Cosmic Ray Neutron Sensing for Simultaneous Soil Water Content and Biomass Quantification in Drought Conditions

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Abstract

Understanding the feedback mechanisms between soil water content (SWC) and biomass production is important for sustainable resources management. Here we present a new method enabling simultaneous noninvasive measurements of SWC and biomass dynamics based on cosmic ray neutron sensing (CRNS). Recently, it was suggested that the neutron ratio (\(N_f\)) between thermal neutron (\(T_N\)) and fast neutron (\(F_N\)) intensity contains information on other hydrogen pools like vegetation, canopy interception, and snow. The aim of this study is to evaluate the accuracy of simultaneous measurements of SWC and biomass dynamics during agricultural drought conditions using CRNS probes. To this end, we instrumented an arable field cropped with sugar beet with CRNS probes and a wireless in situ SWC sensor network. Belowground and aboveground biomass were sampled in monthly intervals. We found a linear relationship between \(N_f\) and the aboveground biomass that allowed to continuously quantify the dry aboveground biomass development throughout the growing season with a root-mean-square error from 0.14 to 0.22 kg/m². This information was used together with measured belowground biomass to correct for the effect of biomass on SWC determination with CRNS probes, which increased the accuracy of the SWC estimates considerably as indicated by the decrease of the root-mean-square error from 0.046 to 0.013 cm³/cm³. We anticipate that future research on the \(N_f\) can further improve the accuracy of SWC and biomass estimates and extend the application of CRNS to include canopy interception, ponding water, and snow water equivalent estimation for both stationary and roving CRNS systems.

1. Introduction

Soil water content (SWC) is one of the key state variables in the soil-vegetation-atmosphere continuum due to its important role in the exchange of water and energy at the soil surface (Vereecken et al., 2015). A decade ago, cosmic ray neutron sensing (CRNS) was proposed as an attractive noninvasive and field-scale method for SWC estimation (Zreda et al., 2008) in a footprint of up to 15 ha with a maximum penetration depth of about 80 cm (Köhli et al., 2015). Since then, more than 200 stationary CRNS stations have been installed worldwide (Andreassen, Jensen, Desilets, Franz, et al., 2017). A range of studies have successfully compared SWC estimates obtained with CRNS to in situ measurements (Baatz et al., 2014, 2015; Bogena et al., 2013, 2015; Franz, Zreda, Ferré, et al., 2012; Rivera Villarreyes et al., 2011; Schrön et al., 2017) and satellite and modeling products (Baatz et al., 2017; Kędzior & Zawadzki, 2016; Montzka et al., 2017; Vinodkumar et al., 2017). Clearly, CRNS has matured into an established noninvasive method for SWC determination that allows to bridge the gap between spaceborne and in situ (point-scale) SWC measurements (Bogena et al., 2015).

CRNS measurements are not only sensitive to SWC but are also influenced by hydrogen stored in other pools (Desilets et al., 2010), such as biomass, litter, snow, and canopy interception (Andreassen, Jensen, Desilets, Zreda, et al., 2017; Bogena et al., 2013; Schattan et al., 2017). To improve the accuracy of SWC estimates, these pools need to be considered. Static hydrogen pools such as soil organic carbon (Franz, Zreda, Rosolem, & Ferré, 2013) and lattice water (Franz, Zreda, Rosolem, & Ferré, 2012) can be accounted for with relatively small effort during the calibration of the CRNS probe. Time-varying hydrogen pools such as atmospheric water vapor content (Rosolem et al., 2013), vegetation biomass (Baroni & Oswald, 2015; Rivera Villarreyes et al., 2011), or the water content of a litter layer (Bogena et al., 2013) can be considered using independent estimates of these confounding variables. Whereas the influence of atmospheric water vapor content on the CRNS measurements can be accurately removed using measurements of air humidity (Rosolem et al., 2013), corrections for dynamic changes in biomass (e.g.,...
growing crops) are much less straightforward because accurate field-scale estimates of biomass are laborious to obtain.

Recently, Tian et al. (2016) proposed to use the ratio of thermal to fast neutron intensity measured with the CRNS probe to estimate aboveground biomass for maize and soybean crops. Obviously, it would be highly attractive to estimate biomass directly using CRNS for at least two reasons. First, it would allow to remove effects of time-varying biomass from SWC estimates obtained with CRNS without the need for additional measurements. Several studies have already reported that biomass and the $N_0$ parameter (the fast neutron count rate over dry soil conditions) of the standard calibration model for CRNS probes are linearly or nonlinearly related (Baatz et al., 2014, 2015; Franz, Zreda, Rosolem, Hornbuckle, et al., 2013; Hawdon et al., 2014; Hornbuckle et al., 2012). In all these studies, the use of the proposed correction methods resulted in a considerable improvement in the accuracy of SWC estimates for sites with constant biomass (e.g., forests) or sites with near-constant biomass (e.g., deciduous forests; Heidbüchel et al., 2016). However, strong deviations were still found for cropped sites with dynamic changes in aboveground and belowground biomass. Clearly, a general method for the correction of biomass effects on CRNS measurements of SWC covering various vegetation types is still not available.

Second, simultaneous measurements of SWC and biomass dynamics at the field scale would be very useful to improve the understanding of relationships between plant growth and SWC deficit, which is essential for the development of adaptation strategies against drought-induced restrictions in crop production. According to Dai (2011), the risk for droughts has increased substantially since the 1970s due to global climate change (e.g., increased atmospheric moisture demand and altered atmospheric circulation patterns). The drought frequency has also increased in temperate climates since the 1980s (Briffa et al., 2009). Although this typically has not yet affected food security as in Sub-Saharan Africa (Webber et al., 2014), the economic losses due to drought have also been considerable in temperate climate regions. For example, the average cost of a drought event in Europe was estimated to be 621 million euros between 1950 and 2014 (Zink et al., 2016). Thus, securing and improving productivity of crops in water-limited conditions has become more important in recent years (Passioura & Angus, 2010).

The overall aim of this study is to evaluate the accuracy of simultaneous measurements of SWC and biomass dynamics using CRNS probes and to show the potential of CRNS measurements for identifying and studying effects of agricultural droughts on both soil water storage and plant growth. For this, we first evaluate available approaches to correct SWC estimates obtained from CRNS for biomass for the case of a highly dynamic crop with high belowground biomass. In a next step, we test the potential of simultaneous measurements of SWC and biomass dynamics using information of calibrated CRNS data only. For this study, we rely on data from an extensive field experiment where cosmic ray neutrons, biomass, and SWC were monitored in an agricultural field site cropped with sugar beet ($Beta$ vulgaris L.) for an entire growing season.

2. Materials and Methods

2.1. The Selhausen Experimental Site

The Selhausen experimental site is part of the TERENO (TERrestrial ENvironmental Observatories) network (Bogena et al., 2012; Zacharias et al., 2011) and is located in Western Germany, 40 km west of Cologne (50°52′00″N 6°27′22″E). In this study, we focus on the F01 field at the Selhausen site that covers an area of 2.77 ha (Bogena et al., 2018). The site is located in the temperate maritime climate zone with a mean annual temperature and precipitation of 10.2 °C and 714 mm, respectively (Korres et al., 2015). The soil was classified as a Cambisol with a silty loam soil texture. The investigated field is located on the upper terrace of the Rhine/Meuse river system and is characterized by Pleistocene sand and gravel sediments (Weihermüller et al., 2007) with irregularly alternating subsurface channels that are filled with fine sediments. The within-field variability of soil properties was determined by Rudolph et al. (2015) using $z$-transformed electrical conductivity ($\sigma_z$) measurements (Figure 1). Lower values indicate a higher content of sand and gravel and thus a lower water-holding capacity, whereas higher $\sigma_z$ values indicate finer material with higher water holding capacity. This heterogeneous sediment distribution leads to spatially variable plant development and leaf area index patterns (Rudolph et al., 2015).
2.2. Auxiliary Data

Air temperature, wind speed, absolute humidity, net radiation, and atmospheric pressure were measured during the experiment. The potential grass reference evapotranspiration (ET_{pot}) was calculated from the meteorological data using the Penman-Monteith equation according to Allen et al. (1998). Actual evapotranspiration (ET_{act}) was measured with an eddy covariance flux tower at approximately 5 m distance from the CRNS station following methods described in Gebler et al. (2015). Finally, we used precipitation data from a TERENO meteorological station approximately 500 m northwest of the Selhausen test site (SE_EC_003, http://teodoor.icg.kfa-juelich.de/ibg3searchportal2/index.jsp).

Several drought indices have been developed to assess and respond to drought based on various hydrological and meteorological parameters, including precipitation, evapotranspiration, and SWC (Narasimhan & Srinivasan, 2005). Here we use the evaporative index (potential evapotranspiration divided by precipitation), the water balance, and data from the German drought monitor (Zink et al., 2016) to characterize the drought situation during the investigation period. The German drought monitor is based on a soil moisture index that considers the modeled average profile SWC of the past 30 days and the average modeled profile SWC for the selected time period for the past 60 years (Zink et al., 2016).

2.3. In Situ SWC Measurements

In situ SWC was measured at each of the sampling sites (1–26, Figure 1) in three depths with the SoilNet wireless sensor network (Bogena et al., 2010) equipped with 156 SMT100 SWC sensors (Truebner GmbH, Neustadt, Germany). Two SMT100 sensors were installed per sampling depth to increase the measurement volume and to enable the identification of sensor malfunctioning. The SMT100 sensors were
individually calibrated using five dielectric reference media (Bogena et al., 2017), and the measured permittivity was related to SWC using the Topp equation (Topp et al., 1980). We considered the soil heterogeneity for the selection of locations 1–18 (Figure 1) for soil sampling (section 2.6) and the in situ SWC measurements. Additional locations were selected near the CRNS probe to consider the greater sensitivity of the detector to neutrons originating closer to the sensor (Köhli et al., 2015; Schrön et al., 2017). Therefore, eight additional locations were positioned radially around the CRNS probes at a distance of 3 m (locations 19–21) and 11 m (locations 22–26). The SMT100 sensors at locations 1–18 were installed in 5-, 20-, and 50-cm depths. At locations 19–26, the sensors were installed in 5-, 10-, and 20-cm depths. This was done to favor a higher resolution close to the soil surface and to also account better for the decreasing sensitivity of the CRNS probes with soil depth (Zreda et al., 2008).

In order to compare CRNS probe and in situ SWC measurements, it is necessary to integrate the distributed SoilNet measurements considering the spatial sensitivity of the CRNS probes. We followed the averaging procedure developed by Köhli et al. (2015) and Schrön et al. (2017), which provides an improved estimate of the spatial sensitivity of the CRNS probe as compared to the simple exponential decay initially suggested by Zreda et al. (2008). The neutron transport simulation used to derive this revised spatial sensitivity also showed that the sensitivity with depth decreases exponentially and not linearly as assumed by Franz, Zreda, Ferré, Rosolem, et al. (2012). A detailed description of the averaging of the distributed SWC measurements used for comparison with CRNS measurements is given in Appendix A.

2.4. Determination of Biomass Dynamics

We sampled sugar beet biomass at nine locations (Figure 1, locations 22–26, 2, 16, 101, and 102) on a monthly basis. The selection of locations 22–26 close to the CRNS probes was based on the assumption that hydrogen sources at shorter distance have a greater influence on the CRNS signal. Some additional biomass sampling locations were used to represent both favorable (locations 2 and 101) and less favorable growing conditions (locations 16 and 102). We used the arithmetic mean of all biomass sampling locations as the best representative estimate of the biomass sensed by the CRNS probe. At each biomass sampling location, 1 m of planting row was harvested. This included both aboveground and belowground biomass down to a depth of ~40 cm, which corresponds to the maximum penetration depth of the CRNS probe for the lowest SWC measured during the measurement period. Areal average biomass was calculated from the average distance between rows (46.5 cm). The biomass samples were bagged and sealed airtight before they were transported to the laboratory. In the laboratory, they were cleaned from soil residues, divided into aboveground and belowground biomass, and weighed. In order to determine dry biomass, subsamples of ~20% of the biomass were oven dried to a constant weight at 65 °C. The vegetation water content was estimated from the weight loss after drying. Total biomass water equivalent (BWE) consists of vegetation water as well as hydrogen present in the biomass tissue. As suggested by Franz, Zreda, Rosolem, and Ferré (2013) and Franz, Zreda, Rosolem, Hornbuckle, et al. (2013), we assume that the water equivalent of the aboveground and belowground biomass can be approximated by the amount of hydrogen and oxygen contained in cellulose ($f_{ew}$), that is, ~55.6% by weight:

$$BWE = [(BM_f - BM_d) + f_{ew}BM_d] / \rho_w \rho_d$$

where $\rho_d$ is the plant density (plants m$^{-2}$), $BM_f$ and $BM_d$ are fresh and dry biomass weights (kilograms), respectively, and $\rho_w$ is the density of water ($10^3$ kg/m$^3$). This equation was used for the determination of

Figure 2. Setup of the cosmic ray neutron sensing probes at the test site Selhausen (three CRS-2000/B [1, 2, and 3], one CRS-1000 [4], and one CRS-cross calibrator [5]).
aboveground BWE ($BWE_a$), belowground BWE ($BWE_b$), and total BWE ($BWE_{tot} = BWE_a + BWE_b$). Between sampling dates, estimates of BWE were obtained by linear interpolation.

### 2.5. Cosmic Ray Neutron Measurements

We used five CRNS probes (one CRS-1000, three CRS-2000/B, and one mobile CRNS probe, Figure 2), each equipped with two detector tubes. Summing up the measured neutron counts from all systems resulted in a much higher neutron intensity accuracy compared to a single probe. All probes were manufactured by Hydroinnova LLC, Albuquerque, NM, United States. The neutron detectors are either filled with $^3$He gas (CRS-1000 and mobile CRNS probe) or $^{10}$BF$_3$ (CRS 2000/B) enriched gas to obtain high neutron absorption cross sections. When neutrons enter the detector tube, the gases absorb part of the neutrons, which creates electrons that are attracted by an anode. This produces electric currents which are amplified, detected, and counted by a pulse module (Zreda et al., 2012). The neutron absorption of $^3$He is more efficient, and thus these detector tubes can be constructed distinctly smaller compared to $^{10}$BF$_3$-filled detector tubes. For this reason, $^3$He detector tubes are installed inside protective housings (Figure 2, tube 4 and CRNS-cross calibrator — no. 5), whereas the larger $^{10}$BF$_3$-filled detector tubes are mounted on poles without a housing (Figure 2, tubes 1–3).

Cosmic ray neutrons can be differentiated into two energetic levels (Köhli et al., 2015): thermal neutrons ($TN$, maximum energy at ~0.025 eV) and fast neutrons ($FN$, energy range from ~0.2 eV to 100 keV). $FN$ are continuously losing energy by collisions with atomic nuclei and other neutrons, a process called moderation, and will eventually be transformed into $TN$. Because of the lower kinetic energy, the probability of absorption reactions is greater for $TN$. Unshielded detector tubes respond mainly to neutrons in the thermal energy range. To detect neutrons in the fast energy range, the detector tube is shielded with polyethylene, which has a high hydrogen content that effectively moderates $FN$ to $TN$ before they enter the detector tube.

It is well established that $FN$ are subject to variations in air pressure (Desilets & Zreda, 2003), incoming cosmic ray neutron intensity (Desilets & Zreda, 2001), and atmospheric water vapor (Rosolem et al., 2013). We applied the established correction methods for all three influences to obtain corrected $FN$ intensity data (see Appendix B). However, the required corrections for $TN$ intensity are still under debate. For instance, Tian et al. (2016) used uncorrected $TN$ intensity to estimate the thermal-to-fast neutron ratio, $Nr$ (see section 2.7), whereas Andreasen, Jensen, Desilets, Zreda, et al. (2017) corrected $TN$ intensity for air pressure and incoming neutron variations. In order to investigate the most appropriate correction procedure, we empirically explored various $TN$ correction procedures (Appendix C). We found that the best results were achieved with $TN$ intensity corrected for pressure and atmospheric water vapor only. This suggests that $TN$ intensity is less dependent on incoming cosmic radiation than $FN$ intensity. At first sight, this may seem surprising as $TN$ are typically produced by thermalization of $FN$. However, absorption (e.g., by Gd, Ti, and B) and diffusion processes become more important in the $TN$ energy range (Schrön, 2017; Zreda et al., 2008), which is expected to weaken the relationship between $FN$ and $TN$. More elaborated studies using neutron transport modeling are needed to better address the determination of the most appropriate correction strategy for $TN$ intensity.

### 2.6. Static Belowground Hydrogen Pools

The CRNS method is affected by all hydrogen pools, which may be divided into desired signals, such as SWC and vegetation biomass, and disturbing influences, such as soil organic matter and lattice water (Zreda et al., 2012). The disturbing belowground hydrogen pools decrease the neutron count and reduce the effective sensing depth of CRNS probes (Bogena et al., 2013; Franz, Zreda, Rosolem, & Ferré, 2012). In this study, soil organic matter, lattice water ($LW$), and soil bulk density were determined using soil cores of 30-cm length and 5-cm diameter taken at locations 1–26 (Figure 1) with a HUMAX soil corer (Martin Burch AG, Rothenburg, Switzerland). The soil cores were divided into 5-cm-long subsamples, and their bulk density was derived using the oven drying method (105 °C, 24 hr). Subsequently, these 156 samples were sieved and merged to six depth-specific bulk samples of which 20-mg subsamples were combusted in oxygen at 1000 °C in order to determine $LW$ using a heat conductivity detector. The total organic carbon ($TOC$ [g/g]) of the bulk subsamples was determined using a VARIO EL Cube (Elementar Analysensysteme GmbH, Rothenburg, Switzerland).
Langenselbold, Germany). The soil organic carbon water content equivalent (SOW [g/g]) was estimated according to Franz et al. (2015):

$$SOW = TOC \times 1.724 \times f_{ew} \quad (2)$$

where the constant 1.724 is used to convert total organic carbon mass into soil organic matter mass, and $f_{ew}$ is the stoichiometric ratio of water to cellulose ($C_6H_{12}O_5$, i.e., ~55.6% of the dry weight). It was found that the SW content averaged over space and depth was 0.0289 ± 0.006 g/g. SOW averaged over all locations and depths was 0.01 ± 0.0025 g/g. The minimum bulk density of 1.2 g/cm$^3$ was measured at location 13, the average bulk density was 1.36 g/cm$^3$, and the maximum bulk density of 1.46 g/cm$^3$ was measured at location 10.

### 2.7. Thermal-to-Fast Neutron Ratio

Tian et al. (2016) found that the ratio of thermal to fast neutron counts ($N_t$) was positively correlated with BWE$_a$ for maize and soybean crops and thus could be used to estimate biomass. This finding was recently confirmed using neutron modeling for agricultural, heathland, and forest sites by Andreasen, Jensen, Desilets, Zreda, et al. (2017). In this study, we used the following definition of the $N_t$:

$$N_t = \frac{TN_{av} F_{av}}{FN} \quad (3)$$

where $FN$ and $TN$ intensity were integrated using a 3-day moving average and $FN_{av}$ and $TN_{av}$ were the arithmetic means for the entire measurement period. The 3-day integration time was chosen to reduce the effect of highly dynamic hydrogen pools (i.e., interception, ponding water, and infiltration fronts succeeding precipitation), which are associated with relatively short time scales (i.e., less than a day). In contrast, biomass changes occur much slower (i.e., time scale of days to weeks; Baroni & Oswald, 2015). The normalization was introduced to enable a better comparison with other studies using different numbers of detector tubes. Following Tian et al. (2016), we related BWE$_a$ to $N_t$ using a linear model:

$$N_t - BWE_a = a N_t + b \quad (4)$$

where $a$ and $b$ are calibration parameters and $N_t$-BWE$_a$ represents BWE$_a$ calculated from the $N_t$. Since dry aboveground biomass ($AGB_d$) instead of BWE$_a$ is used in most agricultural management and environmental modeling applications, we also examined whether this property can be estimated from $N_t$-BWE$_a$. For this, equation (1) was reformulated (see Appendix D):

$$N_t - AGB_d = \frac{N_t - BWE_a}{\left(\frac{1}{AGB_d} + f_{ew} - 1\right)} \cdot \frac{1}{P_w P_d} \quad (5)$$

where $N_t$-AGB$_d$ is the dry aboveground biomass calculated from the $N_t$ and the measured ratio (AGB$_d$) of AGB$_d$ to fresh aboveground biomass (AGB$_f$), which was calculated with

$$AGB_d = \frac{AGB_d}{AGB_f} \quad (6)$$

In typical applications, only a single value for AGB$_d$ (i.e., the average of AGB$_d$ over the growing season) may be available. Therefore, we also tested whether an adequate estimation of AGB$_d$ is possible using a constant AGB$_f$.

### 2.8. Relating Fast Neutron Intensity to SWC and Accounting for Biomass

Baatz et al. (2014) compared three parametrization methods to infer SWC from FN intensity and found that all methods performed reasonably well (root-mean-square error [RMSE] ≤ 0.033 cm$^3$/cm$^3$). We chose the $N_0$ method (Desilets et al., 2010) as it has been successfully applied in various studies (e.g., Baatz et al., 2014, 2015; Baroni & Oswald, 2015; Bogena et al., 2013; Franz, Zreda, Ferré, et al., 2012; Franz, Zreda, Rosolem, &
where $\theta_v$ is the volumetric SWC (cm$^3$/cm$^3$), $N_0$ is the fast neutron count rate over dry soil, $t$ indicates the time dependency, $\rho_{bd}$ is the average dry soil bulk density of all locations (g/cm$^3$), and $a_i$ are fitting parameters.

Using MCNPx simulations for generic silica soils, Desilets et al. (2010) derived $a_0 = 0.0808$, $a_1 = 0.372$, and $a_2 = 0.115$ for values of $\theta > 0.02$ kg/kg. In this study, a 12-hr moving average of $FN$ intensity was used for SWC estimation.

Local calibration of the CRNS probes was done by fitting $N_0$ in equation (7) to in situ SWC measurements. We used three calibration methods: Method 1 calibration of $N_0$ at one specific day (e.g., Desilets et al., 2010), Method 2 calibration of $N_0$ using the continuously measured SWC and $FN$ during the monitoring period (e.g., Bogena et al., 2013), and Method 3 calibration of $N_0$ at one specific day complemented with correction procedures to account for the impact of biomass on the measured $FN$ intensity (e.g., Baatz et al., 2015).

Methods 1 and 2 are used to illustrate the need for biomass correction of CRNS data. The correction functions required for the third approach were obtained by relating time-variable $N_0$ estimates derived from $FN$ intensity and reference SWC with a range of quantities that represent the vegetation influence on $FN$. In particular, the following linear regression functions were considered:

$$N_0(t) = c_{BWEa} \cdot BWEa(t) + N_0,BWEa=0 \quad (8)$$

where $c_{BWEa}$ in counts per hour (cph) per millimeter of $BWEa$ represents the change in $N_0$ with $BWEa$ and $N_0,BWEa=0$ is the intercept of the regression

$$N_0(t) = c_{BWEtot} \cdot BWEtot(t) + N_0,BWEtot=0 \quad (9)$$

where $c_{BWEtot}$ in counts per hour (cph) per millimeter of $BWEtot$ represents the change in $N_0$ with $BWEtot$ and $N_0,BWEtot=0$ is the intercept of the regression, and

$$N_0(N_r(t) = c_{N_r} \cdot N_r(t) + N_0,N_r=0 \quad (10)$$

where $c_{N_r}$ in counts per hour (cph) per one $N_r$ (the $N_r$ is given in arbitrary units; see section 2.7) represents the change in $N_0$ with the $N_r$ and $N_0,N_r=0$ is the intercept of the regression. The different calibration variants used in this study are summarized in Table 1.

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<th>Table 1</th>
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<td><strong>Summary of Correction and Calibration Methods Used in This Study, as Well as Respective RMSE Values, Data Requirements, and Involved Equations and Figures</strong></td>
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<td>Biomass correction</td>
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**Note.** RMSE = root-mean-square error; CRNS = cosmic ray neutron sensing; SWC = soil water content.
3. Results

3.1. CRNS Measurements

The continuously measured $FN$ and $TN$ intensity at the Selhausen site during the growing season is presented in Figure 3e. On average, the count rate of $FN$ was about 5 times higher than the $TN$ count rate (maximum, mean, and minimum count rates per hour for $FN$ and $TN$ were 10,801, 9,484, 8,148, and 2,588, 2,212, 1,820, respectively). This is partly related to the measurement setup with different amount of detectors for $FN$ and $TN$ (three $TN$ vs. seven $FN$ detectors). In a drying period after frequent precipitation in June, a clear increasing trend in $FN$ and $TN$ intensity can be observed. This is because of the progressing decrease in SWC due to low precipitation and increasing evaporative demand, which can also be observed in the water balance for the measurement period (accumulated precipitation minus accumulated actual evapotranspiration, Figure 3c). Sharp decreases in $FN$ (and to a lesser degree in $TN$) are related to strong precipitation events and the associated increases in SWC. These are particularly evident at the end of October where the evaporative demand has already decreased strongly.

3.2. In Situ SWC Measurements

The general course of vertically weighted SWC time series derived from the in situ SWC measurements mirrors the results from the neutron count measurements (Figure 3d). However, relatively strong differences in absolute SWC are also visible between the sampling locations throughout the measurement period. After July, the vertically weighted SWC at locations 19–26, which are closer to the CRNS probes, was generally lower than SWC at the locations further away. An exception is the higher SWC at location 25, which was related to a tractor track with highly compacted soil and low plant density that reduced both infiltration and water extraction by vegetation at this particular location. Although the in situ measurements at stations 19–26 are restricted to the first 20 cm, the vertically weighted SWC data from these stations fall within the overall observed SWC range. Thus, we conclude that the in situ SWC data from the SoilNet stations capture the heterogeneous soil properties within the test field.
3.3. Biomass Development

The measured development of \( BWE_{\text{tot}} \) as well as \( BWE_a \) and \( BWE_b \) are shown in Figure 4c. All three biomass measures increase until the end of July, and \( BWE_a \) makes up the largest proportion of \( BWE_{\text{tot}} \). However, \( BWE_a \) started to decline noticeably in August, which coincides with a 2-month-long period of very low SWC (Figure 3d). During this period, the actual evapotranspiration was also substantially lower than the potential evapotranspiration (Figure 3b), indicating a prolonged drought situation that led to the drying of leaves and leaf loss of the sugar beet plants. The spatially variable health status of the plants can also be observed on a satellite image from 9 August 2016 (Figure 1, top right), and the German drought monitor indicated that the study region experienced a moderate to severe drought during September and October. Such droughts typically occur every 3–6 years and likely result in damage to crops and pasture (Zink et al., 2016).

The drought period was initiated in July where the cumulative actual evapotranspiration exceeded precipitation by a factor of 4 (Figure 4d). Interestingly, the development of belowground biomass was less affected by the summer drought as \( BWE_b \) remained fairly constant after early August and increased strongly in the beginning of September. The drought-induced decrease of \( BWE_a \) and the stagnation of belowground biomass growth led to a strong decrease in \( BWE_{\text{tot}} \) during August. These findings demonstrate that the growth of sugar beets at our test site was strongly influenced by water availability and that aboveground and belowground biomass development were influenced by drought to a different extent.

3.4. SWC Estimation Without Biomass Correction

Figure 4b shows the result of two different calibration approaches, both without the consideration of dynamic changes in biomass. In Method 1, we used the in situ SWC from 15 May for calibration (red arrows, Figure 4b). At this time, the field was free of vegetation. This method represents a calibration strategy used in many CRNS studies (i.e., a single calibration at or shortly after detector deployment). The SWC estimates obtained using this single calibration showed a growing discrepancy with the reference SWC estimates throughout the measurement period, and the resulting RMSE of \(~0.13 \text{ cm}^3/\text{cm}^3\) is high. In Method 2, the whole time series of in situ SWC measurements was used for the calibration of a single value of \( N_0 \). It can be observed that the SWC estimates derived from CRNS measurements using this method also clearly
deviate from the reference SWC. In particular, SWC is underestimated until July and overestimated after July. However, the resulting (RMSE) of 0.046 cm$^3$/cm$^3$ is still reasonably close to previous studies, for example, ~0.039 cm$^3$/cm$^3$ in Rivera Villarreyes et al. (2011) and 0.033 cm$^3$/cm$^3$ in Baatz et al. (2014). These results clearly show that a single value of $N_0$ cannot be used to accurately predict SWC, which we attribute to a strong influence of biomass on the FN intensity.

### 3.5. SWC Estimation With Biomass Correction Using In Situ Measurements

First, we determined the calibration parameter $N_0$ for each biomass sampling date from the measured FN intensity and the reference SWC and correlated it with measured $BWE_a$ and $BWE_{tot}$ (Figure 5). The empirical correction function of Baatz et al. (2015) has a considerably flatter slope in comparison to the site-specific regression function (Figure 5, left). This indicates that site-specific calibration may be preferable for cropped fields with relatively low biomass (i.e., dry aboveground biomass less than 5 kg/m$^2$) as the correction function of Baatz et al. (2015) was developed using data from forest sites with much higher amounts of biomass. The linear regression between $BWE_{tot}$ and $N_0$ provided a higher correlation coefficient compared to the linear regression between $BWE_a$ and $N_0$ ($R^2 = 0.83$ vs. 0.54). Using these linear relationships and interpolated $BWE_a$ and $BWE_{tot}$ estimates (Figure 4c), a temporally variable $N_0$ was estimated and used to derive SWC estimates corrected for dynamic changes in biomass with equations (7) and (8) (i.e., $BWE_a$ correction) or equation (9) (i.e., $BWE_{tot}$ correction). The accuracy of the SWC estimates as expressed by the RMSE improved to 0.036 cm$^3$/cm$^3$ when the temporally variable $N_0$ was estimated from $BWE_a$ and to 0.019 cm$^3$/cm$^3$ when $N_0$ was estimated from $BWE_{tot}$ (Figure 6).

![Figure 5](image1.png)

**Figure 5.** Relationship between $N_0$, calibrated at the times of biomass measurements using equation (7), and $BWE_a$ and $BWE_{tot}$. The left plot also shows the linear regression function proposed by Baatz et al. (2015), which shows a considerably flatter slope.

![Figure 6](image2.png)

**Figure 6.** Reference in situ SWC (black line) and FN-derived SWC estimates corrected using equations (7) and (8) with $BWE_a$ (Method 3b, red line) and equations (7) and (9) with $BWE_{tot}$ (Method 3d, blue line). SWC = soil water content; RMSE = root-mean-square error.
SWC corrected using $BWE_a$ underestimated the reference SWC until the beginning of August, while SWC was overestimated for the remaining period (Figure 6). We attribute this to the variable ratio between aboveground and belowground biomass of sugar beet (Figure 4c), which was not considered in the correction using $BWE_a$. Therefore, we anticipate that $BWE_a$ measurements may be sufficient for the correction of CRNS-derived SWC in the case of vegetation with a relatively constant root-to-shoot ratio (i.e., $BWE_b$ to $BWE_a$ ratio). For the more common case where this ratio is dynamic, a correction considering both $BWE_a$ and $BWE_b$ (i.e., $BWE_{tot}$) will improve the accuracy of CRNS-derived SWC.

When $BWE_{tot}$ is used for correction, notable deviations between estimated and reference SWC still occur during and several days after precipitation events (e.g., in the beginning of August and September, as well as in the last week of the measurement period). This may be due to other hydrogen pools currently not accounted for, such as interception and ponding water, or shallow wetting of the soil surface not captured by the in situ SWC sensors.

### 3.6. $BWE_a$ Estimation From the Neutron Ratio

Figure 7 shows the linear relationship between measured $BWE_a$ and the neutron ratio, $N_n$, determined from the $FN$ and $TN$ intensity at the biomass sampling days. One obvious outlier, which corresponds to the last biomass measurement, was excluded from the regression analysis (Figure 7, marked in green) because the neutron signal was probably influenced by other hydrogen pools (e.g., interception and ponding water) during this time. A comparison of $BWE_a$ estimated from the $N_n$ and measured $BWE_a$ is provided in Figure 8. Periods with overestimation of measured $BWE_a$ corresponded well with the occurrence of strong precipitation events. For instance, the greatest discrepancy with an overestimation of about 4–5 mm occurred at the end of the measurement period during a precipitation event of more than 20 mm/day that may have produced ponding of water at the soil surface. The steep decline in $BWE_a$ in the middle of August is well reflected by the estimated $BWE_a$ obtained from the $N_n$. To improve the accuracy of the $BWE_a$ prediction, we tested the exclusion of $N_n$ measurements obtained up to 3 days after a 24-hr period with precipitation above 1.5 mm. This data filtering further reduced the RMSE of the $BWE_a$ estimation from 1.3 mm to 0.75 mm (Figure 8, red line).

### 3.7. Aboveground Dry Biomass Estimation Using the Neutron Ratio

We found that the aboveground dry biomass $AGB_d$ could be estimated from the $BWE_a$ predicted using the $N_n$ with an RMSE of 0.21 kg/m² ($R^2 = 0.61$) when the measured time-variable $AGB_r$ was used (Figure 9). In the case of a static $AGB_r$, the RMSE increased only slightly to 0.22 kg/m² ($R^2 = 0.52$). Using only the $N_n$ data that were...
not affected by precipitation events (i.e., Figure 9, dashed lines), the RMSE improved to 0.14 kg/m² ($R^2 = 0.92$) and 0.18 kg/m² ($R^2 = 0.67$) for the dynamic and static AGBr, respectively.

The accuracy of the biomass estimates obtained with CRNS compared well with the typical accuracy reported in remote sensing studies. For instance, Bendig et al. (2015) estimated dry aboveground biomass of summer barley based on red-green-blue imaging from an unmanned aerial vehicle with a $R^2$ of 0.83 and RMSE of 0.35 kg/m². Using plant height as an input parameter for a crop model, they achieved a $R^2$ of 0.85 and a RMSE of 0.324 kg/m². Using satellite imagery, Kross et al. (2014) estimated aboveground biomass of soybean and corn with a $R^2$ of 0.95 and 0.97, respectively.

3.8. SWC Estimation With Biomass Correction Using the Neutron Ratio

We tested whether the combined effect of belowground and aboveground biomass on SWC estimates obtained from CRNS measurements can be corrected using the $N_0$. For this, in situ measured BWEb was added to the BWEa estimated from the $N_0$ (Figure 8, green line) in order to obtain an estimate of BWEtot ($N_0$-BWEtot in Figure 10). We found that the use of this $N_0$-BWEtot further improved the linear relationship with $N_0$ as compared to the case with measured BWEtot ($R^2$ increased from 0.83 to 0.94; cf. Figures 5 [right] and Figure 10). When using this relationship to predict SWC, the RMSE between estimated and reference SWC was further reduced from 0.019 to 0.013 cm³/cm³ (Figure 11). Nevertheless, some deviations between predicted and reference SWC are still visible after intensive precipitation events (e.g., beginning of August and September) probably due to effects of ponding of water, intercepted water on leaves, or strong SWC gradients in the soil profile. In comparison to the correction based on measured BWEtot, these deviations were reduced slightly, which may be explained by the implicit inclusion of near-surface water in BWEa determined from the $N_0$ (Tian et al., 2016).

3.9. Relationship Between $N_0$ and the Neutron Ratio

For the correction of the influence of BWEa on SWC estimates obtained from CRNS measurements, a calibration between $N_0$ and BWEa is not strictly necessary as a regression analysis between $N_0$...
(here calibrated for all times with $FN$ intensity measurements) and the $N_r$ and the subsequent use of equation (10) would be sufficient (Figure 12). This regression between $N_0$ and $N_r$ resulted in a relatively low $R^2$ (0.52) due to additional short-term influences on the $N_r$ (e.g., interception storage and ponding). Nevertheless, a significant linear relationship between $N_0$ and the $N_r$ was found. From the perspective of correcting CRNS data for dynamic changes in biomass, this approach is far more convenient (i.e., less work intensive and thus less time consuming) than using in situ measurements of $BWE_a$ to correct CRNS data as suggested in other studies (Baatz et al., 2014; Franz, Zreda, Rosolem, & Ferré, 2013; Hawdon et al., 2014; Hornbuckle et al., 2012; Rivera Villarreyes et al., 2011). We found that the use of a linear relationship between $N_0$ and the $N_r$ was more accurate (RMSE of 0.032 cm$^3$/cm$^3$) than the site-specific linear correction model, which yielded a higher RMSE of 0.036 cm$^3$/cm$^3$ (Figure 13). This higher accuracy may be explained by a better $BWE_a$ representation of the $N_r$ for the interpolated periods in between biomass samplings and by the implicit consideration of hydrogen stored in additional pools.

4. Discussion

4.1. Comparison of Biomass Correction Methods

In this study, we showed that the simultaneous measurement of aboveground biomass and SWC with CRNS is possible. In addition, it was shown that the accuracy of SWC estimates derived from CRNS measurements improved when variations in aboveground and belowground biomass were considered. We tested several correction methods to account for biomass effects, and the data requirements and the resulting measurement accuracy are summarized in Table 1. As expected from previous studies (e.g., Andreasen, Jensen, Desilets, Zreda, et al., 2017; Baatz et al., 2015), calibration during vegetation-free conditions produced the lowest accuracy (Method 1), as the effect of biomass on the SWC estimates is strongest in this case. Using a time series of in situ SWC estimates for the calibration partly incorporates the effect of biomass in the calibration parameter $N_0$ (Method 2), and this resulted in periods with systematic underestimation or overestimation of SWC and a relatively high RMSE of 0.046 cm$^3$/cm$^3$. This value is the highest accuracy that could be achieved in this study without explicit consideration of the dynamical changes in the size of the hydrogen pool contained in vegetation.

The biomass correction approach of Baatz et al. (2015; Method 3a) was not able to account for the strong biomass effect of the sugar beets in our experiment, as indicated by the high RMSE of 0.095 cm$^3$/cm$^3$. A comparison of the linear regression between $N_0$ and $BWE_a$ based on Baatz et al. (2015) and the site-specific
measurements (Method 3b) presented in this study (Figure 5, left) shows a strong difference in the slope of the linear relationship ($/C0$ vs. $/C0$). The difference can be explained by the much broader range of aboveground biomass measurements used for their correction function (from bare soil conditions to dense forest sites). This perhaps provides support for the results of Hawdon et al. (2014), who suggested a nonlinear relationship between $N_0$ and $BWE$ with a steep initial decrease of $N_0$ for low $BWE$ and a moderate decrease in $N_0$ for higher $BWE$. The results also suggest that plant structural properties, such as surface coverage, leaf area index, plant height, and plant phenology, may also influence the relationship between $N_0$ and $BWE$. This dependence was already briefly discussed in Franz, Zreda, Rosolem, and Ferré (2013) for forest ecosystems and should be further investigated, for example, using highly resolved neutron transport simulations. The use of both aboveground and belowground biomass measurements for the correction (Methods 3d and 3e) resulted in the highest SWC accuracy (RMSE of 0.19–0.13 cm$^3$/cm$^3$), which confirms that the belowground biomass has a strong influence on the FN intensity (e.g., Franz, Zreda, Rosolem, & Ferré, 2013). However, the sampling of roots down to 40 cm is very time consuming and the moderate increase in accuracy of the SWC estimates might not justify this extra work. Alternatively, the use of the $N_r$ for the correction of biomass effects (Methods 3c) considerably improved the accuracy of the SWC measurements by CRNS (RMSE of 0.032 cm$^3$/cm$^3$) without the need for biomass determination.

4.2. Potential for Biomass Estimation

The drought conditions in the second half of the measurement period affected the plant development and led to a decrease in aboveground biomass. These conditions provided a good opportunity to test methods to estimate dry aboveground biomass from the $N_r$ and good accuracy could be achieved (RMSE of 0.14–0.22 kg/m$^2$). In this context, it is important to realize that satellite-based methods for biomass estimation typically rely on optical methods, which do not represent the drying of leaf biomass well because of the color change from green to yellowish brown (Butterfield & Malmstrom, 2009). Therefore, we expect that biomass estimates from CRNS outperform satellite-based methods in situations with drought-induced biomass decline. This suggests a high potential for the use of CRNS measurements for simultaneous estimation of SWC and biomass, which will be particularly beneficial in semiarid and arid climates.

4.3. Remaining Uncertainties

The remaining uncertainty in the biomass estimates obtained from CRNS measurements was partly associated with precipitation events, which clearly suggests that the $N_r$ is also sensitive to interception, ponding water (Tian et al., 2016), and possibly also to shallow SWC (Andreasen, Jensen, Desilets, Zreda, et al., 2017). Clearly, the accuracy of biomass estimates obtained from CRNS may suffer from these confounding influences in humid or rainy conditions. In an agricultural context, we therefore recommend that the relationship between $N_r$ and $N_0$ is established using data from periods with dry leaf surfaces and without ponding water.

Figure 13. Time series of measured reference SWC (black line), estimated SWC after correction for measured $BWE_a$ using equations (7) and (8) with the site-specific linear regression (Method 3b, blue line; cf. Figure 5, left), estimated SWC calibrated on 15 May (red arrows) and corrected using measured $BWE_a$ with the empirical vegetation correction found by Baatz et al. (2015; Method 3a, red line), and estimated SWC after correction for $BWE_a$ using equations (7) and (10) and the linear relationship between $N_r$ and $N_0$ (Figure 12, Method 3c, green line). RMSE = root-mean-square error; SWC = soil water content.
At the same time, this sensitivity of the \( N_{r} \) to other hydrogen pools also offers opportunities. For example, it may be possible to estimate the interception storage in addition to biomass from the \( N_{r} \) by assuming that these two processes affect the \( N_{r} \) at different time scales, that is, biomass changes occur on weekly time scales whereas interception occurs on daily time scales (Baroni & Oswald, 2015).

Based on their modeling results, Andreasen, Jensen, Desilets, Zreda, et al. (2017) expected that the \( N_{r} \) was independent of SWC, which contradicted their measurement results that clearly showed a relationship between \( N_{r} \) and SWC. In our study, \( N_{r} \) and average SWC at 5-cm depth were uncorrelated (\( R^2 = 0.008 \)). This may partly be explained by the uppermost part of the sugar beets that extruded from the surface (up to ~5 cm) during the later growth stage, which may have attenuated SWC effects on the \( N_{r} \) to some extent. In addition, it has to be noted that SWC variations near the surface (i.e., <5 cm below ground) were not captured by our in situ measurements. We also explored whether the \( N_{r} \) can be used to directly predict BWE_\text{b} or BWE_\text{tot}, but no meaningful relationships were found.

In this study, we did not consider that the \( F_{N} \) and \( T_{N} \) footprints are likely not the same. This potential scale mismatch may become important in case of strong spatial heterogeneity of soil properties and biomass. However, only the \( F_{N} \) footprint has been characterized in several modeling studies so far (e.g., Köhli et al., 2015; Schrön et al., 2017; Zreda et al., 2008). The size of the \( T_{N} \) footprint and the factors that influence it are still unclear and need to be addressed by dedicated neutron modeling studies. Nevertheless, our results indicate that the proposed methods worked well even for a relatively heterogeneous research site (cf. Figure 1).

The results presented in this study are limited to a single vegetation type, and it is likely that the linear relationships reported here cannot be applied to other crops without adjustments in the parameterization. Therefore, further research with different vegetation types is necessary to allow the derivation of more general corrections functions. In particular, it may be possible to relate plant structural properties, such as leaf area index, vegetation height, and the root-to-shoot ratio, to the variables used for the linear regression models.

The experimental setup in this study relied on multiple neutron detectors in order to increase the CRNS sensitivity to the extent possible. It is well established that higher count rates obtained by using more detectors or longer integration times will significantly increase the SWC measurement accuracy as shown by Bogena et al. (2013). Therefore, we recommend using longer integration times for studies that rely on a single detector, and the challenge here is to find a suitable trade-off between count rate uncertainty and time resolution (e.g., 24 hr). For biomass detection using CRNS, our study showed that a 3-day integration time to obtain reliable estimates of \( N_{r} \) is suitable, which is rather long but not problematic due to expected slow changes in biomass. Alternatively, a new generation of detector devices based on boron-10 layers is emerging, which will enable higher count rates at a relatively low price (e.g., Weimar, 2017). Such detectors are expected to open up new possibilities for the detection of hydrogen pools with low residence time (e.g., interception and ponded water).

Finally, it has to be noted that the unshielded neutron detectors used to determine \( T_{N} \) are also sensitive to \( F_{N} \) to some extent (5% of the measured neutrons) and that the moderated detectors are also sensitive to \( T_{N} \) (45% of the measured neutrons; Andreasen et al., 2016; McJannet et al., 2014). Thus, an improved distinction between \( T_{N} \) and \( F_{N} \), for example, using the cadmium difference method developed by Andreasen et al. (2016), would lead to more accurate estimates of the \( N_{r} \), which may in turn increase the accuracy of the proposed soil moisture and biomass estimation methods.

### 5. Conclusions and Outlook

In our study with sugar beets, we found that the influence of dynamic changes of aboveground biomass on cosmic ray SWC measurements can be corrected using the ratio of \( T_{N} \) to \( F_{N} \) (\( N_{r} \)). This is in agreement with findings of Tian et al. (2016) for other crops (maize and soy bean). We also demonstrated that the \( N_{r} \) approach gives better results compared to the common approach for correcting biomass effects on CRNS data using in situ biomass measurements. Furthermore, we showed that the \( N_{r} \) can also be used for the continuous determination of aboveground BWE and dry aboveground biomass. The impact of dynamic changes in aboveground and belowground BWE could both be considered using linear regressions with the CRNS...
calibration parameter $N_0$. These findings suggest that CRNS measurements can be used for simultaneous measurement of SWC and biomass, for example, to support the investigation of drought effects on crop production.

Future research should aim to confirm the general applicability of the proposed methods for other crops, with a particular focus on crops with less biomass production (e.g., wheat). A particular challenge here is that the $N_i$ is also sensitive to other hydrogen pools located on or close to the soil surface, such as snow, interception, and ponding water. Furthermore, SWC from shallow depth and belowground biomass may also influence the value of the $N_i$. Thus, future studies should consider monitoring these additional hydrogen pools (e.g., interception storage and ponding water) to allow a better discrimination of the various contributions to the CRNS measurements. However, given the large number of hydrogen pools and the involved measurement challenges, we also suggest using appropriate soil hydrological and vegetation models to support the interpretation of CRNS measurements. Promising choices would be the use of vadose zone models (e.g., HYDRUS-1D; Simunek et al., 2008) that simulate the generation of surface ponding, SWC gradients very close to the soil surface (which is difficult to measure), and water stored in the litter layer (cf. Bogena et al., 2013) or models that simulate soil water and carbon fluxes as well as dynamic plant growth in agricultural systems (e.g., AgroC; Klosterhalfen et al., 2017). The combination with crop growth models is particularly interesting because it would allow to obtain information regarding the root-to-shoot-ratio that relates aboveground and belowground biomass, which is required to estimate belowground biomass from the $N_i$.

Within the cosmic ray community, mobile measurement systems (i.e., cosmic rovers) are gaining popularity for monitoring SWC of larger areas (Avery et al., 2016; Franz et al., 2015; McJannet et al., 2014). Accurate biomass and SWC data on scales of tens to hundreds of kilometers, which can be provided by cosmic ray roving systems, bear immense potential for resource management. For instance, SWC and dynamic biomass development data can jointly be used as indicators for the control of irrigation systems, with the aim of maximizing the water use efficiency (Jones, 2004). The work presented here extends the use of cosmic rovers to simultaneous measurements of aboveground biomass and SWC and allows the continuous correction of aboveground biomass effects on SWC prediction without the need for laborious local biomass calibration.

Appendix A: In Situ SWC Weighting

The appropriate weights of the in situ SWC sensors depend on the sensing depth of the CRNS probes. In analogy to Franz, Zreda, Rosolem, and Ferré (2012), the sensing depth ($D_{86}$) is assumed to depend on the soil water equivalent of all hydrogen stored in the soil ($\theta_{eq}$; i.e., $SWC + LW + SOW + BWE_b$) and is defined as the depth above which 86% of the measured neutrons originate. In addition, $D_{86}$ depends on the distance ($r$ [meters]) between the CRNS probe and the in situ SWC sensors (Köhli et al., 2015). For the weighting of point measurements $r$ is rescaled ($r_s$) to adapt to pressure and vegetation height variations (Schrön et al., 2017):

$$r_s = r / f_p / f_{veg}$$

(A1)

where $f_p$ is the scaling factor for atmospheric pressure and $f_{veg}$ is the scaling factor for vegetation height. They are calculated as follows (Schrön et al., 2017):

$$f_p = \frac{0.5}{0.86 - \exp^{-0.41 P/P_{ref}}}$$

(A2)

$$f_{veg} = 1 - 0.17 \cdot (1 - \exp^{-0.41 H_{veg}} \cdot (1 + \exp^{-0.25 \theta_{eq, av}}))$$

(A3)

where $P_{ref}$ is the standard atmospheric pressure at sea level (1,013.25 hPa), $P$ is the measured atmospheric pressure (hPa), $H_{veg}$ is the vegetation height (cm), and $\theta_{eq, av}$ is the average soil water equivalent of each SWC measurement profile and given in cm$^3$/cm$^3$, respectively. According to Köhli et al. (2015), a vegetation height of 2 m corresponds to a BWE of 8.8 kg/m$^2$ in their neutron transport model. We assumed a linear relationship between plant height and aboveground biomass ($BWE_a$) and used the field measurements of $BWE_a$ to calculate the corresponding $H_{veg}$ values. Then, the penetration depth at each measurement location ($D_{86}$) can be calculated:
\[
D_{86} = \frac{1}{p_{bd}} \left( p_0 + p_1 \exp^{-p_2 r_s} + \frac{p_4 + \theta_{eq,av}}{p_5 + \theta_{eq,av}} \right)
\]

(A4)

where the values of the fitting parameters \(p_0, p_1, p_2, p_4, p_5\) are 8.321, 0.14249, 0.96655, 0.01, 20, and 0.0429 (Schrön et al., 2017). The depth-specific weighting factors \(W_d\) for the in situ SWC sensors and the vertically weighted SWC \(\theta_{wd}\) for the reference SWC stations were calculated using

\[
W_d = \exp^{-2d/D_{86}}
\]

(A5)

and

\[
\theta_{wd} = \frac{\sum \theta W_d}{\sum W_d}
\]

(A6)

Now, the horizontal weights \(W_r\) for the SoilNet locations can be calculated using

\[
W_r = \begin{cases} 
F_1 \exp^{-F_2 r_s} + F_3 \exp^{-F_4 r_s}, & 1 \text{ m} \leq r_s \leq 50 \text{ m} \\
F_5 \exp^{-F_6 r_s} + F_7 \exp^{-F_8 r_s}, & 50 \text{ m} < r_s < 600 \text{ m}
\end{cases}
\]

(A7)

The parametric functions \(F_1\)–\(F_8\) in equation (A7) consider the local \(\theta_{wd}\) variations and the influence of atmospheric water content changes. We refer to Schrön et al. (2017) for a full description of the weighting method. They added another parametric function for distances between 0 and 1 m and altered the succeeding parameter functions to be valid from 1 to 50 m. The benefits of the additional parametric function cannot be evaluated in this study, since in situ measurements were only taken at distances larger than 3 m. The final weighted SWC within the CRNS footprint \(\theta_{hv}\) was calculated using

\[
\theta_{hv} = \frac{\sum \theta_{wd} W_r}{\sum W_r}
\]

(A8)

All calculations in Appendix A were iterated until \(\theta_{hv}\) values converged within 1 vol.% accuracy (Schrön et al., 2017). For this, \(\theta_{eq,av}\) was substituted with the depth weighted SWC of each measurement profile, \(\theta_{wd}\) summed with \(LW, SOW,\) and \(BWE_b\).

**Appendix B: Neutron Count Corrections**

Since the cosmic ray flux through the atmosphere is exponentially attenuated as a function of the traversed cumulative mass, measured neutron count rates need to be normalized to standard atmospheric pressure using

\[
N_p = N_{raw} e^{L (P/P_0)}
\]

(B1)

where \(N_p\) is the neutron count rate corrected for atmospheric pressure, \(N_{raw}\) is the raw neutron count rate, \(P_0\) is the reference atmospheric pressure (1,013.25 hPa), \(P\) is the actual atmospheric pressure, and \(L\) denotes the local mass attenuation length (131.6 g/cm²; Desilets & Zreda, 2003). The neutron intensity at ground level also strongly depends on the amount of incoming cosmic radiation. In this study, data from neutron monitors at the Jungfraujoch in Switzerland (stations JUNG and JUNG1 averaged, freely available at www.nmdb.eu) were used to correct for incoming radiation using the following correction function:

\[
N_{pi} = N_p \frac{l_{ref}}{l}
\]

(B2)

where \(N_{pi}\) is the neutron count rate corrected for variations in incoming cosmic radiation, and \(l\) and \(l_{ref}\) (for this study the mean of \(l\) was chosen) are the current and reference neutron monitor count rates, respectively.

In a third step, we accounted for the effect of atmospheric water vapor fluctuations on neutron intensity using the approach of Rosolem et al. (2013):
Table C1
RMSE and $R^2$ (calculated between $N_r$-derived $BWE_a$ and measured $BWE_a$) indicating the quality of $N_r$-based $BWE_a$ estimation using different combinations of TN and FN

<table>
<thead>
<tr>
<th></th>
<th>RMSE</th>
<th>$R^2$</th>
<th>$TN_{raw}$</th>
<th>$TN_p$</th>
<th>$TN_i$</th>
<th>$TN_h$</th>
<th>$TN_{pi}$</th>
<th>$TN_{ph}$</th>
<th>$TN_{h}$</th>
<th>$TN_{ph}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>$FN_{raw}$</td>
<td>1.9</td>
<td>0.8</td>
<td>1.6</td>
<td>0.8</td>
<td>2.3</td>
<td>0.2</td>
<td>1.8</td>
<td>0.8</td>
<td>2.4</td>
<td>0.5</td>
</tr>
<tr>
<td>$FN_{pih}$</td>
<td>1.8</td>
<td>0.5</td>
<td>1.5</td>
<td>0.9</td>
<td>2.1</td>
<td>0.2</td>
<td>1.7</td>
<td>0.7</td>
<td>2.1</td>
<td>0.8</td>
</tr>
</tbody>
</table>

Note: The best performing combination with RMSE of 1.3 mm and $R^2$ of 0.95 is marked in green. RMSE = root-mean-square error.

$$N_{pih} = N_{p} \cdot (1 + 0.0054 \cdot (p_{v0} - p_{v0}^{ref}))$$

where $N_{pih}$ is the neutron count rate corrected for variations in water vapor, $p_{v0}$ the actual absolute humidity (g/m$^3$) and $p_{v0}^{ref}$ the reference absolute humidity (0 g/m$^3$) at 2-m height.

Appendix C: Correction of TN Used in the $N_r$
For our data set, we empirically investigated how TN (and FN) used for the calculation of the $N_r$ should be corrected to obtain the best estimate of $BWE_a$ with equation (4). The performance was evaluated based on RMSE and $R^2$. To test the different corrections, we substituted the TN and FN intensity in equation (3) using combinations of the corrections for pressure (subscript $p$), incoming cosmic radiation (subscript $i$), and atmospheric water vapor (subscript $h$) (see Appendix B). The subscript (raw) indicates the uncorrected neutron intensity measured directly with the cosmic ray probes, which was tested for comparison to Tian et al. (2016). The results are summarized in Table C1. We found the highest $R^2$ (0.95) and lowest RMSE (1.3 mm) when $N_r$ was calculated from $TN_{ph}$ and $FN_{pih}$. Therefore, this combination was consequently used for the calculation of the $N_r$. In the main manuscript, TN is used to indicate $TN_{ph}$ and FN is used to indicate $FN_{pih}$.

Appendix D: Derivation of Equation (5)
Here we present the derivation of equation (5) used for the calculation of $AGB_d$ from the $N_r$. First, we reformulated equation (1) by using $AGB_f$ and $AGB_d$, instead of $BM_f$ and $BM_d$, respectively:

$$BWE_a = [(AGB_f - AGB_d) + f_{ew} \cdot AGB_d] \cdot p_w \cdot p_d$$

Then the combination of equations (D1) and (6) produces equation (D2):

$$BWE_a = \left[ \frac{AGB_d}{AGB_r} + AGB_d \cdot f_{ew} - AGB_d \right] \cdot p_w \cdot p_d$$

Solving for $AGB_d$, we obtain

$$AGB_d = \frac{BWE_a}{\left( \frac{1}{AGB_r} + f_{ew} - 1 \right)} \cdot \frac{1}{p_w \cdot p_d}$$

Finally, $AGB_d$ and $BWE_a$ where replaced with their $N_r$-derived counterparts $N_r$-$AGB_d$ and $N_r$-$BWE_a$, respectively.

References


