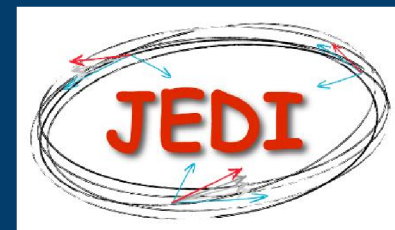


MEASUREMENT OF ELECTRIC DIPOLE MOMENTS AT STORAGE RINGS

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FORSCHUNGSZENTRUM JÜLICH



HISTORY OF

Big Bang

Inflation

High-energy cosmic rays

Accelerator

LHC protons

POSSIBLE DARK MATTER

quark

gluon

electron

muon

tau

neutrino

bosons

meson

baryon

photon

Key

$t = 10^{-32} \text{ s}$
 $E = 10^{16} \text{ GeV}$

$t = 10^{-10} \text{ s}$
 $E = 10^{12} \text{ GeV}$

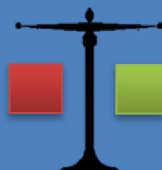
$t = 10^{-10} \text{ s}$
 $E = 10^{12} \text{ GeV}$

$t = \text{Time (seconds, years)}$
 $E = \text{Energy of photons (units GeV} = 1.6 \times 10^{-10} \text{ J)}$

The concept for the above figure originated in a 1998 book by Stephen Hawking and Leonard Mlodin, *A Brief History of Time*.

energy
↓
matter &
antimatter

symmetrie
between
matter &
antimatter



preference of
matter

- baryon number violation
- no thermic equilibrium
- C, CP violation



matter-antimatter annihilation

$$\frac{\text{ratio}}{\text{matter - antimatter}} \\ \text{radiation}$$

observed
(WMAP 2003)
 $(6.14 \pm 0.25)10^{-10}$

- galaxies, stars, planets



Standard Model
 10^{-18}

“empty” universe

Search for CP violation beyond the Standard Model

Outline

- Electric Dipole Moments
 - What are those?
 - How can they help?
- EDM measurements using storage rings
 - Basic principles
 - Options
- R&D and first measurements at COSY

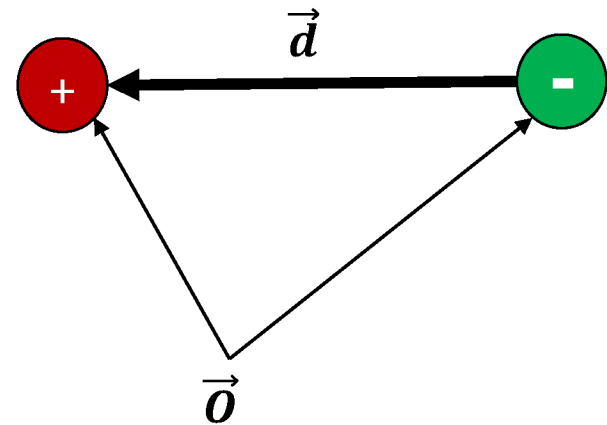
Further information:

<http://collaborations.fz-juelich.de/ikp/jedi>

Electric Dipole Moments (EDM)

Classical definition: $\vec{d} = \sum q_i \vec{r}_i$

charge x distance

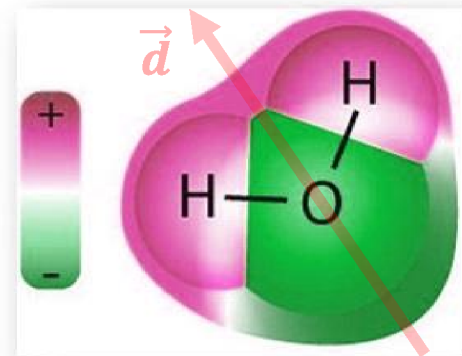


Example: water molecule

charge separation



electric dipole moment
 $d \approx 4 \times 10^{-9} \text{ e cm}$



EDMs of elementary particles

\vec{s} spin

\vec{d} electric dipole moment

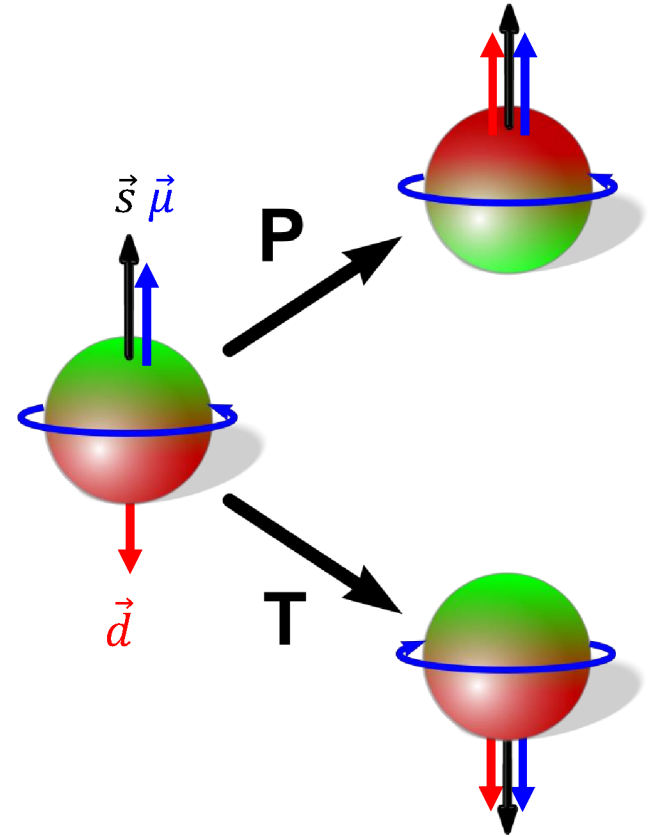
$\vec{\mu}$ magnetic moment

Transformations w.r.t. \mathcal{P} , \mathcal{T}

$$H = -\mu \vec{\sigma} \cdot \vec{B} - d \vec{\sigma} \cdot \vec{E}$$

$$\mathcal{P}: H = -\mu \vec{\sigma} \cdot \vec{B} + d \vec{\sigma} \cdot \vec{E}$$

$$\mathcal{T}: H = -\mu \vec{\sigma} \cdot \vec{B} + d \vec{\sigma} \cdot \vec{E}$$

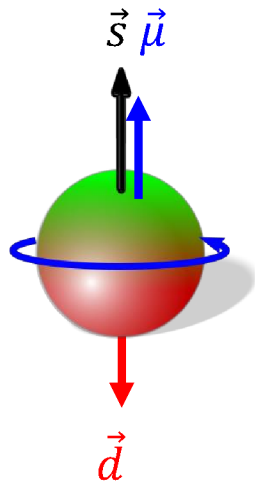


EDM measurements test violation of fundamental symmetries \mathcal{P} , \mathcal{T} and CP (via CPT)

So what is the difference?

elementary particle

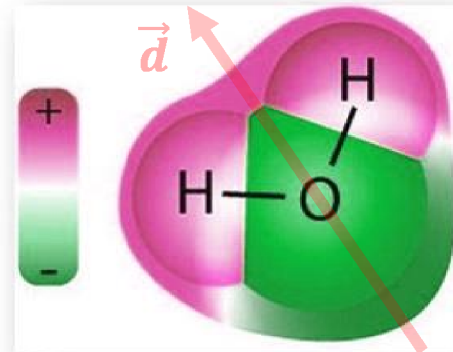
EDM violates \mathcal{P} , \mathcal{T}



defined parity!

water molecule

EDM allowed



degenerated
ground state
with mixed parity!



How can that help?

Reminder: excess of matter in the universe

	Standard Modell	Observed
$\frac{n_B - n_{\bar{B}}}{n_\gamma}$	$\approx 10^{-18}$	6×10^{-10}

Sakharov (1967): CP violation needed for baryogenesis



New sources of CP violation needed
to explain this mismatch



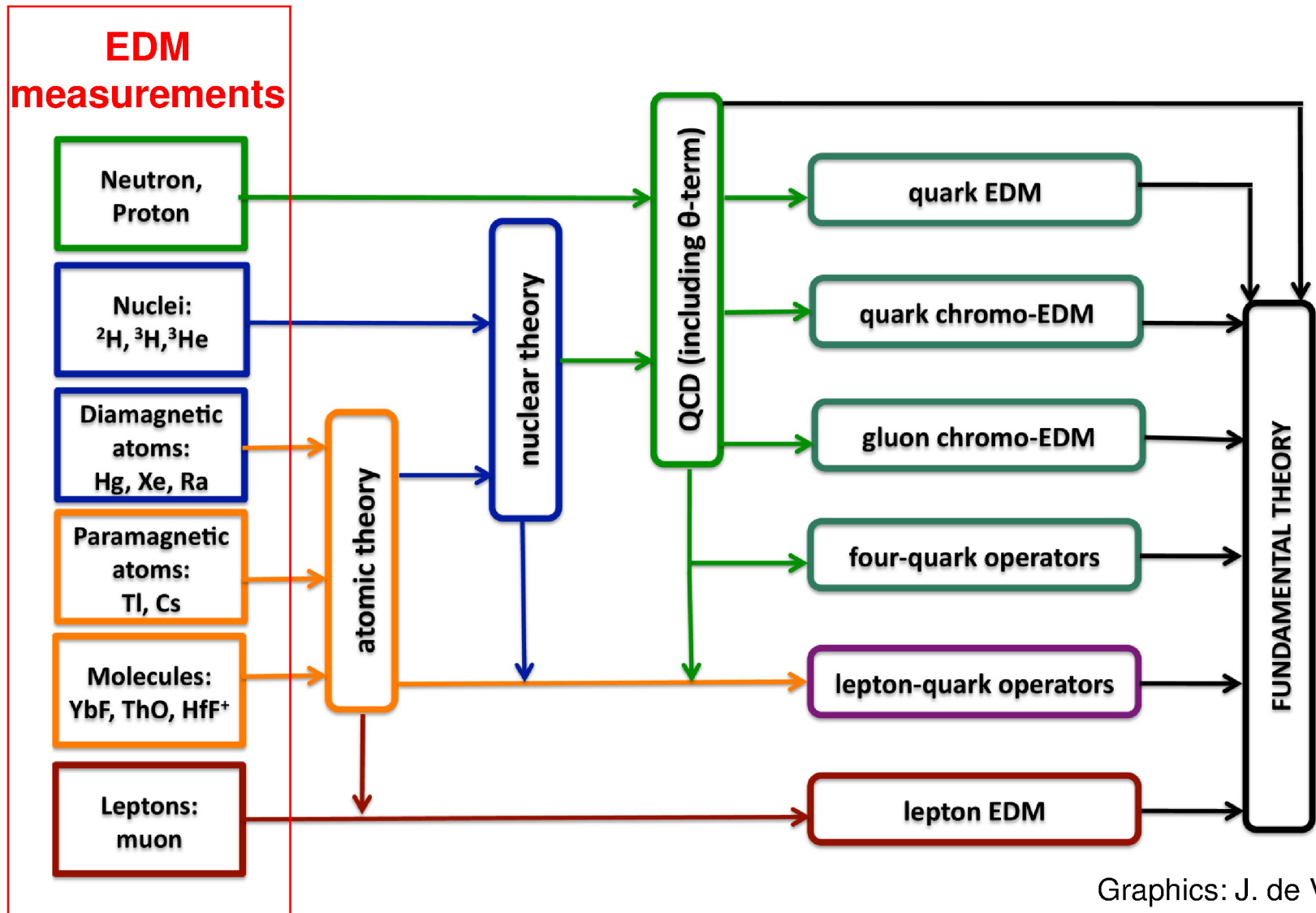
EDMs as a probe for CP violation beyond the
SM

Sources of CP violation

Standard Model		
weak interaction	CKM matrix	unobservably small EDMs
strong interaction	θ_{QCD}	best limit from neutron EDM ($\lesssim 10^{-10}$) “strong CP problem”
beyond Standard Model		
e.g. SUSY	?	accessible by EDM measurements

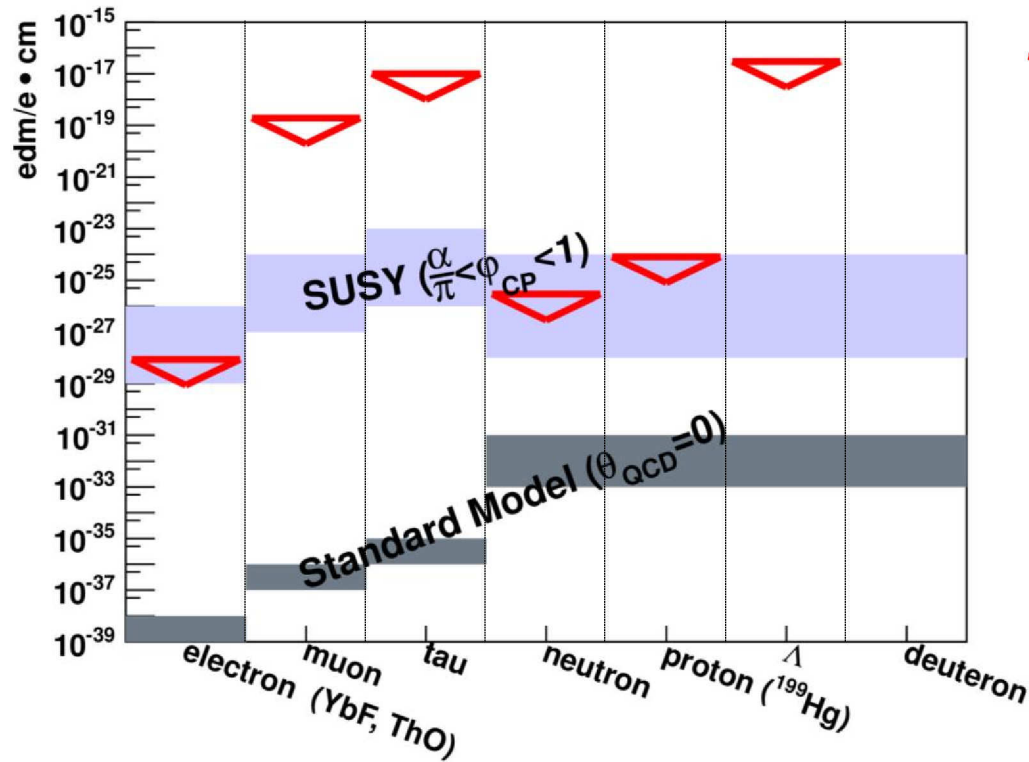
Different sources of CP violation result in a different EDM for different particle types

Disentangling CP violation ...



Graphics: J. de Vries

Current EDM limits



 Upper limits

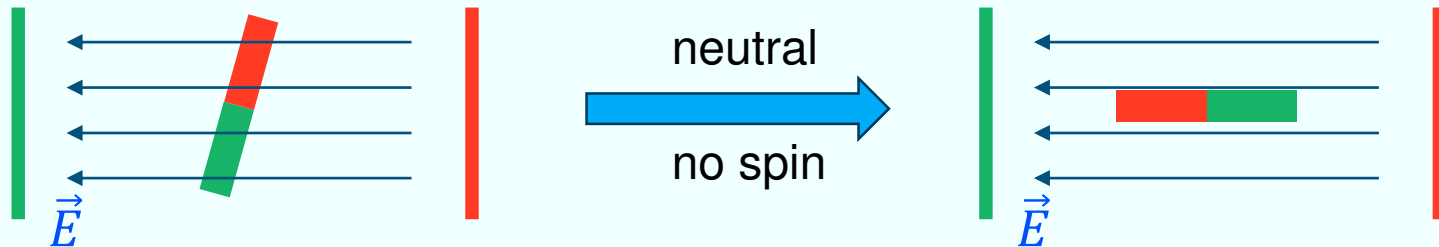
- **proton**
no direct measurement
- **deuteron**
no measurement

Here: EDMs of charged particles

How to measure EDMs?

Common strategy for all EDM measurements:

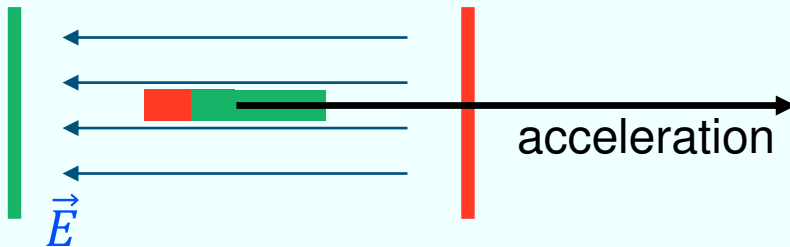
→ measure interaction of \vec{d} with electric field \vec{E}



With spin:

→ precession

For charged particles:



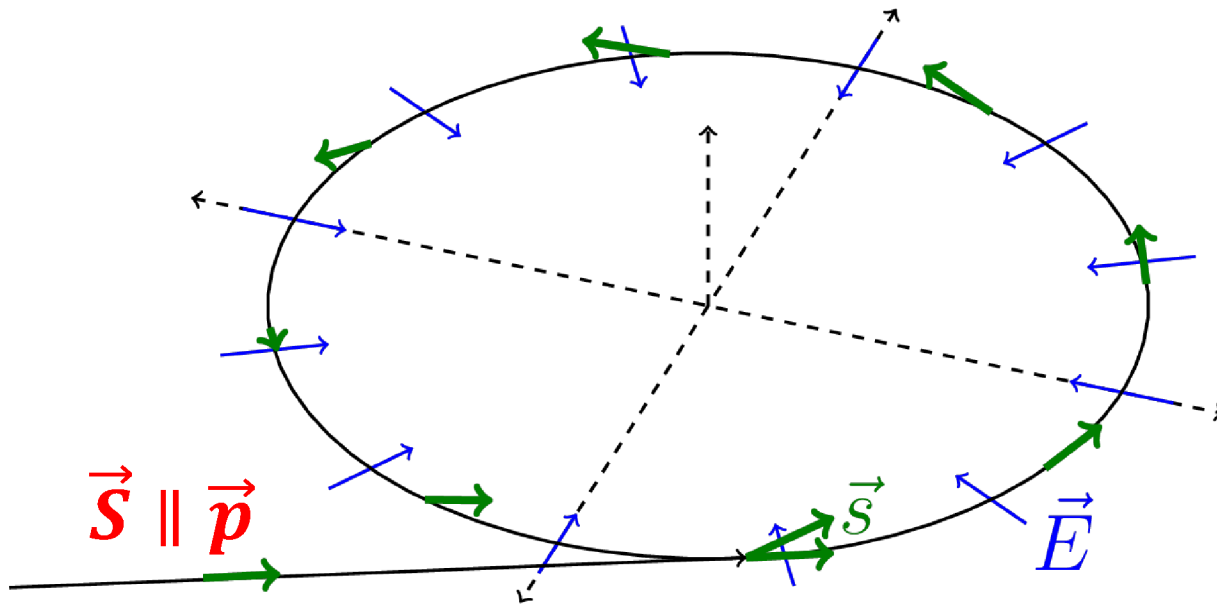
https://www.youtube.com/watch?v=qwM4ensIA_k
by Tales Of a Musing Gator

How to measure EDMs of charged particles?

Electric field accelerates particles

→ use a storage ring

Ideal case:



$$\frac{d\vec{S}}{dt} \propto d\vec{E} \times \vec{S}$$



Build-up of vertical polarisation by slow precession

$$s_{\perp} \propto |d|$$

“Ad-hoc” boundary conditions

Very slow spin precession	Long measurement times ($t \approx 1000$ s) High electric fields ($E \approx 10$ MV/m) High degree of polarization ($P \approx 0.8$) Precise polarisation measurement (analysing power $A \approx 0.6$, acc. $f \approx 0.005$)
Particle ensemble ($N \approx 4 \times 10^{10}$ per fill)	All particles must act identically All spins need to be aligned (“spin coherence time”)
In-plane polarisation \parallel momentum	Control spin motion at high precision
Magnetic moment causes fake rotations	High field quality Magnetic shielding Precise geometrical alignment Fringe fields under control

$$\sigma_{\text{stat}} \approx \frac{1}{\sqrt{Nf\tau PAE}} \Rightarrow \sigma_{\text{stat}}(1 \text{ year}) \approx 10^{-29} \text{ ecm}$$

Major challenge:
get **systematic uncertainties**
to the same level!

Spin motion

Thomas-BMT equation:

magnetic moment

$$\frac{d\vec{S}}{dt} = \vec{\Omega} \times \vec{S} = -\frac{q}{m_0} \left\{ G\vec{B} - \frac{\gamma G}{\gamma + 1} \vec{\beta}(\vec{\beta} \cdot \vec{B}) + \left(\frac{1}{\gamma^2 - 1} - G \right) \frac{\vec{\beta} \times \vec{E}}{c} + d \frac{m_0}{q\hbar S} \left(\vec{E} - \frac{\gamma}{(\gamma + 1)} \vec{\beta}(\vec{\beta} \cdot \vec{E}) + c\vec{\beta} \times \vec{B} \right) \right\} \times \vec{S}$$

EDM

Ω : angular precession frequency

d : electric dipole moment

G : anomalous magnetic moment

γ : Lorentz factor

Storage rings: \vec{B} vertical, \vec{E} radial

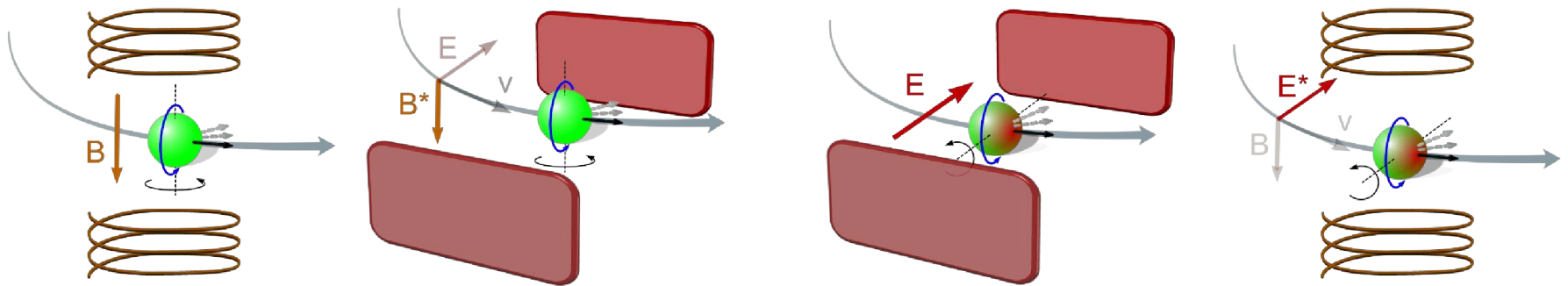
Storage rings: general case

magnetic moment

EDM

Lorentz force

$$\frac{d\vec{S}}{dt} = \vec{\Omega} \times \vec{S} = -\frac{q}{m_0} \left\{ G\vec{B} + \left(\frac{1}{\gamma^2 - 1} - G \right) \frac{\vec{\beta} \times \vec{E}}{c} + d \frac{m_0}{q\hbar S} (\vec{E} + c\vec{\beta} \times \vec{B}) \right\} \times \vec{S}$$



magnetic moment causes
fast spin precession: $\vec{S}_H \nparallel \vec{p}$

- Ω : angular precession frequency
- G : anomalous magnetic moment
- d : electric dipole moment
- γ : Lorentz factor

Storage rings: electric ring

magnetic moment

EDM

$$\frac{d\vec{S}}{dt} = \vec{\Omega} \times \vec{S} = -\frac{q}{m_0} \left\{ G\vec{B} + \underbrace{\left(\frac{1}{\gamma^2 - 1} - G \right)}_{\equiv 0!} \frac{\vec{\beta} \times \vec{E}}{c} + d \frac{m_0}{q\hbar S} (\vec{E} + c\vec{\beta} \times \vec{B}) \right\} \times \vec{S}$$

„frozen spin“ : precession vanishes at magic momentum

$$G = \frac{1}{\gamma^2 - 1} \Rightarrow p = \frac{m}{\sqrt{G}}$$

only possible for $G > 0$

Dedicated ring for protons

Storage rings: combined ring

magnetic moment

EDM

$$\frac{d\vec{S}}{dt} = \vec{\Omega} \times \vec{S} = -\frac{q}{m_0} \left\{ \underbrace{G\vec{B} + \left(\frac{1}{\gamma^2 - 1} - G \right) \frac{\vec{\beta} \times \vec{E}}{c}}_{\equiv 0!} + d \frac{m_0}{q\hbar S} (\vec{E} + c\vec{\beta} \times \vec{B}) \right\} \times \vec{S}$$

„frozen spin“: proper combination of \vec{B} , \vec{E} and γ
also for $G < 0$ (i.e. deuterons, ^3He)

All-in-one ring for protons, deuterons, ^3He

Storage rings: magnetic ring

magnetic moment

EDM

$$\frac{d\vec{S}}{dt} = \vec{\Omega} \times \vec{S} = -\frac{q}{m_0} \left\{ G\vec{B} + \left(\frac{1}{\gamma^2 - 1} - G \right) \frac{\vec{\beta} \times \vec{E}}{c} + d \frac{m_0}{q\hbar S} (\vec{E} + c\vec{\beta} \times \vec{B}) \right\} \times \vec{S}$$

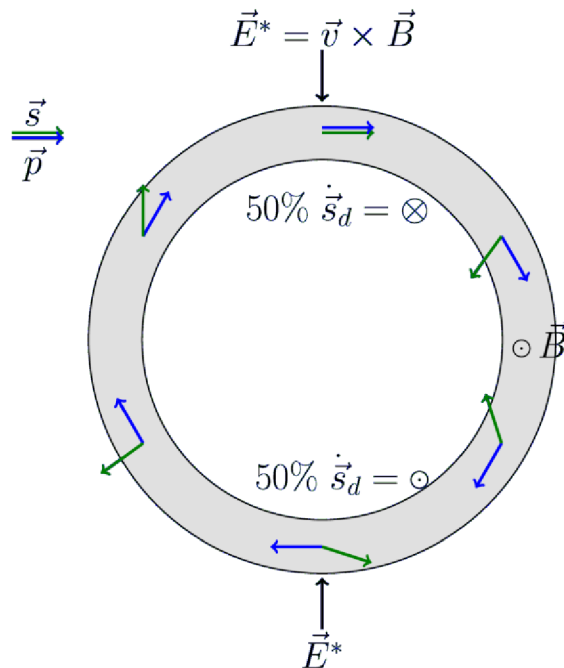
COSY: pure magnetic ring, polarized protons and deuterons

access to **EDM** via motional electric field $c\vec{\beta} \times \vec{B}$

Ideal starting place for R&D and a proof-of-principle experiment

Pure magnetic ring

Due to fast precession **longitudinal** polarization component is
 50% of time parallel
 50% of time anti-parallel
 to momentum



$$\frac{d\vec{S}}{dt} \propto \left(G\vec{B} + d \frac{m_0 c}{q \hbar S} \vec{\beta} \times \vec{B} \right) \times \vec{S}$$

E^* field in the particle rest frame
 tilts spin due to EDM

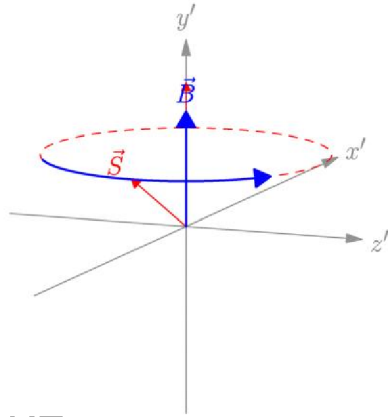
50% of time up and
 50% of time down

→ **no net EDM effect**

Resonant rf Wien filter

Wien filter: Lorentz force vanishes \rightarrow no effect on EDM rotation

Effect on horizontal precession:



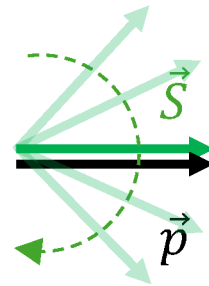
Without WF

Static WF

(precession just faster or slower)

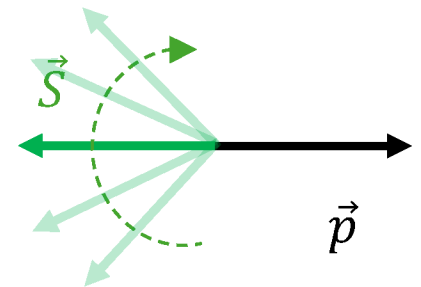
Resonant rf WF

(resonant on precession frequency)



50 %

50 %



50 %

50 %

speed up prec.

<50 %

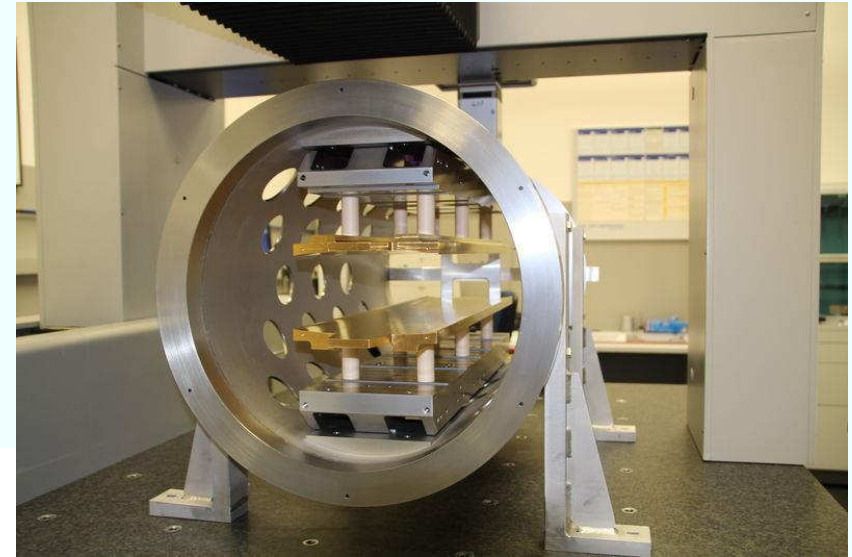
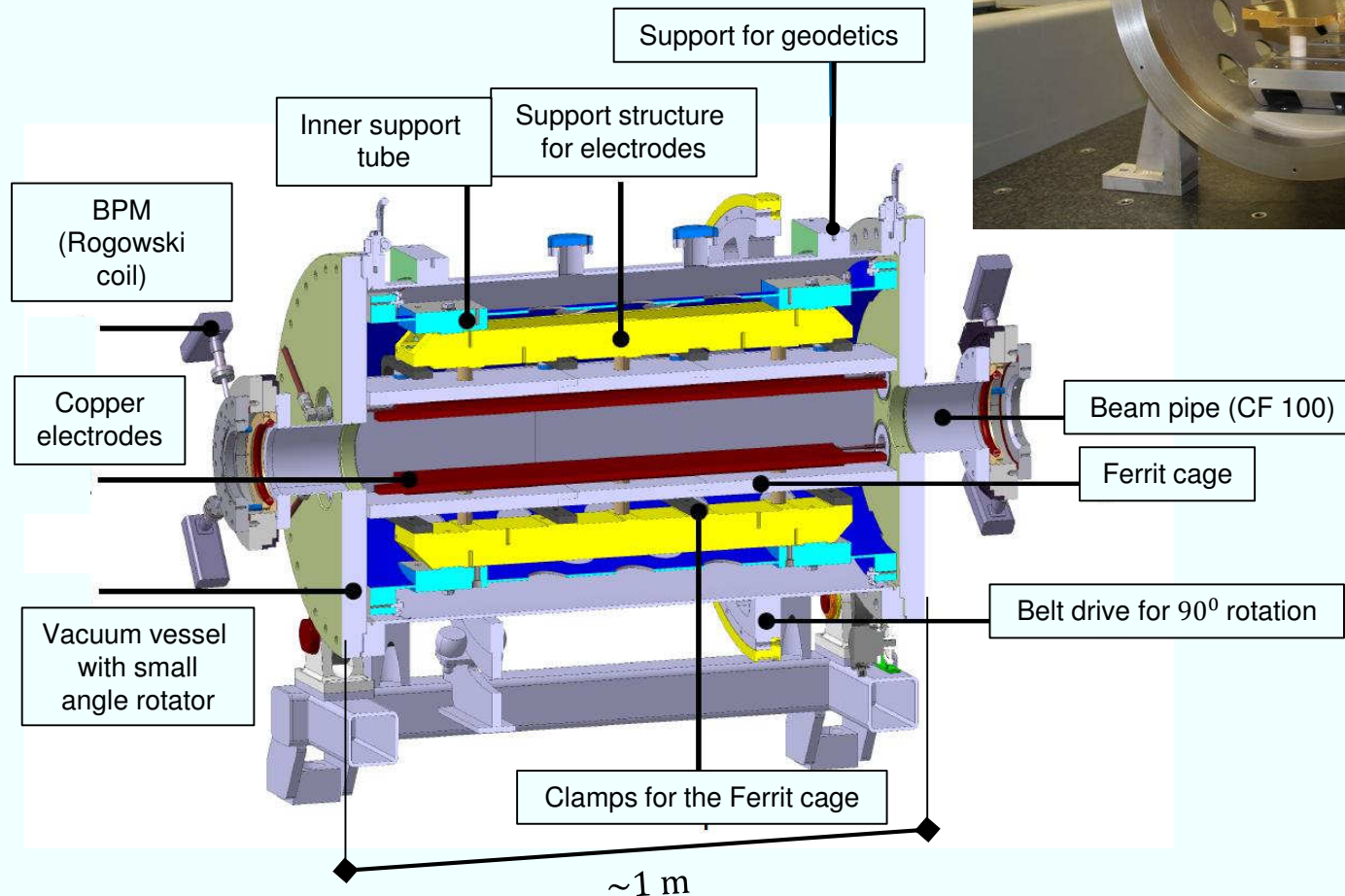
slow down prec.

>50 %

net EDM effect

The RF Wien filter

Waveguide design:
provides $\vec{E} \times \vec{B}$ by design



R&D at COSY

Thomas-BMT equation:

magnetic moment

neglect EDM

$$\frac{d\vec{S}}{dt} = \vec{\Omega} \times \vec{S} = -\frac{q}{m_0} \left\{ G\vec{B} + \left(\frac{1}{\gamma^2 - 1} - G \right) \frac{\vec{\beta} \times \vec{E}}{c} + d \frac{m_0}{q\hbar S} (\vec{E} + c\vec{\beta} \times \vec{B}) \right\} \times \vec{S}$$

$$\text{spin tune } \nu_s = \frac{|\vec{\Omega}|}{|\vec{\omega}_{\text{cycl}}|} = \gamma G$$

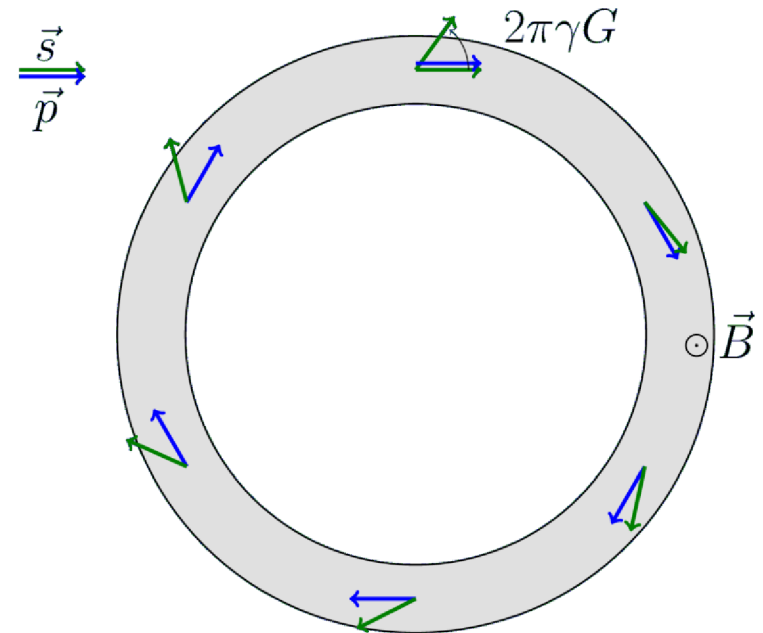
→ phase advance per turn $2\pi\nu_s$

R&D with deuterons

$$p = 1 \text{ GeV}/c$$

$$G = -0.14256177(72)$$

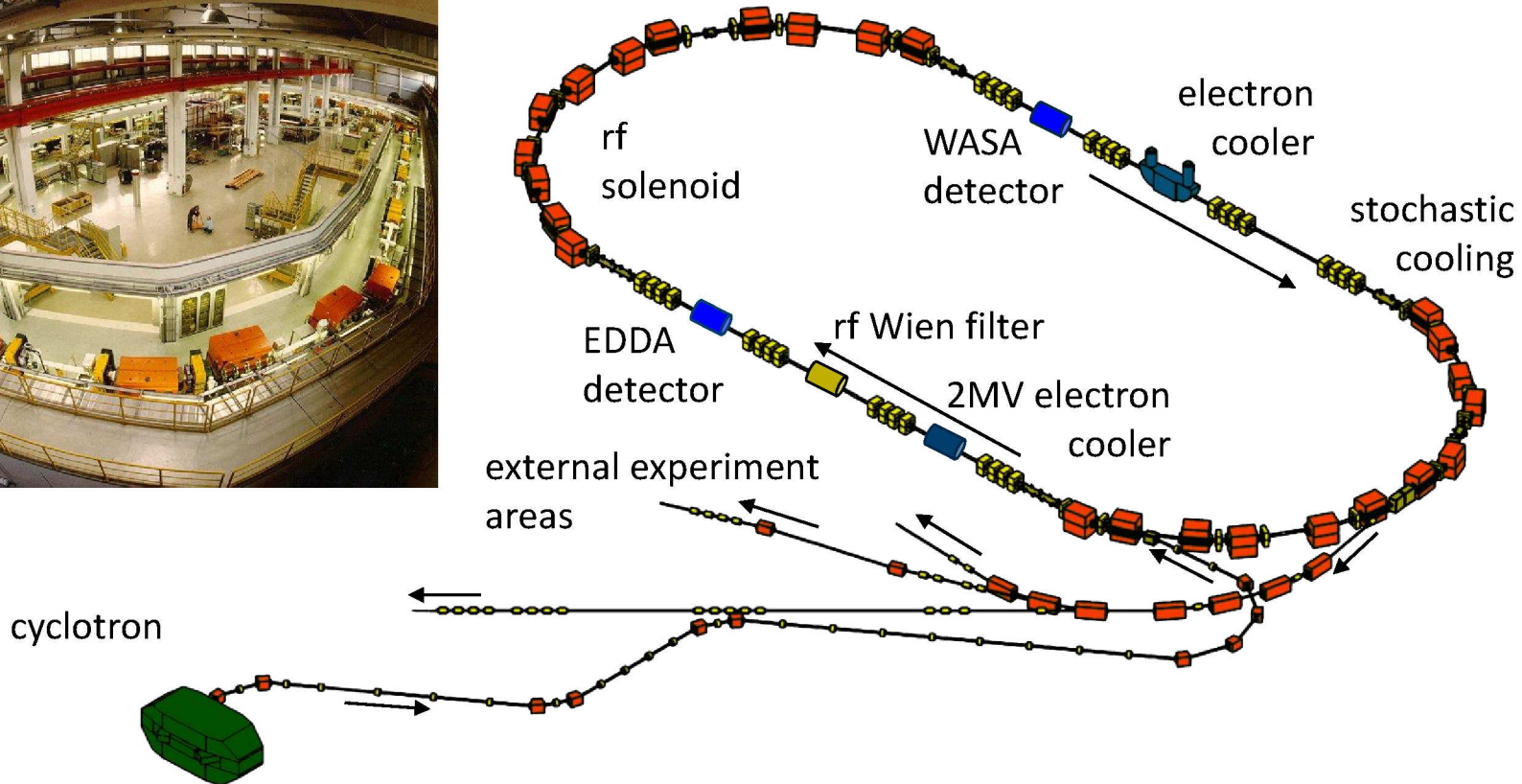
$$\nu_s \approx -0.161 \rightarrow f \approx 120 \text{ kHz}$$



(Some) Questions to be addressed

- Precise measurement of the precession frequency (spin tune)
→ also continuous and online
- Maximizing the spin coherence time (goal: ≈ 1000 s)
- Maintaining the spin direction
→ keep precession frequency stable
→ match frequency and phase to Wien filter radio frequency
- Study effects of field misalignments, orbit distortions, etc.

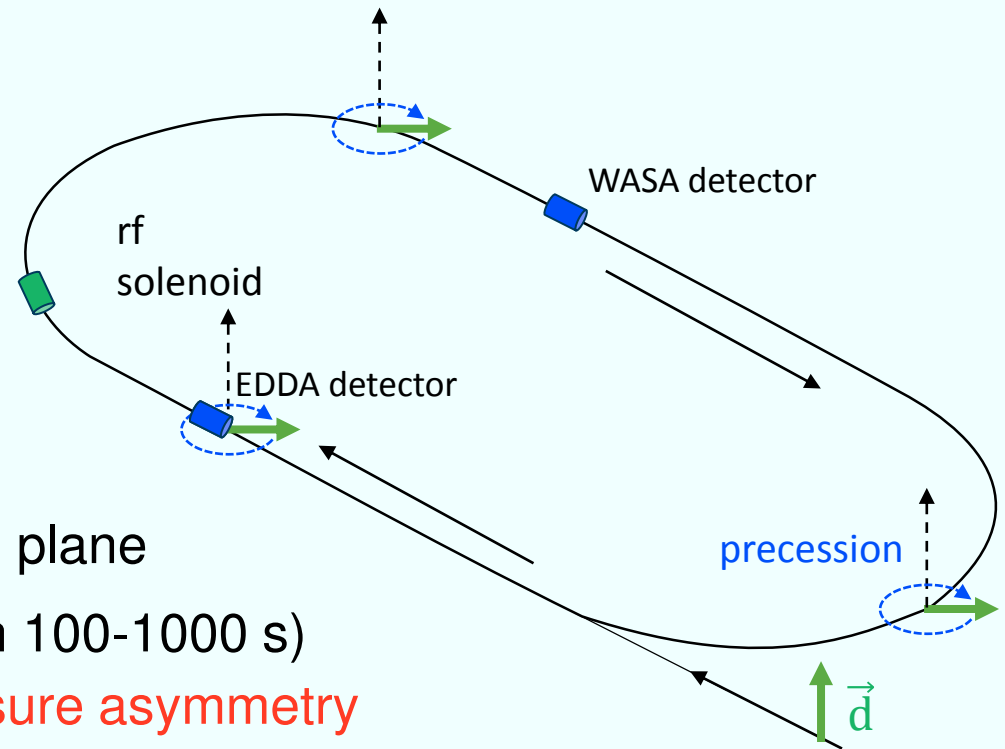
Cooler Synchrotron COSY



COSY provides cooled & polarized protons and deuterons with
 $p = 0.3 - 3.7 \text{ GeV}/c$

Experimental setup

1. inject and accelerate vertically polarized deuterons to $p = 1 \text{ GeV}/c$
2. bunch and (pre-)cool
3. turn spin by means of a RF solenoid into horizontal plane
4. extract beam slowly (within 100-1000 s) onto a carbon target, **measure asymmetry** and precisely **determine spin precession**



spin tune:

$$|\nu_s| = |\gamma G| = \frac{\text{spin precessions}}{\text{particle turn}} = \frac{f_{\text{prec}}}{f_{\text{rev}}} \approx \frac{120 \text{ kHz}}{750 \text{ kHz}} \approx 0.16$$

Polarimetry

- elastic deuteron-carbon scattering
- spin-dependent cross section:

$$\sigma(\varphi) = \sigma_0 \left(1 + \frac{3}{2} PA \sin \varphi \right)$$

$$\sigma_+ = \sigma(90^\circ) = \sigma_0 \left(1 + \frac{3}{2} PA \right)$$

$$\sigma_- = \sigma(-90^\circ) = \sigma_0 \left(1 - \frac{3}{2} PA \right)$$

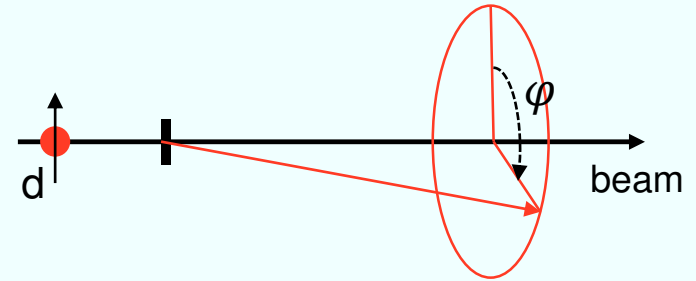
asymmetry:

$$\varepsilon = \frac{\sigma_+ - \sigma_-}{\sigma_+ + \sigma_-} = \frac{3}{2} PA$$

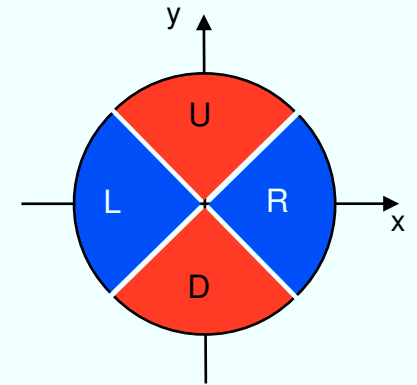
- segmented detector

left – right asymmetry probes polarization along y

up – down asymmetry probes polarization along x

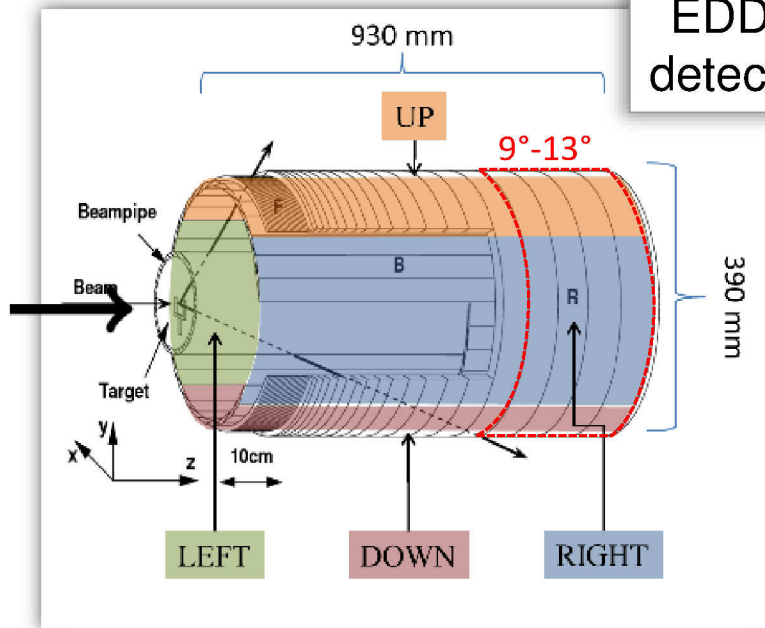


P: polarization
A: analyzing power

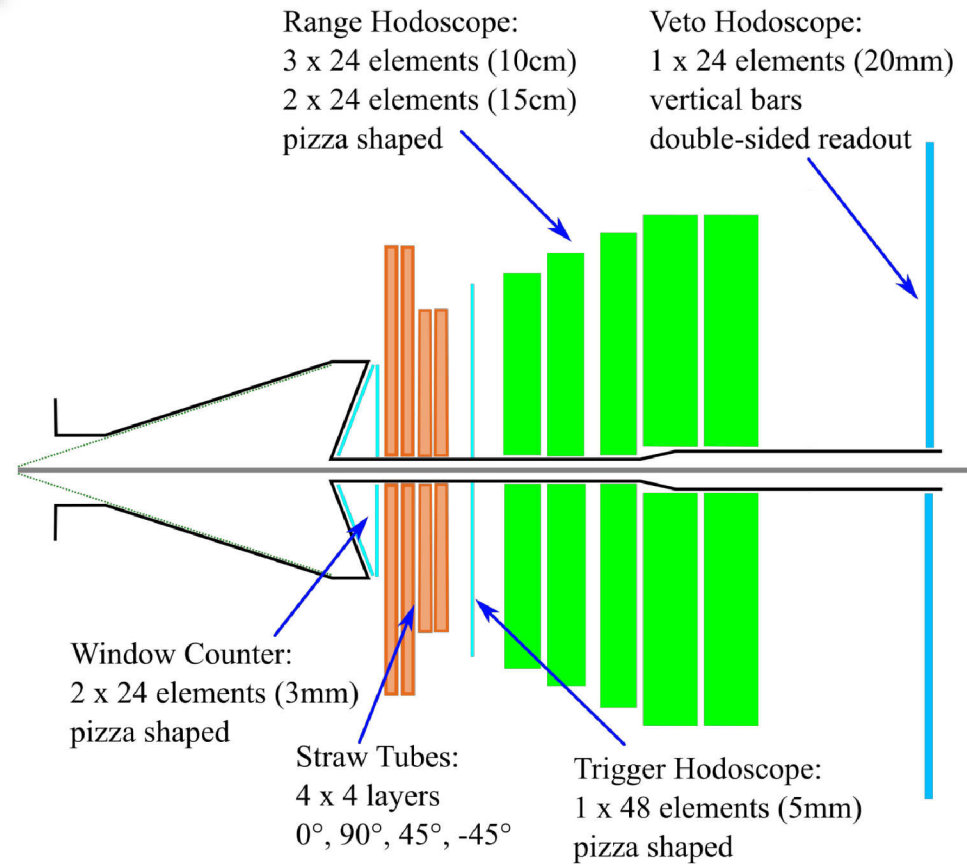


Detector installations

EDDA
detector



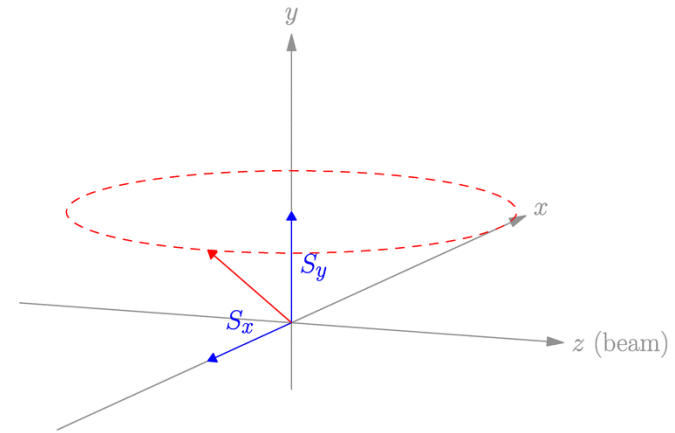
WASA
detector



Spin precession

Time-dependent asymmetry

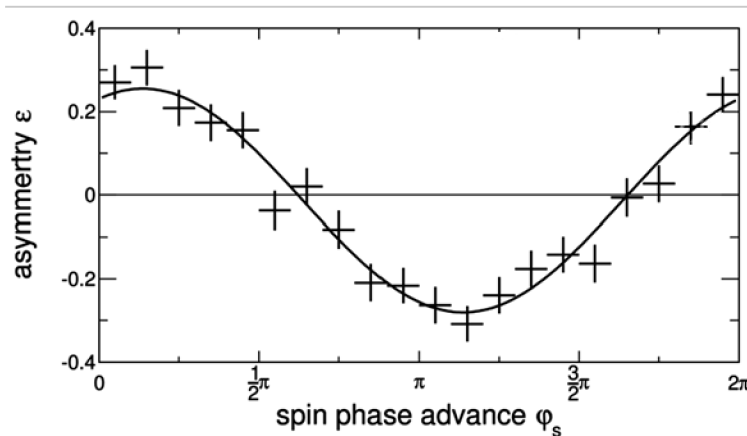
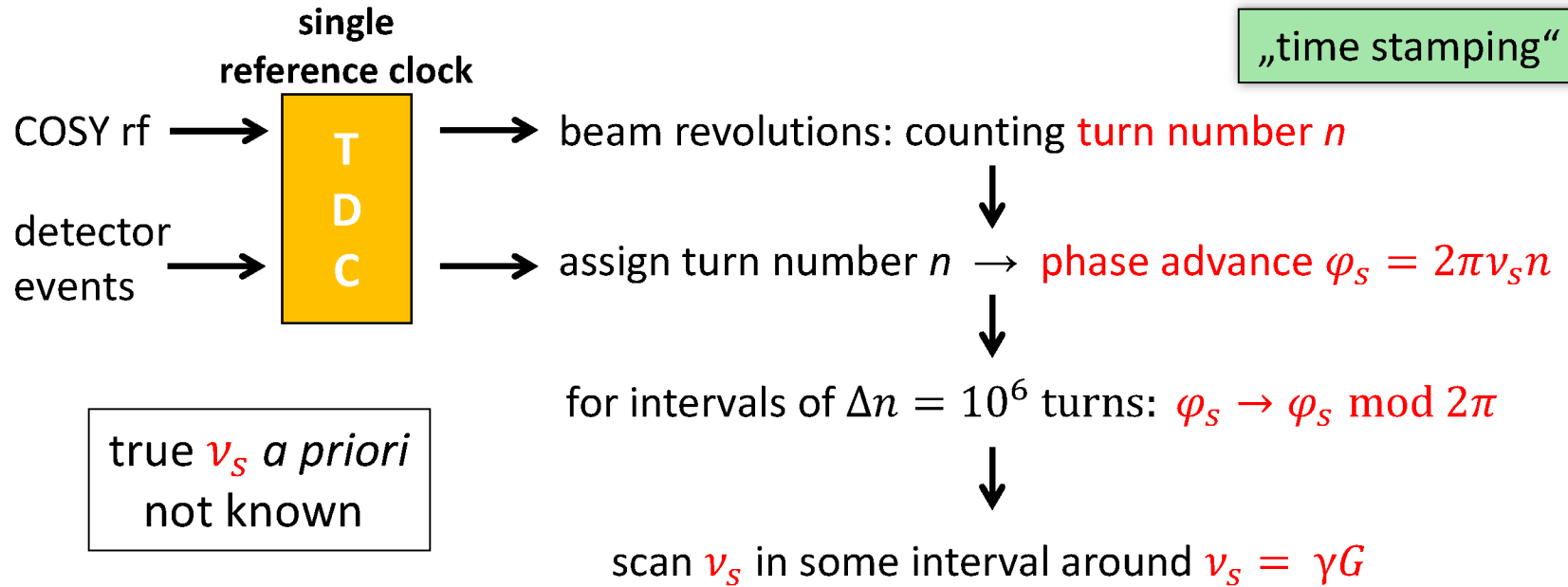
$$\varepsilon_x = \frac{3}{2} PA \sin(2\pi\nu_s \cdot n_{\text{turns}})$$



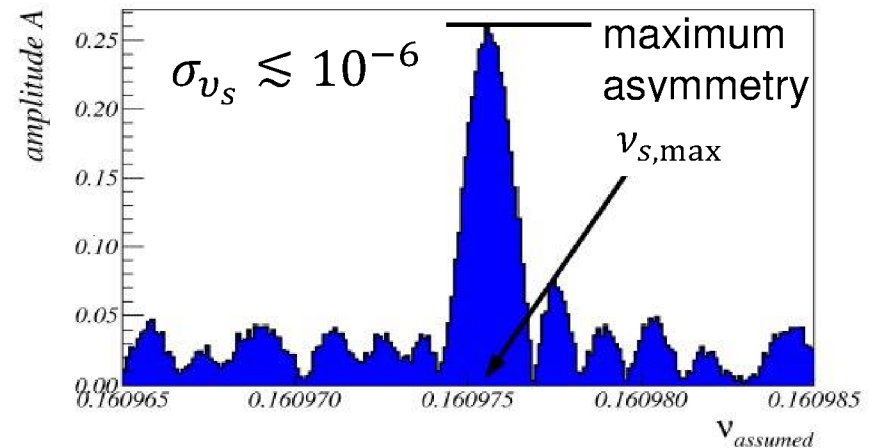
Challenges

- precession frequency $f_{\text{prec}} \approx 120 \text{ kHz}$
- $\nu_s \approx -0.16$ → 6 turns / precession
- event rate $\approx 5000 \text{ s}^{-1}$ → 1 hit / 25 precessions
→ no direct fit of the rates

Unfolding the spin precession

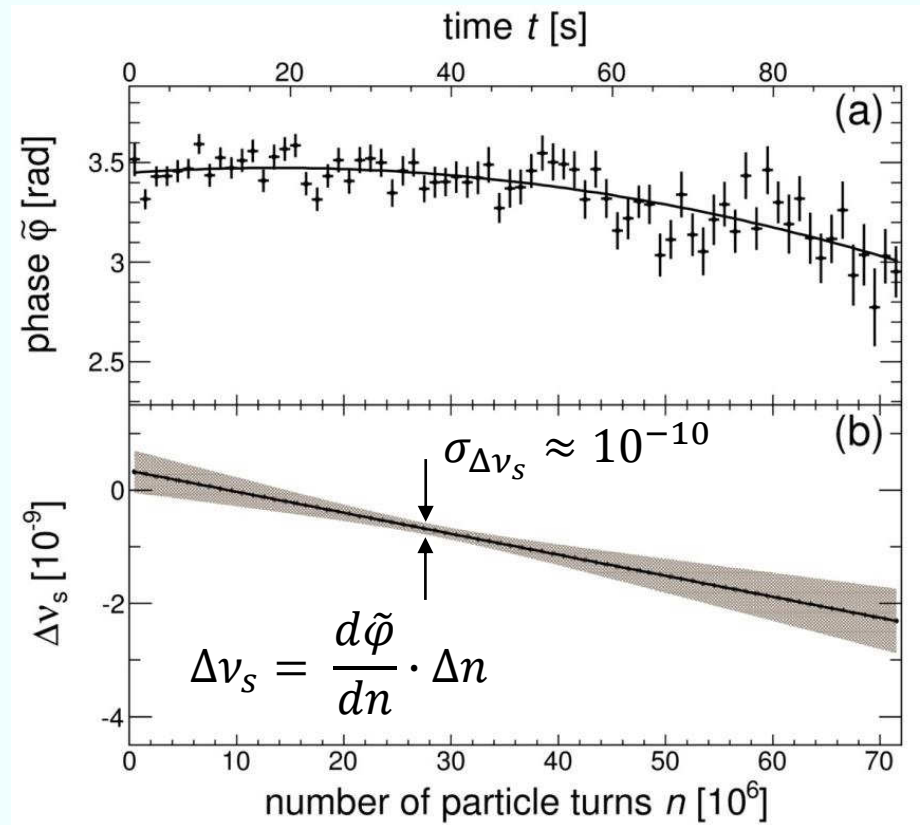
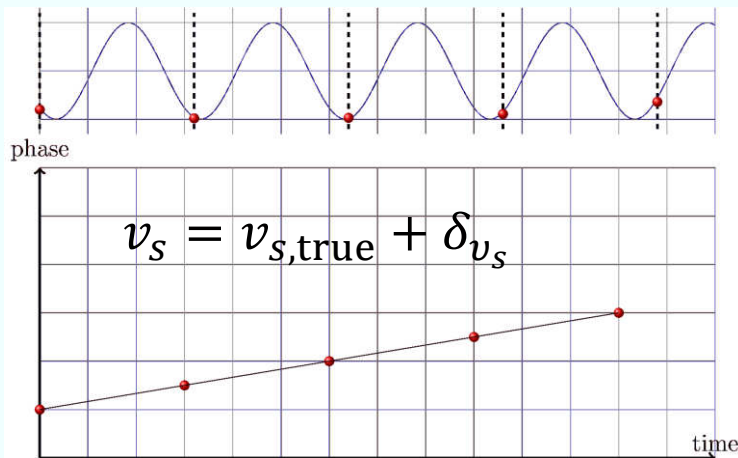
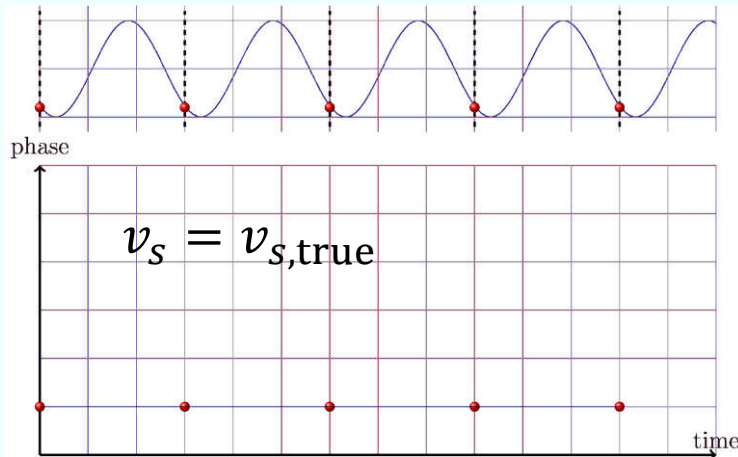


see: Phys.Rev.Lett. 115, 094801 (2015)



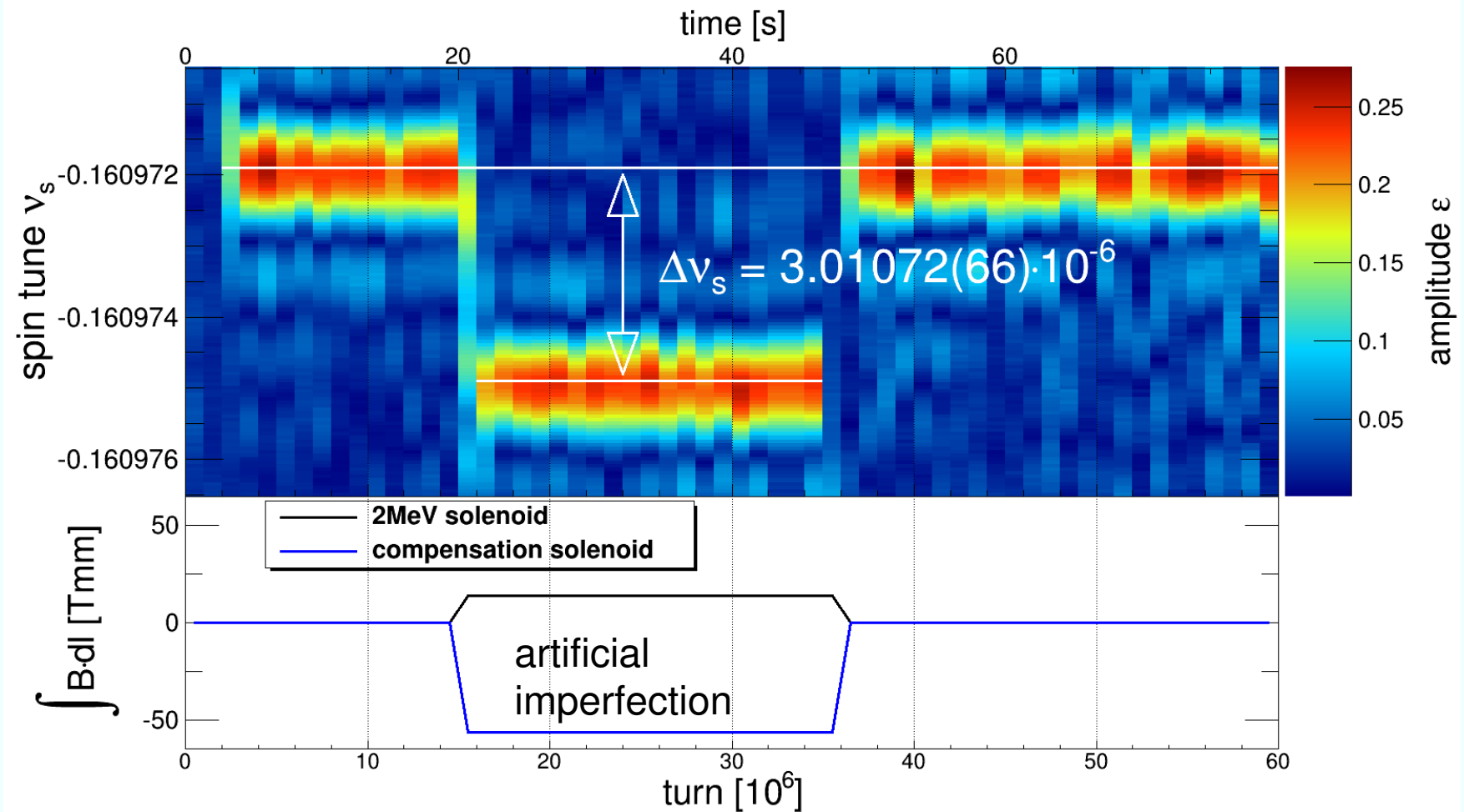
Precise determination of the spin tune

Monitoring phase of asymmetry (ν_s fixed):



see: Phys.Rev.Lett. 115, 094801 (2015)

Spin tune: probing field imperfections



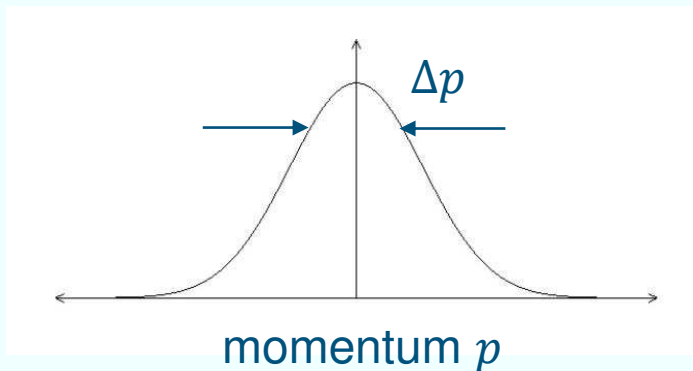
Spin Coherence Time (SCT)

Ensemble of $\approx 10^9$ deuterons: **coherent precession needed!**

Ideal case

- all particles have exactly the same momentum no
- all particles travel the same path (orbit) in the ring no
- all particles see the same fields no

Example



$$\frac{\Delta\gamma}{\gamma} = \overset{0.2}{\beta^2} \overset{10^{-3}}{\frac{\Delta p}{p}} \approx 10^{-4} = \frac{\Delta\nu}{\nu}$$

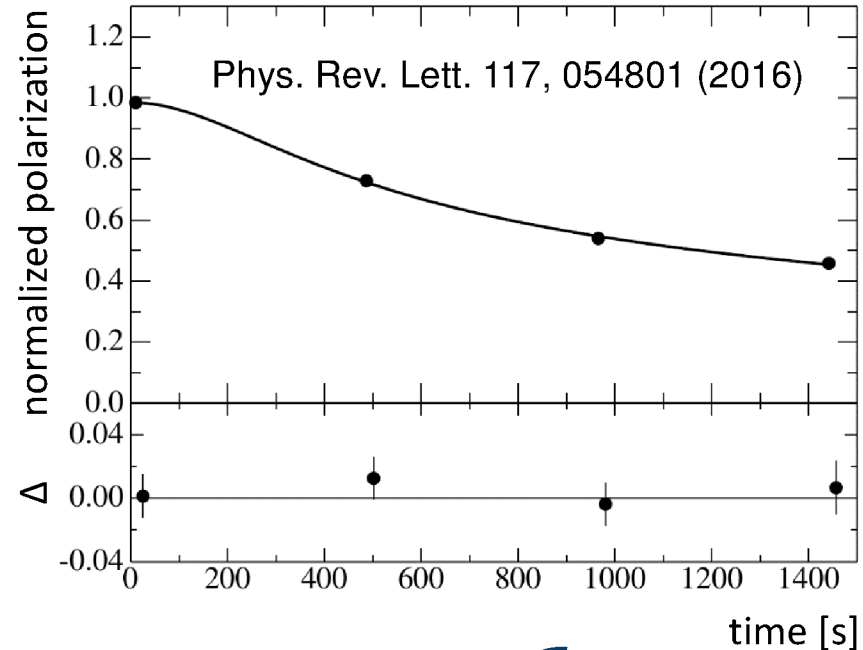
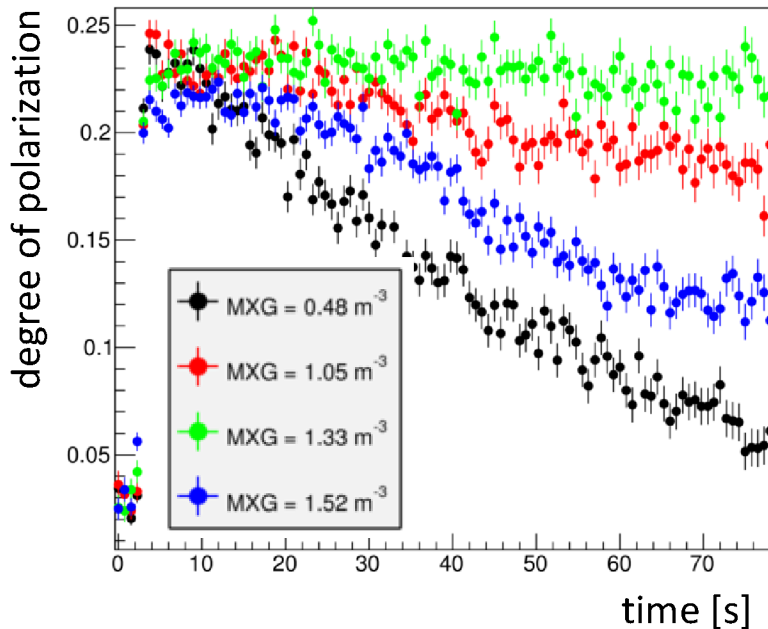
$$\Delta\nu \approx 10^{-4} \cdot 0.16 \approx 10^{-5}$$

↗ revolution frequency

$$\Delta\varphi = 2\pi \cdot 10^{-5} \cdot 10^6 \text{s}^{-1} \approx 60 \text{ rad/s}$$

Spin Coherence Time (SCT)

- unbunched beam: $\frac{\Delta\gamma}{\gamma} \approx 10^{-5} \Rightarrow$ decoherence in < 1 s
- bunching: eliminate effects on $\frac{\Delta p}{p}$ in 1st order $\rightarrow \tau \approx 20$ s
- correcting higher order effects using sextupoles
and (pre-) cooling $\rightarrow \tau \approx 1000$ s

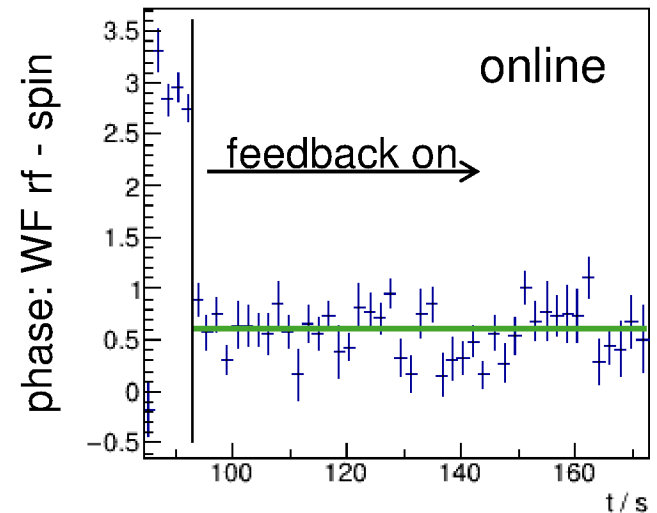
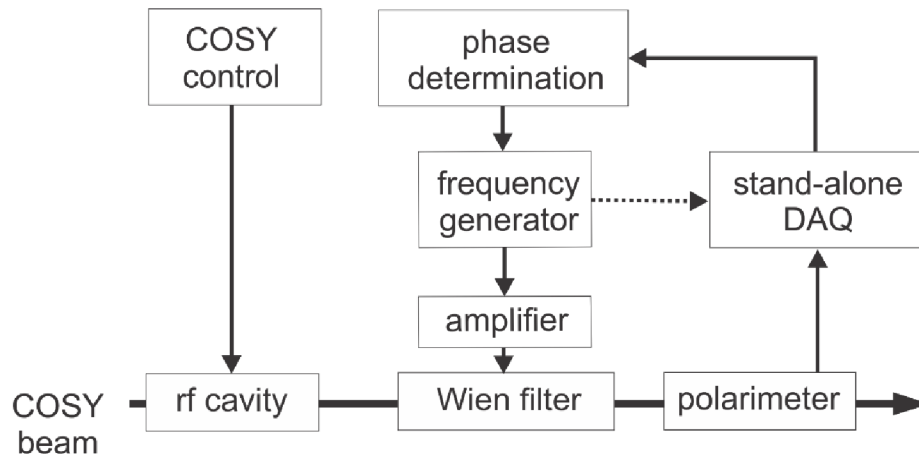


Spin tune: feedback system (phase lock)

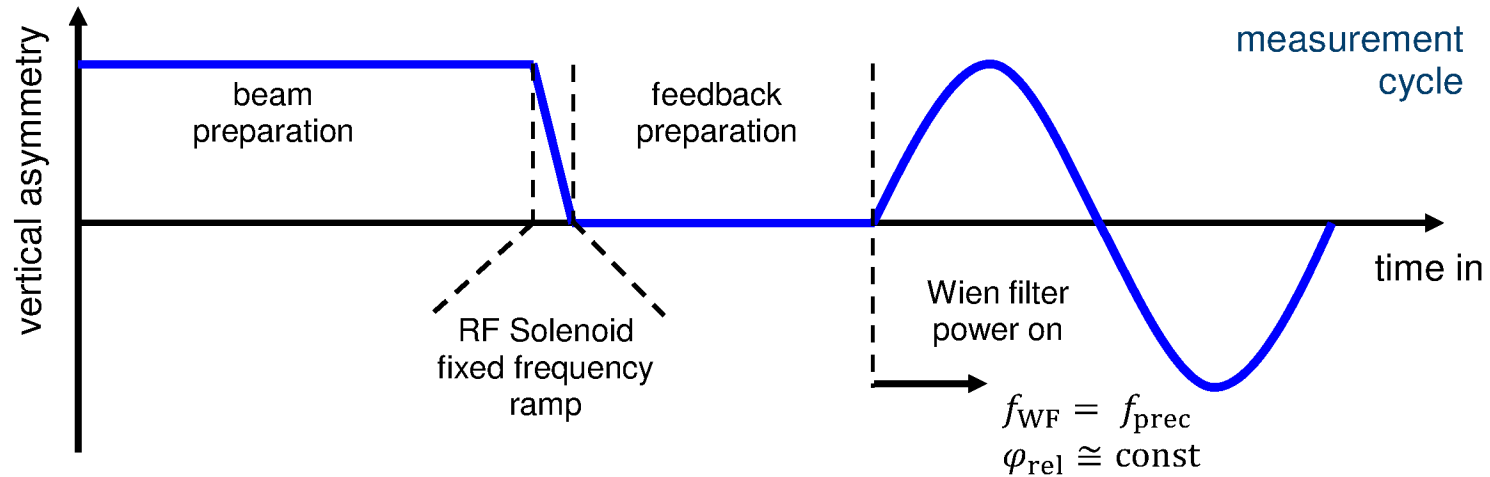
Challenges:

- maintain **resonance frequency** and **phase** between spin precession and Wien filter
- maintain frozen spin condition in a future dedicated ring

Implementation at COSY:



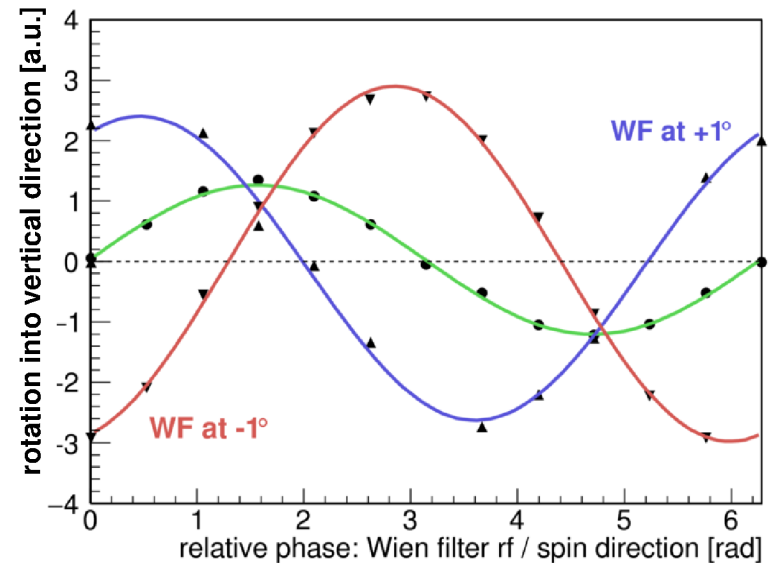
Measurements with the Wien filter



Build-up of vertical component caused by

- EDM effect
- field and alignment errors in the ring

Systematic study by controlled changes of the device alignments and fields



Summary

- EDMs sensitive to new sources of CP violation
- Mechanism for CP violation: EDMs of charged hadrons needed
- Observable: spin precession in electric fields in storage rings
- COSY: ideal starting point for R&D and a pre-cursor experiment

Outlook

- pre-cursor experiment at COSY:
first measurement with lower sensitivity on the way
- dedicated storage ring:
different options are currently under investigation