Original Research

Core Ideas

- The impact of roots on bulk electrical conductivity was studied using a modeling approach.
- The presence of roots affects petrophysical relations.
- The effect of roots is more pronounced in sandy soil than in loamy soil.
- Root surface and soil-root electrical contrast affect ERT measurements the most.

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Impact of Maize Roots on Soil–Root Electrical Conductivity: A Simulation Study

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Electrical resistivity tomography (ERT) has become an important tool for studying root-zone soil water fluxes under field conditions. The results of ERT translate to water content via empirical pedophysical relations, usually ignoring the impact of roots; however, studies in the literature have shown that roots in soils may actually play a non-negligible role in the bulk electrical conductivity (σ) of the soil-root continuum, but we do not completely understand the impact of root segments on ERT measurements. In this numerical study, we coupled an electrical model with a plant-soil water flow model to investigate the impact of roots on virtual ERT measurements. The coupled model can produce three-dimensional simulations of root growth and development, water flow in soil and root systems, and electrical transfer in the soil-root continuum. Our electrical simulation illustrates that in rooted soils, for every 1% increase in the root/sand volume ratio, there can be a 4 to 18% increase in the uncertainty of σ computed via the model, caused by the presence of root segments; the uncertainty in a loam medium is 0.2 to 1.5%. The influence of root segments on ERT measurements depends on the root surface area ($r = \sim 0.6$) and the σ contrast between roots and the soil ($r = \sim 0.6$) \sim 0.9), as revealed by correlation analysis. This study is important in the context of accurate water content predictions for automated irrigation systems in sandy soil.

 $Abbreviations: 3D, three-dimensional; ERT, electrical \ resistivity \ tomography.$

Understanding root water uptake and the associated nutrients is critical for crop management but remains a challenging task because of the inherent difficulty in making and taking observations inside soils (de Dorlodot et al., 2007). Geophysical monitoring of root-zone soil moisture has received much interest in past decades as a way to tackle this challenge. One such method is ERT, which aims at retrieving the two- or threedimensional distribution of σ or its inverse (electrical resistivity) in the soil from electric resistance measurements at discrete electrode locations (Beff et al., 2013). The σ is thus related to the property or state variable of interest, such as the soil water content (θ) , the porosity, the electrical conductivity of the soil fluid (σ_w) , the temperature, or the mineral composition (Friedman, 2005). This is calculated through a proper pedophysical relationship (e.g., quantifying σ as a function of θ). In cropped fields, ERT has been increasingly used for monitoring θ (Michot et al., 2003; Srayeddin and Doussan, 2009; Garré et al., 2013; Cassiani et al., 2015; De Carlo et al., 2015; Brillante et al., 2016; Vanella et al., 2018). More recently, ERT-estimated water content has been used for phenotyping root systems at the field scale (Whalley et al., 2017). Whalley et al. (2017) monitored changes in the σ of the soil root zone under drying conditions at different soil depths, which acted as a proxy for root activity. However, the bulk electrical conductivity (σ_{bulk}) of a vegetated soil potentially containing roots depends not only on θ but also on the roots and their impact on the soil structure (Garg et al., 2019). For example, a recent pot experiment showed that diseased and healthy roots in the soil could generate different ERT measurements (Corona-Lopez et al., 2019). In some field experiments, different pedophysical relationships for soils with and without roots have been observed (Werban et al., 2008; Michot et al., 2016; Ni

et al., 2018). However, in lysimeter experiments, studies showed that pedophysical function was time invariant, despite ongoing root growth (Garré et al., 2011). In Fig. 1, we show the envelope of the σ_{bulk} values of soil without roots $(\sigma_{bulk\text{-soil}})$ and the envelope of the σ of root segments (σ_{root}) as reported by several researchers. Figure 1 shows that the contrast between σ_{root} and $\sigma_{bulk\text{-soil}}$ is a function of plant species in addition to the soil bulk properties or state variables and indicates that roots could have a measurable but variable impact on ERT measurements.

For a given species, $\boldsymbol{\sigma}_{\mathrm{root}}$ is generally a function of root anatomy, which can be related to root age, root order, or root diameter. In their study, Anderson and Higinbotham (1976) found that older maize (Zea mays L.) root segments are electrically more conductive than younger roots. Their study was performed on excised root segments. They showed that the outer layer of the root segment (cortex) has very low electrical resistance (\sim 50 k Ω) in the radial direction compared with the axial direction (\sim 600 k Ω). By treating the cortex and stele as concentric parallel conductors, the reported resistances, when converted into conductivities, are on the order $\sigma_{\rm root} \sim 0.05~S~m^{-1}.$ However, the electrical behavior of intact root segments embedded in the soil might be different from that of excised segments. Another study by Cao et al. (2010) reported that root electrical resistance could be related to root properties such as surface area, the number of lateral roots, and root length. Studies on poplar (Populus sp.) roots showed that the σ_{bulk} of the soil–root medium may increase or decrease with an increase in root mass density, depending on the age of the plant (al Hagrey, 2007; Zenone et al., 2008; Mary et al., 2016). In addition, some studies have found a correlation between the root length or mass density and electrical resistivity obtained through ERT (Amato et al., 2009; Rossi et al., 2011). Along with root geometrical properties such length, surface area, or mass density, the electrical contrast between roots and the soil also plays a role in influencing ERT results. However, it is not clear what proportion of the electrical signature of roots that can be seen in the ERT measurements can be attributed to each of the root parameters (e.g., electrical contrast, root length, surface area, and volume density).

Beyond the impact of σ_{root} , root-related processes such as water uptake, exudation, or solute uptake will also affect the

electrical properties of the rhizosphere (i.e., the soil zone in close proximity to the root segments), thereby affecting the contrast between $\sigma_{\rm root}$ and $\sigma_{\rm bulk\text{-}soil}$. Recent ERT experiments on orange [Citrus × sinensis (L.) Osbeck] orchard fields suggest that ERT results are more sensitive to root water uptake patterns (Vanella et al., 2018) than to resistive lignified roots. Performing such experiments is, however, costly and time consuming and is difficult to reproduce for various species and soil types, hence the need for modeling. Al Hagrey and Petersen (2011) previously studied the impact of roots on ERT imaging by using a root growth model (Wilderotter, 2003) but ignored the inherent heterogeneity of $\sigma_{\rm root}$ and $\sigma_{bulk\text{-soil}}$. To understand the effect of root system connectivity and their impact on σ_{bulk} , a model where functional roots are explicitly represented is needed. Explicit root representations provided by an unstructured finite element mesh have been studied for water and nutrient uptake processes (Wilderotter, 2003; Tournier et al., 2015). In this study, we have extended it to ERT forward simulation coupled to a plant-soil water flow model and a realistic complex root system architecture.

The objective of this study was to investigate the impact of root segments and root water uptake on the effective soil–plant σ . Specifically, we wanted to quantify the effects of soil–root contrast, plant growth, and root water uptake on the pedophysical relations.

Materials and Methods

To achieve our objectives, we developed a soil–plant model that combines electric and hydraulic dynamics and applied it to generate virtual rhizotron experiments. A rhizotron is a thin container (typically around 2 by 20 by 40 cm) filled with a growth substrate in which plant roots develop, allowing observation of the development of the root system architecture and sometimes the substrate water content (Garrigues et al., 2006; Ahmed et al., 2018) and can thus be used to investigate how soil heterogeneity affects root growth and uptake (e.g., Bauke et al., 2017). In this study, the soil–root system was modeled at a fine spatial resolution for the roots via an unstructured mesh for ERT forward simulation. The virtual environment allowed us to account for root architecture, soil water redistribution, soil heterogeneity,

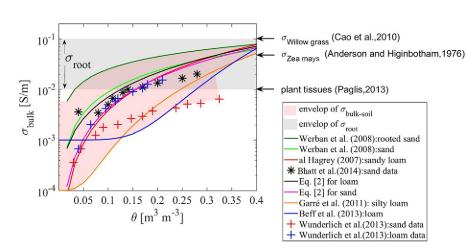


Fig. 1. Comparison of soil and root electrical conductivity ($\sigma_{\rm soil}$ and $\sigma_{\rm root}$ respectively). The envelopes of $\sigma_{\rm soil}$ (some with and some without roots) and $\sigma_{\rm root}$ are shown as shaded areas (Paglis, 2013; Bhatt and Jain, 2014).

root-specific electrical properties, root growth, and transient transpiration. Figure 2 summarizes the various steps of this modeling process as a flowchart.

The Root Growth Experiment and the Soil–Plant Water Flow Model

The two-dimensional root architecture (see Fig. 3) was extracted from real experiments on a rhizotron with 21-d-old maize by the root image analyzing tool smartroot (Lobet et al., 2011; Lobet and Draye, 2013). We used a 5- to 21-d-old root system for our simulations. Because root growth was monitored every day, ages were easily assigned to each root segment. In these experiments, the rhizotrons were weighed daily, thereby allowing us to estimate the average transpiration rates.

The rhizotrons measured 22 by 2 by 42 cm (the corresponding reference axes are $-11 \text{ cm} \le x \le 11 \text{ cm}$, $-1 \text{ cm} \le y \le 1 \text{ cm}$, and $-40 \text{ cm} \le z \le 2 \text{ cm}$). We considered two soil types: sandy and loamy, with the hydraulic properties represented by Mualemvan Genuchten equations (van Genuchten, 1980) in Table 1. Hydraulic parameters for both soils were derived from Carsel and Parrish (1988).

The soil–plant water flow model R-SWMS (Javaux et al., 2008) was used to estimate the evolution of root water uptake, soil water flux, and the θ distributions in the rhizotrons. R-SWMS uses the finite element method on a regular uniform grid to solve Richards' equation to simulate three-dimensional (3D) water flow in the soil:

$$\frac{\partial \theta}{\partial t} = \frac{\partial}{\partial x} \left(K \frac{\partial h}{\partial x} \right) + \frac{\partial}{\partial y} \left(K \frac{\partial h}{\partial y} \right) + \frac{\partial}{\partial z} \left[K \frac{\partial (h+z)}{\partial z} \right] - \text{Sink} \quad [1]$$

where θ is the volumetric soil water content (cm³ cm⁻³), h is the matrix head (cm), K is the isotropic hydraulic conductivity (cm d⁻¹), Sink is the sink term for root water uptake (cm³ cm⁻³ d⁻¹), and x, y, and z are the spatial coordinates; the dot represents divergence. The sink term is estimated on the basis of a weighted averaged of the uptake fluxes in each soil voxel.

The water fluxes into and toward the roots were calculated via a finite difference method in the root system network based on soil and root water potential distributions and the transpiration rate. The transpiration rate increased with root growth. Each root segment was characterized by its radial and axial hydraulic properties,

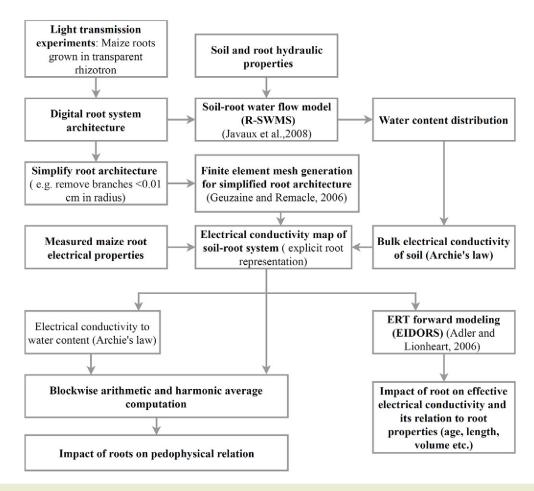


Fig. 2. Flow chart for simulation of the virtual rhizotron drying experiment. First, a simulation of root water uptake and root growth of a maize plant in a rhizotron is run with a soil–plant water flow model (R-SWMS; Javaux et al., 2008), which generates maps of soil water distribution (θ) and development of root architecture. These distributions are then transformed into detailed electrical conductivity (σ) maps through bio- or pedophysical relationships. Third, these distributions are used to simulate a virtual electrical resistivity tomography (ERT) measurement to obtain the apparent conductivity.

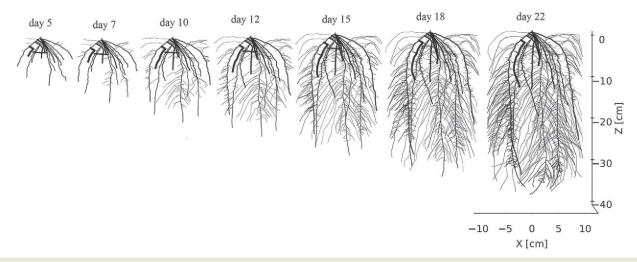


Fig. 3. Root architectural development shown at different times. A digitized root system was generated by smartroot software (Lobet et al., 2011). The thickness of each root segment is plotted proportional to its radius.

which developed with root segment age. Experimentally measured maize root hydraulic conductivity values were used in the R-SWMS model, in which they were age and type dependent (Doussan et al., 2006; Couvreur et al., 2012). The total root length per unit of volume in the R-SWMS simulation was 0.06, 0.22, 0.66, 1.1, and 1.61 cm cm⁻³ on Days 5, 10, 15, 18, and 21, respectively. In a typical field, mature root density can reach values of 1 cm cm⁻³, especially in the topsoil (Gao et al., 2010).

Root growth was simulated by updating the root system architecture at each time step between the beginning (Day 5) and the end (Day 21) of the simulation. The same architecture development pattern was used for sand and loam. We imposed a sinusoidal day–night transpiration as a root boundary condition, with daily transpiration progressively increasing between the beginning (Day 5, 5 cm³) and the end of the simulation (Day 21, 30 cm³), which corresponds to the transpiration rates experimentally observed in greenhouse experiments for similar sized plants (Lobet et al., 2011).

The initial soil condition was hydrostatic equilibrium with a saturated soil at the bottom of the rhizotron (corresponding to the experimental conditions), and root water uptake was the only source or sink term that allowed the total water content to change.

We ignored root exudation and assumed that solute uptake was proportional to the soil solute concentration (i.e., passive uptake) (Hopmans and Bristow, 2002), allowing us to assume a uniform concentration distribution in the liquid solute. Therefore,

Table 1. Soil hydraulic properties.+

Soil	$\theta_{\rm r}$	$\theta_{\rm s}$	а	n	$K_{\rm s}$	λ
$ \text{cm}^3 \text{cm}^{-3}$			cm ⁻¹		${\rm cm}~{\rm d}^{-1}$	
Sand	0	0.35	0.05	2	100.24	0.5
Loam	0.078	0.435	0.036	1.56	25	0.6

 $[\]dagger$ θ_{r} , residual water content, θ_{s} , saturated water content; a, n, and λ , shape parameters in van Genuchten–Mualem equations; K_{s} , saturated soil hydraulic conductivity.

no change in σ caused by solute buildup in the rhizosphere was considered in our simulations.

Electrical Properties of Plant Root Tissues and Soils

To get insight into the maize roots' electrical properties, we followed the method of Ehosioke et al. (2018), who designed specific experiments on intact root segments, where the primary and brace roots from maize plants grown in the laboratory were identified and separated. Roots were then thoroughly washed with demineralized water and dried with absorbent tissue. The electrical resistance of the root segments was measured with a digital multimeter (Fluke 8022A, Fluke Corporation) and were converted into $\sigma_{\rm root}$ by approximating the root segment as having a cylindrical geometry, similar to the method of Cao et al. (2010). The measurement direction of root segments in Cao et al. (2010) was from the root apex toward the root collar, but it was in the opposite direction in the case of the experiment of Ehosioke et al. (2018). In our study, we used the variations of σ_{root} as a function of each segment's distance from the root collar (Fig. 4). The digital maize roots in ERT forward modeling were ~3 wk old, although the brace roots develop only after several weeks in a real maize plant; hence, the brace root data were not included in our model. Figure 4 shows the experimental data of σ_{root} as a function of root age for maize plants. We observed a gradual increase in σ_{root} for intact maize root segments as the distance from the segment to the root collar increased. For each root segment, the Euclidean distance between the midpoint of that segment and the seed location (x = 0, z = 0) was taken as the distance to the root collar and was assigned a $\sigma_{\rm root}$ value according to the polynomial fit, as shown in Fig. 4. However, in our virtual root simulation, the distance to the root collar could be >25 cm in older plants (Fig. 3), for which we do not have corresponding $\sigma_{\rm root}$ values in the measurement data. Hence $\sigma_{\rm root}$ for a distance to the root collar of >25 cm was taken as σ_{root} at a distance to the root collar of 25 cm.

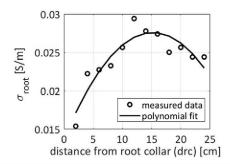


Fig. 4. Measurement data on the electrical conductivity of maize roots (σ_{root}) vs. distance from the root collar. The quadratic fit is shown as a solid line, and the measurement data are represented at discrete locations as circles (primary roots). The polynomial fit $\sigma_{root} = -5.5 \times 10^{-5} (drc^2) + 0.0018 drc + 0.0137$, where drc is distance to the root collar, was used in the model simulations. The black solid curve represents the data incorporated in the electrical resistivity tomography electrical resistivity tomography (ERT) forward modeling: $0.0154 < \sigma_{root} < 0.03$ S m $^{-1}$.

To transform θ maps into σ maps, we used Archie's law (Archie, 1942) with an additional term for the surface conductivity of the solid phase, $\sigma_{\rm surface}$, which is assumed to act in parallel (Waxman and Smits, 1968). The relation between θ and $\sigma_{\rm bulk-soil}$ for unsaturated soil, where Archie's fitting parameters (m and d) vary for different types of soil (Friedman, 2005), is

$$\sigma_{\text{bulk-soil}} = \sigma_{\text{w}} n^m S^d + S^{d-1} \sigma_{\text{surface}}$$
 [2]

where S is the degree of water saturation $(S = \theta/n)$, n is the porosity of the soil (which is assumed to be equal to the saturated water content, θ_s), $\sigma_{bulk-soil}$ is the bulk electrical conductivity of the soil medium without considering roots, σ_w is the conductivity of soil fluid phase, and $\sigma_{surface}$ is the surface σ of the solid phase of the soil. Sand typically has very low surface conductivity $(\sim 10^{-5} \text{ S m}^{-1})$; for loam, we assumed the surface conductivity of the solid phase to be 0.015 S m⁻¹ (Brovelli and Cassiani, 2011). For Archie's fitting parameters, we used the typical values d = 2and m = 1.3 (e.g., Werban et al., 2008). In the rhizotron, $\sigma_{\text{bulk-soil}}$ also depends on the σ_w of the nutrient solution used to grow the plants. We assumed the σ of the nutrient solution to be 0.2 S m⁻¹ and chose n as 0.35 (sand) or 0.435 (loam) to be in the same range as seen in the other observed pedophysical models (Fig. 1). We refer to $\sigma_{\text{bulk-soil}}$ as the soil bulk electrical conductivity when no roots are present; σ_{bulk} is used for studies or datasets where both roots and soil are present.

Note that extremely low values of conductivity in sand (\sim 5 × 10⁻⁹ S m⁻¹) can arise and would need additional mesh refinement in the forward finite element mesh (see below) in regions where there were large conductivity gradients to obtain accurate results. To avoid this scenario and to maintain accuracy, we set a limit of 0.0001 S m⁻¹ as the lowest possible conductivity value.

Meshing the Root Architecture

For the electrical simulation, we generated finite element meshes for the specific root geometry. In the finite element mesh, either a $\sigma_{\rm root}$ or $\sigma_{\rm bulk-soil}$ θ value was assigned to each element (tetrahedron). The primary maize roots in our simulation had a mean radius of \sim 0.025 cm, which is small compared with the dimensions of the rhizotron (20 by 1 by 42 cm), requiring a very high spatial resolution for roots in the forward finite element mesh.

To generate a 3D mesh with a high spatial resolution for the roots but a manageable computational load (<1 million tetrahedrons), we needed to simplify the root system while maintaining a realistic representation of the main structure. First, we removed extremely fine root hairs and root branches that were < 0.01 cm in radius, assuming that such roots have a negligible effect on the voltage measurements. In addition, nearly parallel secondary root branches with a distance of less than double the root radius between them were combined and treated as a single branch. This procedure reduced the total root length in the finite element mesh compared with a real plant. Hence, to preserve the root volume, which we assumed to be the most important factor, in the finite element mesh with the actual measurements we had to increase the mean radius of the root segments. In addition, we discretized each root segment radius in the finite element mesh into two possible values, where all primary roots had one radius but all secondary roots had half the radius of the primary roots; in reality, each segment had unique radii. This simplification affected only the electrical forward model (roots were explicit 3D structures in the electrical mesh) and not the water flow model (roots were treated as a network with no volume in the water flow grid), where we used digitized roots that had identical features (radii and number of segments) to those in the rhizotron experiments.

We compared the time evolution of root volume, total root length, and mean root radius in the finite element mesh with the actual plant (Fig. 5). The root volume in the finite element mesh matched that of the real plant (Fig. 5a). The total root length in the finite element mesh matched the measurements in a younger plant only (Fig. 5b). In older plants, we lost around 50% of the root length through the root simplification procedure. The simplified root architecture represented segments with a mean radius, as shown in Fig. 5c.

The finite element model of the simplified root architecture at Day 5 is shown in Fig. 6. The 3D finite element mesh in Fig. 6c was generated from the simplified root architecture by gmsh software (Geuzaine and Remacle, 2009). Figures 6a and 6b show the simplified architecture at Day 5; Fig. 3 shows the original architecture of a real plant at different times. By comparing these two figures at Day 5, we see that the overall skeleton of the root system and its volume were preserved, although its radii were modified to suit the computational speed. We assumed that root mass density (or root volume) played a bigger role than root length density in affecting the flow of electrical current and hence we prioritized preserving the root volume and, to some extent, the architecture rather than preserving the actual root length and radius, which were modified in the mesh through merging closely adjacent segments. In addition, preserving root radii and root lengths would require a very refined grid and hence would be computationally intensive.

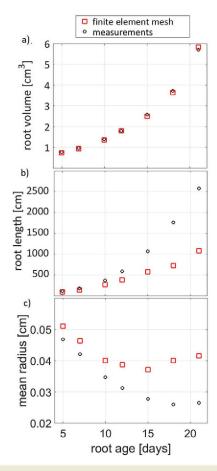


Fig. 5. (a) Root volume vs. root age and (b) root length vs. root age as simulated in the finite element mesh (red squares) or light transmission images (black circles), and (c) mean radius vs. root age in the finite element mesh (red squares) or measurements (black circles).

We also generated additional synthetic data by increasing the mean root radius by factors of two and three (increasing the root volume by fourfold and ninefold). The original mean radii of the root segments in the finite element mesh that matched the experimental volume are shown in Fig. 5d (red squares). Thickening the roots increased the root volume while keeping the root length intact. With seven different root ages (seven different root lengths; see Fig. 3) and three different root radii—actual (Fig. 5d), double of actual, and triple of actual—we had 21 different radii and volumes to be analyzed.

Electrical Resistivity Forward Modeling

We used the finite element based software EIDORS (Adler and Lionheart, 2006) to solve the ERT forward simulation for the generated finite element meshes. The ERT forward simulation solved for the resulting voltages of an electric current of density $\mathbf{J_e}$, injected into a medium of σ , given the proper boundary conditions. The equations governing the physics of electrical resistivity forward modeling are derived from Maxwell's equations for a direct current. Consider a region Ω bounded by its boundary, $d\Omega$. The electric field \mathbf{E} in Ω is related to the scalar electric potential Φ through the gradient operation $\mathbf{E} = -\nabla \Phi$. By applying the conservation of electric charge for a source-free region $(\nabla \cdot \mathbf{J_e} = 0)$ and Ohm's law $(\mathbf{J_e} = \sigma \mathbf{E})$, we obtain the governing equation for ERT inside the medium (also known as the Laplace equation):

$$\nabla \cdot (\sigma \nabla \phi) = 0 \tag{3}$$

The injected current density is specified by the Neumann boundary conditions at the current injecting electrode locations, which are usually located in $d\Omega$:

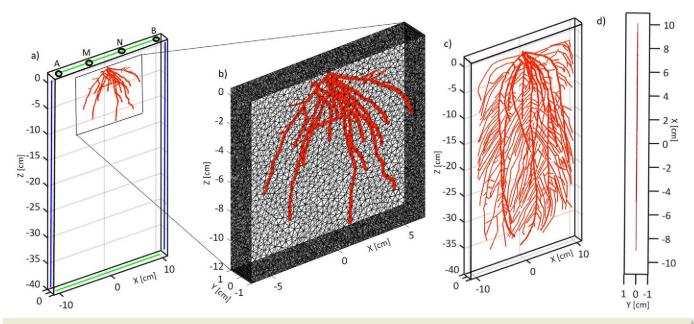


Fig. 6. (a) Finite element model of the virtual rhizotron in EIDORS on Day 5. The vertical line electrodes used to compute the effective electrical conductivity ($\sigma_{\rm effz}$) are shown in blue and the horizontal line electrodes used to compute $\sigma_{\rm effz}$ are shown in green with the mesh hidden. The black circle at the surface denotes the location of point electrodes, denoted by ABMN, used to compute $\sigma_{\rm abmn}$. (b) Close-up view of a section of the forward finite element mesh; (c) model on Day 21 with the mesh hidden. (d) Top view of the finite element model on Day 21. The root tetrahedrons are shown in red.

$$\sigma \nabla \phi \hat{\mathbf{n}} = \sigma \frac{\partial \phi}{\partial \hat{\mathbf{n}}} = \begin{cases} \mathbf{J}_{c} \text{ on the current injecting electrode} \\ -\mathbf{J}_{c} \text{ on the sink electrode} \\ 0 \text{ elsewhere} \end{cases}$$
[4]

The voltage-measuring electrodes dictate the Dirichlet boundary conditions:

$$\phi + Z_{\rm e} \big| \mathbf{J}_{\rm e} \big| = V_{\rm e} \tag{5}$$

where $Z_{\rm e}$ is the contact impedance of the voltage-measuring electrodes (assumed to be 0.01 Ω in this work), ${\bf J}_{\rm e}$ is the current density given by ${\bf J}_{\rm e} = \sigma(\partial \varphi/\partial \, \hat{n} \,)$, $V_{\rm e}$ is the voltage (in V), and $\, \hat{n} \,$ is the unit normal perpendicular to $d\Omega$. Equations [3–5] are the governing equations for the ERT forward problem.

The ERT forward simulation finds voltage or apparent conductivity data by numerically solving Eq. [3-5] for a known distribution of σ . The voltage data (V_e) can be converted to apparent conductivity data, namely that of an equivalent homogeneous medium, with an appropriate geometric factor for the electrodes. The apparent conductivity data measured between the line electrodes in the y = 0 plane (the green and blue lines in Fig. 6a) of each wall (top, bottom, left, and right) gives the effective electrical conductivity (σ_{eff}) in the vertical and horizontal directions, denoted $\sigma_{\rm effz}$ and $\sigma_{\rm effx}$, respectively. Similarly, apparent conductivity measured between the surface quadrupoles (σ_{abmn} , black circles in Fig. 6a) gives the apparent conductivity. The electrical conduction model for the rhizotron is in three dimensions (the same as in the water uptake model in R-SWMS) with the following overall dimensions: -11 cm < x < 11 cm, -1 cm < y < 1 cm,and -40 cm < z < 2 cm.

Upscaled Electrical Properties

To get an insight into how a root-filled soil might differ from bare soil electrical properties, we divided the forward finite element mesh into smaller blocks measuring 2 by 1 by 2 cm and computed the Wiener upper and lower bounds of σ (Wiener, 1912; Jougnot et al., 2018) or the volume-weighted arithmetic and harmonic mean of σ within each block (Fig. 2) via Eq. [6] and [7], respectively:

$$\langle \sigma \rangle = \frac{\sum_{i} V_{i} \sigma_{i}}{\sum_{i} V_{i}} \tag{6}$$

$$\langle \sigma \rangle = \left[\frac{\sum_{i} (V_{i} \sigma_{i})^{-1}}{\sum_{i} V_{i}^{-1}} \right]^{-1}$$
 [7]

where V_i and σ_i are the volume and electrical conductivity of the ith tetrahedron within an averaging block. We also computed the volume-weighted arithmetic mean of water content computed from σ (Archie's law in reverse, as shown in Fig. 2):

$$\theta = \frac{\sum_{i} V_{i} \theta_{i}}{\sum_{i} V_{i}}$$
 [8]

The blockwise-computed arithmetic average of electrical conductivity assumes that the finite elements in each averaging

block are electrically connected in series, whereas the blockwise-computed harmonic average of electrical conductivity assumes the elements to be in parallel. In reality, we expect the true σ_{bulk} to be in between the blockwise-computed arithmetic and harmonic averages of σ , depending on the structural properties of the roots and soil elements. The relationship between the collection of averaged data points from every averaging block and at all times (Days 5–21) will then approximately mimic the impact of roots at the block scale on σ_{bulk} , compared with Archie's law applied in soils only ($\sigma_{bulk\text{-soil}}$). We also investigated the relationship between the effective properties (σ_{effz} and σ_{effx}) and volume-averaged (at the rhizotron scale) water content at different times.

Relative Change in Effective Conductivity Caused by Root Segments

The computation of σ_{eff} (σ_{effz} and σ_{effx}) and σ_{abmn} was repeated for two scenarios: (i) a medium with the soil and root system included and (ii) a medium with only the soil, as if the roots had the same σ than the surrounding soil. The difference in σ_{eff} between the root and soil indicates the specific impact of root segments on the electrical measurements. Similarly, the difference in σ_{abmn} between the root and soil indicates the specific impact of root segments on ERT measurements made by point electrodes at the surface rather than the effective properties.

We define a parameter describing the relative change in σ_{eff} caused by the presence of root segments ($\delta\sigma_{eff-rs}$), which is given by

$$\delta \sigma_{\text{eff-rs}} = \left| \frac{\sigma_{\text{eff-root}} - \sigma_{\text{eff-soil}}}{\sigma_{\text{eff-soil}}} \right|$$
 [9]

where $\sigma_{\text{eff-root}}$ is the σ_{eff} of the medium with both roots and soil and $\sigma_{\text{eff-soil}}$ is the σ_{eff} of the medium with soil only.

Similarly, the relative change in σ_{abmn} computed by point electrodes caused by the presence of root segments is given by

$$\delta \sigma_{\text{abmn-rs}} = \begin{vmatrix} \sigma_{\text{abmn-root}} - \sigma_{\text{abmn-soil}} \\ \sigma_{\text{abmn-soil}} \end{vmatrix}$$
 [10]

where $\sigma_{\rm abmn\text{-}root}$ is the $\sigma_{\rm abmn}$ of the medium with both roots and soil and $\sigma_{\rm abmn\text{-}soil}$ is the $\sigma_{\rm abmn}$ of the medium with soil only.

We investigated the relative change in σ_{eff} at different root ages and with varying soil types (soil and loam; see Table 1). Furthermore, the relative change in σ_{eff} averaged across two perpendicular directions $(\langle \delta \sigma_{eff-rs} \rangle)$ and $\delta \sigma_{abmn-rs}$ are used as the parameters to assess the impact of roots in the following. We refer to $\langle \delta \sigma_{eff-rs} \rangle$ and $\delta \sigma_{abmn-rs}$ as the roots' electrical signature term. We also define a term describing the contrast in σ between σ_{root} and $\sigma_{bulk-soil}$, computed by subtracting the mean of $\sigma_{bulk-soil}$ from the mean of σ_{root} . Here, σ contrast is a single number that is a function of root age and soil type.

Scenario Analysis

We used the simulated synthetic data to achieve the objectives of this study, namely to find simulation-based answers to the question of how root length density, root volume density, root age, and root radius relate to the root electrical signature terms. To answer this question, we assessed the dependence of $\langle \delta \sigma_{eff-rs} \rangle$ for each of the unique cases that corresponded to different root variables such as length, age, volume, surface area, σ contrast, and radius. We investigate the dependence among these variables via correlation and principal component analysis.

Results Bulk Electrical Conductivity as a Function of Time and Soil Type

Simulations showed that the water saturation distribution patterns depended on the soil type (Fig. 7a and 7b). In loam, the normalized water saturation never dropped below 0.2, even on Day 21, whereas in sand, it reached almost zero (0.00034) on Day 21. The same day, when the water depletion reached its greatest, the maximum water saturation values were 0.4 in sand and 0.6 in loam.

In sand, σ_{root} was always larger than $\sigma_{bulk\text{-soil}}$ (Fig. 7c). For loam, however, the contrast changed with time (Fig. 7d). Initially, in loam, $\sigma_{bulk\text{-soil}}$ was larger than σ_{root} ; at intermediate times (Days 10, 12, and 15) at the top of the rhizotron, $\sigma_{bulk\text{-soil}}$ was equal to σ_{root} , and at the bottom of the rhizotron, $\sigma_{bulk\text{-soil}}$ was larger than σ_{root} . At the end (Days 18 and 21), in some regions $\sigma_{bulk\text{-soil}}$ was less than σ_{root} . On Day 21, $\sigma_{bulk\text{-soil}}$ varied from 0.0001 to 0.0087 S m $^{-1}$ in sand and from 0.0057 to 0.0407 S m $^{-1}$ in loam.

Impact of Roots on Pedophysical Relationships

The harmonic and arithmetic blockwise averaged σ data points and their corresponding water content at various times are shown as vertical bars in Fig. 8a and 8b, along with Archie's

pedophysical relationship. The upper limit of the vertical bar represents the maximum of the blockwise-computed arithmetic and harmonic averages of σ ; the lower limit represents their minimum. For each block (4 cm³), the actual effective small-scale (centimeter-scale) σ is supposed to be located within this range.

At a larger rhizotron spatial scale, we illustrate the relationship between $\sigma_{\rm effz}$ or $\sigma_{\rm effx}$ and the volume-averaged water content at various times in Fig. 8a and 8b. Both the effective properties at rhizotron scale and the averaged properties at small block scale deviated from Archie's curve, and the deviation trends were different, as seen in Fig. 8a and 8b. In addition, the difference between the horizontal and vertical effective properties $\sigma_{\rm eff_x}$ and $\sigma_{\rm eff_z}$ indicate the macroscale anisotropy. For both soil types, the derived effective properties σ_{eff_x} and σ_{eff_z} lay below Archie's curve defined at a lower scale because the dry soil acted as a barrier to the electrical current flow, thus decreasing the effective $\boldsymbol{\sigma}_{\text{bulk}}.$ The vertical effective property deviated more than that of the horizontal direction because of horizontal layering developing in the σ distribution as a result of root water uptake (Fig. 8a and 8b). Current was therefore affected more in the vertical direction than in the horizontal direction. For the loam medium, the anisotropic effect was less than that of the sand. In fact, ERT-obtained σ data are known to have a spread around the pedophysical model fitted curve, as observed by Beff et al. (2013) and Garré et al. (2011). Our averaging results in Fig. 8a and 8b hint that this deviation in the σ data around the pedophysical model could be caused by the presence of root segments.

In Fig. 8c and 8d, we show the deviations of σ_{effz} from Archie's curve in sand and loam for three different scenarios:

1. Root water uptake with root segments: Here, we have Fig. 8c and 8d as the forward σ map.

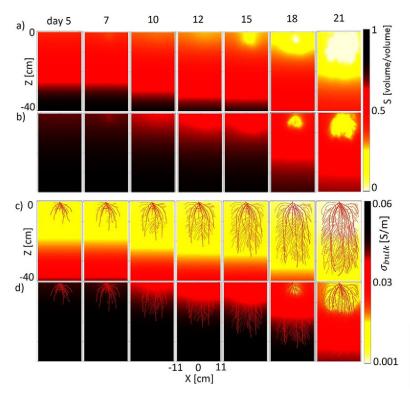


Fig. 7. Volumetric water saturation (S) distribution in (a) sand and (b) loam and its corresponding electrical conductivity (σ_{bulk}) maps in (c) sand and (d) loam in the Y=0 plane at different times.

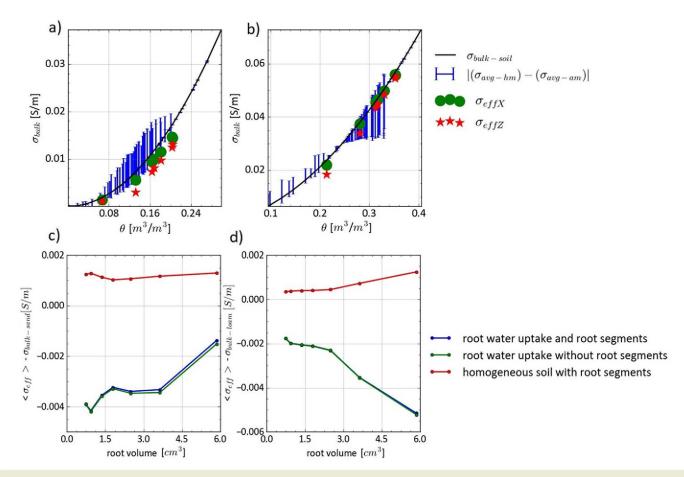


Fig. 8. (a,b) Comparison of Archie's law $(\sigma_{bulk\text{-}soil})$ with blockwise-averaged electrical conductivity $(\langle \theta \rangle)$ vs. blockwise-computed arithmetic average of electrical conductivity $(\langle \sigma_{avg\text{-}hm} \rangle)$, blockwise-computed harmonic average of electrical conductivity $(\langle \sigma_{avg\text{-}am} \rangle)$, and rhizotron-scale effective electrical conductivity in two perpendicular directions $(\sigma_{effv}$ and $\sigma_{effz})$ in (a) sand and (b) loam. The error bar represents the Wiener bound values or the range of variation between $\sigma_{avg\text{-}am}$ and $\sigma_{avg\text{-}hm}$. The water content corresponding to σ_{effz} were obtained by taking the volumetric average of the entire rhizotron. (c,d) Deviation of σ_{effz} from $\sigma_{bulk\text{-}soil}$ as a function of root volume for three different scenarios in (c) sand and (d) loam.

- 2. Root water uptake without root segments: For this scenario, in Fig. 8c and 8d, we removed the root-specific electrical properties and assumed that the roots have the same σ as the surrounding soil but retain the root water uptake pattern in the forward σ map.
- 3. Homogeneous soil with root segments: For this case, we removed the pattern of $\sigma_{bulk\text{-soil}}$ associated with water uptake by roots in Fig. 8c and 8d and replaced it with its spatial average (homogeneous soil). The root-specific electrical properties were retained.

As the $\sigma_{\rm root}$ values are generally higher than those of the dry soil, we see that the deviation is positive for the homogeneous scenario (red lines in Fig. 8c and 8d), whereas with root water uptake, the deviation is negative.

We find that the impact of root water uptake was slightly bigger than that of $\sigma_{\rm root}$ only (the green and red lines, respectively, in Fig. 8c and 8d). However, the additional impact of roots when water uptake was considered was negligible (blue line), demonstrating that root water uptake patterns were the main driver of these deviations. The presence of roots inside the depletion zone only marginally affected the electrical signature.

At small scales, removing root segments results in perfect agreement between blockwise averaged data and Archie's curve (data not shown), as the difference between the two averages in Fig. 8a and 8b was caused only by root segments. This is because at block scale, there is no significant water content heterogeneity present and thus the average water content and average σ (without roots) follow Archie's curve. At large scales, though, the patterns generated by water uptake were more nonlinear and the average water content no longer related to the effective properties dictated by Archie's pedophysical relationship. This illustrates how the relationship between θ and $\sigma_{\rm bulk}$ is scale dependent.

Roots' Electrical Signature

In Fig. 9, we compare $\langle \delta \sigma_{eff-rs} \rangle$ and $\delta \sigma_{abmn-rs}$ with the root/soil volume ratio as a percentage. They show a very high correlation both in sand and loam (r > 0.8). In general, the impact of roots in sand was greater than in loam, as seen by its higher slope. In Fig. 10, we examine the correlation of $\langle \delta \sigma_{eff-rs} \rangle$ with several root segment properties such as radius, surface area, volume, age, and soil–root electrical contrast. The root electrical signature terms depend more strongly on electrical contrast than on other

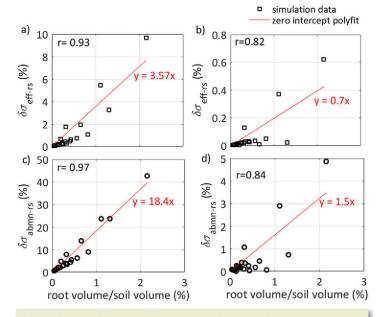


Fig. 9. Relative change in effective conductivity resulting in root segments compared with soil only $(\langle \delta \sigma_{eff-rs} \rangle)$ vs. root volume/soil volume ratio (black squares) in (a) sand and (b) loam. Relative change in apparent conductivity from root segments compared with soil only $(\delta \sigma_{abmn-rs})$ vs. the root volume/soil volume ratio (black squares) in (c) sand and (d) loam. The red line represents the zero-intercept-constrained polynomial fit.

parameters for the root water uptake case. By visual inspection of Fig. 10, we find that age and length varies with $\langle \delta \sigma_{eff-rs} \rangle$ in a similar fashion, whereas surface and volume form another group. The electrical contrast is an independent variable affecting the $\langle \delta \sigma_{eff-rs} \rangle$. Correlation analyses indicate that root surface area and electrical contrast are the two main drivers of the electrical signatures of root systems in soils.

The results of principal component analysis (Fig. 11) confirmed the multivariate dependence among different variables relating to root geometrical and electrical properties. The principal component analysis revealed that the first three principal components explained about 92% of the variability (Fig. 11). Principal Component 1, with 58% of the total variance, captured the variability of root system size (volume, surface, radius, and age), which correlated with electrical contrast and the electrical signature. In other words, large root systems tend to increase their electrical signature.

Principal Component 2 separated the various drivers of variability into three groups. Age and length, which represent the extent of the root system, formed Group 1 and were negatively correlated with $\langle \delta \sigma_{eff-rs} \rangle$. Radius made up Group 2 and was weakly correlated with $\langle \delta \sigma_{eff-rs} \rangle$. Volume and surface, which represent a combination of extension and thickness, formed Group 3 and correlated with $\langle \delta \sigma_{eff-rs} \rangle$. Principal Component 3 captures a small part of the variation, where contrast and $\langle \delta \sigma_{eff-rs} \rangle$ are correlated and are independent of root system size.

Model Limitations

Here, we discuss the limitations of our modeling approach. First, we consider the limitations for the scenario where the process-based model described here is extended to model a real experiment. In agricultural fields as well as in the two-dimensional rhizotron, air-filled cracks can manifest in the soil, potentially influencing ERT measurements that our model does not account for; however, these could easily be integrated into the model. For future validation of the modeling results presented here in a real experiment, limitations in ERT such as bad electrode contact and other artifacts such as soil cracks can be combated through repeated measurements and adjustments during the course of the experiment, which are simpler to implement in a rhizotron experiment than in the field (Huck and Taylor, 1982).

Our model did not consider specific rhizosphere processes such as root exudation, which could also affect the water content estimates. In the model, we assumed that salt did not accumulate near the roots but assumed passive solute uptake only with no active uptake, exclusion, or exudation. Although this has been observed experimentally under field conditions by Beff et al. (2013) and corresponds to a situation where the nutrient solution exactly fits the plants' needs, the assumption is not necessarily always valid. Significant solute gradients may arise around roots through the processes mentioned above. If they were to occur, the forward conductivity map and hence the water content estimates could be impacted by such gradients.

In addition, roots can swell and shrink, causing air gaps that change spatially and temporally between soil and roots under field conditions (Carminati et al., 2009). Studies have found that maize roots in sandy loam have a root–soil contact surface of 40 to 60%

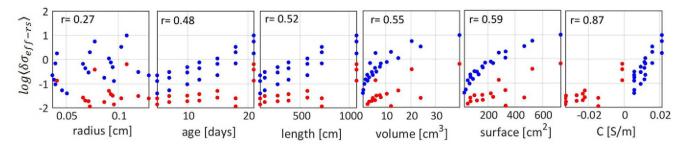


Fig. 10. Correlation plots of different root variables: radius, age, volume, surface area, length, and electrical conductivity contrast between root and soil (C), calculated as mean root electrical conductivity (σ_{root}) – mean Archie's law $(\sigma_{\text{bulk-soil}})$ with the \log_{10} of the root electrical signature. Red dots are loam medium, blue dots are sand; r is the Pearson correlation coefficient calculated for combined sand and loam data.

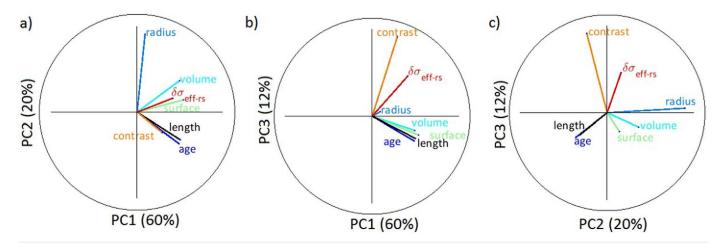


Fig. 11. Principal component (PC) analysis of different root variables: (a) PC1 vs. PC2 decomposition, (b) PC1 vs. PC3 decomposition, and (c) PC2 vs. PC3 decomposition. The percentage values in the parentheses indicate the data variance explained by each PC. The circles have a unit radius going from –1 to 1 on both axes.

(Kooistra et al., 1992; Schmidt et al., 2012). These gaps could strongly influence the electrical signature by causing macroscopic anisotropy. Therefore, the inclusion of gap dynamics should be explored in future modeling studies. Finally, we also ignored the anisotropy of σ inside the root structure (stele–cortex variations), which may have a considerable effect on ERT measurements. Such structural variations may induce an even higher degree of anisotropy in electrical measurements.

Discussion

The modeling work described here is one of the first attempts to understand the impact of roots on ERT data by including processes such as root water uptake. Because of the nature of ERT inversion, a deviation in the forward data, as quantified here, could be amplified in the final inversion results. Thus it is important to be aware of errors in water content estimates that can be caused by root segments. Hence, this model can serve as a tool to quantify errors in ERT-obtained water content estimates arising from the presence of root segments. It can also be used to optimize ERT measurement schemes for maximizing or minimizing root sensitivity to different root architectures and to shed light on whether ERT data provide information on root phenotyping and, if so, what can be done to maximize this information. In addition, this modeling work could also benefit the development of bio-pedophysical relationships in rooted soil that take the morphological features of roots and their electrical properties into account. Such bio-pedophysical models would minimize the error in θ in cropped fields as estimated by the ERT method. Our next step is to validate our model with a real rhizotron experiment.

Conclusions

We used a combination of ERT and plant water flow models to study the impact of root segments on ERT measurements. We

illustrated the model's potential by simulating a growing and transpiring maize root system in a 3D rhizotron and forward ERT measurements.

Analysis of the σ distributions generated by simulated root water uptake and root system architecture showed a scale- and soil-dependent impact on the apparent pedophysical relationships. Upscaling the σ data (through averaging) showed a deviation or spread around Archie's curve with an uncertainty of approximately 0.01 S m⁻¹ (at its peak) for a given water content (Fig. 8 and 8b). This deviation was caused by the presence of root segments. It is worth noting that an uncertainty in the pedophysical relation of \sim 0.01 S m⁻¹ has been observed in some field ERT studies (Garré et al., 2011; Beff et al., 2013). In addition to measurement errors under field conditions, our model shows that the presence of root segments might be an additional reason why ERT-obtained pedophysical data sometimes have an uncertain spread around Archie's curve.

The difference between σ_{effz} and σ_{effz} in Fig. 8a indicates macroscale anisotropy in the soil–root system. There are studies that show that electrical anisotropy could be used as a parameter to monitor soil–root systems (Furman et al., 2013; Rao et al., 2018, 2019). The feasibility of using electrical anisotropy at the field or pot scale for root phenotyping remains to be explored in a future study. Our model helps in predicting and quantifying the electrical anisotropy.

The forward ERT modeling results showed that the evolution of apparent conductivity measurements depended on root growth. The root electrical signature term in effective electrical conductivity $\langle \delta \sigma_{\text{eff-rs}} \rangle$, which is the relative change in effective conductivity caused by the presence of roots, ranged from as low as 0.1% to as high as 10% in sand; in loam, it ranged from 0.02 to 0.6% (negligible). For every 1% increase in the root/soil volume ratio, the uncertainty in σ_{eff} was 4.5% in sand and 0.2% in loam (negligible) (Fig. 9a and 9b). For surface electrode measurements, this uncertainty was 18% in sand and 1.5% in loam (Fig. 9c and 9d).

Correlation analysis between root electrical signature terms and roots' geometrical properties and soil–root σ contrasts suggested that the impact of roots on electrical measurements has multivariate dependency (Fig. 10). We cannot solely attribute the roots' impact on bulk electrical properties to root mass density or root length density, but they somehow affect the results in combination. However, the most important factors influencing the electrical signature were the soil–root electrical contrast, which showed a very high correlation of 0.89, and root surface area ($r \sim 0.6$); the root radius showed the lowest correlation. The principal component analysis biplots in Fig. 11 revealed that length and age were always correlated, as well as surface and volume, demonstrating similar information content.

Supplemental Material

The supplemental material includes the data used to generate Fig. 9. 10, and 11.

Author Contributions

SR developed the theory formalism, performed the calculations and the numerical simulations and took the leading role in writing the manuscript. FM helped in R-SWMS parameterization of the maize roots. SE conducted the experiments on maize roots to measure their electrical properties and helped to generate Fig. 4. NL helped in running the EIDORS software. AK suggested the idea of computing the effective properties with line electrodes. FN, SG, and MJ conceived the original idea and supervised the project. All authors provided critical feedback and helped shape the research, analysis, and manuscript.

Conflict of Interest Disclosure

The authors declare that there is no conflict of interest.

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