PCCP



View Article Online PAPER



Cite this: Phys. Chem. Chem. Phys., 2019, 21, 26525

Size effects on rotational particle diffusion in complex fluids as probed by Magnetic Particle Nanorheology†

Melissa Hess, (1) ab Eric Roeben, a Patricia Rochels, a Markus Zylla, a Samira Webers, c Heiko Wende^c and Annette M. Schmidt 10 *2

Rheological approaches based on micro- or nanoscopic probe objects are of interest due to the low volume requirement, the option of spatially resolved probing, and the minimal-invasive nature often connected to such probes. For the study of microstructured systems or biological environments, such methods show potential for investigating the local, size-dependent diffusivity and particle-matrix interactions. For the latter, the relative length scale of the used probes compared to the size of the structural units of the matrix becomes relevant. In this study, a rotational-dynamic approach based on Magnetic Particle Nanorheology (MPN) is used to extract size- and frequency-dependent nanorheological properties by using an otherwise well-established polymer model system. We use magnetically blocked CoFe₂O₄ nanoparticles as tracers and systematically vary their hydrodynamic size by coating them with a silica shell. On the polymer side, we employ aqueous solutions of poly(ethylene glycol) (PEG) by varying molar mass M and volume fraction ϕ . The complex Brownian relaxation behavior of the tracer particles in solutions of systematically varied composition is investigated by means of AC susceptometry (ACS), and the results provide access to frequency dependent rheological properties. The sizedependent particle diffusivity is evaluated based on theoretical descriptions and macroscopic measurements. The results allow the classification of the investigated compositions into three regimes, taking into account the probe particle size and the length scales of the polymer solution. While a fuzzy cross-over is indicated between the well-known macroscopic behavior and structurally dominated spectra, where the hydrodynamic radius is equal to the radius of gyration of the polymer $(r_h \sim R_0)$, the frequency-related scaling behavior is dominated by the correlation length ξ respectively by the tube diameter a in entangled solutions for $r_h < R_a$.

Received 21st July 2019, Accepted 11th October 2019

DOI: 10.1039/c9cp04083h

rsc.li/pccp

Introduction

In many soft materials, ranging from living tissue to commercially filled polymers, the interaction of nanosized structural units with their direct environment plays a crucial role for the system performance or functionality. Examples of relevance include car tires, 1,2 materials for soft robotics 3,4 and also the distribution of medication in living biological systems.5-7

While steadily more complex and smart materials are under investigation, skillful analytical approaches are required to fully characterize such samples with respect to their structure and dynamics. Yet, the idea to exploit microscopic objects as tools for the rheological characterization of the matrix goes back already to the pioneers Heilbronn⁸ (1922), and Freundlich and Seifriz⁹ (1923). During the last decades, microrheology has developed into an extensively used methodology for the characterization of soft and complex materials. 10-17

Microrheology opens up the access to how viscoelastic materials flow as a function of length scale.¹³ The motion of micrometer sized spheres, either of passive thermal origin or actively driven by an external force (e.g. electric or magnetic field), is tracked and analyzed. Here, the generalized Stokes-Einstein equation relates the diffusivity of the particles' motion to the viscoelastic properties of the sample. 12,13,18 Besides the low amount of sample volume, microrheology benefits from a low degree of invasion to the sample and access to a wide frequency range, as well as the detection of local inhomogeneities. 12,13,15,19,20

^a Institute of Physical Chemistry, Chemistry Department, Faculty of Mathematics and Natural Sciences, University of Cologne, Luxemburger Str. 116, D-50939 Köln, Germany. E-mail: annette.schmidt@uni-koeln.de

^b Institute for Complex Systems, IHRS BioSoft, Forschungszentrum Jülich GmbH, D-52428 Jülich, Germany

^c Faculty of Physics and Center for Nanointegration Duisburg-Essen (CENIDE), University of Duisburg-Essen, Lotharstraße 1, D-47057 Duisburg, Germany

[†] Electronic supplementary information (ESI) available. See DOI: 10.1039/c9cp04083h

Since microscopic probing relates the material mechanical characteristics to its microstructure, there is increased interest in decreasing the probe size to the size of the characteristic length scales within the material. Stringent deviations from the rheological performance, as obtained by conventional methods, are expected and experimentally observed.^{21,22}

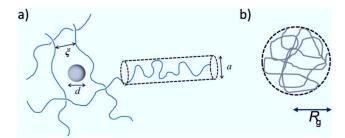
In particular, in polymer-based fluids and soft solids (*e.g.* gels, melts or solutions), specific characteristic length scales (*e.g.* mesh size m, radius of gyration $R_{\rm g}$, tube diameter a or correlation length ξ) are present. By relating the probe particle size to the size of the characteristic length scales of the material, certain regimes connected to characteristic length-and time scales can be identified, yet their interpretation is still the subject of investigation.

For a nanoscopic tracer particle in a polymer solution, the effective viscosity η responsible for the diffusion of the tracer depends on the ratio of particle size d to the correlation length ξ , as already postulated by De Gennes.²³ When the polymer chains begin to overlap, the polymer solution can be described as a transient network with the correlation length ξ defined as the average distance between the two adjacent contact points between the chains. On this basis, Rubinstein and his coworkers classified the tracer behavior into regimes according to their size with respect to the characteristic length scales. 24,25 'Small' tracers have a radius or diameter that is smaller than the correlation length, and their translational diffusion is mainly determined by the solvent viscosity η_S . In contrast, the diffusion of 'large' particles (meaning larger than the tube diameter a) reaches the (quasi-)continuous case for long observation times. Here the tube diameter a is related to the topological confinement of a polymer chain by surrounding chains to a tube-like region.²⁴ For 'intermediate' particle sizes, we expect at long lime scales that diffusion related to an effective viscosity $\eta_{\rm eff}$ occurs. This effective viscosity is lower than the one experienced for a macroscopic object.²⁵ Based on scaling approaches for polymer solutions, further prediction of the frequency-dependent behavior is also available.

In other studies, the impact of the radius of gyration $R_{\rm g}$ is addressed by molecular dynamics simulation, and it is found that the classical Stokes–Einstein relation fails if the particle size is below the radius of gyration $R_{\rm g}$ of the polymer. The radius of gyration $R_{\rm g}$ is defined *via* the mean square distance of the building blocks to the center of gravity of the molecule. A schematic drawing of the important length scales in polymer solutions is provided in Scheme 1.

The influence of the relation of probe size to characteristic length scales in polymer solutions and a correlated breakdown of the Stokes–Einstein equation are focused in several scientific studies. 13,21,22,28,29 The role of $R_{\rm g}$ as a cross-over quantity for the tracer size is obvious from the majority of studies. The nature of the underlying scaling quantity, however, to date is not fully clear.

In this study, we systematically investigate the rotational dynamics of magnetic nanoparticles using the method of Magnetic Particle Nanorheology (MPN)^{30–32} in a series of model polymer solutions of different molar masses and concentrations, with the aim to better understand specific size-dependent



Scheme 1 Schematic drawing of (a) correlation length ξ , imaginary tube diameter a and particle size d and (b) radius of gyration $R_{\rm q}$.

particle-matrix interactions, and to explore the impact of the probe size in relation to the characteristic length scales of the matrix.

As polymer model systems, we employ aqueous solutions of linear poly(ethylene glycol) (PEG) by varying molar mass $M_{\rm n}$ and volume fraction ϕ . In order to obtain a systematic variation of the tracer size, we use magnetically blocked CoFe₂O₄ (CF) nanoparticles that are coated with a silica (SiO₂) shell. We use AC susceptometry (ACS) in order to obtain information on the rotational (Brownian) relaxation process of the tracer particles in the complex fluid environment of the solutions. By comparing with a theoretical scaling model²³ we obtain semiquantitative access to frequency-dependent rheological properties, among these the frequency dependent viscosity η^* , loss modulus G'' and diffusion properties, with an emphasis on the size-dependent particle diffusion.

Materials and methods

Fe(acac)₃, dibenzyl ether and oleyl alcohol were obtained from ABCR. Oleyl amine, tetraethyl orthosilicate (TEOS) and water (pure, demineralized) were received from Acros Organics. Sodium hydroxide (0.1 M) and oleic acid were purchased from Fisher Scientific. Technical ethanol was received from Hofmann. Poly(ethylene glycol)s (PEGs), Co(acac)₂ and poly(acrylic acid) (PAA, $M_{\rm W}$ = 1800 g mol⁻¹) were obtained from Sigma Aldrich.

Synthesis and coating of nanoparticles

All probe particles employed in this study are based on the same batch of $CoFe_2O_4$ nanoparticles as a core. The $CoFe_2O_4$ particles are synthesized by thermal decomposition of $Fe(acac)_3$ and $Co(acac)_2$ and four subsequent growth steps according to protocols from the literature. $^{30-33}$ Dibenzyl ether is used as a solvent and oleic acid, oleyl amine and oleyl alcohol are added as stabilizers. The spherical magnetic cores are electrostatically stabilized using poly(acrylic acid) (PAA) in water.

For a variation in the diameter of the probe particles, the identical magnetic cores are coated with a silica shell. Therefore, magnetic cobalt ferrite particles in water are diluted to obtain a solution with 1×10^{-5} m% CF particles and 95 v% ethanol. The solution is treated in an ultrasonic bath for a few minutes. Ammonium hydroxide solution (with a total ammonium hydroxide concentration for the different particle batches of 0.08 mmol mL⁻¹,

PCCP

 $0.12 \text{ mmol mL}^{-1}$, $0.25 \text{ mmol mL}^{-1}$ and $0.26 \text{ mmol mL}^{-1}$) is added, and the reaction vial is placed on a shaking plate.

Tetraethyl orthosilicate (TEOS, 0.09 mmol mg⁻¹ CF) diluted in ethanol (0.09 mmol $\mathrm{mL^{-1}}$ EtOH) is added dropwise within 2 hours to the shaking reaction mixture at a rate of 5.0 mL h⁻¹. Subsequently, the CF particles are shaken for an additional 19 hours at room temperature. The reaction mixture is centrifuged at 6500 rpm for 40 min, washed three times with ethanol and twice with water, and finally dispersed in water. In the following, the magnetic cores are labeled as CF x, while silica coated particles are labelled as $CF@SiO_2_x$, with x representing the hydrodynamic diameter of the respective particles in water, as obtained by ACS.

Sample preparation

For the nanorheological measurements by means of AC susceptometry, the polymer component as summarized in Table 1 is mixed with water and dissolved overnight on a shaking plate. The aqueous-dispersed probe particles are freshly treated in an ultrasonic bath before addition to the respective PEG aqueous solution to reach a final volume fraction of the magnetic core of 7.2×10^{-5} . This corresponds to a total volume fraction of probe particles of 1.1×10^{-3} for CF@SiO₂_25 particles, and of 3.5×10^{-3} for CF@SiO₂_29 particles. The polymer systems are labelled as Pyk $_{\phi}$ with y indicating the molar mass of the polymer in units of 1000 g mol $^{-1}$, and ϕ the volume fraction.

Methods

AC susceptometry (ACS) and Magnetic Particle Nanorheology (MPN)

ACS experiments are performed at room temperature using a DynoMag Imego device with a magnetic field amplitude H_0 up to 0.4 kA m⁻¹ in the frequency range between 1 Hz-250 kHz. For low frequency measurements between 0.01 Hz-1500 Hz, a Quantum Design MPMS-5S SQUID magnetometer with an implemented AC option using an applied magnetic AC amplitude H_0 of 0.3 kA m⁻¹ at 300 K is used.

A direct connection between the rotational diffusion 12,22,32 of the magnetically blocked probe particles, as extracted from the phase lag between excitation and response, and the rheological properties of the matrix is provided by the generalized Stokes-Einstein relation for rotation (eqn (1)).

$$D_{\rm r}^* = \frac{1}{\tau_{\rm B}} = \frac{k_{\rm B}T}{8\pi\eta_0^* r_{\rm h}^3} \tag{1}$$

Here, D_r^* denotes the generalized rotational diffusion coefficient, τ_B is the Brownian relaxation time, k_B is the Boltzmann

Table 1 Specifications (M_n : number-average molar mass of the polymer; $M_{\rm W}$: mass-average molar mass of the polymer; PDI: polydispersity index) of the investigated polymers

PEG	$M_{\rm n} \left[{ m g \ mol}^{-1} ight]$	$M_{ m w} \left[{ m g \ mol}^{-1} ight]$	PDI
P4k	4245	4308	1.01
P20k	19 560	20 810	1.06
P35k	31 870	33 100	1.04

constant, T is the temperature, η_0^* is the generalized zero shear viscosity of the matrix and r_h is the hydrodynamic radius of the particles. As introduced in our previous studies, 30-32 extraction of frequency-dependent nanorheological properties from the susceptometry data is possible by the transfer of the Gemant-DiMarzio-Bishop (GDB)³⁴ model to the magnetic case. Accordingly, the storage $G'(\omega)$ and the loss modulus $G''(\omega)$ as well as the real part of the viscosity $\eta'(\omega)$ are obtained from the AC susceptometry results using eqn (2)–(4).

$$G'(\omega) = \frac{\frac{\chi'_{N}(\omega)}{\left(\chi'_{N}(\omega)^{2} + \chi''_{N}(\omega)^{2}\right)} - 1}{K}$$
 (2)

$$G''(\omega) = \frac{\chi_{N}''(\omega)}{K\left(\chi_{N}'(\omega)^{2} + \chi_{N}''(\omega)^{2}\right)}$$
(3)

$$\eta'(\omega) = \frac{G''(\omega)}{\omega} \tag{4}$$

Here, K is a geometry factor, χ_N' is the normalized real part and χ_N'' is the normalized imaginary part of the susceptibility under consideration of subtraction of the minor Néel signal contribution to χ' at high frequencies.

Dynamic light scattering (DLS)

Information on the translational diffusion coefficient and the hydrodynamic parameter of the particles is obtained using a High Performance Particle Sizer (HPPS, Malvern Instruments, laser 633 nm, angle 173°). All measurements are performed at 25 °C in water in polystyrene cuvettes. The particle diameter distribution is averaged from five measurements. The measurements are evaluated using a Non-Negative Least-Squares (NNLS) algorithm.

Infrared (IR) spectroscopy

A Shimadzu IRAffinity-1 FTIR Spectrometer with an ATR (Attenuated Total Reflectance) setup is used. The measurement range is 4500-600 cm⁻¹.

Rheology

The macrorheological measurements are carried out using an AR-G2 rheometer (TA Instruments) at 25 °C. The measuring geometry is based on either a plate-plate system with a diameter of 40 mm or a concentric cylinder. Amplitude sweeps are carried out in the strain range of 0.1-10% at 1 Hz, and frequency sweeps in the linear-viscoelastic range of 1.592×10^{-2} Hz-100 Hz at 1.5% strain.

Transmission electron microscopy (TEM)

The electron microscopy images are taken using a Zeiss LEO 912. For this, the respective sample is drop-cast to a coppercoated carbon grid and left for slow evaporation. The instrument is equipped with a 120 kV LaB₆ cathode and a Moorweis Slow Scan with a CCD camera Sharp:Eye 2048 \times 2048 TRS.

Vibrating sample magnetometry (VSM)

The magnetization measurements of liquid or dried samples are performed using an ADE Magnetics EV7 Vibrating Sample Magnetometer at room temperature. The sample is placed in a Teflon vessel and immobilized on a glass sample holder. A GMW electromagnet 3472-70 with a maximum field strength of 1.6 \times 10⁶ A m⁻¹ and a vibrator with a frequency of 75 Hz are used.

ζ potential measurements

A Zetasizer Nano ZS (Malvern Instruments, $\lambda = 633$ nm) is used to measure the ζ potential. The measurements are performed in polystyrene capillary cuvettes. The pH value is adjusted with 0.1 M HCl and 0.1 M NaOH solutions.

Results

In this work, we investigate the size-dependent rotational diffusivity of well-defined nanoscopic magnetic tracer particles in aqueous polymer solutions using Magnetic Particle Nanorheology (MPN). Focusing on size effects concerning the particle size related to the characteristic length scales in the respective polymer, we employ magnetically blocked, CoFe₂O₄-based tracer particles with a diamagnetic SiO₂ shell of variable thickness. The tracer particles are spherical in shape, possess a narrow size distribution, exhibit excellent dispersion stability in water at a broad range of pH and ionic strength, and are predominantly magnetically blocked, so that the preferred relaxation process is Brown relaxation. The size-dependent nanorheological properties of aqueous poly(ethylene glycol) solutions in a broad range of molar mass and volume fraction are investigated, and the results are compared to the outcomes of recent theoretical and experimental methods.

1. Description and characterization of the tracer particles and the investigated system

1.1 Choice of probe particles: synthesis and coating. Our strategy to obtain spherical, magnetically blocked tracer particles with comparable magnetic properties, but variable hydrodynamic sizes is based on core-shell nanoparticles with a cobalt ferrite (CF) core and a silica (SiO₂) shell. For the ACS experiments, we employed tracer particles that are based on the same batch of CF cores, obtained by a cyclic growth process by a controlled thermal decomposition procedure of Co(II) and Fe(III) acetylacetonates (four growth steps).^{30,33} The obtained CF cores show a geometric radius r_g of 8.2 nm and a lognormal, narrow size distribution (σ = 0.13). The hydrodynamic radius as obtained from ACS is $r_{\rm h,ACS}$ = 11.6 nm (σ = 0.13, CF_12) resulting from fitting a single Debye relaxation process with lognormal distribution of the particle size.

The core particles are subsequently individually coated with a SiO₂ shell using a modified Stöber process.^{35,36} A variation of the shell thickness is achieved by increasing the particle size through an increase of the base concentration during the synthesis. The TEM images of the resulting particles (Fig. 1)

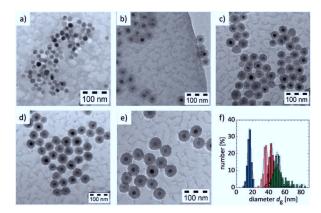


Fig. 1 TEM images of tracer particles of the same magnetic core size and varying SiO₂ shell thickness (a) CF_12, (b) CF@SiO₂_25, (c) CF@SiO₂_29, (d) CF@SiO₂_37 and (e) CF@SiO₂_42. (f) Histograms of the geometrical diameter d_q with the corresponding lognormal function for the different probe particles (CF_12 (blue); CF@SiO2_25 (orange); CF@SiO2_29 (red); CF@SiO₂_37 (light cyan); CF@SiO₂_42 (green)).

show mainly single coated particles with only one magnetic core. The corresponding particle sizes as obtained by different methods are listed in Table 2. The results confirm that the shell thickness of the tracer particles increases with the base concentration, and that the size distribution of the tracers remains low.

In addition to the basic architecture of the tracers, it is important to collect relevant information on their surface properties, their hydrodynamic behavior and their magnetic properties.

The surface properties of the tracers are analyzed by attenuated total reflection infrared (ATR-FT IR) spectroscopy (see Fig. S1, ESI†). For SiO₂-coated particles, dominant Si-O-Si stretching modes are found. All particles are negatively charged on the surface at pH 6 (the pH of the investigated polymer solutions is 6-7) with deprotonated acid groups on the magnetic cores, which are stabilized with polyacrylic acid, and deprotonated hydroxy groups on the surface of the silica particles. The ζ potential is shown for a wide pH range for the magnetic cores and exemplarily at pH 6 for the silica particles used for the measurements in Fig. S2 (ESI†). All batches show at pH 6 a ζ potential of approximately 50 mV in water which ensures good stability of the particles in aqueous solutions at that pH.

The hydrodynamic properties of the tracers are investigated independently based on the translational and rotational diffusion of the particles. Dynamic light scattering (DLS) is used to determine the number- and volume-averaged hydrodynamic radius $r_{\rm h,DLS}$ of the particles (see Table 2) based on translational diffusion. Accordingly, the hydrodynamic radii are slightly larger than $r_{\rm g}$ as expected, representing the impact of the solvation shell and confirming that mainly single-dispersed particles are present.

The quasi-static magnetic properties of the samples are analyzed by vibrating sample magnetometry (VSM) measurements in the dried state as well as in aqueous solution and are shown in Fig. 2 and Table 3.

Table 2 Summary of geometrical particle radius r_q and lognormal standard deviation σ determined by TEM, number $(r_{n,D,LS})$ and volume $(r_{v,D,LS})$ weighted hydrodynamic radius determined by DLS and hydrodynamic radius $r_{\text{h.ACS}}$, the Brownian relaxation time of the particles τ_{Brown} and lognormal σ determined by AC susceptometry measurements for different probe particles

Sample	TEM		DLS		ACS		
	$r_{\rm g} [{ m nm}]$	σ	$r_{ m n,DLS}$ [nm]	$r_{ m v,DLS}$ [nm]	$r_{ m h,ACS}$ [nm]	σ	τ_{Brown} [s]
CF_12	8.2	0.13	10.7	13.3	11.6	0.31	4.3×10^{-6}
CF@SiO ₂ _25	18.3	0.07	25.6	28.2	24.8	0.24	$4.2 imes 10^{-5}$
CF@SiO ₂ _29	21.7	0.07	28.4	33.6	29.2	0.35	6.8×10^{-5}
CF@SiO ₂ _37	25.3	0.07	32.2	37.5	37.0	0.46	1.4×10^{-4}
CF@SiO ₂ _42	25.1	0.09	38.8	46.4	42.3	0.36	2.1×10^{-4}

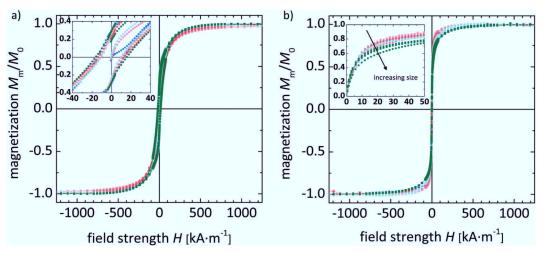


Fig. 2 Normalized magnetization curves of different probe particles (CF_12 (blue); CF@SiO2_25 (orange); CF@SiO2_29 (red); CF@SiO2_37 (light cyan); CF@SiO₂_42 (green)) in (a) the dried state and (b) in aqueous solution.

In the dried state, all particle batches show at ambient temperature a hysteretic magnetization curve, and the saturation magnetization $M_{\rm S}$ is according to the expected range by taking into account the volume and diamagnetism of the SiO2 shell. The normalized curves are of similar shape, and the coercive field H_c and normalized remanence M_R/M_S do not significantly depend on the shell thickness.

In aqueous dispersion, all particle batches show pseudosuperparamagnetic behavior, characterized by Langevin-type behavior and the absence of hysteresis. With increasing particle size, the normalized initial susceptibility of the virgin curve, $\chi_{\rm ini}/M_{\rm S}$, shows a decrease which is attributed to the diamagnetic contribution of the SiO2 shell.

With respect to rotational diffusion-based hydrodynamic properties, dynamic magnetometry based AC susceptometry is employed. These experiments also serve as an important reference for the MPN experiments discussed in the following chapters. The AC susceptograms of the tracers are shown in Fig. 3. All tracer particles show a typical Debye-type relaxation behavior in water, with a sigmoidal shape of the real part of the susceptibility χ' , and a maximum for the imaginary part χ'' . The fit of the single Debye relaxation process including a particle size distribution is exemplarily shown in Fig. S3 (ESI†). With increasing diameter of the tracer particles, the transition is shifted to lower frequencies as expected. All susceptograms can

be fitted according to a single Debye relaxation process in a Newtonian fluid with a minor distribution of relaxation times (due to the minor size distribution of the tracer particles), the average characteristic relaxation time τ_B is estimated, and by employing the viscosity of water at 25 °C, $\eta_0 = 0.89$ mPas, 30 the volume-weighted hydrodynamic radius r_h of the respective tracer particles and its distribution are determined. A summary of the obtained hydrodynamic sizes of the probe particles in water is given in Table 2.

According to the results discussed above, all particle batches show spherical shape, narrow size distribution, and welldefined hydrodynamic and magnetic properties and are predominantly magnetically blocked, suggesting that the particles are well suited as magnetic tracer particles for Magnetic Particle Nanorheology based on dynamic magnetometry.

1.2 Choice of a polymer system and characterization. As a suitable polymer model system, aqueous solutions of PEG in water are identified. The structure and flow characteristics of these solutions are well known to follow the expected physical behavior in an exemplary manner. Therefore, they are used as an experimental model system in many investigations on the structure and dynamics of nanostructured fluids.³⁷⁻⁴⁰ Accordingly, in this study, we employ aqueous PEG solutions spanning a wide range of molar mass $M_{\rm w}$ and volume fraction ϕ of the polymer.

Paper

Table 3 Overview of magnetic parameters determined from the VSM measurements of probe particles in the dried state for M_S, μ_{maq} , H_c and M_R/M_S . χ_{ini}/M_S and m are determined from the measurements in water

Probes	CF_12	$CF@SiO_2_25$	$CF@SiO_2_29$	$CF@SiO_2_37$	$CF@SiO_2_42$
$M_{\rm S} \left[\text{A m}^2 \text{ kg}^{-1} \right]$	74.1	11.1	10.6	10.5	10.2
$\mu_{\mathrm{mag}} \left[\mathrm{m}\% \right]$	98.1	14.6	14.1	13.9	13.5
$H_{\rm c}$ [kA m ⁻¹]	13.8	10.8	13.5	10.2	16.0
$M_{ m R}/M_{ m S}$	0.30	0.25	0.28	0.27	0.29
$\chi_{\rm ini}/M_{\rm S}$ [m A ⁻¹]	3.2×10^{-5}	3.0×10^{-5}	2.9×10^{-5}	2.7×10^{-5}	2.3×10^{-5}
m [A m ²]	3.6×10^{-19}	3.0×10^{-19}	2.8×10^{-19}	2.6×10^{-19}	2.2×10^{-19}

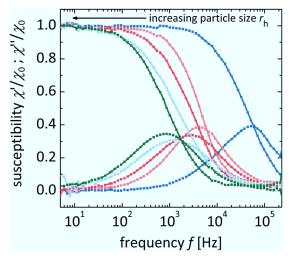


Fig. 3 Real (χ') and imaginary (χ'') part of the susceptibility normalized by the initial susceptibility (χ_0) in dependence on frequency f measured in water for probe particles CF_12 (blue), CF@SiO2_25 (orange), CF@SiO2_29 (red), CF@SiO2_37 (light cyan) and CF@SiO2_42 (green).

The structure and dynamics of polymer solutions are characterized by various parameters. First of all, the concentration regime of the polymer solution is important, and thus information on the overlap volume fraction ϕ^* , the entanglement volume fraction ϕ_e and the critical molar mass M_e is required. With $M_e = 5870 \text{ g mol}^{-1}$ is accessible from the literature, ⁴¹ we can expect that P4k solutions are not entangled independent of the polymer volume fraction, since the critical molar mass of PEG with $M_{\rm e}$ is not reached.

 ϕ^* and ϕ_e of the aqueous PEG solutions are molar-massdependent and obtained from static macroscopic rheological measurements. The zero shear viscosity η_0 is extracted from rheometric steady-state flow curves by extrapolating the viscosity η to $\sigma \to 0$. In Fig. 4, the dependence of η_0 on the volume fraction ϕ and molar mass $M_{\rm w}$ of the polymer component is shown. For each polymer solution series, there are two concentration regimes with different scaling exponents m_1 and m_2 , corresponding to the semi-diluted regime and to the concentrated regime, respectively. From the cross-section of the linear fits in the double-log plot, the critical polymer volume fraction ϕ_c is obtained and found to be close to the literature values for the overlap volume fraction ϕ^* , or the entanglement volume fraction $\phi_{\rm e}$ (Table 4).^{24,31}

With increasing molar mass $M_{\rm w}$, $\phi_{\rm c}$ decreases as expected, and the scaling of η_0 with ϕ is in good agreement with

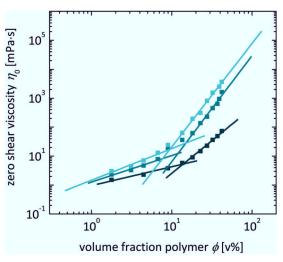


Fig. 4 Zero shear viscosities η_0 obtained from macrorheology in dependence on the volume fraction of polymer ϕ for aqueous solutions of P4k (dark cyan), P20k (cyan) and P35k (light cyan). The entanglement volume fraction $\phi_{\rm e,exp}$ is obtained from intersections of linear fits, whereas the scaling exponents m_1 and m_2 result from the slopes of the fits. In parts reproduced with permission from reference 31.

Table 4 Theoretical overlap volume fraction ($\phi_{\text{theo.}}$ *) as well as entanglement volume fraction ($\phi_{ ext{e,theo}}$) and the experimental critical volume fraction $\phi_{c,exp}$ obtained from the cross-section of the two scaling regimes with scaling exponents m_1 and m_2 resulting from theoretical calculations and macroscopic measurements for the investigated PEG solutions

Sample	$\phi_{ m theo.}^* \ [m v\%]$	$\phi_{ m e,theo} \ [m v\%]$	$\phi_{ m c,exp} \ [m v\%]$	$m_1 \ (\phi < \phi_{ m c,exp})$	$m_2 \ (\phi < \phi_{ m c,exp})$
Theo.	_	_	_	$m_{1,\text{theo}} = 1.000$	$m_{2,\text{theo}} = 3.927$
P4k	7.59	n. a.	13.88^{a}	0.65 ± 0.08	2.26 ± 0.11
P20k	2.22	14.35	11.94	0.92 ± 0.11	3.66 ± 0.23
P35k	1.45	9.36	9.46	1.09 ± 0.15	3.57 ± 0.13

^a Apparent, since theoretically not defined for this molar mass.

the theoretical predictions. The deviations present can be ascribed to the finite molar mass distribution of the polymer component.

When considering the relevance of the tracer size, it becomes further important to estimate the characteristic length scales within the solutions based on theoretical predictions. Of relevance are the radius of gyration R_g , the correlation length ξ , and, for entangled solutions, the tube diameter a.

The radius of gyration R_g , defined via the mean square distance of the building blocks to the center of gravity of the

molecule, is weakly dependent on the polymer volume fraction ϕ (eqn (5)).²⁴

$$R_{\rm g}(\phi) = b\sqrt{\frac{N}{6}}\phi^{-(\nu-1/2)/(3v-1)}$$
 (5)

$$R_{\rm F} = b \left(\frac{\nu}{b^3}\right)^{2\nu - 1} \tag{6}$$

Here, b is the length of a Kuhn segment (b = 1.1 nm), $N = M/M_0$ is the number of Kuhn segments of the polymer with the molar mass of a Kuhn monomer being $M_0 = 132 \text{ g mol}^{-1}$ and ν being the Flory exponent (ν = 0.588) for a polymer in an athermal solvent. 24,25,41 $R_{\rm F}$ is defined as $R_{\rm g}$ ($\phi \rightarrow 0$) at infinite dilution of the polymer solution (eqn (6)).²⁵

The correlation length ξ is defined as the average distance between one monomer unit of a polymer chain to the nearest monomer unit of another polymer chain, while a is related to the topological confinement of a polymer chain by the surrounding chains to a tube-like region.²⁴ Both parameters are independent of M_n , but depend on the polymer volume fraction ϕ . (eqn (7) and (8)). 24,25

$$\xi(\phi) = b\phi^{-\nu/(3\nu - 1)} \tag{7}$$

$$a(\phi) = a(1)\phi^{-\nu/(3v-1)}$$
 (8)

with a(1) = 3.73 nm being the tube diameter of PEG in melts.⁴¹ The dependence of R_F on M is shown in Fig. 5(left) and indicates its relation to the characteristic tracer particle size r_h . $R_{\rm F}$ increases with M, indicating that by varying the molar mass $M_{\rm n}$ of the polymer and the size $r_{\rm h}$ of the tracer particles, it is possible to selectively study different regimes of r_h with respect to $R_{\rm F}$. The correlation length ξ and the imaginary tube diameter a are shown in dependence on the polymer volume fraction ϕ in Fig. 5(right). Both parameters decrease with increasing ϕ , with a being always larger than ξ . By relating a and ξ to the probe particle size r_h , one obtains critical concentrations where $\xi(\phi_{\xi}) = r_{\rm h}$ or $a(\phi_{\rm a}) = r_{\rm h}$, as listed in Table S1 (ESI†). Based on these parameters, the particles can be classified into small, intermediate and large particles as suggested by Rubinstein, as shown in Fig. 12.25 Upon systematic variation of the polymer molar mass $M_{\rm n}$, the polymer volume fraction ϕ and the probe particle size r_h , a whole bandwidth of polymer concentration regimes and relations of particle size to polymer size is accessible and its specific influence on the nanorheological results can be studied. In the investigated polymer fraction and molar mass regime, the particles CF_12 undergo all of the three different regimes (large particles: $d_h < a$; intermediate particles: $a < d_h < \xi$; small particles: $\xi < d_h$), whereas the two larger particles are expected to mainly behave as intermediate and large particles.

Accordingly, the polymer solutions under investigation are well-suited as model systems, and thus in line with recent experimental studies, the system is particularly suited to allow the prediction of characteristic time- and length scales based on the theoretical findings and experimental results of others.

2. Investigation of complex fluids with variable probe sizes

In the following, we discuss the MPN-based nanorheological results based on tracer particles with three different hydrodynamic diameters (CF_12, CF@SiO₂ 29 and CF@SiO₂ 42). After a general discussion on the spectra, we will gain more insight from the discussion of the impact of the tracer size, polymer molar mass, and volume fraction.

2.1 ACS measurements in complex fluids. To extract sizerelated rheological information on the polymer solutions under investigation, the samples are doped with magnetically blocked tracer particles with varied hydrodynamic diameter, and are analyzed by ACS at ambient temperature. By employing three polymers with different molar mass $(M_n = 4000 \text{ g mol}^{-1} \text{ to})$

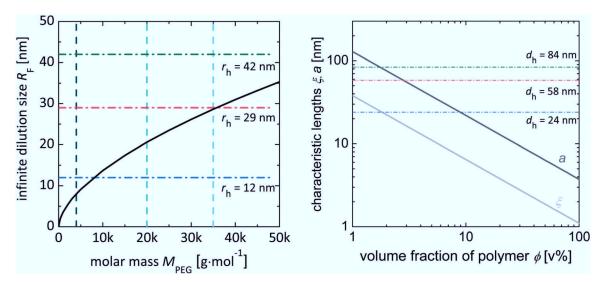


Fig. 5 Characteristic sizes of aqueous PEG solutions: (left) radius of gyration for infinite dilution R_f in dependence of the investigated molar mass M (dark curve) with indication of the solutions employed in this study (P4k (dark cyan), P20k (cyan), P35k (light cyan)); (right) correlation length ζ (light grey) and tube diameter a (dark grey) in dependence on the polymer volume fraction ϕ . In both plots, the tracer hydrodynamic radius r_h is indicated for CF_12 (blue), CF@SiO2_29 (red) and CF@SiO2_42 (green).

35 000 g mol⁻¹) and spanning a wide range of polymer volume concentrations between 0 v% and 42 v%, the experiments comprise a large range of characteristic size ranges. With an extensive number of different combinations of tracers and polymer solutions, the full range of relations between the tracer particle size and length scales in the polymer system is covered, and a detailed and complete picture on the influence of size effects on tracer dynamics is targeted.

In Fig. 6, the AC susceptograms based on three different tracer particles and solutions of three different polymers are shown. Generally, the spectra are shifted to lower frequencies with increasing polymer concentration ϕ , in accordance with an increase in viscosity η (see 1.2). Similarly, the spectra shift to lower frequencies with increasing particle size r_h , in accordance with an increased rotational relaxation time $\tau_{\rm B}$.

The spectra based on the two larger tracer types mainly show a symmetric shift with a conserved curve shape, indicating that even at high volume fractions the particles experience a single Debye relaxation process in these solutions, similar to the one observed in water. In contrast, the spectra of CF_12 are more complex. They show a broadening of the peak and partly even bimodal behavior with increasing volume fraction ϕ .

Analyzing the susceptograms by means of the Gemant-Bishop-diMarzio model allows the detailed investigation of the influence of the intrinsic parameters of the polymer solutions on the rotational particle diffusivity. For this purpose, we calculate the mechanical loss modulus G''(f) according to eqn (2), and compare it to the results of the macrorheological frequency sweeps (see Fig. 7a and Fig. S4-S6, ESI†) with emphasis on the influence of different parameters such as the polymer volume fraction ϕ , the molar mass of the polymer M, and the particle size r_h .

While the macroscopic results for all samples show a Newtonian behavior for all samples in the investigated frequency

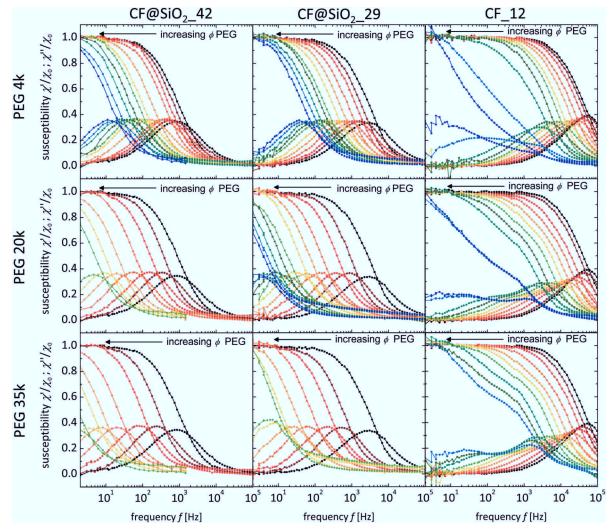


Fig. 6 AC susceptograms for P4k (upper row), P20k (middle row) and P35k (lower row) aqueous solutions for probe particles CF@SiO₂_42 (left column), CF@SiO₂_29 (middle column) and CF_12 (right column). The volume concentration is varied between 0-42.0 v% (black: ϕ = 0 v%; dark red: ϕ = 1.8 v%; red: ϕ = 4.5 v%; orange: ϕ = 9.0 v%; light orange: ϕ = 13.5 v%, yellow: ϕ = 18.1 v%, light green: ϕ = 22.8 v%; olive green: ϕ = 27.5 v%; turquoise: ϕ = 32.3 v%; light blue: ϕ = 35.2 v% (ϕ = 37.2 v% for P4k); blue: ϕ = 37.2 v% (ϕ = 42.0 v% for P4k). The graphs show the real (squares) and imaginary part (circles) of the susceptibility χ^* in dependence on the frequency f.

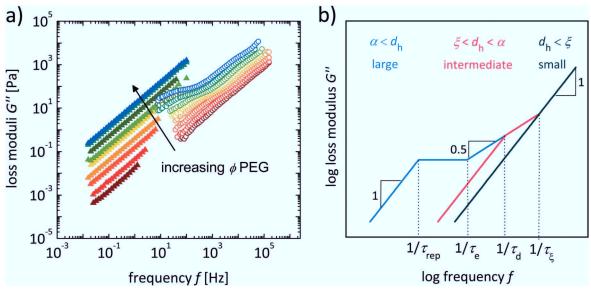


Fig. 7 (a) Loss moduli determined by macrorheology (full symbols) and nanorheology (empty symbols) in dependence on frequency f for P35k aqueous solutions for probe particles CF_12. The volume concentration is varied between 1.8–35.2 v% (dark red: $\phi = 1.8$ v%; red: $\phi = 4.5$ v%; orange: $\phi = 9.0$ v%; light orange: $\phi = 13.5$ v%, yellow: $\phi = 18.1$ v%, light green: $\phi = 22.8$ v%; olive green: $\phi = 27.5$ v%; turquoise: $\phi = 32.3$ v%; light blue: $\phi = 35.2$ v%) and (b) schematic representation of loss moduli curve course in dependence on frequency for different relations of probe particle size to structural units of the polymer based on the theory set up by Rubinstein for translational motion of particles in complex and structured solutions.²⁵ (blue: large particles $(a < d_{\rm h})$, red: intermediate particles $(\xi < d_{\rm h} < a)$, and green: small particles $(d_{\rm h} < \xi)$). Here, τ_{ξ} is the relaxation time of the polymer connected to the correlation length, τ_{d} is the relaxation time of a polymer segment with the same size as the particle size, τ_{e} represents the relaxation time of an entanglement strand and τ_{rep} is the relaxation time of a whole polymer chain.

range, generally the correspondence between macroscopically and nanoscopically derived data is the best for large particles, low polymer fractions and low molar mass of the polymer component. For increasing $M_{\rm p}$ and polymer fraction, the smaller particles show deviations between the methods, and a frequencydependent behavior is observed for the smaller tracer particles. In the following, these observations are analyzed in more detail.

2.2 Influence of polymer volume fraction ϕ

In the macroscopic rheology frequency-sweep experiments the Newtonian behavior of the solutions within the macroscopically accessible frequency range (up to $f = 10^2$ Hz) is confirmed by a scaling exponent of ~ 1 for G''(f) and f for all investigated polymer solutions. In comparison, the nanoscopic results enlarge the accessible frequency range (1 Hz-250 kHz) and thus allow also the detection of frequency-dependent moduli, along with the influence of the probe size. Here, the slope of G''(f) passes through different regimes, ascribed to different dominating relaxation modes and tracer dynamics. The concentration dependence of this behavior is discussed exemplarily in the case of CF_12 tracer particles in P35k solutions (Fig. 7a).

First of all, it is important to point out that the absolute values in the overlapping frequency region of macroscopic and nanoscopic measurements show a good agreement for the two larger (SiO₂-coated) particle batches, in particular at low molecular mass M and polymer volume fraction ϕ . In contrast to this, with decreasing particle size, the increasing volume fraction of the polymer ϕ and molar mass M the discrepancies

between the two measurement methods increase. For the P35k solutions investigated with CF_12 particles, for the two lowest polymer volume fractions a good correspondence between the nanoscopic and macroscopic results is found. Here, the particles are expected to behave as 'small probe particles' (compare to Fig. 5 and 7b) with a slope of 1, resulting in a constant viscosity and this is experimentally found. For higher polymer fractions a deviation in the frequency-dependent behavior as well as in the extrapolated apparent viscosity at low frequencies is found. This can be explained since the particles go through the transition from 'intermediate' to 'large particles' with a frequency dependent scaling behavior.

A theoretical description of the scaling of G'' with f for different relations of probe particle size to structural units is based on the theory set up by Rubinstein²⁵ for translational motion of particles in polymer solutions. According to this approach, a different scaling behavior is expected for the so-called 'large particles' (larger than the tube diameter of the solution a), for 'intermediate-sized particles' with a radius or diameter between the correlation length and the tube diameter, and for 'small particles' that are smaller than the correlation length ξ , as schematically shown in Fig. 7b.

Accordingly, in the series discussed here, we expect a scaling (G'' vs. f) of 1 over the full frequency range for volume fractions below ϕ_{ξ} = 4.5%, since the particles dynamics are mostly affected by an effective viscosity of the polymer solution. Since $r_{\rm h} < R_{\rm F}$, a reduction in effective viscosity as compared to the macroscopic behavior is present, as the particles mainly diffuse the solvent-rich domains of the solution. Hence, the apparent

viscosity as obtained from these experiments is lower than the macroscopic zero-shear viscosity η_0 and closer to the viscosity of the solvent η_s . For entangled solutions between $\phi_{\xi} < \phi < \phi_a$, we expect a behavior as 'intermediate-sized' tracer, and this is in accordance with the observed subdiffusive behavior at intermediate frequencies for solutions between $\phi = 4.5\%$ and 22.8%.

According to the theory, the subdiffusive regime is found at time scales between τ_{ξ} (relaxation time of the polymer connected to the correlation length) and τ_d (relaxation time of a polymer segment with the same size as the probe particle size). In the polymer volume fraction regime where $\phi > \phi_a$, the tracers are expected to behave as 'large particles. In entangled solutions and at long observation times ($t < \tau_{\text{rep}}$, reptation time of a polymer chain), the diffusion of 'large' particles is determined by bulk viscosity of the polymer system, and a slope of 1 is predicted for G''(f). At shorter times $(\tau_{rep} > t > \tau_e)$, the relaxation time of an entanglement strand), the tracer particles have to wait for the polymer mesh to relax, and strongly subdiffusive behavior or even a plateau is predicted. Below τ_e , the particle diffuses within its mesh with a behavior similar to intermediate particles. For CF_12 tracer particles in P35k solutions, this is clearly confirmed for $\phi > 22.8\%$.

It is thus experimentally shown that the nanorheological behavior as extracted from MPN is in accordance with the predicted behavior and that for the investigated polymer solutions, the smallest tracer particles CF_12 allow the observation of the transition from small via intermediate-sized to large tracers. The volume fractions of the transitions observed are close to the expected volume fractions ϕ_{ξ} = 4.5% and ϕ_{a} = 21.9% as calculated for the CF_12 particles.

Accordingly, this classification seems feasible for the detailed discussion of the size-related results, and is later used to establish a phase diagram of the entire system (see Section 2.6).

2.3 Influence of the molar mass *M* of the polymer component. To investigate the impact of the molar mass M_n of the polymer

component on the system, we exemplarily discuss the molar mass dependence of the frequency-dependent real part of the viscosity $\eta'(f)$ calculated using eqn (3) and (4). All respective results are compared to the macroscopic measurements (see Fig. S7-S9, ESI†). In Fig. 8, $\eta'(f)$ is exemplarily shown for experiments based on CF@SiO₂ 29 as tracer particles for solutions based on P4k, P20k and P35k, for two series with each a constant volume fraction of polymer; ϕ = 4.5 v% and ϕ = 22.8 v%. For both series it is observed that with increasing $M_{\rm n}$, the viscosity in general increases as would be expected. In addition, in the nanoscopically accessible size- and frequency range, a frequencydependent behavior is observable in contrast to the (mainly Newtonian-like) macroscopic measurements.

In the series with ϕ = 4.5 v%, the tracer particles are expected to be in the 'intermediate' size regime, as for CF@SiO₂_29, ϕ_{ξ} = 1.4 v% and ϕ_{a} = 7 v%. Experimentally, the results confirm a nearly Newtonian-like behavior for f > 100 Hzat a viscosity close to the macroscopic one, however, also a reduced effective viscosity at lower frequencies. The deviations at low frequencies can result from the fact that in the correction procedure for the evaluation of the data using the GDB model a distribution of hydrodynamic size and viscosity resulting from the measurements in Newtonian fluids is assumed and the direct transfer of these parameters to complex fluids might account for the errors. This latter effect is not very exposed due to the fact that the tracer radius is larger than or close to R_f , and it should be pointed out that none of these solutions is entangled. The deviations at high frequencies may be caused by the application of a frequency-independent value of $\chi_{N}{}'$ at χ_{∞} for the correction of the data.

It will be helpful to compare this behavior to higher concentrated, entangled and non-entangled solutions.

Accordingly, the results of the series employed with the same tracer particles (CF@SiO2_29) at a polymer volume fraction of ϕ = 22.8 v% show a more complex behavior. Again, for

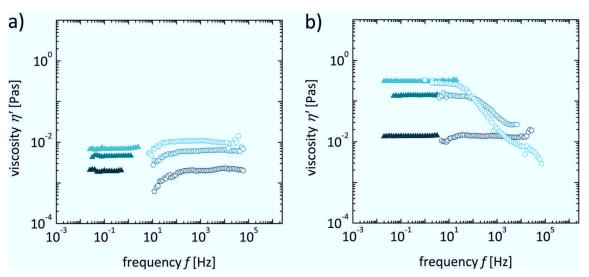


Fig. 8 Viscosity determined by macrorheology (full symbols) and nanorheology (empty symbols) in dependence on frequency f for P4k (dark cyan), P20k (cyan), P35k (light cyan) aqueous solutions for probe particles CF@SiO $_2$ _29 at (a) ϕ = 4.5 v% and (b) ϕ = 22.8 v%.

the P4k solution there is a good agreement between the macroscopic and the nanoscopic measurements. This is expected, since the molar mass of P4k is below the critical value for the occurrence of entanglements $M_{\rm e}$, and thus the solution in all regimes behaves principally similar to a simple Newtonian fluid for all length scales considerably larger than $R_{\rm F}$ (or $R_{\rm g}$) and ξ .

The nanoscopic measurements of the higher molar mass polymers at ϕ = 22.8 v% show a strong decrease of the apparent viscosity η' at higher frequencies. This behavior is attributed to the diffusion of a tracer particle within its mesh of the entangled networks of the P20k and P35k solutions. According to the theoretical predictions, 25 the respective transition is expected at time scales between τ_e (or τ_d) and τ_{rep} , which is addressed further in Section 2.6.

2.4 Influence of particle size $r_{\rm h}$. To illustrate the influence of the particle size $r_{\rm h}$ on the effective loss modulus G'', we exemplarily discuss two series of experiments on P35k aqueous solutions with each a constant polymer volume fraction of $\phi=4.5$ v% and $\phi=22.8$ v%, based on three differently sized tracer particles (Fig. 9). For the semi-diluted as well as the unentangled, but overlapped regime at $\phi=4.5$ v%, the macroscopic and nanoscopic measurements correspond sufficiently to the larger tracers CF@SiO2_29 and CF@SiO2_42, while a reduced effective viscosity is observed in the smallest particle batch CF_12. In contrast to the other two tracers, CF_12 is considerably smaller than the radius of gyration $R_{\rm g}$ of the employed polymer, and its diffusion is therefore partly dominated by the solvent.

For the entangled solutions at ϕ = 22.8 v%, a good agreement between macroscopic and nanoscopic measurements is found for the two silica coated particle batches in the frequency overlap region, while a plateau is observed in the intermediate frequency range. CF_12 tracers show additionally a deviation in the effective viscosity to lower values in the lowest accessible

frequency range. Such a plateau is in accordance with the predictions and is expected between τ_e (or τ_d) and τ_{rep} (see Section 2.6).

2.5 Zero shear viscosity and rotational diffusion coefficient

In addition to the frequency-dependent scaling behavior of G''the long-time rotational diffusion coefficient $D_{r,0}$ is extracted from the low-frequency-related viscosity $\eta_{0,GDB}$ for all investigated tracers and investigated polymer solutions, in order to gain more insight into the long-time size-dependent diffusion behavior. For this purpose, we determine $\eta_{0,\text{GDB}}$ by extrapolation of G'' to f = 1 Hz, and the rotational diffusion coefficient D_r is calculated using eqn (1) by implementation of $\eta_{0,GDB}$ from the measurements. The data are further normalized by the rotational diffusion coefficient of the particles in water $D_{\rm S}$. The results are displayed in Fig. 10 versus the reduced polymer volume fraction ϕ/ϕ_a , with respect to the effective polymer mesh size in entangled polymer solutions. We would like to point out that while in some of the literature ϕ_a is defined by relating the tracer particle diameter to a, we found an excellent agreement with expectations by using r_h instead of d_h .

For all investigated systems, a decrease in the normalized rotational diffusion is found with increasing reduced volume fraction ϕ/ϕ_a . Depending on the tracer particle size and the molar mass of the polymer, up to three distinct regimes of scaling with the reduced polymer fraction are observed.

For all particle batches, we observe a decrease of $D_{\rm r}$ with $\phi^{-1.5}$ for volume fractions between ϕ_{ξ} and $\phi_{\rm a}$, and the results are thus principally in agreement with theoretical predictions.²⁵ Deviations are observed for P4k, where at this low molar mass, $\phi_{\rm a}$ is not defined.

At volume fractions larger than ϕ_a , for the two larger particle batches, a good agreement between the macroscopic and nanoscopic experiments is shown, as indicated by the scaling behavior and cross-over frequency of the two regimes identified. For the

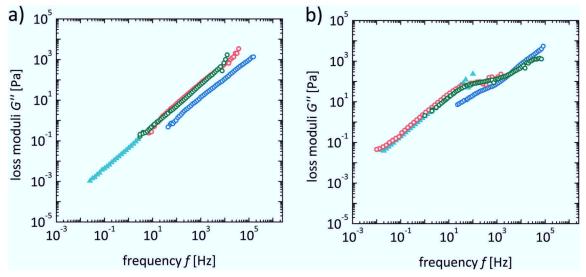


Fig. 9 Loss moduli determined by macrorheology (full symbols) and nanorheology (empty symbols) in dependence on frequency f for P35k (light cyan) aqueous solutions for probe particles CF_12 (blue), CF@SiO2_29 (red) and CF@SiO2_42 (green) at (a) ϕ = 4.5 v% and (b) ϕ = 22.8 v%.



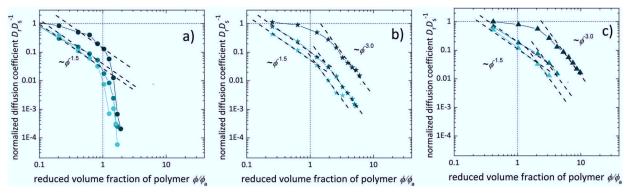


Fig. 10 Rotational diffusion coefficient normalized by the diffusion coefficient in pure solvent D_r/D_s in dependence on the reduced volume fraction of polymer ϕ/ϕ_a determined with probe particles (a) CF_12 (circles), (b) CF@SiO2_29 (stars) and (c) CF@SiO2_42 (triangles) for polymer systems P4k (dark cyan), P20k (cyan) and P35k (light cyan).

smallest tracer particles CF_12 though, a particularly sharp transition as compared to the larger tracers is observed at ϕ_a , and a sharp decrease of D_r at increasing volume fraction is found, in accordance with an arrest of the particle within the entanglement mesh. This behavior is in good accordance with the predictions from Rubinstein's theory, predicting a scaling behavior of 0 for $\phi < \phi_{\xi}$, of -1.52 for $\phi_{\xi} < \phi < \phi_{\rm a}$, with a sharp step of $D_{\rm r}$ at $\phi = \phi_a$ for the case of small particles. For intermediate-scaled particles, we obtain a scaling exponent of about -3.0 from these results, in accordance with Fig. S10 (ESI†).

2.6 Refinement of theoretical expectations

When overlooking the entire set of rheograms (Fig. S2-S4, ESI†), with an emphasis on the frequency overlap region, it is generally noticed that for CF@SiO2_29 and CF@SiO2_42 a good quantitative agreement between macroscopic and nanoscopic data points is found, confirming the versatility of the method to extract general rheometric data as long as the tracer particles are considerably larger that the structural units of the system to be analyzed. In addition to the extension of the frequency range (as compared to the usual microrheological experiments, where mostly $f < 10^3$ Hz), the method shows potential for extracting relaxation times with respect to the polymer as well as also the tracer particles, thus allowing information on the sizedepending dynamics in the nanostructured fluids. This can clearly be seen by focusing on the CF_12 tracer particles that show a predicted subdiffusive behavior at intermediate time scales, and the relation of particle size to structural length scales present in the solution plays a major role.

By analyzing the frequency dependence of the loss moduli G" in detail, all experiments can be classified into 'small', 'intermediate-sized' or 'large' tracer behavior. Therefore, the scaling behavior of the different curve segments is analyzed and compared to the theoretical expectations (e.g., Fig. 7b). From this, also the inherent characteristic time for reptation, τ_{rep} , is extracted for experiments on entangled solutions with 'large' tracer particles (compare Fig. 11) which is discussed later in this section.

For a comprehensive overview on the results obtained for the entire investigated system, a phase diagram is constructed

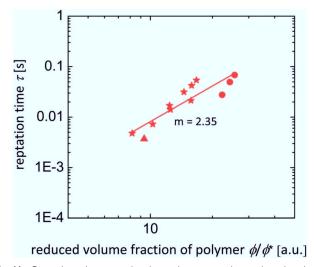


Fig. 11 Reptation time τ_{rep} in dependence on the reduced volume fraction of polymer ϕ/ϕ^* determined with probe particles CF_12 (circles), CF@SiO₂_29 (stars) and CF@SiO₂_42 (triangles). The experimental scaling is approximately $\phi^{2.35}$.

(Fig. 12), in which the hydrodynamic particle radius r_h normalized over the radius of gyration at infinite dilution $R_{\rm F}$ is plotted against the reduced polymer volume fraction ϕ/ϕ^* . From theoretical calculations ξ , a, $R_{\rm F}$ are calculated in dependence on ϕ/ϕ^* and included in the phase diagram.

The results can be summarized as follows: for three series of experiments, the tracers are considerably larger than the radius of gyration at infinite dilution, $R_{\rm F}$: CF@SiO₂_42 tracer particles in P4k and P20k, as well as CF@SiO2_29 tracers in P4k. In these experiments it is observed that the behavior is nearly Newtonian for most concentrations (indicated by the green color of the data point in the phase diagram), and that subdiffusive behavior is observed at intermediate time scales, in case the concentration becomes large enough ($\phi \sim \phi_a$ or ϕ_{ξ}). This is indicated by red symbols in the phase diagram.

The increasing polymer molar mass and/or decreasing particle size results in $r_{\rm h} \sim R_{\rm F}$. This is the case for CF@SiO₂_42 This article is licensed under a Creative Commons Attribution-NonCommercial 3.0 Unported Licence.

Open Access Article. Published on 28 November 2019. Downloaded on 2/28/2020 7:13:43 AM.

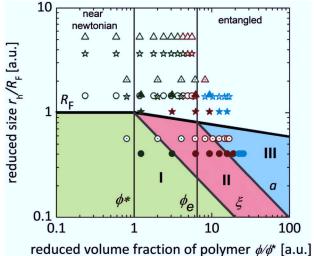


Fig. 12 Reduced size r_h/R_F in dependence on the reduced volume fraction of polymer ϕ/ϕ^* determined with probe particles CF_12 (circles), CF@SiO2_29 (stars) and CF@SiO2_42 (triangles) for P4k (open symbols), P20k (open dotted symbols) and P35k (filled symbols). Region I (green) belongs to small particles, II (red) to intermediate particles and III (blue) to large particles, after the classification of Rubinstein et al.

in P35k, CF@SiO2_29 in P20k, and for CF_12 in P4k. Principally, we observe a similar behavior, however, in the entangled or overlapped solutions with $\phi > \phi^*$, the predicted plateaubehavior expected for 'large' tracers can be observed (indicated by blue symbols in the diagram).

Finally, the tracer size is clearly lower than $R_{\rm F}$ for the series of CF@SiO₂_29 in P35k, as well as for CF_12 in P20k and in P35k. In these series, the predictions on all three regions ('small', green symbols; 'intermediate', red symbols; and 'large' tracers, blue) are excellently met with the predictions from theory. On the other hand, when the particles are slightly larger than the polymer size, still, the different regimes are found, but here the border between the different regimes seems to be dominated by the entanglement volume fraction ϕ_e/ϕ^* . The picture that arises here is, that below ϕ_e/ϕ^* the particles diffuse nearly Newtonian, whereas above ϕ_e/ϕ^* the response of the particles is mainly dominated by the entanglements of the system.⁴²

Accordingly, the other important result is that $R_{\rm F}$ (or $R_{\rm o}$) is the relevant cross-over quantity in order to classify macro- to nanoscopic rheological behavior. However, it should be stated that for $r_h > R_F$, still time-related processes are detected, and for the scaling with tracer size in this regime a good theoretical description is not available to date.

As a final step in our evaluation, we confirm the suitability of this size-dependent method to obtain realistic information on the solution dynamics. For this purpose, we exemplarily extract the reptation time τ_{rep} as a well-defined property from the curves of sufficiently concentrated and entangled solutions. The data are plotted in Fig. 11 and compared to the theoretical prediction. Taking into account the available data points we determine an experimental scaling with $\phi^{2.35}$, whereas the theoretical expected scaling is $\phi^{1.65}$. This requires more theoretical and experimental consideration in upcoming studies.

Taking further into account that Rubinstein's theory is set up for the passive translation of tracer particles in similar systems, the agreement with our data, that is exclusively on the rotational relaxation of magnetically deflected tracer particles, is not fully unexpected, but still surprising.

Based on the experimental and theoretical considerations of others, $^{27,38,43-45}$ e.g. the scaling behavior of η_{app} vs. ϕ is expected to be weaker for rotation than for translation, and might further be affected by a depletion layer. 38,43,45,46

Even if the latter was not the focus of the present study, we hope that our results foster the development of a more developed theoretical framework for rotational diffusion in complex fluids and might give rise to upcoming detailed theoretical description focusing on rotation. In view of the versatility and broad applicability of the method, along with the actual development of similar or related approaches, this would be very attractive.

Conclusions

Using a nanorheological approach based on Magnetic Particle Nanorheology (MPN), and by employing magnetic probe particles of variable particle sizes, we investigate the sizedependent rotational diffusivity of the tracers in a model system of aqueous poly(ethylene glycol) (PEG) solutions of varying molar masses and volume fractions. We emphasize the significance of the relation of probe particle size to the characteristic length scales within the polymer solution and its relevance for the frequency-dependent nanorheological results.

For this purpose, we use spherical, magnetically blocked tracer particles of different hydrodynamic size, and determine the frequency dependent rheological properties, such as viscosities η , loss moduli G'' and diffusion properties of the probes, e.g. the rotational diffusion coefficient, from the real and imaginary part of the AC susceptometry spectra. The results are compared and complemented by macroscopic measurements as well as theoretical approaches to obtain a complete picture on the dynamic behavior of this system.

Our results show that it is possible to classify the solutions and their combination with the tracers into three important regimes, by considering the tracer size and the polymer-derived length scales in the solution, as long as the tracers are in the size range of the gyration radius R_g . Our experimental findings are consistent and show good semi-quantitative agreement with theoretical expectations for the passive, translational diffusion of particles in such solutions, as predicted by Rubinstein and coworkers. In particular, for tracer particles smaller than the radius of gyration of the polymer solutions, the predictions for 'large', intermediate-sized' or 'small' tracer behavior are excellently met, while partly pronounced deviations from macrorheological measurements are found. If the tracer particles are larger than $R_{\rm F}$, the nanorheological results are closer to the expectations from macrorheology, and are strongly affected if entanglements are present.

This detailed study on the size-dependent rheological properties of polymer solutions can serve as a basis for the advancement of the present rheological descriptions, and is suitable to serve as a basis for further investigations of more complex polymer systems such as dynamic networks,32 covalently crosslinked gels or biological systems. In particular, MNP can be used to specifically address particle-matrix interactions and to determine for example mesh sizes in less known systems.

Conflicts of interest

There are no conflicts to declare.

Acknowledgements

We gratefully acknowledge the financial support from the DFG (SPP 1681 (grant SCHM 1747/10 and WE2623/7)). Melissa Hess acknowledges support from the International Helmholtz Research School of Biophysics and Soft Matter (IHRS BioSoft). We would like to thank J. Allgaier, M. Kruteva and L. Fruhner from FZ Jülich (JCNS-1/ICS-1) for GPC measurements of the polymers.

Notes and references

- 1 G. Agostini, U. E. Frank, T. F. E. Materne, F. Visel and R. J. Zimmer, US Pat., 5580919, 1996.
- 2 F. Zhang, L. Liao, Y. Wang, Y. Wang, H. Huang, P. Li, Z. Peng and R. Zeng, J. Rare Earths, 2016, 34, 221–226.
- 3 T. Santaniello, L. Migliorini, Y. Yan, C. Lenardi and P. Milani, J. Nanopart. Res., 2018, 20, 250.
- 4 S. I. Rich, R. J. Wood and C. Majidi, Nat. Electron., 2018, 1, 102-112.
- 5 S. K. Sahoo and V. Labhasetwar, Drug Discovery Today, 2003, 8, 1112-1120.
- 6 L. A. L. Fliervoet and E. Mastrobattista, Adv. Drug Delivery Rev., 2016, 106, 63-72.
- 7 K. E. Uhrich, S. M. Cannizzaro, R. S. Langer and K. M. Shakesheff, Chem. Rev., 1999, 99, 3181-3198.
- 8 A. Heilbronn, Jahrb. Wiss. Bot., 1922, 61, 284-338.
- 9 H. Freundlich and W. Seifriz, Zeitschrift für Phys. Chemie, 1923, 233-261.
- 10 B. R. Dasgupta, S.-Y. Tee, J. C. Crocker, B. J. Frisken and D. A. Weitz, Phys. Rev. E: Stat., Nonlinear, Soft Matter Phys., 2002, 65, 51505.
- 11 R. E. Mahaffy, C. K. Shih, F. C. MacKintosh and J. Kas, Phys. Rev. Lett., 2000, 85, 880-883.
- 12 T. A. Waigh, Rep. Prog. Phys., 2005, 68, 685.
- 13 T. A. Waigh, Rep. Prog. Phys., 2016, 79, 74601.
- 14 A. Papagiannopoulos, K. Sotiropoulos and S. Pispas, Food Hydrocolloids, 2016, 61, 201-210.
- 15 W. Liu and C. Wu, Macromol. Chem. Phys., 2018, 219, 1700307.

- 16 J. Liu, V. Boyko, Z. Yi and Y. Men, Langmuir, 2013, 29, 14044-14049.
- 17 E. M. Furst, Curr. Opin. Colloid Interface Sci., 2005, 10, 79-86.
- 18 T. M. Squires and T. G. Mason, Annu. Rev. Fluid Mech., 2010, 42, 413-438.
- 19 A. Mukhopadhyay and S. Granick, Curr. Opin. Colloid Interface Sci., 2001, 6, 423-429.
- 20 F. C. MacKintosh and C. F. Schmidt, Curr. Opin. Colloid Interface Sci., 1999, 4, 300-307.
- 21 A. Tuteja, M. E. Mackay, S. Narayanan, S. Asokan and M. S. Wong, Nano Lett., 2007, 7, 1276-1281.
- 22 L. Maldonado-Camargo and C. Rinaldi, Nano Lett., 2016, 16, 6767-6773.
- 23 P.-G. De Gennes, Scaling concepts in polymer physics, Cornell University Press, 1979.
- 24 M. Rubinstein and R. H. Colby, Polymer physics, OUP, Oxford, New York, 2003.
- 25 L.-H. Cai, S. Panyukov and M. Rubinstein, *Macromolecules*, 2011, 44, 7853-7863.
- 26 J. Liu, D. Cao and L. Zhang, J. Phys. Chem. C, 2008, 112, 6653-6661.
- 27 R. Holyst, A. Bielejewska, J. Szymański, A. Wilk, A. Patkowski, J. Gapiński, A. Żywociński, T. Kalwarczyk, E. Kalwarczyk and M. Tabaka, Phys. Chem. Chem. Phys., 2009, 11, 9025-9032.
- 28 R. A. Omari, A. M. Aneese, C. A. Grabowski and A. Mukhopadhyay, J. Phys. Chem. B, 2009, 113, 8449-8452.
- 29 A. Wisniewska, K. Sozanski, T. Kalwarczyk, K. Kedra-Krolik and R. Holyst, Macromolecules, 2017, 50, 4555-4561.
- 30 E. Roeben, L. Roeder, S. Teusch, M. Effertz, U. Deiters and A. M. Schmidt, Colloid Polym. Sci., 2014, 292, 2013-2023.
- 31 M. Hermes, E. Roeben, L. Kibkalo and A. M. Schmidt, Annu. Trans. - Nord. Rheol. Soc., 2017, 25, 97-105.
- 32 M. Hess, E. Roeben, A. Habicht, S. Seiffert and A. M. Schmidt, Soft Matter, 2019, 15, 842-850.
- 33 S. Sun, H. Zeng, D. B. Robinson, S. Raoux, P. M. Rice, S. X. Wang and G. Li, J. Am. Chem. Soc., 2004, 126, 273-279.
- 34 E. A. DiMarzio and M. Bishop, J. Chem. Phys., 1974, 60, 3802-3811.
- 35 W. Stöber, A. Fink and E. Bohn, J. Colloid Interface Sci., 1968, 26, 62-69.
- 36 Q. Dai, M. Lam, S. Swanson, R.-H. R. Yu, D. J. Milliron, T. Topuria, P.-O. Jubert and A. Nelson, Langmuir, 2010, 26, 17546-17551.
- 37 B. R. Dasgupta, S. Tee, J. C. Crocker, B. J. Frisken and D. A. Weitz, Phys. Rev. E: Stat., Nonlinear, Soft Matter Phys., 2002, 65, 1-10.
- 38 N. Ziębacz, S. A. Wieczorek, T. Kalwarczyk, M. Fiałkowski and R. Hołyst, Soft Matter, 2011, 7, 7181-7186.
- 39 R. Holyst, A. Bielejewska, J. Szymański, A. Wilk, A. Patkowski, J. Gapiński, A. Zywociński, T. Kalwarczyk, E. Kalwarczyk, M. Tabaka, N. Zibacz and S. A. Wieczorek, Phys. Chem. Chem. Phys., 2009, 11, 9025-9032.
- 40 T. Yanagishima, D. Frenkel, J. Kotar and E. Eiser, J. Phys.: Condens. Matter, 2011, 23, 194118.

- 41 L. J. Fetters, D. J. Lohse and R. H. Colby, *Physical properties of polymers handbook*, Springer, Berlin, 2006.
- 42 L. H. Cai, S. Panyukov and M. Rubinstein, *Macromolecules*, 2015, **48**, 847–862.
- 43 G. H. Koenderink, S. Sacanna, D. G. A. L. Aarts and A. P. Philipse, *Phys. Rev. E: Stat., Nonlinear, Soft Matter Phys.*, 2004, **69**, 1–12.
- 44 A. Wiśniewska, K. Sozański, T. Kalwarczyk, K. Kędra-Królik, C. Pieper, S. A. Wieczorek, S. Jakieła, J. Enderlein and R. Hołyst, *Polymer*, 2014, 55, 4651–4657.
- 45 S. Alam and A. Mukhopadhyay, *Langmuir*, 2015, 31, 8780–8785.
- 46 L. Maldonado-Camargo, C. Yang and C. Rinaldi, *Nanoscale*, 2017, **9**, 12039–12050.