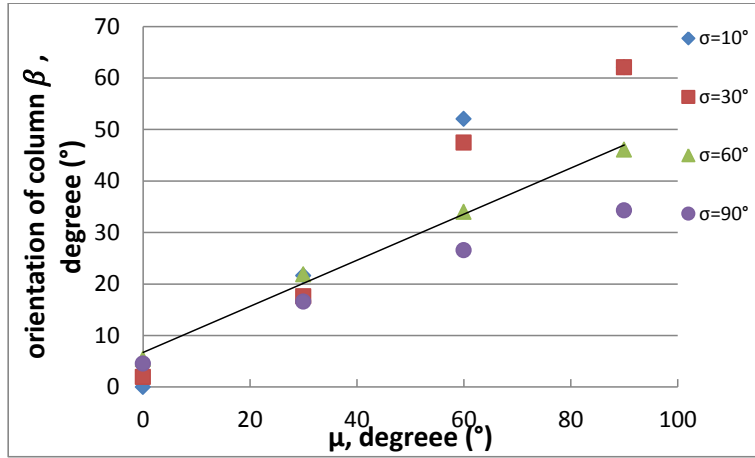


Figure 5-48. The influence of the vapor incidence angle on the orientation of columns.

Hodgkinson *et al.* [190] suggested the tangent rule by inserting a constant E , for the empirical observation, such that $\tan(\beta) = E \tan(\alpha)$. D. J. Srolovitz *et al.* claim that due to self-shadowing the tangent rule is approximately valid, while diffusion reduces the inclination angle of the column [191]. The columnar inclination angle (β) with a vapor incident angle (α) can also be well fitted by $\tan(\beta) = \frac{1}{2} \tan(\alpha)$ [192, 193]. These equations are not derived from any basic principles, but were found to correlate well with the predicted tendency of experimental results. In contrast to these publications, it can be concluded that we also find a comparable expression.

In the future, in order to build up the relationship between the modeling of PS-PVD process and the Monte Carlo simulation of the growth of the columns, the morphology and surface roughness of columnar coatings is investigated. Columnar coatings produced by PS-PVD process will be presented to compare the simulated microstructures by the Monte Carlo model. Then, the surface roughness of deposited columnar coatings will be combined with the plasma jet flow field around the substrate to evaluate the angle of the impingement of the vapor flux onto the substrate. Finally, the relationship between the incident vapor flux and the orientation of the columns can be evaluated from the modeling and the experiment.

5.3.5 Microstructures of PS-PVD Coatings

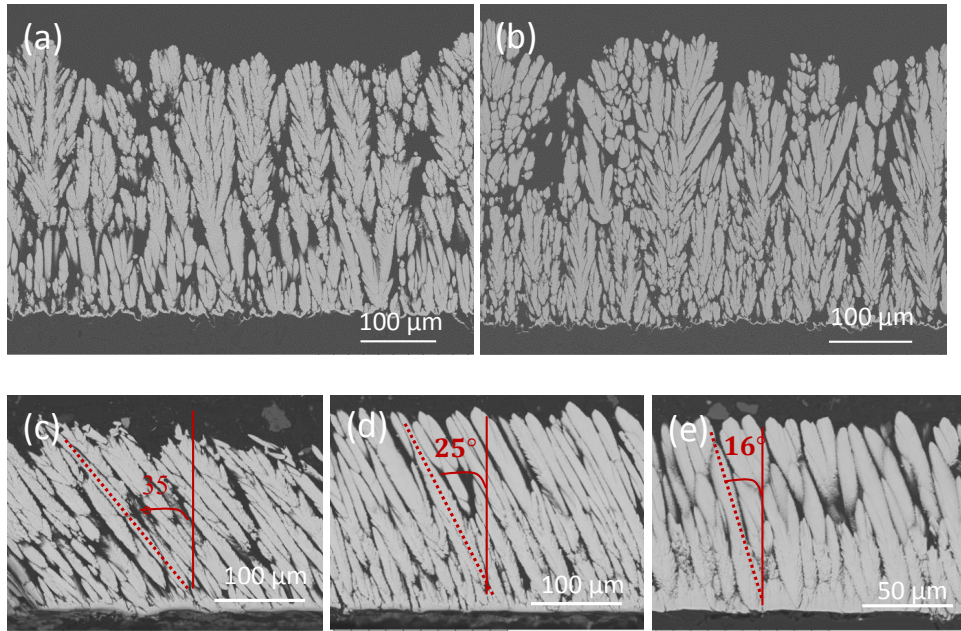


Figure 5-49. SEM (back-scattered electron) images of columnar microstructures from W.He's experiment, (a)-(b) $\mu = 0^\circ$, in contrast to [194], (c)-(e) $\mu = 90^\circ$.

Figure 5-49 shows the SEM images of columnar microstructures that are produced by 35Ar-60He plasma jet at a pressure of 200 Pa at a stand-off distance of 1 m in two different conditions. The two top images (a)-(b) result from a vapor flux coming from the substrate normal. Figure 5-49(a) shows the microstructure in the edge of the substrate, and Figure 5-49(b) shows the microstructure located at the center of the substrate. In the edge, the orientation of column is slightly tilted due to the change of the vapor flux vector. The three bottom images (c)-(e) were obtained from a deposition with a horizontal substrate. In the experiment, the morphology of columns is related to the substrate temperature and the deposition rate. On one hand, the change morphology of the columns is enhanced due to surface diffusion as it should be hotter at the edge, as shown in Figure 5-30. On the other hand, the deposition rate is smaller the further away from the leading edge, so that columns are thinner shown in Figure 5-49 (c)-(e).

The analysis of the orientation of the columns shows that the columns grow toward the direction of the vapor flux. In contrast to Figure 5-48, Figure 5-49(c)-(e) shows the predicted orientation angle is slightly bigger than the orientation angle in the experiment. The tilted angle of the columns decreases along the direction of the flow. Two reasons explain the variation. The first is the presence of the boundary layer with varying thickness. Especially in the case of the horizontal substrate, the boundary layer flow is related with the distance to edge along the substrate surface, as shown in Figure 5-51. Eddies will change the direction of the impingement of flow onto the substrate surface. The second is the influence of surface roughness on the deposited coatings influence.

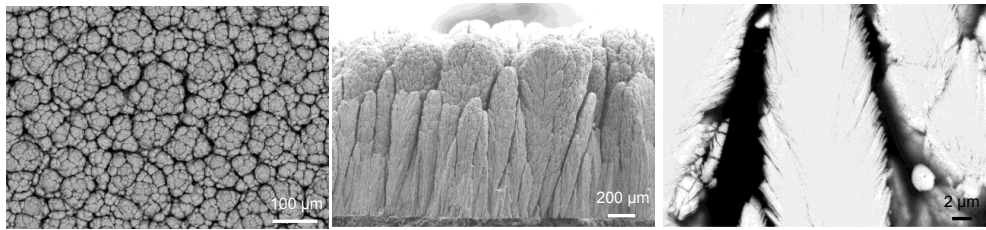


Figure 5-50. SEM (back-scattered electron) images of columnar microstructures [61], (a)-(b) $\mu > 0^\circ$.

Figure 5-50 produced by Hospach [61] presents an evident cauliflower microstructures where the coatings are deposited on a tilted substrate in a 35Ar-60He plasma jet at a chamber pressure of 200 Pa at a stand-off distance of 1 m, which is comparable to Figure 5-43(a). As the substrate is tilted, the angle between the incident vapor flux and the substrate surface increases, which leads to the growth of cauliflower-like columns.

5.3.6 Surface Morphology

Figure 5-51 illustrates the boundary layer around the substrate surface for the case of a parallel deposition. When the plasma jet flows over the substrate surface, a velocity boundary layer is developed over the surface due to fluid viscosity. Velocity boundary layer thickness (σ_t) grows with the square root of distance from the leading edge of the sample. For the hot plasma jet flows surround the substrate, the temperature boundary layer is also formed around the substrate surface. The temperature boundary layer is the

region where the plasma jet temperature changes from its free-stream value to that at the substrate surface. Heat transfer can take plasma from the plasma jet into the substrate through the velocity boundary layer. For the ideal case, the temperature profile is the same as the velocity profile through the entire boundary layer over the substrate surface. For different positions at the substrate surface, the turbulence properties are distinct, leading to different orientation of columns, as shown in Figure 5-49(c)-(e). In the laminar boundary layer, the temperature profile gradually changes from the plasma jet value to the surface as a parabolic shape, but in the turbulent boundary layer, the temperature profile remains uniform and then suddenly changes to the surface value due to turbulent mixing in the direction of back and forth or up and down. Therefore, along the downstream of the plasma jet, the flow vector could change greatly.

To evaluate the surface roughness of columnar microstructures, samples with YSZ coatings deposited by 35Ar-60He plasma jet at a standoff distance of 1 m at a chamber pressure of 200 Pa were carried out on substrates with different orientation. Different columnar microstructures were obtained; the results indicated that coatings on the vertical sample may have lower roughness than that on the horizontal sample.

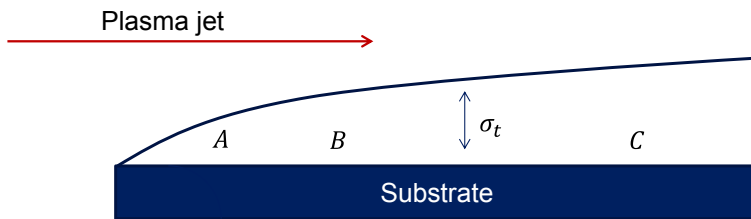


Figure 5-51. The boundary layer for the horizontal sample orientation.

Figure 5-52 shows three distinct roughness of the substrate surface before and after coating deposited. Figure 5-52(a) depicts the graphite surface before the deposition. It is a rather smooth with a roughness of maximum of $46.7\ \mu\text{m}$. For coatings deposited on the vertical substrate, columns grow in the direction perpendicular to the substrate, the width of resulting columns are smaller and the surface roughness of the coating is smoother compared to that deposited on the horizontal sample (surface roughness of $82.8\ \mu\text{m}$ vs $256.6\ \mu\text{m}$).

The orientation and width of columns is determined by the incident vapor flux. According to the modeling of the built-up of columns in Chapter 5.3.2, broader oblique vapor flux results in broader columns, and the resultant surface roughness is rougher, which is comparable to the measurement shown in Figure 5-52(b) and 5-52(c).

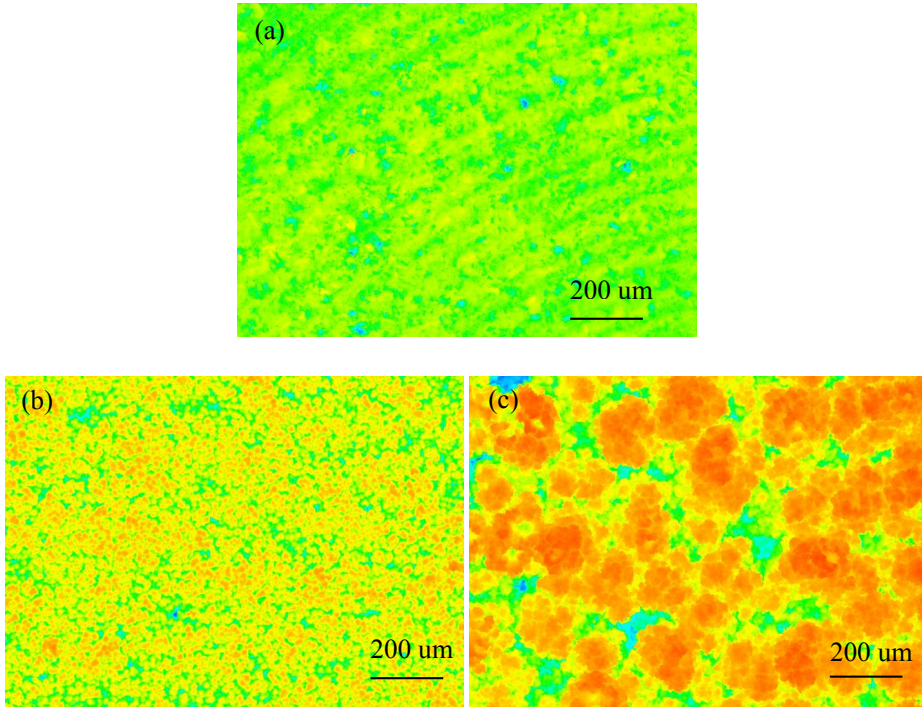


Figure 5-52. The surface roughness of the substrate, (a) before the deposition with maximum values of $46.7\text{ }\mu\text{m}$, (b) coating surface after deposition on the vertical substrate with maximum values of $82.8\text{ }\mu\text{m}$, (c) coating surface after deposition on the horizontal substrate with surface maximum values of $256.6\text{ }\mu\text{m}$ (center).

6 Summary and Conclusions

This dissertation was focused on the modeling of the PS-PVD, as shown in Figure 6-1. Five main topics were investigated: (1) thermodynamic and transport properties for different plasma mixtures (35Ar-60He, 35Ar-60He-10H₂, and 100Ar-10H₂) depending on the pressure and the temperature; (2) vacuum plasma spray; (3) plasma spray-physical vapor deposition; (4) built-up of columnar coatings using the Monte-Carlo method; (5) the validation by the experiment.

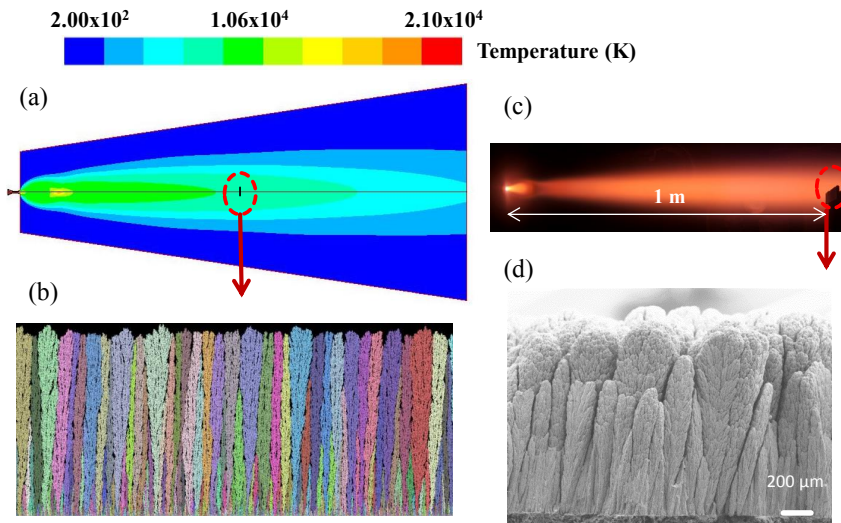


Figure 6-1. Images revealing the main topics in this work: (a) the plasma jet modeling, (b) the Monte Carlo simulation of the columns, (c) photograph of the plasma jet, (d) columnar microstructures produced by PS-PVD process [61].

Studies on the photographs of plasma jets validated the plasma properties of the simulated plasma spray with varying chamber pressures. Measurements of optical emission spectroscopy highlighted the accuracy of the modeling of the temperature distribution of plasma spray physical vapor deposition. Investigations on the influence of the roughness of the substrate surface on the flow direction give further insight of the built-up of columnar PS-PVD coatings. The conclusion of this work is that plasma jet

simulation using the 2-D SST $k-\omega$ turbulence model, with the consideration of virtual nozzle geometry but neglecting the arc dynamics in the torch, has the potential to result in a reliable and precise investigation of the distribution of the temperature and turbulence properties. The Monte-Carlo simulation, reflecting the fundamentals of the PS-PVD process, reveals a promising and predictive method to simulate the microstructure of PS-PVD columnar coatings. Detailed conclusions and remarks follow below.

In the first section, investigations of thermodynamics and transport suggest that 35Ar-60He and 35Ar-60He-10H₂ mixtures have a higher capacity to evaporate the feedstock particles than 100Ar-10H₂ in the PS-PVD process at a chamber pressure of 200 Pa, this is experimentally validated by the microstructures produced by PS-PVD process [195]. The recombination of hydrogen atoms at 2500 K plays an important role to increase the enthalpy, specific heat capacity, and thermal conductivity of H₂-containing plasma mixtures to increase the substrate temperature.

In the second section, vacuum plasma spray was modeled at chamber pressures from 200 Pa to 10000 Pa of a 35Ar-60He plasma. The plasma jet is laminar and homogeneous for a lower chamber pressure. Results of the simulation suggested that the length of the plasma jet, the turbulence, the analysis of Mach disk, which were comparable to photographs of the plasma jet. However, the two dimensional computational model cannot give a comprehensive description of the jet turbulence, particularly, the formation of vortices.

The PS-PVD process at a chamber pressure of 200 Pa was modeled utilizing three types of plasma mixtures (35Ar-60He, 35Ar-60He-10H₂, and 100Ar-10H₂). The jet using 35Ar-60He plasma yields the highest temperature of 18000 K while applying 100Ar-10H₂ plasma results in the lowest temperature of 12500 K at the nozzle outlet. At a stand-off distance of 1 m from the exit of the nozzle, the temperature of a 35Ar-60He plasma jet is the highest with 8000 K, while the temperature of a 35Ar-60He-10H₂ plasma jet is the lowest with 5000 K. The maximum velocity for 35Ar-60He and 35Ar-60He-10H₂ plasma jets is roughly 10000 m/s, while for the 100Ar-10H₂ jets the maximum velocity is approximately 6000 m/s. At the standoff distance of 0.21 m from the nozzle exit, fluctuations occur due to the sharp decrease of the velocity. Photographs of the plasma

jets show a comparable result. The velocity is about 2000 m/s at the standoff distance of 1 m for the three cases investigated.

The Saha ionization law was used to determine the distributions of plasma compositions of PS-PVD processes at a chamber pressure of 200 Pa using 35Ar-60He mixtures. Spectral line intensities were calculated utilizing the Boltzmann distribution depending on the plasma composition and the temperature profile of the plasma jet modeling. Intensities of Ar I 763.5 nm and Ar II 487.9 nm were estimated along the radial direction at a stand-off distance of 1 m. It has shown that the parameter of the non-equilibrium plays a role in determining the relative spectral line intensities. Results suggested that intensities were not strong enough to be detected by OES at equilibrium. The non-equilibrium parameter was estimated to be around 1.3.

Finally, a two-dimensional Monte Carlo simulation was employed to investigate the formation of columnar growth in the physical vapor deposition process. Particularly, in the case of the PS-PVD process, the surface diffusion in the coating can be neglected because of the high deposition rate. As the incident angle of vapor flux changes from a narrow to a broad fluctuation, the morphology of growth changes from a densely packed structure to a clearly columnar structure, then to a cauliflower-like structure with large gaps between the columns due to self-shadowing. Furthermore, the columns are oriented towards to the direction of the vapor flux; the angle of columns equals almost half the value of the angle of the incident vapor. As to the orientation and the morphology of the columns, it can be concluded in the modeling of the built-up of columns that oblique vapor flux results in broader columns and the resultant surface roughness is rougher, which is comparable to the microstructures produced by a PS-PVD process. The results also indicate that the porosity increases when the vapor flux becomes broadly distributed. However, the influence of the initial seed distance on the porosity of structures proved to be neglected.

However, in the future, since the composition is known, in the conditions of non-equilibrium, thermodynamic and transport properties can also be calculated. Depending on these properties, fluid dynamic simulation could also evaluate the temperature and the turbulent properties of the plasma jet. When feedstock particles are injected, melted, and

evaporated, the melting processes and vapor distributions of feedstocks can be evaluated in the plasma jet to analyze the plasma-particle interactions. Another possible topic is when continuum flow breaks down at very low chamber pressure by intense and numerous shocks, the rarefaction phenomenon lead to the transition from continuum flow to slip flow and eventually to free molecular flow.

Furthermore, the surface roughness of coatings could be normalized and compared to the surface of simulated columnar microstructures. Computational fluid dynamics will be used to simulate the flow direction surrounding the substrate. So the orientation of titled columns growth could be investigated by the influence of the surface roughness on the flow direction. The influence of substrate temperature and the deposition rate on the coating thickness and the detailed structural formation of coatings could be investigated by this Monte Carlo method.

7 References

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Appendix

Matlab code for Monte-Carlo Simulation with neighbor's consideration

```
function [ A ] = mc_pspvd_fly_neighbours_coder(nx,ny,skip,alpha0,alphasigma)
%MC_PSPVD Summary of this function goes here
% Detailed explanation goes heres
% example im=image(flipud(mc_pspvd(400,1000,10,20,0.1))); im.CDataMapping = 'scaled';
% eps=1e-5;
%c_pspvd_fly_neighbours_coder_mex(int32(5000),int32(1000),int32(1),double(0),double(30));
coder.extrinsic('imagesc');
assert(isa(nx, 'int32'));
assert(isa(ny, 'int32'));
assert(isa(skip, 'int32'));
assert(isa(alpha0, 'double'));
assert(isa(alphasigma, 'double'));

A=zeros(ny,nx,'uint16'); % orientation matrix
B=A(ny,skip+1:skip:nx-1);
[~,ix]=size(B);
r=randperm(double(floor(nx/skip)),ix)+double(floor(nx/(skip*5)));
A(ny,int32(skip+1):int32(skip):int32(nx-1))=uint16(r);
A(ny,int32(skip+2):int32(skip):int32(nx))=uint16(r);

%%A(ny,skip+1:skip:nx-skip)=randperm(floor(nx/skip),floor((nx-skip-1)/skip))+floor(nx/(skip*5));
nc=int32(0);
nstep=int32(round(1000000/nx*10));
if nstep==0
    nstep=int32(1);
end

% for r= 1:row*column
% steps=0; % each new walk
%%oldtime=now;

ytop=ny;

smallangle=5;
xmoveoffset=int32([-1 -1 0 0 0;-1 -1 0 1 1;1 1 0 0 0]);
ymoveoffset=int32([0 1 1 0 0;0 1 1 1 0;0 1 1 0 0]);
nmoveoffset=int16([3 5 3]);

while nnz(A(1,:))==0
    ystart=max(ytop-5,1);
    %%ystart=1;
```

```

xstart=int32(randi([1 nx])); % starts of the incoming particles, random interger numbers in the range 1
to n
alpha=double(random('Normal',alpha0,alphasigma)); % random alpha, mean value=alpha0,
standdeviations=alphasigma, normal distribution
while abs(alpha)>90
    alpha=random('Normal',alpha0,alphasigma); % control random alpha in the range of -90 to 90
end

xhit=int32(0);
yhit=int32(0);
xlast=int32(0);
ylast=int32(0);
xfly=int32(0);
yfly=int32(0);
xfly=int32(xstart);
yfly=int32(ystart);
xflytmp=double(xstart);
yflytmp=double(ystart);
maxnb=int16(0);
xnew=int32(0); ynew=int32(0);

if abs(alpha)>45
    % count x direction // columns
    m=abs(cotd(alpha));
    m=max(m,0.001);
    dir=sign(alpha);
    while yfly<ny
        xlast=xfly;
        ylast=yfly;
        xfly=xfly+dir;
        if xfly<=0 %% periodic boundary
            xfly=nx;
        elseif xfly>nx
            xfly=int32(1);
        end
        yflytmp=yflytmp+m; %% non integer
        yfly=round(yflytmp); %% integer
        %%display(yfly);
        yfly=min(ny,yfly);
        if(A(yfly,xfly)~=0)
            yhit=yfly;
            xhit=xfly;
            yfly=ny+1; %% terminate while loop
        end
    end
else
    m=tand(alpha);
    while yfly<ny
        xlast=xfly;
        ylast=yfly;

```

```

xflytmp=xflytmp+m;
xfly=int32(round(xflytmp));
if xfly<=0 %% periodic boundary
    xfly=nx;
    xflytmp=double(nx);
elseif xfly>nx
    xfly=int32(1);
    xflytmp=1;
end
yfly=yfly+int32(1);
if(A(yfly,xfly)~=0)
    yhit=yfly;
    xhit=xfly;
    yfly=ny+1; %% terminate while loop
end
end
end

if(xhit>0 && yhit>0) %% hit some existing position
    if(A(ylast,xlast)==0)
        nb=int16(count_neighbours(A,nx,ny,xlast,ylast));
        if nb >= int16(2)
            A(ylast,xlast)=A(yhit,xhit);
            ytop=min(ylast,ytop);
        else
            if(abs(alpha)<smallangle) dir=int16(2); else dir=int16(sign(alpha))+int16(2); end; % 1: -90..-5
2: -5..5 3: 5..90
            xold=xlast; yold=ylast;
            while yold<=ny;
                maxnb=int16(0); xnew=int32(0); ynew=int32(0);
                for i=1:nmoveoffset(dir)
                    yfly=yold+ymoveoffset(dir,i);
                    if(yfly>0 && yfly<=ny)
                        xfly=xold+xmoveoffset(i);
                        if xfly<=0 xfly=nx; elseif xfly>nx xfly=int32(1); end
                        if(A(yfly,xfly)==0)
                            nb=count_neighbours(A,nx,ny,xfly,yfly);
                            if nb>maxnb
                                maxnb=nb; xnew=xfly; ynew=yfly;
                            end
                        end
                    end
                end
                if maxnb==1
                    xold=xnew; yold=ynew;
                else
                    break;
                end
            end
        end
    end
end

```

```

        if maxnb>int16(0)
            A(ynew,xnew)=A(yhit,xhit);
            ytop=min(ynew,ytop);
        %%%
        else
            A(ylast,xlast)=A(yhit,xhit);
            ytop=min(ylast,ytop);
        %%%
        end
    end
    %%%      display(ytop);
end
end

nc=nc+int32(1);
if (mod(nc,nstep)==0)
    imagesc(A);
    drawnow;
end
end
imagesc(A);

%plot((sum(transpose(A)==0))/nx);
%display((sum(transpose(A)==0))/nx);

% %    lsline
% grid on
% grid minor

end

function nb=count_neighbours(A,nx,ny,x,y)
xdiagoffset=int32([0 1 1 1 0 -1 -1 -1]);
ydiagoffset=int32([1 1 0 -1 -1 -1 0 1]);
nb=int16(0);

for i=1:8
    yfly=y+ydiagoffset(i);
    if(yfly>0 && yfly<=ny)
        xfly=x+xdiagoffset(i);
        if xfly<=0 %%% periodic boundary
            xfly=nx;
        elseif xfly>nx
            xfly=int32(1);
        end
        if(A(yfly,xfly)>0) nb=nb+int16(1); end
    end
end
end
end

```

Matlab code for Monte-Carlo Simulation without neighbors' consideration

```
function [ A ] = mc_pspvd_fly_coder(nx,ny,skip,alpha0,alphasigma)
%MC_PSPVD Summary of this function goes here
% Detailed explanation goes heres
% example im=image(flipud(mc_pspvd(400,1000,10,20,0.1))); im.CDataMapping = 'scaled';
% eps=1e-5;
coder.extrinsic('imagesc');
assert(isa(nx, 'int32'));
assert(isa(ny, 'int32'));
assert(isa(skip, 'int32'));
assert(isa(alpha0, 'double'));
assert(isa(alphasigma, 'double'));

A=zeros(ny,nx,'uint16'); % orientation matrix
B=A(ny,skip+1:skip:nx-skip);
[~,ix]=size(B);
r=randperm(double(floor(nx/skip)),ix)+double(floor(nx/(skip*5)));
A(ny,int32(skip+1):int32(skip):int32(nx-skip))=uint16(r);

%%A(ny,skip+1:skip:nx-skip)=randperm(floor(nx/skip),floor((nx-skip-1)/skip))+floor(nx/(skip*5));

nc=int32(0);
nstep=int32(round(10000000/nx*10));
if nstep==0
    nstep=int32(1);
end

% for r= 1:row*column
% steps=0; % each new walk
%%oldtime=now;

ytop=ny;

while nnz(A(1,:))==0
    ystart=max(ytop-5,1);
    %ystart=1;
    xstart=int32(randi([1 nx])); % starts of the incoming particles, random interger numbers in the range 1
to n
    alpha=double(random('Normal',alpha0,alphasigma)); % random alpha, mean value=alpha0,
standdeviations=alphasigma, normal distribution
    while abs(alpha)>90
        alpha=random('Normal',alpha0,alphasigma); % control random alpha in the range of -90 to 90
    end

    xhit=int32(0);
    yhit=int32(0);
```

```

xlast=int32(0);
ylast=int32(0);
xfly=int32(xstart);
yfly=int32(ystart);
xflytmp=double(xstart);
yflytmp=double(ystart);
if abs(alpha)>45
    % count x direction // columns
    m=abs(cotd(alpha));
    m=max(m,0.001);
    dir=sign(alpha);
    while yfly<ny
        xlast=xfly;
        ylast=yfly;
        xfly=xfly+dir;
        if xfly<=0 %% periodic boundary
            xfly=nx;
        elseif xfly>nx
            xfly=int32(1);
        end
        yflytmp=yflytmp+m; %% non integer
        yfly=round(yflytmp); %% integer
        %%display(yfly);
        yfly=min(ny,yfly);
        if (A(yfly,xfly)~=0)
            yhit=yfly;
            xhit=xfly;
            yfly=ny+1; %% terminate while loop
        end
    end
else
    m=tand(alpha);
    while yfly<ny
        xlast=xfly;
        ylast=yfly;
        xflytmp=xflytmp+m;
        xfly=int32(round(xflytmp));
        if xfly<=0 %% periodic boundary
            xfly=nx;
            xflytmp=double(nx);
        elseif xfly>nx
            xfly=int32(1);
            xflytmp=1;
        end
        yfly=yfly+1;
        if (A(yfly,xfly)~=0)
            yhit=yfly;
            xhit=xfly;
            yfly=ny+1; %% terminate while loop
        end
    end
end

```

```

    end
end

if(xhit>0 && yhit>0) %% hit some existing position
    if(A(ylast,xlast)==0)
        A(ylast,xlast)=A(yhit,xhit);
        ytop=min(ylast,ytop);
        %%      display(yt op);
    end
end

nc=nc+int32(1);
if (mod(nc,nstep)==0)
    imagesc(A);
    drawnow;
end
end
imagesc(A);
figure;

%plot((sum(transpose(A)==0))/nx);
%display((sum(transpose(A)==0))/nx);

% %    lline
% grid on
% grid minor

End

```

Monte-Carlo Simulation for Angle Analysis of Columns

```

function [ angles ] = angle_analysis( A )
%ANGLE_ANALYSIS Summary of this function goes here
% Detailed explanation goes here

[ny,nx]=size(A);% 100, 100
[dummy,dummy,v]=find(A(floor(ny/3*2,:))); % , v non-zero values important
values=unique(v); % special
[dummy,nv]=size(values);%
angles=zeros(size(values));

[dummy,dummy,v1]=find(A(1,:));
values_1=unique(v1)

[dummy,dummy,v2]=find(A(ny,:));
values_2=unique(v2)

[dummy,dummy,v3]=find(A(:,1));

```

```

values_3=unique(v3)

[dummy,dummy,v4]=find(A(:,nx));
values_4=unique(v4)

newvalues=[values_1 values_2 transpose(values_3) transpose(values_4)];

values_5=unique(newvalues);
[dummy,nv1]=size(values_5);

figure

hold on
for iv=1:nv
    [rows,cols]=find(A==values(iv)); % values of nonzero element
    xvalues=unique(cols);

    [rows1,cols1]=find(A(ny,:)==values(iv)); % question values of nonzero element

    xstart=mean(cols1); % question values of nonzero element
    %%
    if(min(xvalues)== 1 && max(xvalues) == nx)
        xgap=1;
        while(xgap<nx && xvalues(xgap)==xgap) xgap=xgap+1; end;

        if xstart<xgap
            if (nv1>0)
                [idx,dummy]=find(cols>xgap); % nonzero element idx, indices dummy
                cols(idx)=cols(idx)-2*nx;
            else
                [idx,dummy]=find(cols>xgap); % nonzero element idx, indices dummy
                cols(idx)=cols(idx)-nx;
            end

        else
            [idx,dummy]=find(cols<xgap);
            cols(idx)=cols(idx)+nx;
        end
    end
    %%
    cols0=xstart-cols;
    rows0=rows-1;
    B=rows0\cols0;
    angles(1,iv)=atan2(B);
    scatter(cols,nx-rows);
end
hold off

end

```

Acknowledgement

I have my doctorate time in Forschungszentrum Jülich GmbH in Institute of Energy and Climate Research (Materials Synthesis and Processing, IEK-1) during Sep. 2014-Nov. 2017. I thank all colleagues for a nice working environment and cooperation.

My special thanks to Prof. Dr. Olivier Guillon, Prof. Dr. Robert Vaßen, and Dr. Robert Mücke for giving me an opportunity and inviting me to join in the modeling group to do doctorate research. I learn a lot from numerous constructive discussions from their outstanding expertise and experience.

I thank Prof. Armelle Vardelle for her interest in my work and reviewing my dissertation, Prof. Dr.-Ing. Roland Span for working as the chairman of the exam committee.

My special thanks to Dr. Robert Mücke, he always stands by my side and helps me from the beginning. His excellent professional knowledge, discussions and suggestions contribute significantly to the success in this work. In addition to the technical support, Dr. Robert Mücke was always a role model.

I appreciate Dr. Georg Mauer for his suggestions and supports. Office discussions contribute me greatly to combine experiment and modeling. I thank Wenting He for nice cooperation. Their help and pronounced discussions contribute notably to the work.

I thank current and former office colleagues Dr. Markus Mutter, Unoaku Unije, João G. Pereira da Silva for discussions in work and friendly working environment. My special thanks to Mr Rainer Kriescher, Dr. Emine Bakan, Dr. Diana Marcano, Prof. Laptev Alexander, Mr Bowen Lu, Dr. Ma Qianli, Dr. Zheng Hao, Ms Yang Liu, Ms Hiltrud Moitroux, and Mr Dapeng Zhou. I thank Ms Vicky Rostin and Mr Stefan Weitz for administrative support.

I thank all colleagues in IEK-1.

I thank my parents and grandparents for their endless love and support. To my sisters and brothers, thank you and all the best.

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