Spin-Glass Ground State in a Triangular-Lattice Compound YbZnGaO₄

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We report on comprehensive results identifying the ground state of a triangular-lattice structured YbZnGaO₄ as a spin glass, including no long-range magnetic order, prominent broad excitation continua, and the absence of magnetic thermal conductivity. More crucially, from the ultralow-temperature ac susceptibility measurements, we unambiguously observe frequency-dependent peaks around 0.1 K, indicating the spin-glass ground state. We suggest this conclusion holds also for its sister compound YbMgGaO₄, which is confirmed by the observation of spin freezing at low temperatures. We consider disorder and frustration to be the main driving force for the spin-glass phase.

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Quantum spin liquids (QSLs) represent a novel state of matter in which spins are highly entangled, but neither order nor freeze at low temperatures [1,2]. There is accumulating experimental evidence suggesting that such a state is realized in YbMgGaO₄ [3-11]. The magnetic specific heat C_m is proportional to T^{α} with $\alpha \approx 2/3$ [3,5,12]. It has a negative Curie-Weiss temperature of $\Theta \sim -4$ K [3,4] but does not show a long-range magnetic order at low temperatures [5,6]. Moreover, diffusive continuous magnetic excitations have been observed by inelastic neutron scattering (INS) measurements [5,6], which are interpreted as resulting from the fractional spin excitations of a QSL [13,14]. However, there are also reports challenging this idea: (i) the thermal conductivity κ study in Ref. [12] reveals no contributions to κ from magnetic excitations despite the large magnetic specific heat at low temperatures, casting doubts on the existence of itinerant quasiparticles expected for a QSL [15]; (ii) since Mg²⁺ and Ga³⁺ in the nonmagnetic layers are randomly distributed [3,4,16], the disorder effect, which is detrimental to the QSL phase for this compound [17], can be significant [5,8].

In this Letter, we report comprehensive measurements on a closely related system, YbZnGaO₄. We show that the most natural conclusion that is consistent with the microand macroscopic data presented here is that the system is a spin glass. We suggest this conclusion to be also true for YbMgGaO₄, further supported by the observation of spin

freezing at low temperatures. We believe disorder [5,8,11,16,17] and frustration [4,5,11,18–22] to be largely responsible for this phase.

High-quality single crystals of YbZnGaO₄ were grown by the floating-zone technique, overcoming the problem caused by the volatile nature of ZnO [3,23]. The dc and ac magnetic susceptibility and specific heat were measured in a Quantum Design physical property measurement system (see the Supplemental Material [24] for details). INS experiments on the single crystals were carried out on PANDA located at MLZ at Garching, Germany [27]. In the measurements, the 11 coaligned single crystals weighed 1.2 g in total with a sample mosaic of 0.98° and were mounted in the (H, K, 0) plane. INS experiments on the 14-g powder sample were carried out on SIKA located at ANSTO at Lucas Heights, Australia. The wave vector Q was expressed as the (H, K, L) reciprocal lattice unit (r.l.u.)of $(a^*, b^*, c^*) = (4\pi/\sqrt{3}a, 4\pi/\sqrt{3}b, 2\pi/c)$ with a = b =3.414(2) Å and c = 25.140(2) Å.

YbZnGaO₄ is isostructural to YbMgGaO₄, both of which have the YbFe₂O₄-type structure (space group $R\bar{3}m$, No. 166) [23,28,29]. Schematics of the crystal structure and the two-dimensional triangular lattice of Yb³⁺ are illustrated in Figs. 1(a) and 1(b), respectively. The magnetic ground state of Yb³⁺ ions is a spin-1/2 Kramers doublet [see Fig. 1(d) or Refs. [3,5,8]]. In YbZnGaO₄, the dc magnetic susceptibility of the effective spin follows the Curie-Weiss

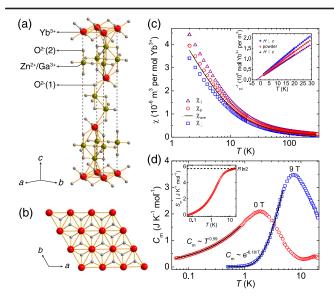


FIG. 1. (a) Schematic crystal structure for YbZnGaO₄ and YbMgGaO₄. (b) Top view of the triangular layer of YbO₆ octahedra. (c) dc magnetic susceptibility for fields applied parallel ($\chi_{||}$) and perpendicular (χ_{\perp}) to the c axis for the single crystal, and polycrystalline sample (χ_p), measured with a 0.1-T field. The data have been corrected by the Van Vleck paramagnetic susceptibility, as discussed in Ref. [24]. The solid line is the averaged susceptibility χ_{ave} . The inset shows the inverse susceptibility and the accompanying Curie-Weiss fits. (d) Magnetic specific heat C_m measured at zero and 9-T fields. C_m is obtained by subtracting the contribution from the lattice using a nonmagnetic reference sample LuZnGaO₄. Solid lines are fits to the data described in the main text. The inset shows the zero-field magnetic entropy S_m , obtained using $S_m = \int_0^T C_m/T dT$. The dashed line indicates $R \ln 2$ (R = the ideal gas constant).

law from 2 to 30 K. In the inset of Fig. 1(c), we show the inverse susceptibility and the Curie-Weiss fits up to 30 K. From the fits, we find Θ to be -2.70(2), -2.38(3), and -2.46(2) K, for the single crystal with magnetic fields perpendicular and parallel to the c axis and for the polycrystalline sample, respectively. The negative sign shows

that the magnetic ground state is dominated by antiferromagnetic interactions. The superexchange coupling constant J is estimated to be 1.73(5) K. These parameters are summarized in Table I, together with other values for this material, in comparison with YbMgGaO₄.

In Fig. 1(d) we plot the magnetic specific heat C_m down to 0.05 K for YbZnGaO₄. From the zero-field data, we do not observe a λ -type peak expected for a well-defined phase transition. Instead, there is a broad peak at $T^+ \approx 1.86(5)$ K, below which C_m decreases. Below T^+ , we fit C_m to T^{α} and determine α to be 0.59(2). We have also attempted to fit the low-temperature data using $C_m \sim \exp(-\Delta/T)$, and obtained a small gap of 0.05(3) K, consistent with the large magnetic specific heat arising from the gapless magnetic excitations at low temperatures. With increasing fields, T^+ gets higher, and the hump becomes narrower. At 9 T, T^+ should correspond to a transition from the paramagnetic to the ferromagnetic state, as the system is in a fully polarized state at low temperatures [see Fig. S2(a)]. When we fit the 9-T data with $C_m \sim \exp(-\Delta/T)$, we obtain $\Delta = 6.18(3)$ K, which corresponds to a magnon gap induced by an external magnetic field, as also observed in YbMgGaO₄ [5,12]. In the inset of Fig. 1(d), we show that the magnetic entropy S_m is precisely $R \ln 2$ (R = the ideal gas constant) at 20 K, expected for a Kramers doublet in the ground state [3–5].

We now explore the system by carrying out INS experiments, which reveal similar behaviors to YbMgGaO₄ [5,6]. In Figs. 2(a) and 2(b), we present the contour maps of the excitation spectra at energy transfers of E=0.3 and 0.6 meV, respectively. The broad diffusive excitations spreading along edges of the two-dimensional (2D) Brilouin zone, and decreasing in intensity with increasing Q, indicate that the system is dominated by antiferromagnetic correlations but without long-range order, consistent with the macroscopic results in Figs. 1(c) and 1(d). Magnetic dispersions along two high-symmetry paths are plotted in Fig. 2(c), which exhibit a continuum over the whole energy range measured. The excitations are gapless (see also Fig. S4 [24]), consistent with the specific heat

TABLE I. Some parameters for YbZnGaO₄ and YbMgGaO₄.

Compound	Θ_{\perp} (K)	$\Theta_{ }(K)$	Θ_p (K)	J(K)	g_{\perp}	$g_{ }$	g_p	T ⁺ (K)	α	Δ (K)	T_f (K)	ΔP
YbZnGaO ₄ YbMgGaO ₄		-2.38(3) -3.20									0.093(6) 0.099(6)	

 Θ_{\perp} , Θ_{\parallel} , and Θ_p are the Curie-Weiss temperatures for the single crystal with magnetic fields perpendicular and parallel to the c axis, and for the polycrystalline sample, respectively. J is the superexchange coupling constant, approximated by $[4]J = (4J_{\pm} + J_{zz})/3$, where $J_{\pm} \approx -\Theta_{\perp}/3 = 0.90(1)$ K, and $J_{zz} \approx -2\Theta_{\parallel}/3 = 1.59(2)$ K. g_{\perp} , g_{\parallel} , and g_p are the Landé g factors, obtained by fitting the magnetization data in Fig. S2 [24]. T^+ is the peak temperature of the zero-field magnetic specific heat. α is the fitted index using $C_m \sim T^{\alpha}$. Δ is the magnon gap obtained by fitting the 9-T data with $C_m \sim \exp(-\Delta/T)$. Corresponding values for YbMgGaO₄ are from Refs. [3,4,6,12].

 T_f is the peak temperature of the real part of the ac susceptibility χ' at 100 Hz. ΔP is the peak shift $\{(\Delta T_f)/[T_f\Delta \lg(f)]\}$ from 100 to 10 000 Hz. These two parameters for both YbZnGaO₄ and YbMgGaO₄ are obtained from our own measurements. ^aNote that in our discussions, we take J to be 2.83 K for YbMgGaO₄, larger than the 1.5 K reported in Ref. [4]. The larger J is obtained by calculating with the Curie-Weiss temperatures given in Ref. [6].

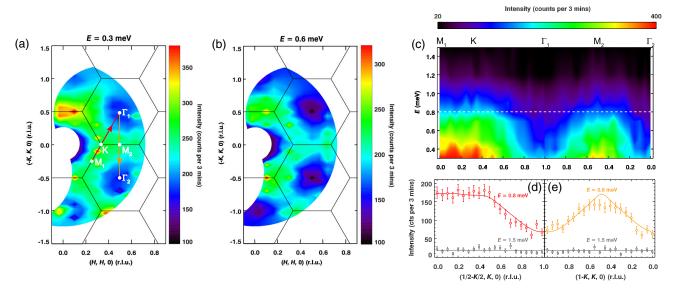


FIG. 2. (a) and (b) are contour maps of the INS spectra at E=0.3 and 0.6 meV, respectively, measured at T=0.47 K. The maps are obtained by plotting together a series of constant-energy scans along the [H,0,0] direction with a step size of 0.1 r.l.u., and an interval of 0.1 r.l.u. along the [0,K,0] direction. Solid lines indicate Brillouin zone boundaries. The additional bright feature around (-0.5,0.5,0) in (a) does not represent a magnetic Bragg peak [24]. (c) Magnetic dispersion along the $M_1 - K - \Gamma_1$ and $\Gamma_1 - M_2 - \Gamma_2$ directions as illustrated by the arrows in (a). The dispersion is obtained by plotting together a series of constant-energy scans as shown in (d) and (e), with an energy interval of 0.1 meV. The dashed line indicates constant-energy scans at E=0.8 meV. In (d) and (e), lines through the data are the calculated results extracted from Fig. 3. Errors represent 1 standard deviation throughout the Letter.

data. Constant-energy scans along $M_1 - K - \Gamma_1$ at two representative energies are shown in Fig. 2(d); similar scans along $\Gamma_1 - M_2 - \Gamma_2$ are shown in Fig. 2(e). At E = 0.8 meV, intensities remain roughly constant from M_1 to (1/4, 1/2, 0), and then decrease as Q approaches Γ_1 . The scan along the $\Gamma_1 - M_2 - \Gamma_2$ direction results in a broad peak centering at M_2 , and the spin-spin correlation length is estimated to be 3 Å from this scan. This length scale is close to those obtained in YbMgGaO₄ [5,6] and other QSL candidates [13,14].

As is shown in Refs. [5,6], a QSL phase can give rise to the observed INS spectra. However, we notice that the cations in the nonmagnetic layers are randomly distributed [3,4,8,11,16]. As a result, there should be a strong variation in the magnetic couplings due to the disordered charge environment [8,17]. In addition, the small J will further exaggerate the disorder effect. Can disorder make the magnetic excitations mimic those expected for a QSL [17]? In this context, we consider introducing disorder into a stripe-order phase, which is suggested to be the ground state for YbMgGaO4 in the absence of disorder [17,30]. We use an anisotropic spin model with nearestneighbor and next-nearest-neighbor exchange interactions, which has been justified in Refs. [5,17], and perform calculations with the linear spin-wave theory [31]. Without disorder, gapless spin-wave excitations disperse up from the M point. With increasing disorder, the welldefined spin-wave dispersions become broader both in momentum and energy. An example is presented in Fig. 3, and the calculated intensities are plotted together with the experimental data in Figs. 2(d) and 2(e). The calculated results agree with the experimental data quite well, demonstrating that an antiferromagnet with disorder can also exhibit the continuumlike INS spectra.

We further show thermal conductivity κ results in Fig. 4(a). At T=0.1 K, κ is only about half of that of the nonmagnetic sample LuMgGaO₄ in which only phonons contribute to κ . This reduction is quite likely due to the scattering of phonons off the gapless magnetic excitations [12]. This also manifests itself in the magnetic-field measurements: in a field of 9 T that opens a gap of 6.18 (3) K, there are almost no magnetic excitations to scatter phonons, so κ increases. We fit the zero-field data with $\kappa/T = \kappa_0/T + nT^{\beta-1}$ up to 0.4 K. Here, the first term κ_0 and

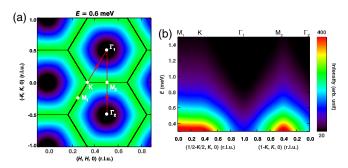


FIG. 3. (a) Contour map of the calculated spectra at E=0.6 meV. (b) Calculated dispersions along the two high-symmetry paths illustrated in (a).

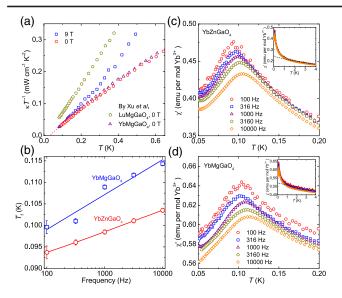


FIG. 4. (a) Thermal conductivity results on YbZnGaO₄ under zero and 9-T magnetic fields applied parallel to the c axis. The dashed line is a fit to the data described in the main text. For comparison, results on YbMgGaO₄ and the nonmagnetic reference compound LuMgGaO₄ are also plotted [12]. (b) Frequency dependence of the freezing temperature for both YbZnGaO₄ and YbMgGaO₄, extracted from the temperature dependence of the real part of the ac susceptibility χ' shown in (c) and (d). Lines through data are guides to the eye. In the insets of (c) and (d), χ' in an extended temperature range up to 4 K is plotted. Dashed lines indicate the Curie-Weiss fits for the 100-Hz data.

second term nT^{β} represent nonphonon and phonon contributions, respectively. From the fit, we obtain $\kappa_0/T = -0.011(2) \text{ mW K}^{-2} \text{ cm}^{-1}, \text{ and } \beta = 1.97(2). \text{ In}$ the nonmagnetic sample LuMgGaO4, it is shown that $\kappa_0/T = -0.007 \text{ mW K}^{-2} \text{ cm}^{-1}$, and $\beta = 2.07$ [12]. In both materials, κ_0/T is virtually zero, similar to the case of YbMgGaO₄ [12]. In contrast, another QSL candidate EtMe₃Sb[Pd(dmit)₂]₂ has a high $\kappa_0/T = 2$ mW K⁻² cm⁻¹, considered to be a signature of highly mobile quasiparticles in the QSL state [15]. We therefore believe that a gapless QSL is not an applicable description for YbZnGaO₄, because its magnetic excitations will contribute to κ [32,33]. On the other hand, the thermal conductivity results can be understood within a disordered-magnet picture, in which the mean-free path of the magnons is reduced with disorder, and they are not expected to conduct heat.

Taking all of the aforementioned observations into account, we believe that YbZnGaO₄ is a spin glass, with frozen, short-range correlations below the freezing temperature T_f [34–36]. Such a phase can be identified from the ac susceptibility. Thus, we perform the measurements with temperatures spanning about three decades, ranging from 0.05 to 4 K. The results are shown in Fig. 4(c). At a measuring frequency of 100 Hz, the real part of the susceptibility χ' shows a broad peak at $T_f \approx 0.093(6)$ K. The peak height decreases, and the peak temperature

increases, with increasing driving frequency f. The frequency dependence of T_f is shown in Fig. 4(b). As a quantitative measure, $\Delta P = \{(\Delta T_f)/[T_f\Delta \lg(f)]\}$ is 0.053 (2) with f changing from 100 to 10 000 Hz. This value is close to those observed in other insulating spin glasses [34–38]. The strong frequency dependence evidences a broad distribution of the spin relaxation times around T_f , typical of a spin glass [34–36].

We also measure the ac susceptibility for YbMgGaO₄. As shown in Fig. 4(d), the behaviors are similar to those of YbZnGaO₄, albeit with a slightly higher T_f of 0.099(6) K at 100 Hz. For YbMgGaO₄, the peak shift from 100 to 10 000 Hz ΔP is 0.068(4) [Fig. 4(b)], larger than that for YbZnGaO₄. In the insets of Figs. 4(c) and 4(d), we plot χ' in the whole temperature range measured. At high temperatures, it follows the Curie-Weiss law. Below ~2 K, it rises more rapidly with cooling. Remarkably, this temperature coincides with T^+ , below which the magnetic specific heat decreases.

The spin-glass phase identified from the ac susceptibility is a natural ground state for YbZnGaO₄. (i) Disorder and frustration, the two ingredients for a spin glass [34–36,39], are present and strong in such materials [4,5,8,11, 16–22,40,41]. (ii) A spin glass maintains short-range spin-spin correlations [34–36], consistent with the absence of a long-range magnetic order. (iii) The observed INS spectra can be nicely reproduced by bringing disorder into an ordered state. (iv) Macroscopically, a spin glass is disordered, and thus the magnons do not conduct heat due to the short mean-free path. This explains the lack of a contribution to the thermal conductivity from the gapless magnetic excitations. (v) Finally, we estimate the fraction of frozen moment to be 13(3)% from our INS results shown in Fig. S4 [24], close to the 16(3)% in YbMgGaO₄ [5], but smaller than the 33% expected from theory [42]. We consider it to be a consequence of the strong frustration in this compound.

We also note that some findings in YbZnGaO₄ suggest deviations from a generic spin glass. For instance, T^+ is about 20 times T_f , much larger than that expected for a typical spin glass [34–36]. We believe that this indicates the existence of strong frustration. In addition to the geometrical frustration inherent in the triangular structure [1,2], the spin-space anisotropy induced by the spin-orbit coupling of the Yb³⁺ ions, recognized in our anisotropic spin model and in Refs. [4,5,11,18–22], should further reduce T_f . Moreover, the strong disorder [5,8,11,16,17] is expected to result in a reduced T_f . In some spin glasses, $C_m \sim T^\alpha$ with $\alpha = 1$ at low temperatures [43,44], but disorder may reduce this exponent [45].

In summary, we have successfully grown high-quality single crystals for YbZnGaO₄, and our comprehensive measurements on these crystals provide concrete evidence that it is a spin glass. We show this conclusion is also applicable to YbMgGaO₄. We suggest that the spin-glass phase in both compounds is driven by disorder and

frustration. Our work reveals the very similar characteristics between QSL and spin-glass phases, including the broad "continuum" of magnetic excitations, and is a cautionary tale about labeling such materials without a full study of the spin system.

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