A Tale of Two Tails: Molecular Exchange Kinetics of Telechelic Polymer Micelles

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(Dated: February 5, 2020)

Telechelic polymers contain two chain ends that are able to promote self-assembly into "flowerlike" or interconnected micellar structures. Here we investigate the molecular exchange kinetics of such micelles using time-resolved small-angle neutron scattering (TR-SANS). We show that the activation energies of monofunctional and telechelic chain exchange are identical. This demonstrates that the two chain ends are not simultaneously released in a single event. Instead, the results show that contrary to regular micelles, the kinetics occurs in a multi-step process involving a collision-induced single-molecule exchange mechanism which gives rise to a characteristic $k \sim \phi$ dependence. We show that this novel mechanism can be quantitatively explained by a simple kinetic model.

Hydrophobically endcapped polymers, e.g., telechelic polymers bearing two hydrophobic stickers in terminal positions of a water-soluble backbone, are well-studied model systems for self-assembly. Telechelic polymers have attracted a lot of interest because their properties encompass many interesting aspects in soft matter physics, including hierarchical self-assembly, non-Newtonian flow behavior, and colloidal interactions. [1– 11] Aside from a purely academic point of view, telechelic polymers are very important as associative thickeners in daily life products, e.g., paints and cosmetics. In water, telechelic polymers spontaneously self-assemble into a variety of different nano-structures. These are, depending on concentration and hydrophobic chain end ("sticker") length, flowerlike micelles, clusters of micelles and nanostructured hydrogels; where telechelic chains interconnect individual micelles.

All these structures commonly show a continuous exchange of chains to reach and maintain their thermal equilibrium. In recent years the exchange kinetics of diblock copolymer micelles has been thoroughly studied experimentally and by computer simulation. In particular time-resolved small-angle neutron scattering (TR-SANS) employing H/D contrast variation proved to be the method of choice to explore the mechanisms of chain exchange under (quasi-)equilibrium conditions.[12] TR-SANS applied to different diblock copolymer micellar systems has shown that single-chain expulsion/insertion is the prevailing mechanism for chain exchange with the expulsion as the rate determining step [13–16]—in line with computer simulation [17, 18] and scaling theory [19, 20]. The expulsion is a thermally activated first-order kinetic process, which is characterized by a single exponential relaxation $R(t) = \exp(-kt)$, with t the time and k the exchange rate constant. The temperature dependence is

expressed in terms of an Arrhenius equation

$$k = \frac{1}{\tau_0} \cdot \exp(-E_a/k_B T),\tag{1}$$

with E_a the activation barrier, τ_0 the hypothetical attempt time of the core block to escape from the micelle and k_BT the thermal energy. E_a is essentially determined by the extra interface created by the insoluble block exposed to the solvent. It has been found that E_a depends linearly on the length of the insoluble block, which suggests contact between all monomers and solvent rather than collapse into a spherical globule. [14, 21]

In contrast to amphiphilic diblock copolymers, the exchange mechanism of telechelic micelles in aqueous solution has not yet been experimentally explored—despite their importance as materials. There are three possible scenarios:

- i) The expulsion of the two core blocks occurs simultaneously. In this case the exchange rate is expected to be proportional to the product of the two individual rates leading to a process with doubled activation energy compared to diblock exchange.
- ii) The expulsion of the two core blocks proceeds in two consecutive steps with free telechelic chains diffusing in solution. That means the exchange rate exhibits a more complicated temperature dependence and is independent of concentration (see SI for a more detailed discussion).
- iii) The expulsion of the two core blocks proceeds in two consecutive steps but with the first block reinserted into another micelle forming a bridge before the second block escapes. The exchange thus depends on collision of micelles and the rate would exhibit a clear concentration dependence. Such a mechanism is related to the "walking" diffusion

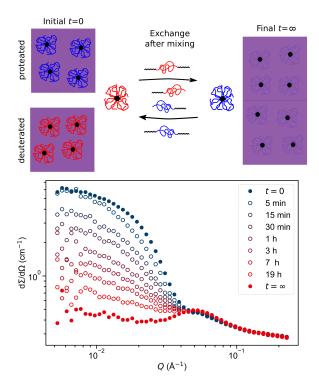


FIG. 1. Top: Illustration of the kinetic zero average contrast technique to monitor chain exchange in diblock/triblock mixed micelles. Bottom: Corresponding TR-SANS data of C_{28} -PEO5/ C_{28} -PEO10- C_{28} micelles obtained at 37 °C and 1.0% polymer volume fraction after mixing equal amounts of the deuterated and proteated reservoirs.

suggested by Yokoyama and Kramer [22, 23] for triblock copolymer melts forming mesocrystal domains.

According to classical transient network theory, the microscopic exchange dynamics in telechelic polymer gels play a key role for the macroscopic rheological properties. [24] This was recently confirmed by Zinn et al.[10] who found the same E_a for the macroscopic relaxation time of a telechelic network determined by linear oscillatory shear experiments and the molecular exchange time for the monofunctional polymers determined by TR-SANS. Lu et al. [25] found that the characteristic exchange time of the triblock copolymer PS-PEP-PS in squalane increases massively compared to a PS-PEP diblock with the same PS block and half the PEP length. The exchange rate was significantly faster than expected for simultaneous release, pointing towards a sequential activation. However, a clear picture for the mechanism is not apparent from that publication.

In this work we report a detailed study of the exchange kinetics of telechelic polymers by TR-SANS including a derivation of a kinetic model that accounts for the observed experimental findings. TR-SANS experiments were performed on mixtures of mono- and difunc-

tionalized (telechelic) poly(ethylene oxide) n-alkyl ethers: C_n -PEO5 and C_n -PEO10- C_n , with n=22,28 the alkane chain lengths and 5 and 10 the approximate PEO molecular weights in kg/mol. It has been shown by Laflèche et al. [26] that phase separation, usually occurring in aqueous solutions of telechelic polymers, is avoided by blending telechelic and monofunctionalized PEO chains. This is utilized here similar to previous works [10, 27]

For this study, mixtures with mole fractions of the telechelic chains of $f_{\rm tel} = 0.5$ for C_{22} (C22F50) and $f_{\rm tel} = 0.4$ for C_{28} (C28F40), were used. Solutions do not show any sign of demixing in a temperature range between 5 °C and 60 °C, where the TR-SANS experiments have been performed. The structural details of aqueous solutions of the mixtures have been published earlier.[27] In brief, for solutions of C_{28} mixtures, flowerlike micelles with looped telechelic chains are favored over cluster formation, which is the principal structure of the C_{22} samples. An inherent property of this system is partial crystallization of the n-alkane chains inside the micellar cores which leads to a larger activation barrier for exchange amounting to the enthalpy of fusion.[21, 28] Accordingly, equation (1) needs to be rewritten as

$$k = \frac{1}{\tau_0} \cdot \exp\left(\frac{\Delta S_m}{k_B}\right) \cdot \exp\left(-\frac{E_a + \Delta H_m}{k_B T}\right), \quad (2)$$

with ΔH_m and $\Delta S_m \approx \Delta H_m/T_m$ the melting enthalpy and entropy, respectively, and T_m the melting temperature.

The exchange of chains was monitored by TR-SANS employing the kinetic zero average contrast (KZAC) technique [29] described in detail in ref. [12]. The principles of the KZAC technique are schematically illustrated in Fig. 1(top) for exemplary flowerlike micelles. Two reservoirs, containing proteated and deuterated micelles in an $\rm H_2O/D_2O$ solvent mixture with zero contrast to the average of h-PEO/d-PEO, are mixed. Initially, the contrast and correspondingly the scattered intensity is maximal, but then decreases as a function of time due to the exchange of mono- and difunctional chains. At $t=\infty$, the contrast in the mixture is minimal as the corona chains are matched out by the solvent mixture.

As an example, time-resolved scattering curves are shown in Fig. 1(bottom) for a 1:1 mixture of d and h C_{28} -PEO5/ C_{28} -PEO10- C_{28} micelles at 37 °C and polymer volume fraction $\phi=1.0$ %. At low scattering vector Q, the plot reveals a continuous decrease of the scattered intensity with time, indicating a decrease of contrast of the PEO corona due to chain exchange. At high Q, the intensity is time-independent and predominantly results from the proteated n-alkane cores and from small contributions of segmental correlations of the PEO polymer.[30] Importantly, the scattered intensity after 19 hours reaches almost the intensity of a pre-equilibrated sample reflecting the final state. This indicates that both types of chains, monofunctional and telechelic, are ex-

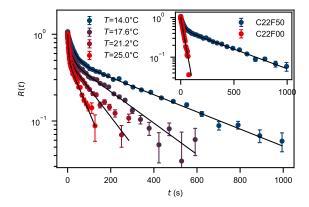


FIG. 2. Relaxation functions R(t) of C22F50 at selected temperatures. Black lines represent fits according to eq. (5). The inset shows a comparison of R(t) of C22F50 and C22F00 (pure monofunctional) at 14 °C. The data were obtained using a stopped-flow apparatus.

changing within the experimentally accessible time window.

To simplify data analysis, only the integrated scattering intensity,

$$I(t) = \int \frac{\mathrm{d}\Sigma}{\mathrm{d}\Omega}(Q, t) \,\mathrm{d}Q,\tag{3}$$

was used, with the time-dependent macroscopic scattering cross section $\mathrm{d}\Sigma/\mathrm{d}\Omega(Q,t)$, i.e., the scattering intensity. This procedure is equivalent to analyzing the full scattering curve.[15] The integrated intensities were then analyzed in terms of a dimensionless relaxation function R(t) defined as

$$R(t) = \sqrt{\frac{I(t) - I(\infty)}{I(0) - I(\infty)}},\tag{4}$$

where I(0) denotes the intensity at t=0 and $I(\infty)$ the intensity of a pre-equilibrated sample. Fig. 2 depicts typical relaxation curves of C22F50 at different temperatures.

The plot clearly reveals two well-separated processes, which we intuitively assign to the exchange of monofunctional C_{22} -PEO5 and difunctional C_{22} -PEO10- C_{22} copolymers, respectively. The assignment is further supported by comparing R(t) of C_{22} F50 with that of pure C_{22} -PEO5 micelles (C_{22} F00) at $T=14\,^{\circ}$ C as depicted in the inset of Fig. 2. The plot clearly shows that R(t) of C_{22} F00 coincides with the fast process of the mixture. Based on this we have fitted the relaxation curves by a sum of two exponential functions with prefactors corresponding to the molar fraction of the mixture,

$$R(t) = f_{\text{tel}} \cdot \exp(-k_{\text{tel}}t) + (1 - f_{\text{tel}}) \cdot \exp(-k_{\text{mon}}t). \quad (5)$$

Excellent fits were obtained as shown with solid lines in Fig. 2, yielding the rate constants for monofunctional

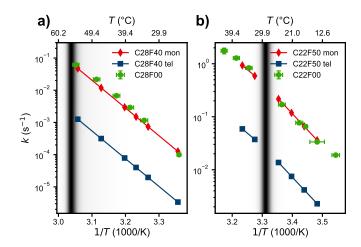


FIG. 3. Arrhenius representation of the rate constants of C_{28} and C_{22} monofunctional (mon) and telechelic (tel) polymers, obtained via a simultaneous fit of all temperatures. For comparison, previous data of the pure monofunctional samples (F00) are included.[28] The grey shades are contour plots of the DSC traces indicating the melting transitions of the micellar cores.

TABLE I. Parameters of simultaneous fits at $\phi = 1 \text{ vol}\%$ and different temperatures as well as important thermodynamic parameters of C_{28} and C_{22} polymer mixtures. Values for monofunctional polymer micelles are taken from a previous study [28] and added for comparison.

	C22F50	$C22F00^a$	C28F40	$C28F00^a$
$-\log_{10}(\tau_{0,\text{mon}}(s))$	15.5 ± 1.2	13.5 ± 3.0	18.7 ± 1.5	19.7 ± 2.5
$-\log_{10}(au_{0,\mathrm{tel}}(\mathrm{s}))$	14.3 ± 1.3	-	17.1 ± 1.6	-
E_a (kJ/mol)	92 ± 7	80 ± 15	125 ± 10	130 ± 15
T_m (°C)	29 ± 1	29 ± 1	57 ± 1	57 ± 1
$\Delta H_m \; (kJ/mol)$	24 ± 1	25 ± 1	40 ± 3	40 ± 3
$\Delta S_m (\mathrm{J/mol/K})$	79 ± 2	84 ± 2	121 ± 8	121 ± 8
$\tau_{1/2}^{b}$ (s)	4.6	5.1	7.9×10^{3}	6.3×10^{3}
$ au_{1/2, \text{tel}}^b$ (s)	73	-	3.0×10^{5}	-

^a taken from ref. [28]

 $k_{\rm mon}$ and telechelic $k_{\rm tel}$ chain exchange at each temperature. A preliminary Arrhenius evaluation of the fitted rate constants has shown that the E_a for chain escape is identical for both mono- and difunctional polymers. Subsequently the data could be re-analysed to further stabilize the fit using $E_a = E_{a,\rm mon} = E_{a,\rm tel}$ and perform simultaneous fits at all temperatures. Thus only E_a , $\tau_{0,\rm mon}$ and $\tau_{0,\rm tel}$ were free fit parameters. T_m and ΔH_m have been determined independently by calorimetry as described recently [30]; the data are shown in Fig. S3 in the SI, together with experimental relaxation curves and fits for each individual temperature for both polymers (Fig. S1 and S2). Fit values and thermodynamic parameters are summarized in Table I.

^b half-exchange time calculated for $T=25\,^{\circ}\mathrm{C}$ via eq. (2)

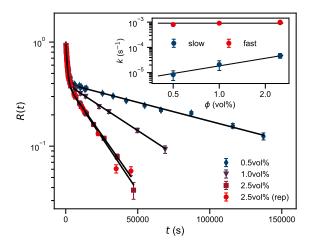


FIG. 4. Relaxation curves of C28F40 measured at $T=37\,^{\circ}\mathrm{C}$ and three different polymer volume fractions. The inset shows the respective rate constants obtained by fitting eq. (5). The fast process is concentration-independent while the slow process exhibits a $k\sim\phi$ dependence.

Arrhenius plots of the fitted parameters of mono- and difunctional chain exchange are presented for C_{22} and C_{28} in Fig. 3, together with rate constants obtained from an earlier study [28] of pure C_n -PEO5 polymers for comparison. The Arrhenius representations display two parallel lines as E_a was found to be identical for monofunctional and telechelic chain exchange. The numerical values of E_a are in good agreement with values obtained earlier for pure diblock polymer exchange [21, 28], see Table I. Because of the exponential dependence, the obtained attempt times τ_0 are rather uncertain but still similar to earlier results. Following the assumptions made above, we can unambiguously rule out the simultaneous escape of the two core blocks, as this would correspond to twice the activation energy.

From the above results we can already conclude that the exchange of telechelic chains proceeds via a consecutive release of the two chain ends. Either the two hydrophobic blocks are released step-wise and then diffuse freely (scenario ii)) or short-lived clusters are formed (scenario iii)). Now, in order to distinguish between the two mechanisms, we have measured C_{28} relaxation curves at different concentrations because the latter mechanism is collision-based and therefore concentration-dependent. Fig. 4 shows relaxation curves of C_{28} -PEO5/ C_{28} -PEO10- C_{28} micelles measured at three different polymer volume fractions, ϕ =0.5 vol%, 1.0 vol% and 2.5 vol%.

As seen, the three relaxation curves superimpose at short times indicating a concentration independent escape of monofunctional PEO chains, whereas the telechelic chains show a distinct acceleration of chain exchange with increasing ϕ . The kinetic data were quantitatively analysed by fitting with eq. (5) and the obtained

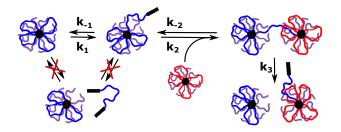


FIG. 5. Visualization of the exchange mechanism of telechelic chains in flowerlike micelles and clusters of micelles via a sequence of consecutive equilibrium steps involving collision-induced exchange. Diffusion of free telechelic chains as an important pathway is excluded.

rate constants extracted for the fast and slow process are plotted vs. ϕ in the inset of Fig. 4. The rate constant of the fast process, associated with $k_{\rm mon}$, is basically constant, which confirms that the exchange is not affected by micellar collisions. However, the slow process, associated with k_{tel} , on the other hand, scales linearly with ϕ suggesting that collision-induced chain exchange is the dominating mechanism for telechelic chain exchange. To ascertain that not, incidentally, the exchange mechanism changes with concentration but the ϕ dependence is in fact intrinsic to the exchange mechanism, we performed concentration- and temperature-dependent measurements on C28F40—compare Fig. S4 and S5 and the SI. We were able to fit all relaxation curves with one set of parameters in agreement with the values given in Tab. I. Particularly, E_a is the same for all three concentrations, proving that the exchange mechanism does not change with concentration.

The proposed mechanism is similar to the "walking diffusion" suggested by Yokoyama and Kramer [22, 23] in polymer melts but differs by the lack of micellar crystalline order. Instead, the exchange events are triggered by random collisions between micelles where at least one chain is in an "activated state", i.e., with a chain end outside the micelle. It also resembles a collision-based exchange mechanisms recently found in lipid nanodiscs[31]. For the present case of telechelic molecules in solution, we propose the three-step kinetic model sketched in Fig. 5. This can be written as:

1) Expulsion of one telechelic hydrophobic chain-end while the other one is still buried in the micellar core

$$P \underset{k_{-1}}{\overset{k_1}{\rightleftharpoons}} P^* \tag{6a}$$

2) Insertion of the free chain end into another micelle, i.e., bridging

$$P^* + M \stackrel{k_2}{\underset{k_{-2}}{\rightleftharpoons}} P^{**}$$
 (6b)

3) Release of the second chain-end that was still in the

original micelle

$$P^{**} \stackrel{k_3}{\to} M + \bar{P}^* \tag{6c}$$

Here, P represents telechelic polymer molecules that have not exchanged yet and both chain ends are buried in the original micelle. P^* are molecules that are also still attached to their original micelle but with one chain end free in solution and M is an arbitrary micelle. P^{**} is a molecule that bridges between its original micelle and another one and \bar{P}^* is a chain that has exchanged at least once and has one free chain end.

Applying a steady-state approximation for the unstable intermediates, P^* and P^{**} , this leads to a single exponential (see SI for a more detailed discussion)

$$[P](t) = [P]_0 \cdot \exp(-k_{\text{eff}} t), \tag{7}$$

with the concentration-dependent decay constant $k_{\text{eff}} =$ $k_1k_2[M]/(2k_{-1}+k_2[M])$. For low micelle concentrations and $k_2 \leq k_{-1}$, a Taylor expansion in [M] yields $k_{\text{eff}} = k_1 k_2 [M]/(2k_{-1}) + \mathcal{O}([M]^2)$. Thus, in the leading order the rate constant depends linearly on [M] and, since k_{-1} and k_2 have approximately the same enthalpic contribution, the temperature dependence is governed by k_1 . Moreover, the model provides an equilibrium constant $K = k_1/k_{-1} \ll 1$, which controls release of a single chain end. This naturally describes the effective reduction of the exchange rate of telechelic chains, $k_{\text{eff}} = K k_2 [M]/2$. These findings are in perfect agreement with our experimental results. In addition, the telechelic PEO block is longer than the corresponding monofunctional one which is known to slow down chain exchange [19, 32].

In conclusion, we have shown that the molecular exchange of telechelic polymers in flowerlike micelles and clusters of micelles proceeds in consecutive steps via a collision-induced single-chain exchange mechanism that so far has not been reported experimentally. TR-SANS in combination with the KZAC - H/D contrast variation method was applied to monitor the chain exchange in a well-defined archetypical model system for self-assembly. By carefully analyzing the TR-SANS data at different temperatures and concentrations, we can rule out a simultaneous release of the two chain ends. In addition, we have developed a kinetic model that explains the experimental findings and provides a rather complete picture of the equilibration mechanism and diffusion processes in such systems. The discovered collision-induced exchange mechanism is relevant also to other self-assembled structures, in which multi-valency plays a role, e.g., in supramolecular networks, lipid membranes, multi-domain proteins, lipoproteins, and conventional hydrogels.

This work is based on experiments performed at the KWS-2 instrument [33] operated by JCNS at Heinz Maier-Leibnitz Zentrum, Garching, Germany, and the Sans2d instrument [34, 35] at STFC ISIS Neutron and

Muon Source, United Kingdom. We thank Bente A. Breiby (School of Pharmacy, UiO) and Thomas Zinn (ESRF - The European Synchrotron) for providing the DSC data.

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